

**VISVESVARAYA TECHNOLOGICAL  
UNIVERSITY**

“JnanaSangama”, Belgaum -590014, Karnataka.



**LAB RECORD**

**Bio Inspired Systems (23CS5BSBIS)**

*Submitted by*

**Prerana P Jois (1BM23CS250)**

*in partial fulfillment for the award of the degree of*

**BACHELOR OF ENGINEERING  
*in*  
COMPUTER SCIENCE AND ENGINEERING**



**B.M.S. COLLEGE OF ENGINEERING**

(Autonomous Institution under VTU)

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**B.M.S. College of Engineering,  
Bull Temple Road, Bangalore 560019**  
(Affiliated To Visvesvaraya Technological University, Belgaum)  
**Department of Computer Science and Engineering**



**CERTIFICATE**

This is to certify that the Lab work entitled “Bio Inspired Systems (23CS5BSBIS)” carried out by **Prerana P Jois (1BM23CS250)**, who is bonafide student of **B.M.S. College of Engineering**. It is in partial fulfillment for the award of **Bachelor of Engineering in Computer Science and Engineering** of the Visvesvaraya Technological University, Belgaum. The Lab report has been approved as it satisfies the academic requirements of the above mentioned subject and the work prescribed for the said degree.

Dr. Namratha M Assistant Professor Department of CSE, BMSCE	Dr. Kavitha Sooda Professor & HOD Department of CSE, BMSCE
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Github Link:

[https://github.com/preranapjois/BIS\\_LAB.git](https://github.com/preranapjois/BIS_LAB.git)

**Program 1:**  
Genetic algorithm

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Genetic algorithms

Algorithm about  $i \in \{1, 2, \dots, n\}$

Genetic algo (G)

input ( $i$ ):  $S \rightarrow$  set of blocks  
output:  $\min$  Superstring of  $S$

initialization:  $P_0$

initialize the population, to  $t=0$

EVALUATE:  $f(S, P_t)$

while termination condition not met

do

- select individuals from  $P_t$
- Recombine individuals
- Mutate individuals

EVALUATE - FITNESS - MA ( $S$ , modified individual)

$P_{t+1} \leftarrow$  newly created individuals

$t \leftarrow t + 1$

between (Supersetting derived from  
best individual in  $P_t$ )

(2) ~~strategic~~ 3.6.3.2. evalute

procedure EVALUATE-FITNESS( $S, P_t$ )

$S$  - set of blocks

$P_t$  - population of individuals

for each individual  $i \in P_t$

do {  
    general derived by using  $S_{\text{ci}}$   
     $m \leftarrow$  all blocks from  $S$  that  
    are not covered by  $S_{\text{ci}}$  }

$s'_{(i)} \leftarrow$  concatenation of  $S_{\text{ci}}$  &  $m$   
     $\text{fitness}(i) \leftarrow$   $\text{fitness}(s'_{(i)})$

    } // iteration over all individuals  
    // distribution over all individuals  
    // crossover - individuals ( $S, P_t, P_{t+1}$ )  
    // mutation

for  $i$  in range( $P_t$ . length);

$p = \text{random.random}()$

if  $p < 0.5$

    New [ $i$ ]  $\leftarrow P_t$ [ $i$ ];

    diff  $p < 0.9$

Neue  $i \in [0, n]$ ; mutation  
else  
    Neue  $c_i \in \text{mutatz}(G)$   
return Neue;

Steps:

- (1) initialize population
- (2) Evaluate fitness
- (3) while termination not reached:
  - \* Select best individuals
  - \* Apply crossover & mutation
    - \* Evaluate new individuals
    - \* Replace old population with new one.
- Example in Neural Network

## Code :

```
import numpy as np

inputs = np.array([
    [0, 0],
    [0, 1],
    [1, 0],
    [1, 1]
])
expected = np.array([[0], [1], [1], [0]])

def sigmoid(x):
    return 1 / (1 + np.exp(-x))

def sigmoid_derivative(x):
    return x * (1 - x)

def forward_pass(weights, x):
    w1 = weights[:4].reshape((2, 2))
    b1 = weights[4:6]
    w2 = weights[6:8].reshape((2, 1))
    b2 = weights[8]
    z1 = np.dot(x, w1) + b1
    a1 = sigmoid(z1)
    z2 = np.dot(a1, w2) + b2
    a2 = sigmoid(z2)
    return a2

def fitness(weights):
    predictions = forward_pass(weights, inputs)
    error = np.mean((predictions - expected) ** 2)
    return -error

pop_size = 100
num_weights = 9
generations = 200
mutation_rate = 0.1

population = np.random.uniform(-1, 1, (pop_size, num_weights))

for generation in range(generations):
    fitness_scores = np.array([fitness(ind) for ind in population])
    sorted_idx = np.argsort(fitness_scores)[-1]
    population = population[sorted_idx]
    fitness_scores = fitness_scores[sorted_idx]
```

```

top_n = int(0.2 * pop_size)
parents = population[:top_n]
children = []

while len(children) < pop_size - top_n:
    p1, p2 = parents[np.random.randint(0, top_n, 2)]
    crossover = np.random.randint(1, num_weights)
    child = np.concatenate((p1[:crossover], p2[crossover:]))
    if np.random.rand() < mutation_rate:
        mutation_point = np.random.randint(num_weights)
        child[mutation_point] += np.random.uniform(-0.5, 0.5)
    children.append(child)

population = np.vstack((parents, children))

if generation % 10 == 0 or generation == generations - 1:
    print(f'Generation {generation+1} | Best fitness: {fitness_scores[0]:.4f}')

best_weights = population[0]
print("\nFinal predictions:")
preds = forward_pass(best_weights, inputs)
for i in range(len(inputs)):
    print(f'Input: {inputs[i]} => Predicted: {preds[i][0]:.4f} | Expected: {expected[i][0]}')

print("\nDataset: XOR dataset")

```

Output:

---

```

Generation 1 | Best fitness: -0.2497
Generation 11 | Best fitness: -0.2430
Generation 21 | Best fitness: -0.2329
Generation 31 | Best fitness: -0.2196
Generation 41 | Best fitness: -0.2029
Generation 51 | Best fitness: -0.1898
Generation 61 | Best fitness: -0.1626
Generation 71 | Best fitness: -0.1423
Generation 81 | Best fitness: -0.1184
Generation 91 | Best fitness: -0.0898
Generation 101 | Best fitness: -0.0751
Generation 111 | Best fitness: -0.0538
Generation 121 | Best fitness: -0.0463
Generation 131 | Best fitness: -0.0312

```

---

Generation 141 | Best fitness: -0.0221

Generation 151 | Best fitness: -0.0142

Generation 161 | Best fitness: -0.0098

Generation 171 | Best fitness: -0.0060

Generation 181 | Best fitness: -0.0036

Generation 191 | Best fitness: -0.0021

Generation 200 | Best fitness: -0.0012

Final predictions:

Input: [0 0] => Predicted: 0.0440 | Expected: 0

Input: [0 1] => Predicted: 0.9750 | Expected: 1

Input: [1 0] => Predicted: 0.9643 | Expected: 1

Input: [1 1] => Predicted: 0.0331 | Expected: 0

Dataset: XOR dataset

This is a classic non-linear classification problem (cannot be solved by a single perceptron; needs hidden layers or non-linear models).

**Program 2:**  
Gene Expression algorithm

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Gene expression

Input:

- Population size ( $N$ )
- Number of generations ( $n$ )
- Mutation probability ( $P_m$ )
- Crossover probability ( $P_c$ )
- Transposition probability ( $P_t$ )
- Problem-specific fitness function  $F$

Initialization

```
Population ← generate random chrom
for each chromosome  $c$  in population do
    Expression  $\leftarrow$  decode( $c$ ) // convert gen-to-ex
    Fitness( $c$ )  $\leftarrow F(Expression)$ 
end for
```

For gen = 1 to n do

```
New population  $\leftarrow \emptyset$ 
while size(New Population) < N do
    Parent 1  $\leftarrow$  select(Population)
    Parent 2  $\leftarrow$  select(Population)
    with Probability  $P_c$ :
        ( $child_1, child_2$ )  $\leftarrow$  crossover
        (Parent 1, Parent 2)
```

otherwise:

child1 ← copy (Parent 1)

child2 ← copy (Parent 2)

with probability  $p_m$ :

child1 ← mutate (child1)

with probability  $p_m$ :

child2 ← mutate (child2)

with probability  $p_t$ :

child1 ← transpose (child1)

with probability  $p_t$ :

child2 ← transpose (child2)

II evaluate fitness

Expression1 ← decode (child1)

Expression2 ← decode (child2)

Fitness (child1) ← F(Expression1)

Fitness (child2) ← F(Expression2)

Add child1, child2 to NewPopulation

End while

III Replacement

Population ← select Best (Newpopulation, n)

End For



Best ← chromosome with highest fitness in population

Best Expression ← decode (Best)

Return Best Expression

End.

- Execute in the field of IP

- Include the result, observed &

- point out the difference of GA to EC one

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## Code:

```
import numpy as np
import matplotlib.pyplot as plt
import random
import cv2

rows, cols = 128, 128
x = np.tile(np.linspace(0, 255, cols, dtype=np.uint8), (rows, 1))
noise = np.random.randint(0, 40, (rows, cols), dtype=np.uint8)
img = cv2.add(x, noise)

def fitness(threshold):
    foreground = img[img > threshold]
    background = img[img <= threshold]
    if len(foreground) == 0 or len(background) == 0:
        return 0
    w0 = len(background) / (rows * cols)
    w1 = len(foreground) / (rows * cols)
    m0 = np.mean(background)
    m1 = np.mean(foreground)
    return w0 * w1 * ((m0 - m1) ** 2)

pop_size = 30
generations = 40
population = np.random.randint(0, 255, size=pop_size)

for g in range(generations):
    scores = np.array([fitness(t) for t in population])
    best_idx = np.argmax(scores)
    best_threshold = population[best_idx]
    print(f"Generation {g+1} | Best threshold: {best_threshold}")
    sorted_idx = np.argsort(scores)[::-1]
    parents = population[sorted_idx[:pop_size // 2]]
    children = []
    while len(children) < pop_size - len(parents):
        p1, p2 = random.sample(list(parents), 2)
        child = (p1 + p2) // 2
        if random.random() < 0.3:
            child += random.randint(-10, 10)
        child = np.clip(child, 0, 255)
        children.append(child)
    population = np.concatenate((parents, children))

best_threshold = int(best_threshold)
print("\nGA Result → Best threshold found =", best_threshold)
```

```

_, ga_result = cv2.threshold(img, best_threshold, 255, cv2.THRESH_BINARY)

rule_threshold = int(0.65 * np.mean(img) + 40)
_, rule_result = cv2.threshold(img, rule_threshold, 255, cv2.THRESH_BINARY)
print("Rule-based threshold result =", rule_threshold)

plt.figure(figsize=(10, 8))
plt.subplot(2, 1, 1)
plt.imshow(ga_result, cmap='gray')
plt.title(f'GA Threshold = {best_threshold}')
plt.subplot(2, 1, 2)
plt.imshow(rule_result, cmap='gray')
plt.title("GAE Rule-based")
plt.tight_layout()
plt.show()

print("\n* GA Result → Best threshold found =", best_threshold)
print("* GAE Rule-based result =", rule_threshold)
print("1) Original: synthetic gradient + noise")
print("2) GA thresholding result =", best_threshold)

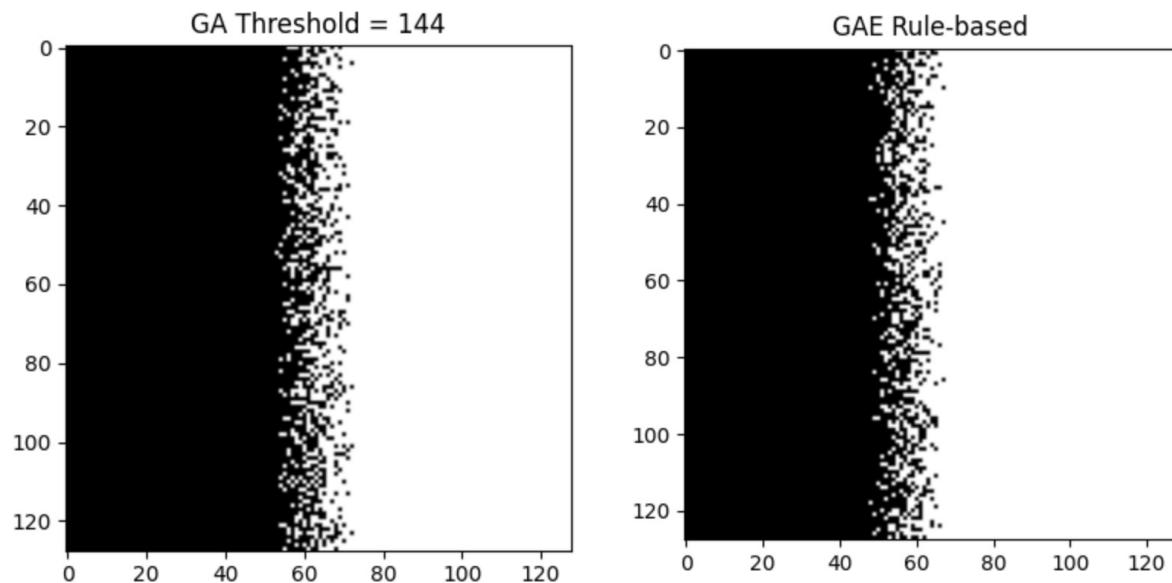
```

Output:

```

Generation 1 | Best threshold: 146 Generation 2 | Best threshold: 144 Generation 3 | Best threshold: 144
Generation 4 | Best threshold: 144 Generation 5 | Best threshold: 144 Generation 6 | Best threshold: 144
Generation 7 | Best threshold: 144 Generation 8 | Best threshold: 144 Generation 9 | Best threshold: 144
Generation 10 | Best threshold: 144 Generation 11 | Best threshold: 144 Generation 12 | Best threshold: 144
Generation 13 | Best threshold: 144 Generation 14 | Best threshold: 144 Generation 15 | Best threshold: 144
Generation 16 | Best threshold: 144 Generation 17 | Best threshold: 144 Generation 18 | Best threshold: 144
Generation 19 | Best threshold: 144 Generation 20 | Best threshold: 144 Generation 21 | Best threshold: 144
Generation 22 | Best threshold: 144 Generation 23 | Best threshold: 144 Generation 24 | Best threshold: 144
Generation 25 | Best threshold: 144 Generation 26 | Best threshold: 144 Generation 27 | Best threshold: 144
Generation 28 | Best threshold: 144 Generation 29 | Best threshold: 144 Generation 30 | Best threshold: 144
Generation 31 | Best threshold: 144 Generation 32 | Best threshold: 144 Generation 33 | Best threshold: 144
Generation 34 | Best threshold: 144 Generation 35 | Best threshold: 144 Generation 36 | Best threshold: 144
Generation 37 | Best threshold: 144 Generation 38 | Best threshold: 144 Generation 39 | Best threshold: 144
Generation 40 | Best threshold: 144 GA Result → Best threshold found = 144 Rule-based threshold result =
134

```



\* GA Result → Best threshold found = 144

\* GAE Rule-based result = 134

- 1) Original: synthetic gradient + noise
- 2) GA thresholding result = 144

**Program 3:**  
Particle swan optimization

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Particle Swan optimization

Algorithm of PSO

Input :

- + MaxIter      || no. of particles, iterations
- + w, c<sub>1</sub>, c<sub>2</sub>    || PSO parameters
- + x<sub>min</sub>, x<sub>max</sub>
- + F(x)           || fitness function

Output :

- + g<sub>best</sub>      || global best

Begin

- // Step 1: Initialize particles
- For i = 1 to N do
- Position [i] ← random (x<sub>min</sub>, x<sub>max</sub>)
- velocity [i] ← random (-1 \* x<sub>max</sub> - x<sub>min</sub>, x<sub>max</sub> - x<sub>min</sub>)

For Iter = 1 to MaxIter

- Pbest [i] ← Position [i]
- fitness Pbest [i] ← f (Position [i])

End For

g<sub>best</sub> ← best of Pbest

11 Step 2: Iteration

For iter = 1 to MaxIter do

For i = 1 to N do

    11 update velocity

    velocity [i] ← w \* velocity [i]

        + c1 \* rand(0, 1) \* (pbest [i] - position [i])

        + c2 \* rand(0, 1) \* (gbest - position [i])

    11 update position

    position [i] ← position [i] +

    velocity [i]

    11 Boundary check

        if Position [i] < xmin then

            position [i] ← xmin

        if position [i] > xmax then

            position [i] ← xmax

    11 Evaluate fitness

        if gbest.Fitness < f(position [i])

            gbest ← position [i] // update personal best

        gbest ← position [i] // update global best

        if fitness better than

            the old fitness pbest [i] then

                pbest [i] ← position [i]

                gbest.Fitness ← pbest [i].Fitness

        end if

    end for

End for

Returns gbest

End.

## Code :

```
import numpy as np
def energy_function(position):
    x, y = position
    return (x**2 + y**2) + 10 * np.sin(x) * np.sin(y)

num_particles = 30
dimensions = 2
iterations = 100

w = 0.7
c1 = 1.5
c2 = 1.5
positions = np.random.uniform(-10, 10, (num_particles, dimensions))
velocities = np.random.uniform(-1, 1, (num_particles, dimensions))
pbest_positions = np.copy(positions)
pbest_scores = np.array([energy_function(p) for p in positions])

gbest_position = pbest_positions[np.argmin(pbest_scores)]
gbest_score = np.min(pbest_scores)

for t in range(iterations):
    for i in range(num_particles):
        fitness = energy_function(positions[i])
        if fitness < pbest_scores[i]:
            pbest_scores[i] = fitness
            pbest_positions[i] = positions[i]

    best_particle = np.argmin(pbest_scores)
    if pbest_scores[best_particle] < gbest_score:
        gbest_score = pbest_scores[best_particle]
        gbest_position = pbest_positions[best_particle]
    r1, r2 = np.random.rand(), np.random.rand()
    for i in range(num_particles):
        velocities[i] = (w * velocities[i] +
                        c1 * r1 * (pbest_positions[i] - positions[i]) +
                        c2 * r2 * (gbest_position - positions[i]))
        positions[i] += velocities[i]

    print(f'Iteration {t+1}: Best Fitness = {gbest_score:.12e}')
print("\nBest Solution Found:")
print(gbest_position)
print("\nBest Objective Function Value:")
print(gbest_score)
```

Output:

Iteration 1: Best Fitness = -2.569029538935e-01  
Iteration 2: Best Fitness = -4.739972162755e+00  
Iteration 3: Best Fitness = -4.895159615348e+00  
Iteration 4: Best Fitness = -4.895159615348e+00  
Iteration 5: Best Fitness = -4.980324627255e+00  
Iteration 6: Best Fitness = -5.226913277912e+00  
Iteration 7: Best Fitness = -5.226913277912e+00  
Iteration 8: Best Fitness = -5.391303100542e+00  
Iteration 9: Best Fitness = -5.391303100542e+00  
Iteration 10: Best Fitness = -5.391303100542e+00  
Iteration 11: Best Fitness = -5.866209539629e+00  
Iteration 12: Best Fitness = -5.899624748247e+00  
Iteration 13: Best Fitness = -5.899624748247e+00  
Iteration 14: Best Fitness = -5.899624748247e+00  
Iteration 15: Best Fitness = -5.899624748247e+00  
Iteration 16: Best Fitness = -5.899624748247e+00  
Iteration 17: Best Fitness = -5.903361933188e+00  
Iteration 18: Best Fitness = -5.904170911460e+00  
Iteration 19: Best Fitness = -5.904170911460e+00  
Iteration 20: Best Fitness = -5.904170911460e+00  
Iteration 21: Best Fitness = -5.904470092450e+00  
Iteration 22: Best Fitness = -5.904470092450e+00  
Iteration 23: Best Fitness = -5.904470092450e+00  
Iteration 24: Best Fitness = -5.904470092450e+00  
Iteration 25: Best Fitness = -5.904473550935e+00  
Iteration 26: Best Fitness = -5.904473550935e+00  
Iteration 27: Best Fitness = -5.904473550935e+00  
Iteration 28: Best Fitness = -5.904473550935e+00  
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Iteration 35: Best Fitness = -5.904473550935e+00  
Iteration 36: Best Fitness = -5.904473550935e+00  
Iteration 37: Best Fitness = -5.904490733230e+00  
Iteration 38: Best Fitness = -5.904490733230e+00  
Iteration 39: Best Fitness = -5.904490765753e+00  
Iteration 40: Best Fitness = -5.904490765753e+00  
Iteration 41: Best Fitness = -5.904490765753e+00  
Iteration 42: Best Fitness = -5.904490765753e+00  
Iteration 43: Best Fitness = -5.904490765753e+00

Iteration 44: Best Fitness = -5.904490791690e+00  
Iteration 45: Best Fitness = -5.904490791690e+00  
Iteration 46: Best Fitness = -5.904490791690e+00  
Iteration 47: Best Fitness = -5.904491355488e+00  
Iteration 48: Best Fitness = -5.904491355488e+00  
Iteration 49: Best Fitness = -5.904491355488e+00  
Iteration 50: Best Fitness = -5.904491355488e+00  
Iteration 51: Best Fitness = -5.904491355488e+00  
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Iteration 53: Best Fitness = -5.904491355488e+00  
Iteration 54: Best Fitness = -5.904491366230e+00  
Iteration 55: Best Fitness = -5.904491366230e+00  
Iteration 56: Best Fitness = -5.904491507256e+00  
Iteration 57: Best Fitness = -5.904491507256e+00  
Iteration 58: Best Fitness = -5.904491547815e+00  
Iteration 59: Best Fitness = -5.904491547815e+00  
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Iteration 63: Best Fitness = -5.904491547815e+00  
Iteration 64: Best Fitness = -5.904491547815e+00  
Iteration 65: Best Fitness = -5.904491560085e+00  
Iteration 66: Best Fitness = -5.904491560085e+00  
Iteration 67: Best Fitness = -5.904491560085e+00  
Iteration 68: Best Fitness = -5.904491560085e+00  
Iteration 69: Best Fitness = -5.904491560085e+00  
Iteration 70: Best Fitness = -5.904491560085e+00  
Iteration 71: Best Fitness = -5.904491560085e+00  
Iteration 72: Best Fitness = -5.904491560085e+00  
Iteration 73: Best Fitness = -5.904491560085e+00  
Iteration 74: Best Fitness = -5.904491560085e+00  
Iteration 75: Best Fitness = -5.904491646024e+00  
Iteration 76: Best Fitness = -5.904491663358e+00  
Iteration 77: Best Fitness = -5.904491665196e+00  
Iteration 78: Best Fitness = -5.904491665196e+00  
Iteration 79: Best Fitness = -5.904491670423e+00  
Iteration 80: Best Fitness = -5.904491670423e+00  
Iteration 81: Best Fitness = -5.904491670423e+00  
Iteration 82: Best Fitness = -5.904491670423e+00  
Iteration 83: Best Fitness = -5.904491670423e+00  
Iteration 84: Best Fitness = -5.904491670423e+00  
Iteration 85: Best Fitness = -5.904491670423e+00  
Iteration 86: Best Fitness = -5.904491670423e+00  
Iteration 87: Best Fitness = -5.904491670423e+00  
Iteration 88: Best Fitness = -5.904491670423e+00  
Iteration 89: Best Fitness = -5.904491670423e+00

Iteration 90: Best Fitness = -5.904491670423e+00  
Iteration 91: Best Fitness = -5.904491670423e+00  
Iteration 92: Best Fitness = -5.904491670423e+00  
Iteration 93: Best Fitness = -5.904491670423e+00  
Iteration 94: Best Fitness = -5.904491670610e+00  
Iteration 95: Best Fitness = -5.904491670610e+00  
Iteration 96: Best Fitness = -5.904491670610e+00  
Iteration 97: Best Fitness = -5.904491670610e+00  
Iteration 98: Best Fitness = -5.904491670610e+00  
Iteration 99: Best Fitness = -5.904491670610e+00  
Iteration 100: Best Fitness = -5.904491670610e+00

Best Solution Found: [-1.29786271 1.29787174]  
Best Objective Function Value: -5.904491670609598

## Program 4:

Ant colony optimization for the travelling salesman problem

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Ant colony optimization for the travelling salesman problem

Algorithm:

1) Initialize pheromone matrix  $\tau$  on all solution components  
Set parameters  $\alpha$  (pheromone influence),  $\beta$  (heuristic influence), evaporation rate  $\rho$ , number of ants  $m$

2) Input: number of cities  $n$ , cost function  $cost(i, j)$  for distance matrix, parameters  $\alpha, \beta, \rho$  (evaporation),  $\tau_0$ ,  $m$  ants -  $n$  iterations

while stopping criteria not met:  
for each ant  $k$  in 1 to  $m$ :  
    initialize an empty solution  $S_k$   
    while solution  $S_k$  is incomplete:  
        Select next solution component  $c$  based on probability proportional to:  
$$[\tau(c)]^\alpha * [n(c)]^\beta$$
  
        where  $n(c)$  is heuristic desirability of component  $c$   
        add component  $c$  to solution  $S_k$

evaluate the quality of solutions

for each solution component  $c$ :

evaporate pheromone:

$$T(c) = (1 - \rho) * T(c)$$

for each solution ant  $k$ :

deposit pheromone on component  
in solution  $s_k$ :

$$T(c) = \alpha T(c) + \Delta t - k c$$

amount  $\Delta t - k c$  depends on quality  
of solution  $s_k$

between the best solution found

[Note:

$\alpha \rightarrow$  Pheromone influence

$\beta \rightarrow$  Heuristic influence

$\gamma \rightarrow$  Evaporation rate

$m \rightarrow$  number of ants

~~Ants~~ Points in  $\Delta t - k c \rightarrow$  reward signal

(that guides future ants  
towards better solution)

$\Delta t(i, j) =$  the amount of pheromone  
deposited

$\Delta t \rightarrow$  change in pheromone]

## Code:

```
import numpy as np
import random

num_stops = 6
np.random.seed(42)

distances = np.random.randint(10, 100, size=(num_stops, num_stops))
for i in range(num_stops):
    distances[i][i] = 0
    for j in range(i + 1, num_stops):
        distances[j][i] = distances[i][j]

num_ants = 10
num_iterations = 100
alpha = 1.0
beta = 5.0
evaporation_rate = 0.5
Q = 100

pheromone = np.ones((num_stops, num_stops))

def route_distance(route):
    total = 0
    for i in range(len(route) - 1):
        total += distances[route[i]][route[i + 1]]
    total += distances[route[-1]][route[0]]
    return total

best_route = None
best_distance = float("inf")

for iteration in range(num_iterations):
    all_routes = []
    all_distances = []

    for ant in range(num_ants):
        route = [random.randint(0, num_stops - 1)]
        while len(route) < num_stops:
            i = route[-1]
            unvisited = [j for j in range(num_stops) if j not in route]

            probabilities = []
            for j in unvisited:
```

```

pheromone_factor = pheromone[i][j] ** alpha
distance_factor = (1.0 / (distances[i][j] + 1e-10)) ** beta
probabilities.append(pheromone_factor * distance_factor)

probabilities = np.array(probabilities)
probabilities /= probabilities.sum()

next_stop = np.random.choice(unvisited, p=probabilities)
route.append(next_stop)

total_distance = route_distance(route)
all_routes.append(route)
all_distances.append(total_distance)

if total_distance < best_distance:
    best_distance = total_distance
    best_route = route

pheromone *= (1 - evaporation_rate)
for r, dist in zip(all_routes, all_distances):
    for i in range(len(r) - 1):
        pheromone[r[i]][r[i + 1]] += Q / dist
        pheromone[r[-1]][r[0]] += Q / dist

print(f"Iteration {iteration+1}: Best Distance (Traffic-Aware) = {best_distance:.4f}")

print("\nOptimal Bus Route Found:")
print(" → ".join(str(stop) for stop in best_route))
print(f"Optimal Total Travel Distance (with traffic): {best_distance:.4f}")

```

Output:

```

Iteration 1: Best Distance (Traffic-Aware) = 234.0000
Iteration 2: Best Distance (Traffic-Aware) = 234.0000
Iteration 3: Best Distance (Traffic-Aware) = 234.0000
Iteration 4: Best Distance (Traffic-Aware) = 234.0000
Iteration 5: Best Distance (Traffic-Aware) = 234.0000
Iteration 6: Best Distance (Traffic-Aware) = 234.0000
Iteration 7: Best Distance (Traffic-Aware) = 234.0000
Iteration 8: Best Distance (Traffic-Aware) = 234.0000
Iteration 9: Best Distance (Traffic-Aware) = 234.0000
Iteration 10: Best Distance (Traffic-Aware) = 234.0000
Iteration 11: Best Distance (Traffic-Aware) = 234.0000
Iteration 12: Best Distance (Traffic-Aware) = 234.0000
Iteration 13: Best Distance (Traffic-Aware) = 234.0000

```



Iteration 60: Best Distance (Traffic-Aware) = 234.0000  
Iteration 61: Best Distance (Traffic-Aware) = 234.0000  
Iteration 62: Best Distance (Traffic-Aware) = 234.0000  
Iteration 63: Best Distance (Traffic-Aware) = 234.0000  
Iteration 64: Best Distance (Traffic-Aware) = 234.0000  
Iteration 65: Best Distance (Traffic-Aware) = 234.0000  
Iteration 66: Best Distance (Traffic-Aware) = 234.0000  
Iteration 67: Best Distance (Traffic-Aware) = 234.0000  
Iteration 68: Best Distance (Traffic-Aware) = 234.0000  
Iteration 69: Best Distance (Traffic-Aware) = 234.0000  
Iteration 70: Best Distance (Traffic-Aware) = 234.0000  
Iteration 71: Best Distance (Traffic-Aware) = 234.0000  
Iteration 72: Best Distance (Traffic-Aware) = 234.0000  
Iteration 73: Best Distance (Traffic-Aware) = 234.0000  
Iteration 74: Best Distance (Traffic-Aware) = 234.0000  
Iteration 75: Best Distance (Traffic-Aware) = 234.0000  
Iteration 76: Best Distance (Traffic-Aware) = 234.0000  
Iteration 77: Best Distance (Traffic-Aware) = 234.0000  
Iteration 78: Best Distance (Traffic-Aware) = 234.0000  
Iteration 79: Best Distance (Traffic-Aware) = 234.0000  
Iteration 80: Best Distance (Traffic-Aware) = 234.0000  
Iteration 81: Best Distance (Traffic-Aware) = 234.0000  
Iteration 82: Best Distance (Traffic-Aware) = 234.0000  
Iteration 83: Best Distance (Traffic-Aware) = 234.0000  
Iteration 84: Best Distance (Traffic-Aware) = 234.0000  
Iteration 85: Best Distance (Traffic-Aware) = 234.0000  
Iteration 86: Best Distance (Traffic-Aware) = 234.0000  
Iteration 87: Best Distance (Traffic-Aware) = 234.0000  
Iteration 88: Best Distance (Traffic-Aware) = 234.0000  
Iteration 89: Best Distance (Traffic-Aware) = 234.0000  
Iteration 90: Best Distance (Traffic-Aware) = 234.0000  
Iteration 91: Best Distance (Traffic-Aware) = 234.0000  
Iteration 92: Best Distance (Traffic-Aware) = 234.0000  
Iteration 93: Best Distance (Traffic-Aware) = 234.0000  
Iteration 94: Best Distance (Traffic-Aware) = 234.0000  
Iteration 95: Best Distance (Traffic-Aware) = 234.0000  
Iteration 96: Best Distance (Traffic-Aware) = 234.0000  
Iteration 97: Best Distance (Traffic-Aware) = 234.0000  
Iteration 98: Best Distance (Traffic-Aware) = 234.0000  
Iteration 99: Best Distance (Traffic-Aware) = 234.0000  
Iteration 100: Best Distance (Traffic-Aware) = 234.0000

Optimal Bus Route Found:

$0 \rightarrow 1 \rightarrow 5 \rightarrow 2 \rightarrow 4 \rightarrow 3$

Optimal Total Travel Distance (with traffic): 234.0000

**Program 5:**  
Cuckoo Search algorithm

cuckoo search algorithm

(1) Initialize population (nests):

For  $i = 1$  to  $n$ :

    Initialize nest  $i$  with a random solution  $x_i$  within search bounds

    Evaluate fitness  $f_i = f(x_i)$

End for

(2) Find the current best solution:

$x_{best}$  = nest with minimum (or maximum) fitness value

(3) Repeat until stopping criterion  
(MaxIter or convergence):

For  $t = 1$  to MaxIter:

    For each cuckoo ( $i = 1$  to  $n$ ):

        Generate a new solution

$x_{i,new}$  by Levy flight:

$$x_{i,new} = x_i + \alpha \cdot \text{Le'vy}(z)$$

        Evaluate fitness  $f_{i,new} =$

$$f(x_{i,new})$$

        Randomly choose a nest  $j$  with ( $j \neq i$ )

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If  $F_{i\_new} < F_j$ :  
 Replace  $n_{i,j}$  with  $x_{i,j\_new}$   
 End if  
 End for

For each nest  $i$ :  
 with probability  $p_a$ :  
 Replace  $n_i$  with a new  
 random solution  
 End if  
 End for

Find  $a_{best} = nest$  with best  
 fitnum  
 End for. *beta=1.5*

~~Optimal for~~

## Code:

```

import numpy as np
from math import gamma, sin, pi

def electrical_grid_loss(x):
    x = np.array(x)
    return np.sum(x**2 - 10 * np.cos(2 * np.pi * x) + 10)

def cuckoo_search(obj_func, n=15, d=2, lb=-5, ub=5, pa=0.25, iterations=100):
    beta = 1.5
    sigma = (gamma(1 + beta) * sin(pi * beta / 2) /
             (gamma((1 + beta) / 2) * beta * 2 ** ((beta - 1) / 2))) ** (1 / beta)

    nests = np.random.uniform(lb, ub, (n, d))
  
```

```

fitness = np.array([obj_func(nest) for nest in nests])
best_nest = nests[np.argmin(fitness)]
best_fitness = np.min(fitness)

for t in range(iterations):
    new_nests = np.copy(nests)
    for i in range(n):
        step = np.random.normal(0, sigma, size=d) / (abs(np.random.normal(0, 1, size=d)) ** (1 /
beta))
        new_nest = nests[i] + 0.01 * step * (nests[i] - best_nest)
        new_nest = np.clip(new_nest, lb, ub)
        new_nests[i] = new_nest

    new_fitness = np.array([obj_func(nest) for nest in new_nests])

    for i in range(n):
        if new_fitness[i] < fitness[i]:
            fitness[i] = new_fitness[i]
            nests[i] = new_nests[i]

    abandon_mask = np.random.rand(n, d) < pa
    random_nests = np.random.uniform(lb, ub, (n, d))
    nests = np.where(abandon_mask, random_nests, nests)
    fitness = np.array([obj_func(nest) for nest in nests])

    if np.min(fitness) < best_fitness:
        best_fitness = np.min(fitness)
        best_nest = nests[np.argmin(fitness)]

print(f"Iteration {t+1}: Best Grid Loss = {best_fitness:.10e}")

return best_nest, best_fitness

best_solution, best_value = cuckoo_search(electrical_grid_loss, n=20, d=3, lb=-5, ub=5,
iterations=100)

print("\nOptimal Electrical Grid Configuration:")
print(best_solution)
print("\nMinimum Power Loss (Objective Value):")
print(best_value)

```

Output:

Iteration 1: Best Grid Loss = 1.1953471974e+01  
Iteration 2: Best Grid Loss = 1.1953471974e+01  
Iteration 3: Best Grid Loss = 1.1953471974e+01  
Iteration 4: Best Grid Loss = 5.2025691754e+00  
Iteration 5: Best Grid Loss = 5.2025691754e+00  
Iteration 6: Best Grid Loss = 5.2025691754e+00  
Iteration 7: Best Grid Loss = 5.2025691754e+00  
Iteration 8: Best Grid Loss = 5.2025691754e+00  
Iteration 9: Best Grid Loss = 5.2025691754e+00  
Iteration 10: Best Grid Loss = 5.2025691754e+00  
Iteration 11: Best Grid Loss = 5.2025691754e+00  
Iteration 12: Best Grid Loss = 5.2025691754e+00  
Iteration 13: Best Grid Loss = 5.2025691754e+00  
Iteration 14: Best Grid Loss = 5.2025691754e+00  
Iteration 15: Best Grid Loss = 5.2025691754e+00  
Iteration 16: Best Grid Loss = 5.2025691754e+00  
Iteration 17: Best Grid Loss = 5.2025691754e+00  
Iteration 18: Best Grid Loss = 5.2025691754e+00  
Iteration 19: Best Grid Loss = 5.2025691754e+00  
Iteration 20: Best Grid Loss = 5.2025691754e+00  
Iteration 21: Best Grid Loss = 5.2025691754e+00  
Iteration 22: Best Grid Loss = 5.2025691754e+00  
Iteration 23: Best Grid Loss = 5.2025691754e+00  
Iteration 24: Best Grid Loss = 5.2025691754e+00  
Iteration 25: Best Grid Loss = 5.2025691754e+00  
Iteration 26: Best Grid Loss = 5.2025691754e+00  
Iteration 27: Best Grid Loss = 5.2025691754e+00  
Iteration 28: Best Grid Loss = 5.2025691754e+00  
Iteration 29: Best Grid Loss = 5.2025691754e+00  
Iteration 30: Best Grid Loss = 5.2025691754e+00  
Iteration 31: Best Grid Loss = 5.2025691754e+00  
Iteration 32: Best Grid Loss = 5.2025691754e+00  
Iteration 33: Best Grid Loss = 5.2025691754e+00  
Iteration 34: Best Grid Loss = 5.2025691754e+00  
Iteration 35: Best Grid Loss = 5.2025691754e+00  
Iteration 36: Best Grid Loss = 5.2025691754e+00  
Iteration 37: Best Grid Loss = 5.2025691754e+00  
Iteration 38: Best Grid Loss = 5.2025691754e+00  
Iteration 39: Best Grid Loss = 5.2025691754e+00  
Iteration 40: Best Grid Loss = 5.2025691754e+00  
Iteration 41: Best Grid Loss = 5.2025691754e+00  
Iteration 42: Best Grid Loss = 5.2025691754e+00  
Iteration 43: Best Grid Loss = 5.2025691754e+00  
Iteration 44: Best Grid Loss = 5.2025691754e+00



Iteration 91: Best Grid Loss = 5.2025691754e+00  
Iteration 92: Best Grid Loss = 5.2025691754e+00  
Iteration 93: Best Grid Loss = 5.2025691754e+00  
Iteration 94: Best Grid Loss = 5.2025691754e+00  
Iteration 95: Best Grid Loss = 5.2025691754e+00  
Iteration 96: Best Grid Loss = 5.2025691754e+00  
Iteration 97: Best Grid Loss = 5.2025691754e+00  
Iteration 98: Best Grid Loss = 5.2025691754e+00  
Iteration 99: Best Grid Loss = 5.2025691754e+00  
Iteration 100: Best Grid Loss = 5.2025691754e+00

Optimal Electrical Grid Configuration:  
[-1.9760426 0.07752152 -0.00891342]

Minimum Power Loss (Objective Value):  
5.202569175412648

**Program 6:**  
Grey wolf optimization algorithm

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Grey wolf optimization

Initialize population of grey wolves  
 $x_i (i=1, 2, \dots, N)$

Initialize  $a, A, c$   
Evaluate fitness of each wolf

I identify alpha (best), beta (2nd best)  
delta (3rd best)

$t = 0$   
while  $t < \text{max\_iterations}$   
 $a = 2 * (1 - t / \text{max\_iterations})$

for each wolf  $i = 1 \dots N$ :  
 $a_{ii} = \text{rand}(0, 1)$

(IP)   
Foreground  $\rightarrow$  image differentiation  
Background  $\rightarrow$  ~~image~~

$A_1 = 2 * a * a_{ii} - a$   
 $c_1 = 2 * a_{ii}$   
~~D\_alpha = abs(c\_1 \* x\_alpha - x\_i)~~  
 $x_1 = x_alpha - A_1 * D_alpha$

~~$a_{ii} = \text{rand}(0, 1);$~~

$g_2 = \text{rand}(0, 1)$

$A_2 = 2 * \alpha * g_1 - \alpha$

$C_2 = 2 * g_2$

$D_{\text{beta}} = \text{abs}(C_2 * x_{\text{beta}} - x_i)$

$x_2 = x_{\text{beta}} - A_2 * D_{\text{beta}}$

$g_1 = \text{rand}(0, 1)$

$g_3 = \text{rand}(0, 1)$

$A_3 = 2 * \alpha * g_1 - \alpha$

$C_3 = 2 * g_3$

$O_{\text{delta}} = \text{abs}(C_3 * x_{\text{delta}} - x_i)$

$x_3 = x_{\text{delta}} - A_3 * O_{\text{delta}}$

$x_{\text{i\_new}} = (x_1 + x_2 + x_3) / 3$

$x_{\text{i\_new}} = \text{clip to bounds } (x_{\text{i\_new}},$   
lower bound, upper bound)

end for

Evaluate  $\text{fitness}(x_{\text{i\_new}})$  for all values  
(using  $x_{\text{i\_new}}$ )

~~update alpha, beta, delta based  
on new fitness values~~

$t = t + 1$

Returns alpha (best solution found)

## Code:

```
import cv2
import numpy as np
import matplotlib.pyplot as plt
from google.colab import files

print("Upload an image (JPG/PNG):")
uploaded = files.upload()
filename = list(uploaded.keys())[0]
img = cv2.imread(filename, cv2.IMREAD_GRAYSCALE)
img = cv2.resize(img, (256, 256))

def fitness(threshold):
    threshold = int(threshold)
    foreground = img[img >= threshold]
    background = img[img < threshold]
    if len(foreground) == 0 or len(background) == 0:
        return 0
    w0 = len(background) / img.size
    w1 = len(foreground) / img.size
    u0 = np.mean(background)
    u1 = np.mean(foreground)
    return w0 * w1 * (u0 - u1)**2

def grey_wolf_optimization(fitness_func, lb, ub, dim=1, n_wolves=20, iterations=50):
    alpha_pos = np.zeros(dim)
    beta_pos = np.zeros(dim)
    delta_pos = np.zeros(dim)
    alpha_score = float('-inf')
    beta_score = float('-inf')
    delta_score = float('-inf')
    positions = np.random.uniform(lb, ub, (n_wolves, dim))

    for t in range(iterations):
        a = 2 - t * (2 / iterations)
        for i in range(n_wolves):
            score = fitness_func(positions[i])
            if score > alpha_score:
                alpha_score = score
                alpha_pos = positions[i].copy()
            elif score > beta_score:
                beta_score = score
                beta_pos = positions[i].copy()
            elif score > delta_score:
                delta_score = score
```

```

    delta_pos = positions[i].copy()
    for i in range(n_wolves):
        for j in range(dim):
            r1, r2 = np.random.rand(), np.random.rand()
            A1, C1 = 2 * a * r1 - a, 2 * r2
            D_alpha = abs(C1 * alpha_pos[j] - positions[i][j])
            X1 = alpha_pos[j] - A1 * D_alpha

            r1, r2 = np.random.rand(), np.random.rand()
            A2, C2 = 2 * a * r1 - a, 2 * r2
            D_beta = abs(C2 * beta_pos[j] - positions[i][j])
            X2 = beta_pos[j] - A2 * D_beta

            r1, r2 = np.random.rand(), np.random.rand()
            A3, C3 = 2 * a * r1 - a, 2 * r2
            D_delta = abs(C3 * delta_pos[j] - positions[i][j])
            X3 = delta_pos[j] - A3 * D_delta

            positions[i][j] = (X1 + X2 + X3) / 3

    positions = np.clip(positions, lb, ub)
    print(f"Iteration {t+1}: Best Fitness = {alpha_score:.5f}, Threshold = {alpha_pos[0]:.2f}")

    return int(alpha_pos[0])

best_threshold = grey_wolf_optimization(fitness, lb=0, ub=255, dim=1, n_wolves=20,
iterations=50)
print(f"\nOptimal Threshold Found by GWO: {best_threshold}")

_, foreground = cv2.threshold(img, best_threshold, 255, cv2.THRESH_BINARY)
background = cv2.bitwise_not(foreground)

plt.figure(figsize=(12, 4))
plt.subplot(1, 3, 1)
plt.imshow(img, cmap='gray')
plt.title("Original Image")
plt.axis('off')

plt.subplot(1, 3, 2)
plt.imshow(foreground, cmap='gray')
plt.title("Foreground (GWO)")
plt.axis('off')

plt.subplot(1, 3, 3)
plt.imshow(background, cmap='gray')
plt.title("Background")

```

```
plt.axis('off')
```

```
plt.show()
```

Output:

Upload an image (JPG/PNG):

Screenshot 2025-11-13 at 21.35.18.png(image/png) - 902667 bytes, last modified: n/a - 100%  
done

Saving Screenshot 2025-11-13 at 21.35.18.png to Screenshot 2025-11-13 at 21.35.18.png

Iteration 1: Best Fitness = 354.43253, Threshold = 137.21

Iteration 2: Best Fitness = 379.28291, Threshold = 118.82

Iteration 3: Best Fitness = 380.05984, Threshold = 121.81

Iteration 4: Best Fitness = 380.05984, Threshold = 121.81

Iteration 5: Best Fitness = 380.05984, Threshold = 121.81

Iteration 6: Best Fitness = 380.05984, Threshold = 121.81

Iteration 7: Best Fitness = 380.05984, Threshold = 121.81

Iteration 8: Best Fitness = 380.05984, Threshold = 121.81

Iteration 9: Best Fitness = 380.05984, Threshold = 121.81

Iteration 10: Best Fitness = 380.05984, Threshold = 121.81

Iteration 11: Best Fitness = 380.05984, Threshold = 121.81

Iteration 12: Best Fitness = 380.05984, Threshold = 121.81

Iteration 13: Best Fitness = 380.05984, Threshold = 121.81

Iteration 14: Best Fitness = 380.05984, Threshold = 121.81

Iteration 15: Best Fitness = 380.05984, Threshold = 121.81

Iteration 16: Best Fitness = 380.05984, Threshold = 121.81

Iteration 17: Best Fitness = 380.05984, Threshold = 121.81

Iteration 18: Best Fitness = 380.05984, Threshold = 121.81

Iteration 19: Best Fitness = 380.05984, Threshold = 121.81

Iteration 20: Best Fitness = 380.05984, Threshold = 121.81

Iteration 21: Best Fitness = 380.05984, Threshold = 121.81

Iteration 22: Best Fitness = 380.05984, Threshold = 121.81

Iteration 23: Best Fitness = 380.05984, Threshold = 121.81

/tmp/ipython-input-1969087285.py:21: DeprecationWarning: Conversion of an array with ndim > 0 to a scalar is deprecated, and will error in future. Ensure you extract a single element from your array before performing this operation. (Deprecated NumPy 1.25.)

threshold = int(threshold)

Iteration 24: Best Fitness = 380.05984, Threshold = 121.81

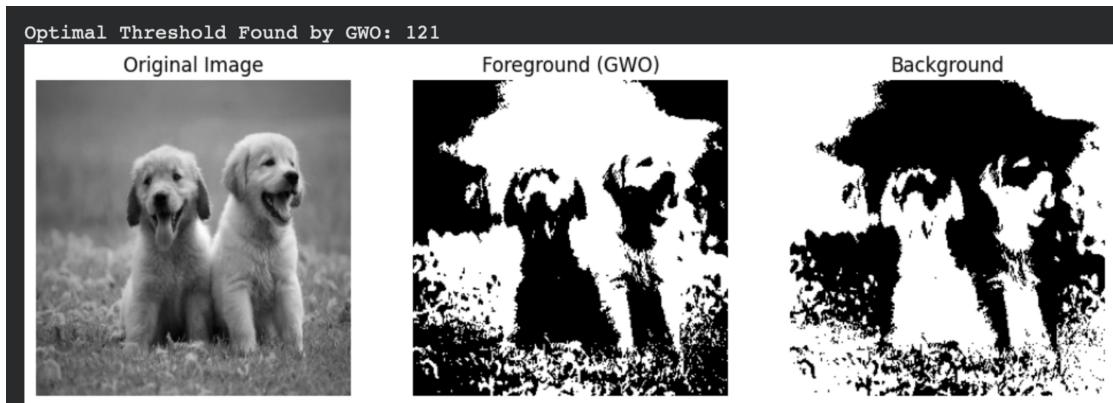
Iteration 25: Best Fitness = 380.05984, Threshold = 121.81

Iteration 26: Best Fitness = 380.05984, Threshold = 121.81

Iteration 27: Best Fitness = 380.05984, Threshold = 121.81

Iteration 28: Best Fitness = 380.05984, Threshold = 121.81

Iteration 29: Best Fitness = 380.05984, Threshold = 121.81



**Program 7:**  
Paralell cellular algorithm

Handwritten notes on Parallel Cellular Algorithm

Parallel cellular algorithm

Begin

Step 1: Define objective function  $f(x)$

Step 2: Initialize parameters  
Set number of cells  $\leftarrow N$   
Set max iterations  $\leftarrow T$   
Define grid structure and neighbourhood patterns

Step 3: Initialize population  
for each cell  $i$  from 1 to  $N$  do  
    Initialize cell state  $x_{it}$  with a random solution  
END FOR

Step 4: Evaluate fitness  
for each cell  $i$  from 1 to  $N$  do  
    fitness  $y_{it} \leftarrow f(x_{it})$   
END for

Iteration  $\leftarrow 0$

for each cell  $i$  from 1 to  $N$  do  
    PARALLEL  
        Identity Neighbors( $i$ )

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```

new_state[i] ← update rule (cell.state[i],
    neighbour set(i))
END for

state (synchronous update)
for each cell i from 1 to n do
    cell.state[i] ← new state[i]
    fitness[i] ← f (cell.state[i])
End for
situation ← situations

END WHILE

output cell.state as Best solution

```

~~END detection~~  
✓ ~~object in SF~~

## Code:

```

import cv2
import numpy as np
import matplotlib.pyplot as plt
from google.colab import files

# Upload
print("Upload an image:")
uploaded = files.upload()
filename = list(uploaded.keys())[0]

# Preprocess
img = cv2.imread(filename, 0)
img = cv2.resize(img, (256, 256))
blur = cv2.GaussianBlur(img, (5, 5), 0)
binary = cv2.threshold(blur, 0, 255, cv2.THRESH_BINARY + cv2.OTSU)[1]
grid = (binary // 255).astype(np.uint8)

```

```

# PCA update
def pca_update(grid):
    kernel = np.array([[1,1,1],[1,0,1],[1,1,1]])
    neighbors = cv2.filter2D(grid, -1, kernel)
    return np.where(neighbors >= 4, 1, 0)

# PCA iterations
for _ in range(10):
    grid = pca_update(grid)

# Detect objects
num_labels, labels, stats, _ = cv2.connectedComponentsWithStats((grid*255).astype("uint8"), 8)

detected = np.zeros_like(grid)
for i in range(1, num_labels):
    if stats[i][4] > 30:
        detected[labels == i] = 255

# Display
plt.figure(figsize=(12,4))
plt.subplot(131); plt.imshow(img,cmap='gray'); plt.title("Original"); plt.axis('off')
plt.subplot(132); plt.imshow(grid,cmap='gray'); plt.title("After PCA Evolution"); plt.axis('off')
plt.subplot(133); plt.imshow(detected,cmap='gray'); plt.title("Detected Objects"); plt.axis('off')
plt.show()

```

Output:

