

# CSL 461 / CSL617

## Digital Image Analysis

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*“One picture is worth more than ten thousand words”*

### Course Info

#### Reference Books:

- Rafael C. Gonzalez, Richard E. Woods, "Digital Image Processing" , 3Ed, Pearson
- Anil K. Jain, "Fundamentals of Digital Image Processing" , Prentice Hall India
- W. Burger, M. J. Burge, "Principles of Digital Image Processing: Core Algorithms", Springer

#### Prerequisites :

- CSL 201 Data Structures

#### Anti-requisites :

- EEL 484

## Evaluation Criteria

### Evaluation Criteria :

- **Exams – ≈65%:**
  - Midterm – ≈20%
  - EndTerm – ≈30%
  - Quizzes – ≈15%
- **HWs/Lab-Assessments/Projects – ≈35%**
- **Attendance (beyond 75%) – ≈1% bonus**
  
- Min 70% in Exams and 80% in Total for “A” grade
- Min 25% in Exams and 30% in Total for passing grade
- N Quizzes ( $N \geq 5$  likely). Best  $N-1$  marks would be chosen.
- Programming Language:
  - Matlab for CBME students
  - OpenCV with C++ for other students
- Academic dishonesty/ Plagiarism of any kind (even identified later after assignment evaluation) will attract strict penalty

## Course Content

Tentatively

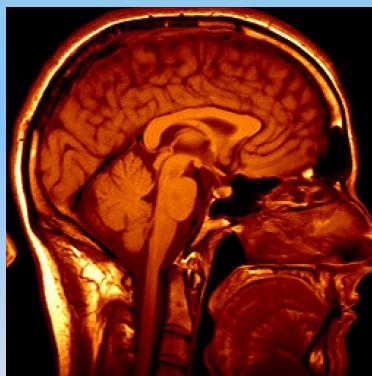
- Digital Image Fundamentals;
- Image Enhancement in Spatial Domain; Gray Level Transformation, Histogram Processing, Spatial Filters;
- Image Transforms; Fourier Transform and their properties, Fast Fourier Transform, Other Transforms; Image Enhancement in Frequency Domain;
- Morphological operators;
- Image Segmentation; edge detection,
- Hough transform, region based segmentation;
- Image Compression;
- Image restoration;
  
- Colour Image Processing, and/or Other recent topics and applications related to Image Processing

## Credits/Acknowledgments

- Rich Course content from Open sources
  - Reference books and corresponding online content
  - Stanford , MIT, NUS and other Universities (incl. IITs) lecture/tutorial notes
  - Brian Mac Namee, School of Computing at the Dublin Institute of Technology
  - Online resources

*Intent : To provide enriching learning experience*

## Medical imaging



3D imaging  
MRI, CT



Image guided surgery  
[Grimson et al., MIT](#)

## Vision-based interaction (and games)




**Digimask:** put your face on a 3D avatar.

Nintendo Wii has camera-based IR tracking built in. See [Lee's work at CMU](#) on clever tricks on using it to create a [multi-touch display!](#)



*"Game turns moviegoers into Human Joysticks"*, CNET  
Camera tracking a crowd, based on [this work](#).

Credits: I. Nwogu, CSE 473/573 Lecture notes, University at Buffalo

## Smart cars



**Mobileye**

- Vision systems currently in high-end BMW, GM, Volvo models
- Back-up camera requirement for all new cars and light trucks
- [Video demo](#)

Credits: I. Nwogu, CSE 473/573 Lecture notes, University at Buffalo

### Earthquake Analysis from Space

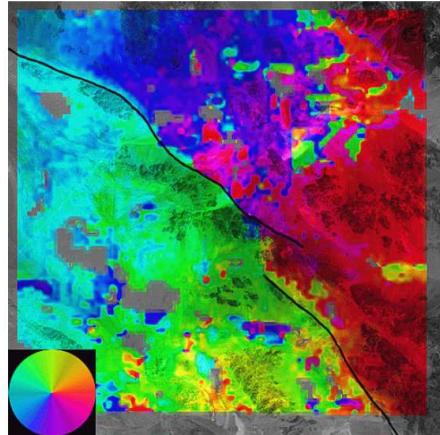
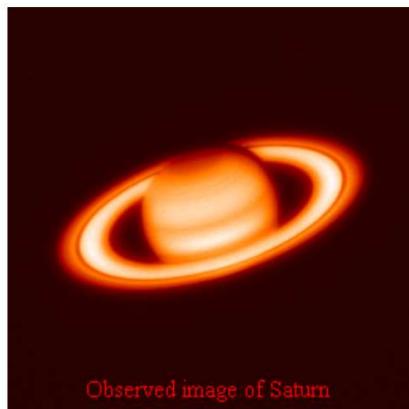


Image shows the ground displacement due to Landers earthquake in CA, 1992

Source: JPL, Pasadena. QUAKEFINDER project

### Restoration of image from Hubble Space Telescope



Source: IVPL Northwestern University, Chicago

## Login without a password...



Fingerprint scanners on many new laptops, other devices



Face recognition systems now beginning to appear more widely  
<http://www.sensiblevision.com/>

Credits: I. Nwogu, CSE 473/573 Lecture notes, University at Buffalo

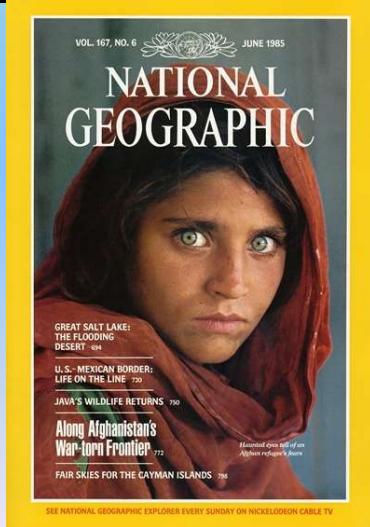
## Object recognition (in mobile phones)



- Microsoft Research
- [Lincoln Point & Find](#), [Nokia](#)
- [SnapTell.com](#) (now amazon)

Credits: I. Nwogu, CSE 473/573 Lecture notes, University at Buffalo

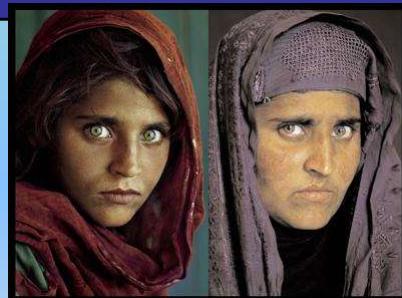
## Face recognition



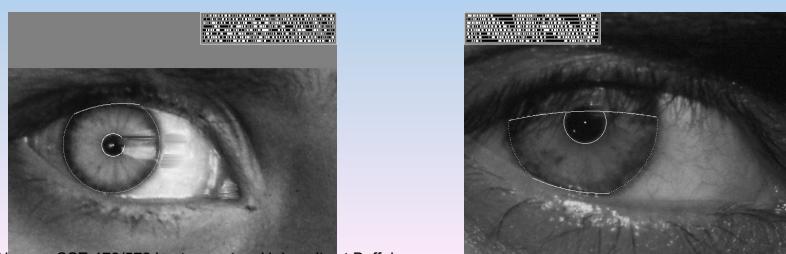
Who is she?

Credits: I. Nwogu, CSE 473/573 Lecture notes, University at Buffalo

## Vision-based biometrics



*"How the Afghan Girl was Identified by Her Iris Patterns"* Read the [story](#)



Credits: I. Nwogu, CSE 473/573 Lecture notes, University at Buffalo

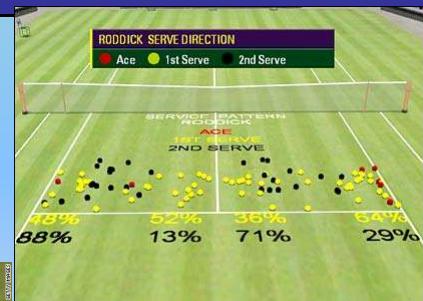
## Sports



*Sportvision first down line*  
Nice [explanation](#) on [www.howstuffworks.com](http://www.howstuffworks.com)

Credits: I. Nwogu, CSE 473/573 Lecture notes, University at Buffalo

## Sports



*Brief explanation on how hawk-eye works can be found [here](#)*

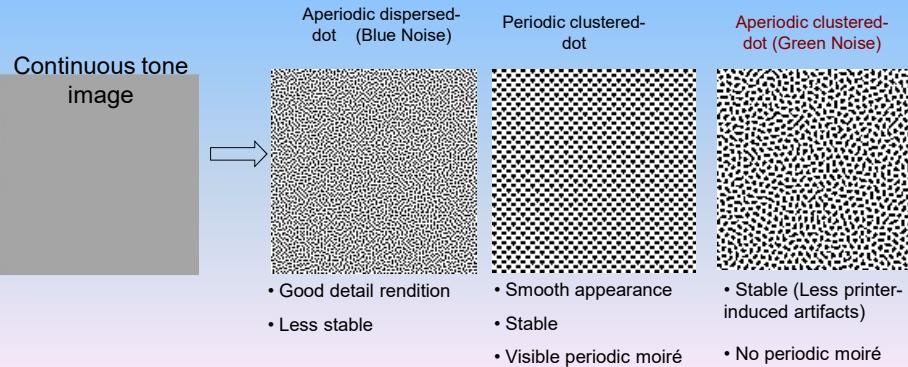
Credits: I. Nwogu, CSE 473/573 Lecture notes, University at Buffalo

## Digital Halftoning

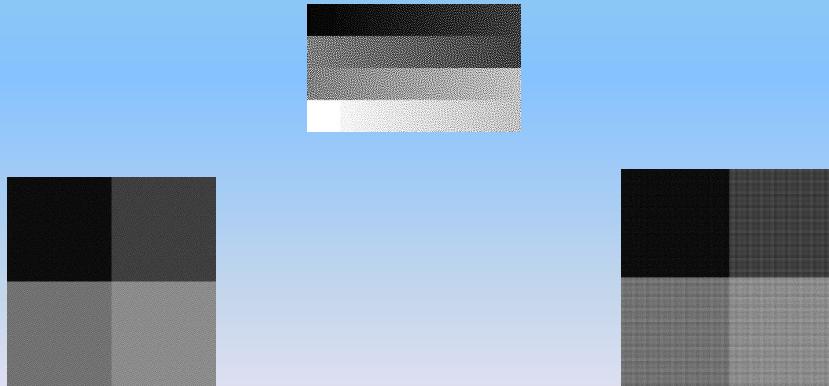
➤ **Digital Halftoning:** The process of rendering a continuous-tone image on devices, such as printers, that can only produce a small set of tone levels.

➤ Halftoning works because *human visual system* (HVS), to a first degree of approximation, acts as a *spatial low-pass filter* that blurs the rendered pixel pattern, so that it is perceived as a continuous-tone image.

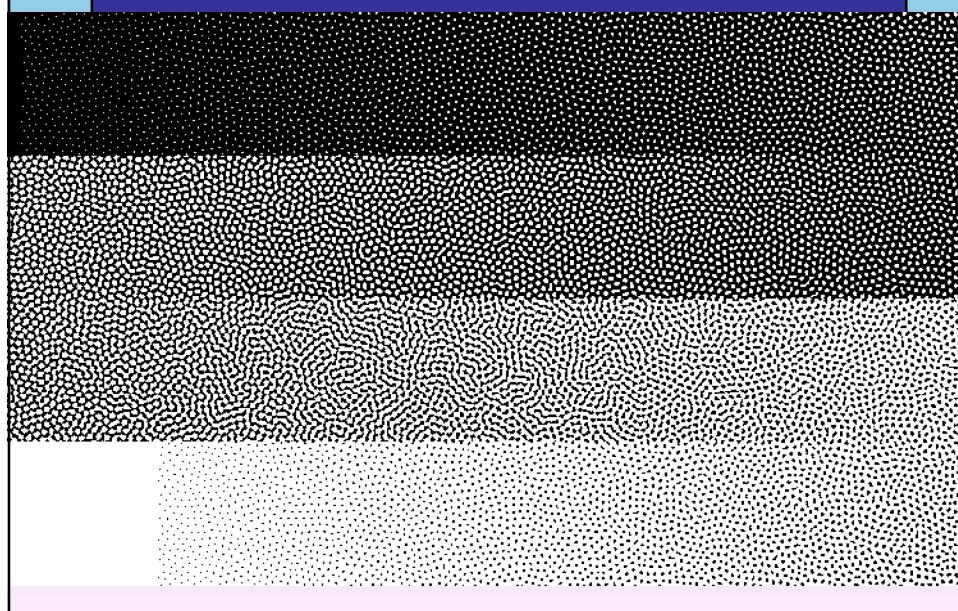
### Three important types of halftones



## Some Halftone Images



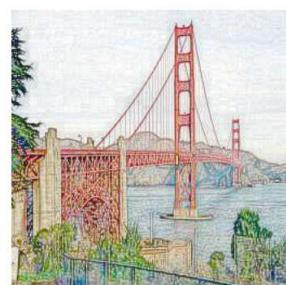
## Ramp – Halftone Image



Special Effects



Photo



Simulated  
color pencils



Simulated  
oil painting

source: Feng Xiao, EE368 class project, spring 2000.



**Face Detection**

source: Henry Chang, Ulises Robles, EE368 class project, spring 2000.

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Bernd Girod: EE368 Digital Image Processing

Introduction no. 11

**Mosaic from 33 source images**

**Mosaic from 21 source images**

source: M. Borgmann, L. Meunier, EE368 class project, spring 2000.

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Bernd Girod: EE368 Digital Image Processing

Introduction no. 15

### Face morphing

Source: Yi-Wen Liu and Yu-Li Hsueh, EE368 class project, spring 2000

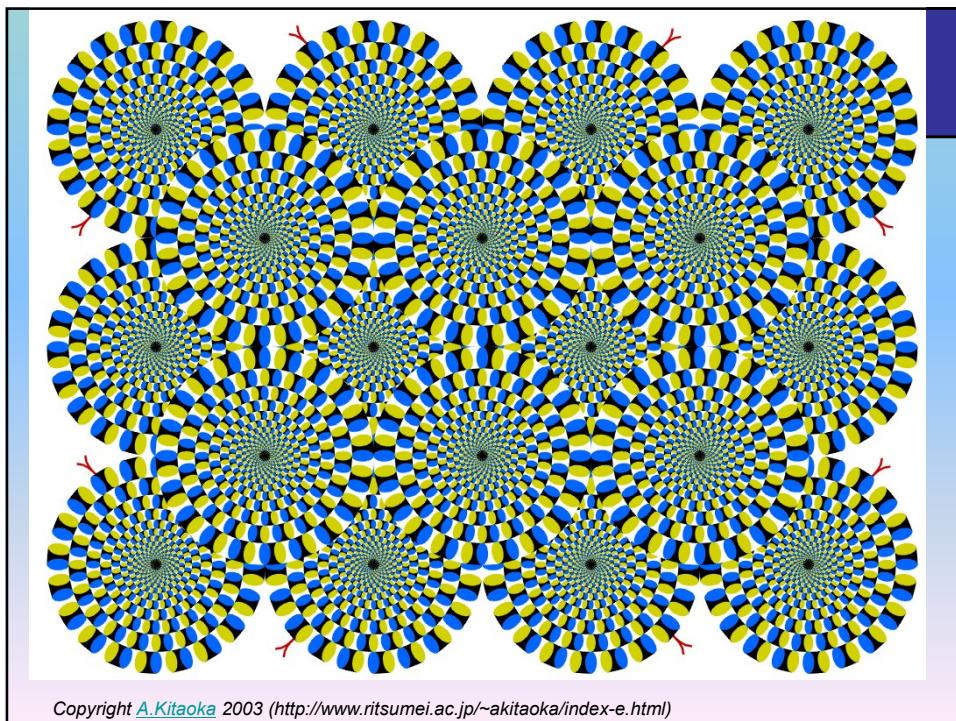
Bernd Girod: EE368 Digital Image Processing      Introduction no. 16

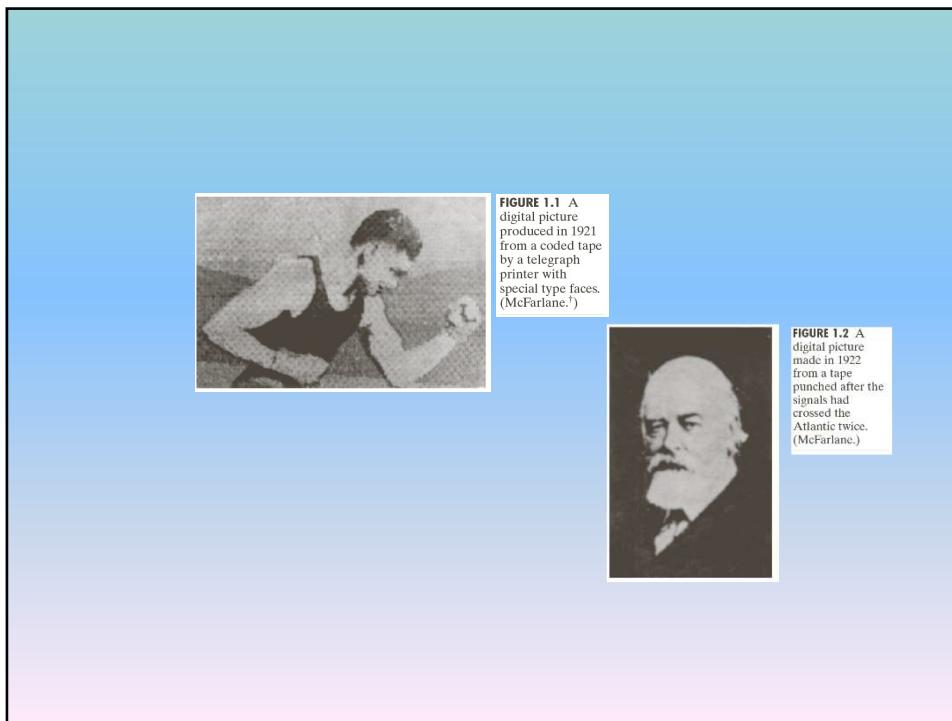
### Handwriting recognition

(a)                                  (b)

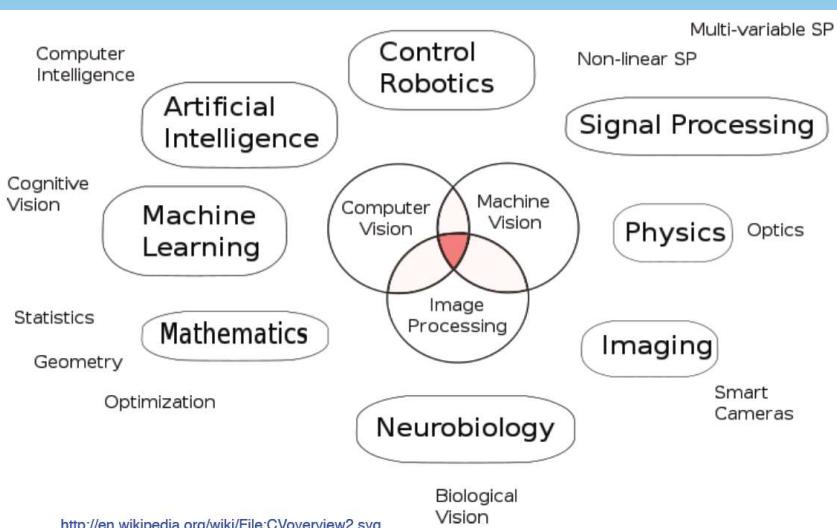
(c)                                  (d)

Bernd Girod: EE368 Digital Image Processing      Introduction no. 17





## Image Processing and Related Fields



## Image

Two dimensional light intensity function  
 $f(x,y)$  where  $x$  and  $y$  are spatial coordinates  
 and  $f$  at  $(x,y)$  is related to brightness or color  
 of the image at that point



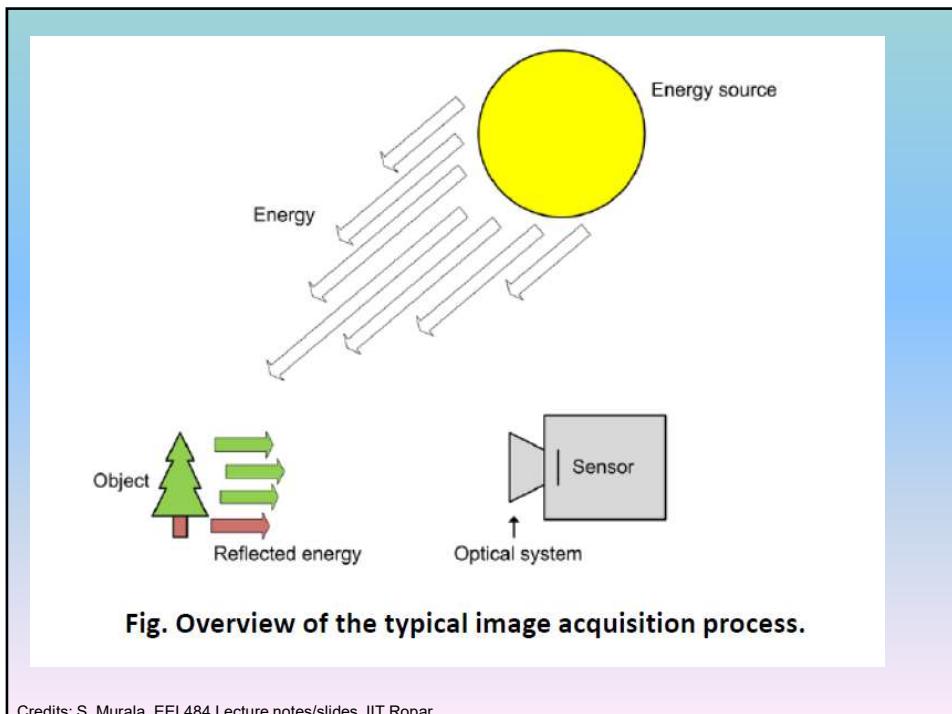
## Energy

- ✓ To capture an image a camera requires some sort of measurable energy.
- ✓ Light or **electromagnetic waves (Photon)**. It is massless entity.
- ✓ **Electromagnetic wave:** electric and magnetic fields vary sinusoidally
  1. A photon can be described by its energy  $E$ , which is measured in [eV]
  2. A photon can be described by its frequency  $f$ , which is measured in Hertz [Hz]. A frequency is the number of cycles or wave-tops in one second.
  3. A photon can be described by its wavelength  $\lambda$ , which is measured in meters [m]. A wavelength is the distance between two wave-tops.

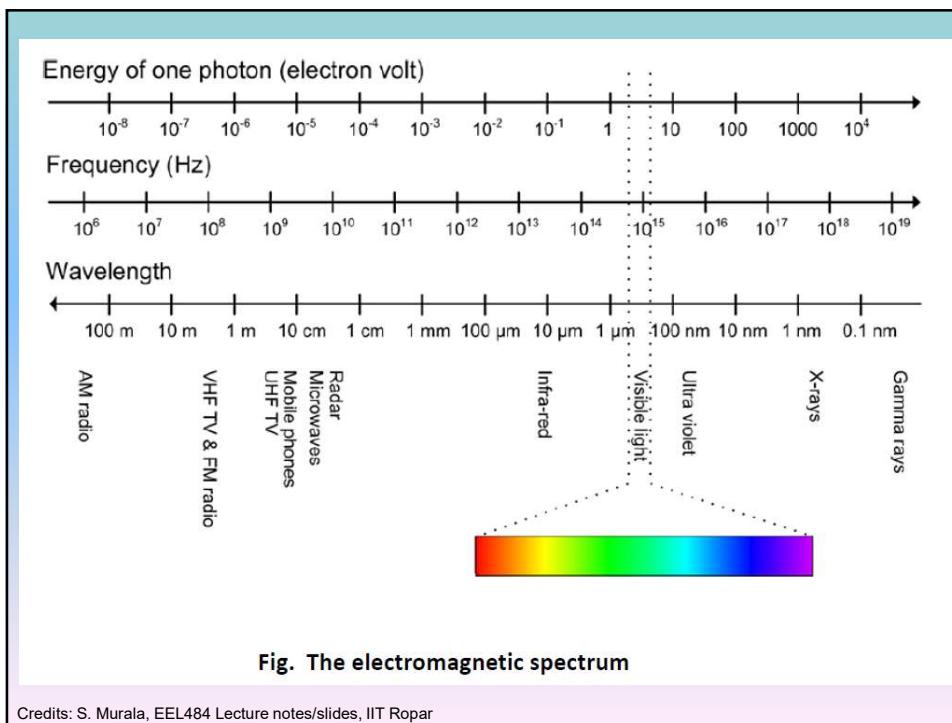
$$\lambda = \frac{c}{f}, \quad E = h \cdot f \quad \Rightarrow \quad E = \frac{h \cdot c}{\lambda}$$

$$c = 2.998 \times 10^8 \text{ m/s}$$

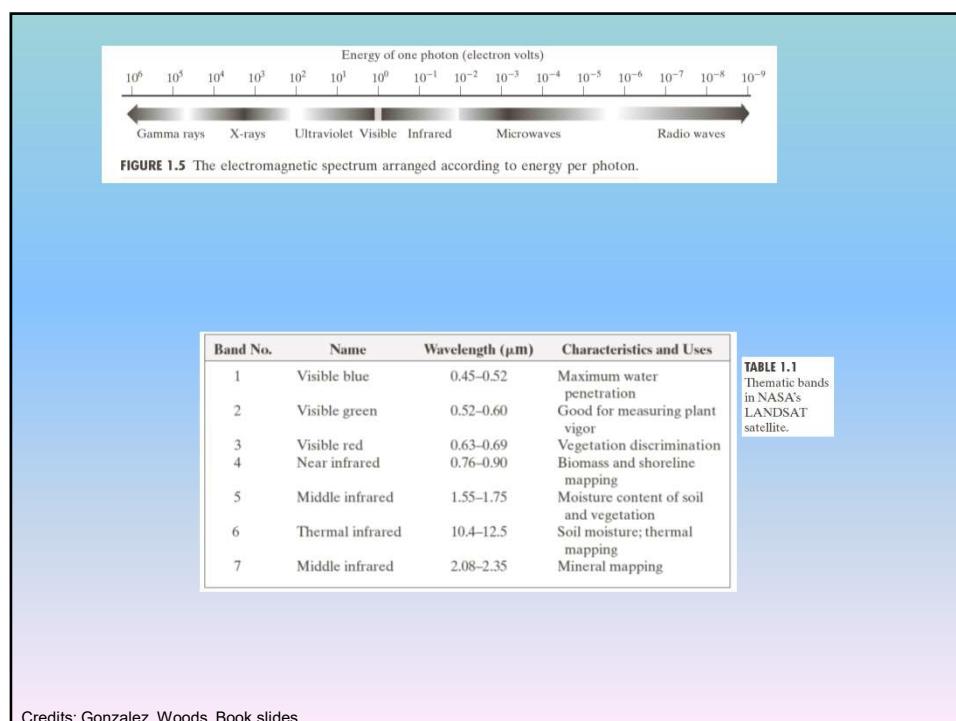
$$h = 6.626176 \times 10^{-34} \text{ joule-seconds}$$



Credits: S. Murala, EEL484 Lecture notes/slides, IIT Ropar



Credits: S. Murala, EEL484 Lecture notes/slides, IIT Ropar



## What is a Digital Image?

Pixel values typically represent gray levels, colours, heights, opacities etc

**Remember** *digitization* implies that a digital image is an *approximation* of a real scene

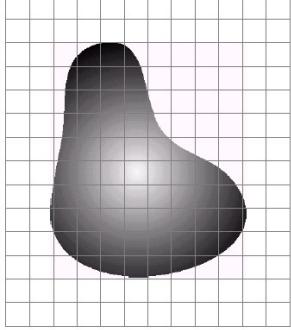
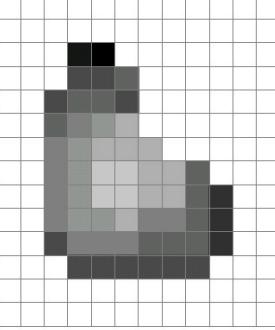
Images taken from Gonzalez & Woods, Digital Image Processing (2002)

*Digital Image Processing, 2nd ed.*

[www.imageprocessingbook.com](http://www.imageprocessingbook.com)

## Image Sampling and Quantization

- **Sampling:** digitizing the 2-dimensional spatial coordinate values
- **Quantization:** digitizing the amplitude values (brightness level)

**a b**

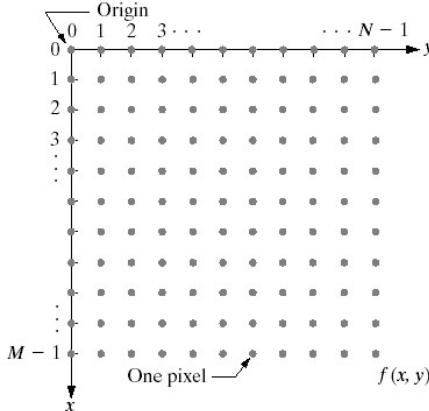
**FIGURE 2.17** (a) Continuous image projected onto a sensor array. (b) Result of image sampling and quantization.

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*Digital Image Processing, 2nd ed.*

[www.imageprocessingbook.com](http://www.imageprocessingbook.com)

## Representing Digital Images



**FIGURE 2.18**  
Coordinate convention used in this book to represent digital images.

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## Spatial Resolution

*The spatial resolution* of an image is determined by how sampling was carried out

Spatial resolution simply refers to the smallest discernable detail in an image

- Vision specialists will often talk about pixel size
- Graphic designers will talk about *dots per inch* (DPI)



Digital Image Processing, 2nd ed. [www.imageprocessingbook.com](http://www.imageprocessingbook.com)

**Spatial and Gray-Level Resolution**

**Spatial Resolution**

Line pairs per unit distance (lpi), dpi, ppi

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**FIGURE 2.19** A  $1024 \times 1024$ , 8-bit image subsampled down to size  $32 \times 32$  pixels. The number of allowable gray levels was kept at 256.

## Spatial Resolution (cont...)



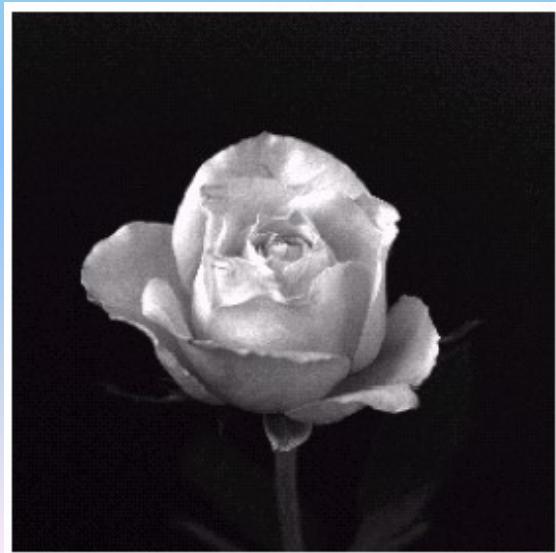
Images taken from Gonzalez & Woods, Digital Image Processing (2002)

## Spatial Resolution (cont...)



Images taken from Gonzalez & Woods, Digital Image Processing (2002)

## Spatial Resolution (cont...)



Images taken from Gonzalez & Woods, Digital Image Processing (2002)

## Spatial Resolution (cont...)



Images taken from Gonzalez & Woods, Digital Image Processing (2002)

## Spatial Resolution (cont...)

Images taken from Gonzalez & Woods, Digital Image Processing (2002)



## Spatial Resolution (cont...)

Images taken from Gonzalez & Woods, Digital Image Processing (2002)



## Intensity Level Resolution

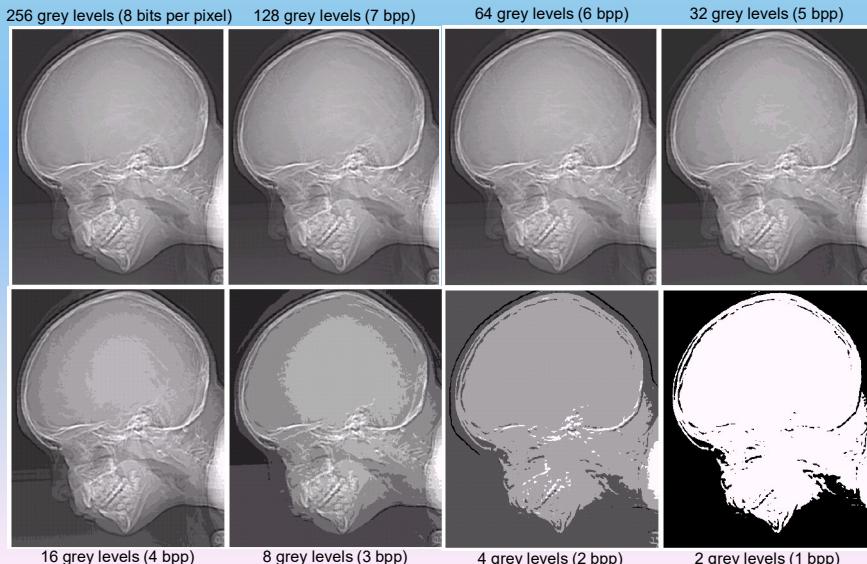
*Intensity level resolution* refers to the number of intensity levels used to represent the image

- The more intensity levels used, the finer the level of detail discernable in an image
- Intensity level resolution is usually given in terms of the number of bits used to store each intensity level

Number of Bits	Number of Intensity Levels	Examples
1	2	0, 1
2	4	00, 01, 10, 11
4	16	0000, 0101, 1111
8	256	00110011, 01010101
16	65,536	1010101010101010

## Intensity Level Resolution (cont...)

Images taken from Gonzalez & Woods, Digital Image Processing (2002)



## Intensity Level Resolution (cont...)

Images taken from Gonzalez & Woods, Digital Image Processing (2002)



## Intensity Level Resolution (cont...)

Images taken from Gonzalez & Woods, Digital Image Processing (2002)



## Intensity Level Resolution (cont...)

Images taken from Gonzalez & Woods, Digital Image Processing (2002)



## Intensity Level Resolution (cont...)

Images taken from Gonzalez & Woods, Digital Image Processing (2002)



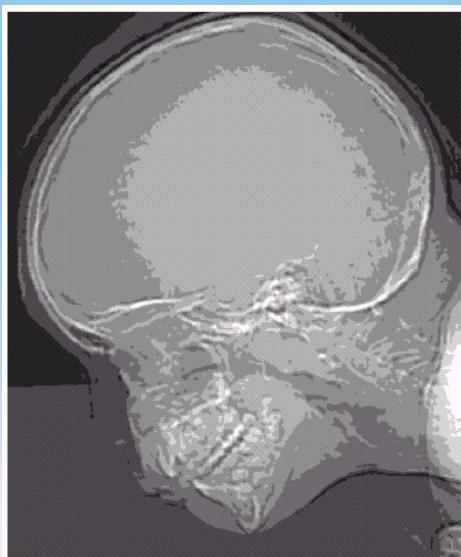
## Intensity Level Resolution (cont...)

Images taken from Gonzalez & Woods, Digital Image Processing (2002)



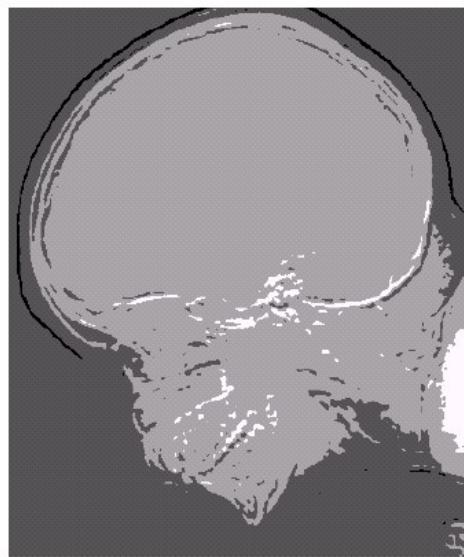
## Intensity Level Resolution (cont...)

Images taken from Gonzalez & Woods, Digital Image Processing (2002)



## Intensity Level Resolution (cont...)

Images taken from Gonzalez & Woods, Digital Image Processing (2002)



## Intensity Level Resolution (cont...)

Images taken from Gonzalez & Woods, Digital Image Processing (2002)



## What is a Digital Image?

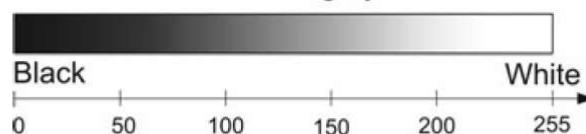
Common image formats include:

- 1 sample per point (B&W or Grayscale)
- 3 samples per point (Red, Green, and Blue)
- 4 samples per point (Red, Green, Blue, and “Alpha”, a.k.a. Opacity)

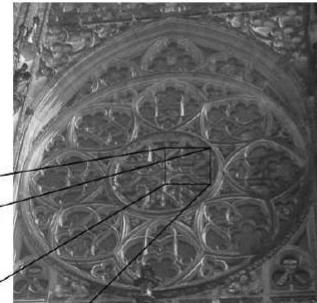


## The Digital Image

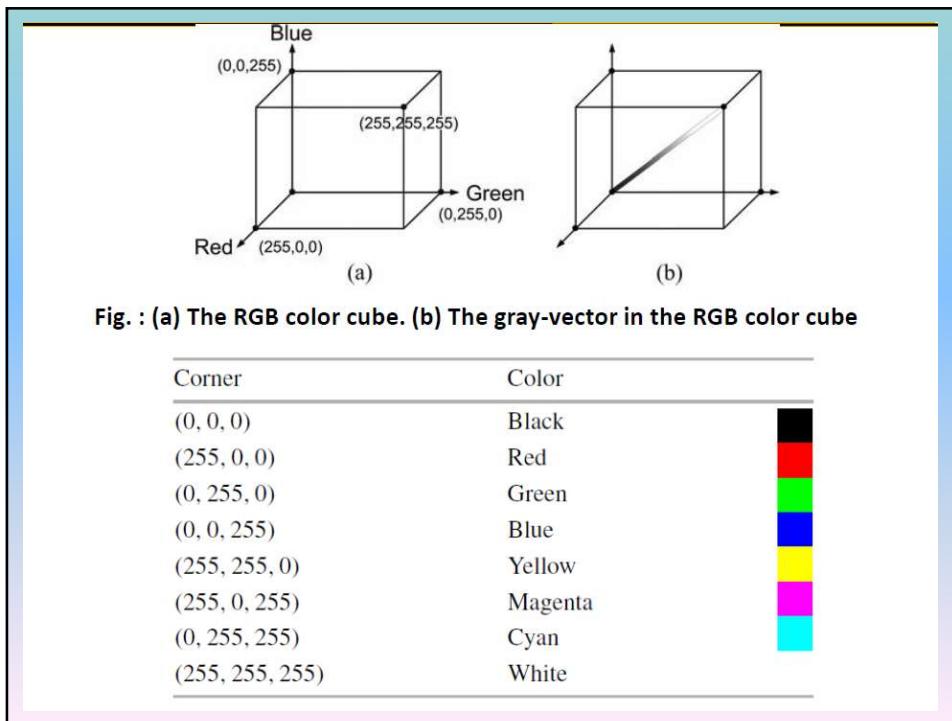
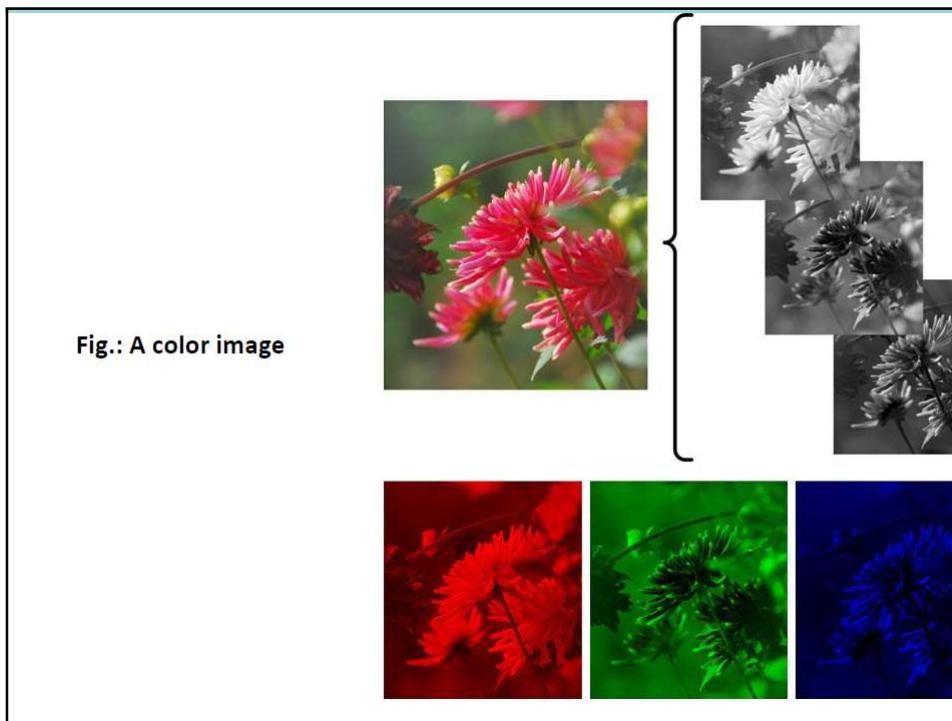
Shades of grey



202	134	112	122	...	112
209	133	112	128	...	102
223	151	94	108	...	105
233	166	109	115	...	128
...	...	...	...	...	...
132	138	147	131	...	95



Credits: S. Murala, EEL484 Lecture notes/slides, IIT Ropar



## RGB to GRAY

$$I = W_R \cdot R + W_G \cdot G + W_B \cdot B$$

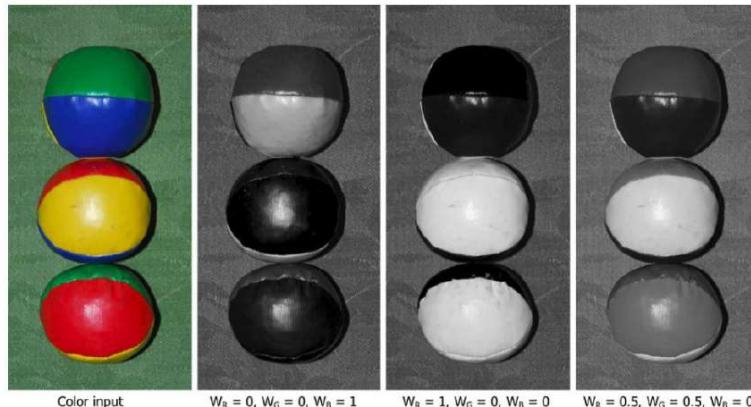
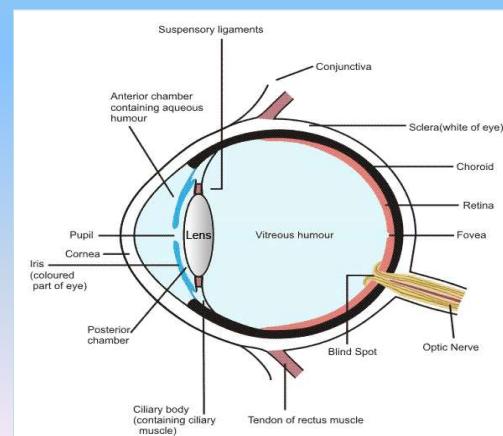
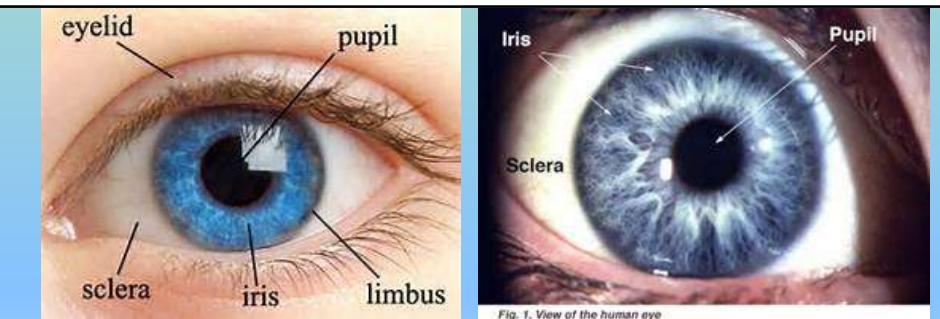


Fig.: A color image and how it can be mapped to different gray-scale images depending on the weights

## How do humans perceive images ? Human Visual System

- The exact process by which humans interpret visual scene content is still not fully understood.
- The human visual system, though powerful enough, still has certain physical limitations
- Consider a brief overview of the anatomical structure of the human eye





Credit: fstoppers.com

Credit: webvision.med.utah.edu

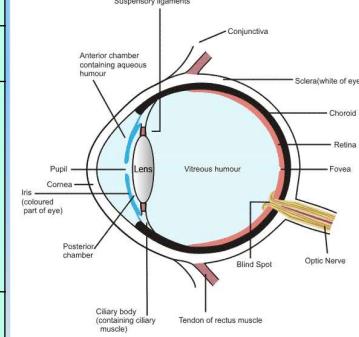
Behind the cornea is the iris, the colored part of the eye. The iris acts as a diaphragm, like a shutter on a camera, regulating the amount of light that enters through the pupil. The pupil appears as a black hole at the center of the iris. It is the opening through which light enters the eye. Some iris muscles contract to enlarge the pupil when more light is needed; others reduce it when there is too much light, to protect the inside of the eye. The pupil dilates and constricts in response to changes in lighting but excitement, attractive sights and some drugs also have this effect.

**The iris contracts and expands, adjusting the size of the pupil and amount of light that enters the eye.**

The amount of pigment in the iris determines the color of the eye. Blue eyes have the least amount of pigment, while brown eyes have the most. The random patterns on the iris are unique to each individual. Each person has a distinct pattern of filaments, pits and striations. Infants' eyes often change color as they become toddlers but from this age forward, the iris color and pattern is stable throughout life.

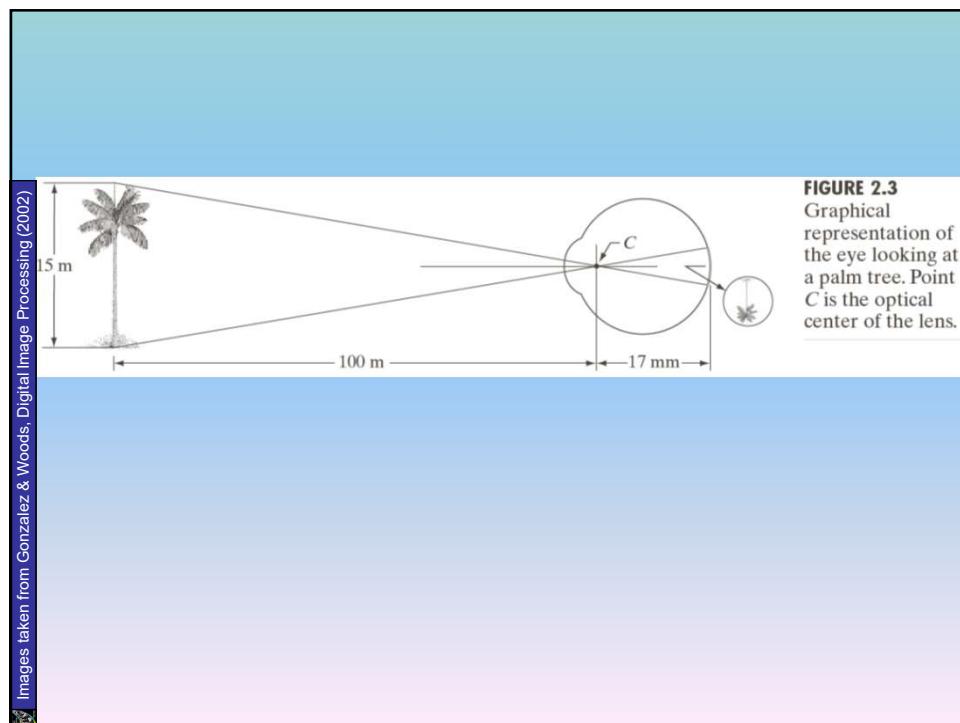
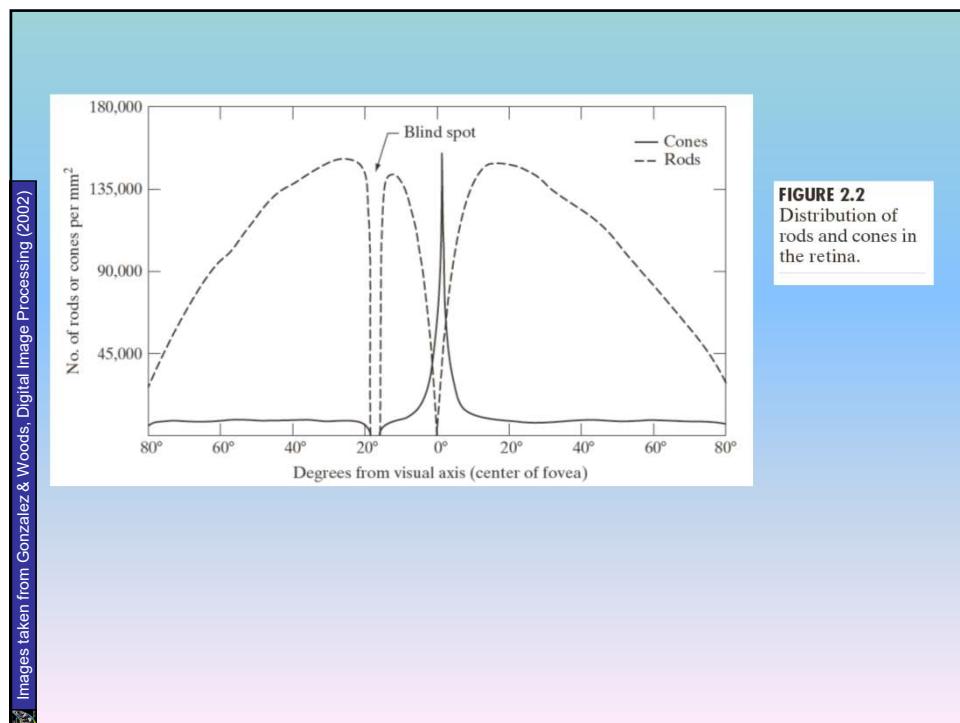
Credits: [https://www.visionweb.com/content/consumers/dev\\_consumerarticles.jsp?RID=30](https://www.visionweb.com/content/consumers/dev_consumerarticles.jsp?RID=30)

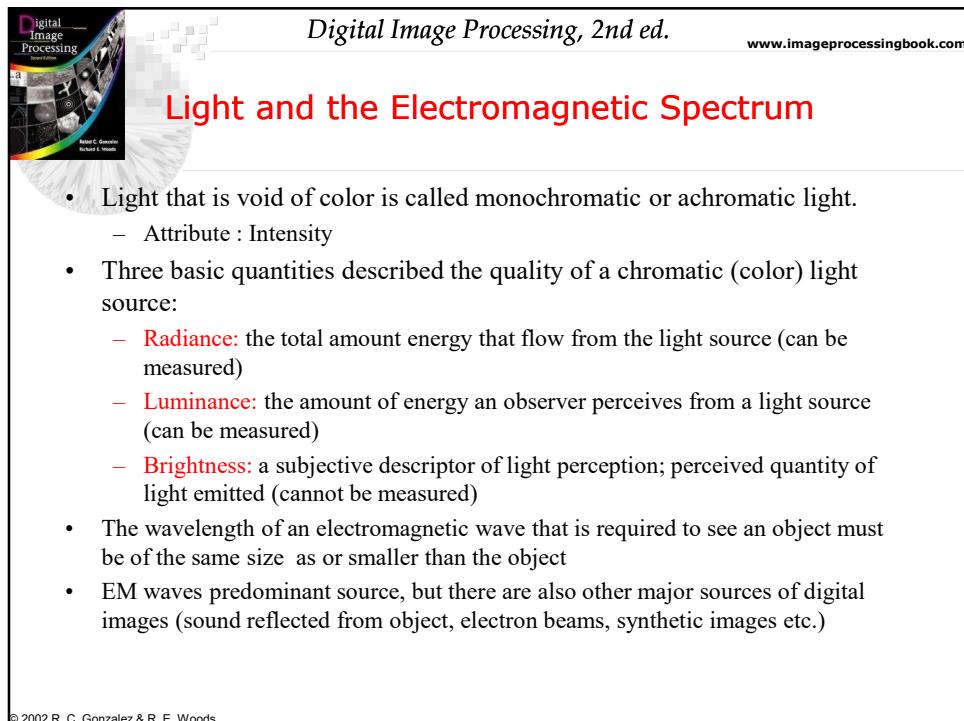
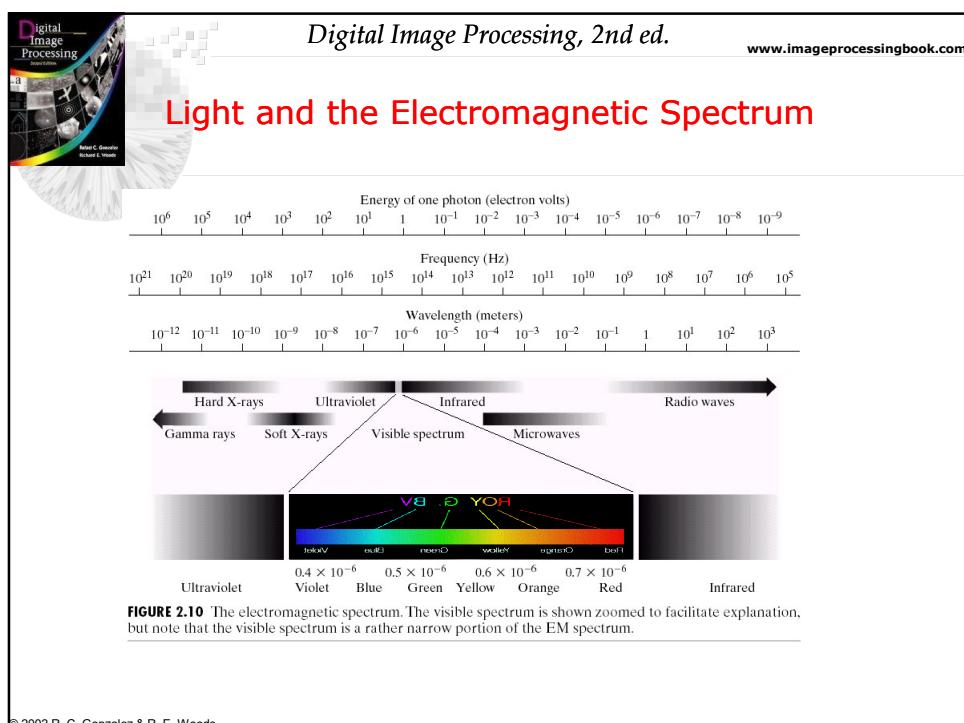
The eye ball	The eye ball is approximately spherical. The vertical measure of an eye ball is approximately 24 mm and is slightly less than the horizontal width. The eye offers a field of view covering 160°(width) × 135° height area. The anterior of the eye has the outer coating cornea while the posterior has the outer layer of sclera.	
Cornea	The cornea is a transparent, curved, refractive window through which the light enters the eye. The corneal segment (typically 8 mm in radius) is linked to the larger unit, the sclera, which extends and covers the posterior portion of the optic globe. The cornea and sclera are connected by a ring called the limbus.	
Iris	The light entering the cornea is blocked by the visible colored and opaque surface of the iris. The back of the iris is coated with a black pigment.	
Pupil	The pupil is the opening at the center of the iris. The pupil controls the amount of light entering the eye ball. Its diameter varies from 1 to 8 mm in response to illumination changes. In low light conditions it dilates to increase the amount of light reaching the retina. Behind the pupil is the lens of the eye.	
Lens	The lens is suspended by the ciliary body by the suspensory ligament (Zonule of Zinn), made up of fine transparent fibers. The lens is transparent (has 70% water) and absorbs approximately 8% of the visible light spectrum. The protein in the lens absorbs the harmful infrared and ultraviolet light and prevents damage to the eye.	

Choroid	Beneath the sclera is a membrane called choroid. It contains blood vessels to nourish the cells in the eye. Like the iris, it is pigmented to prevent light from entering the eye from any other direction other than the pupil.	 <p>The diagram illustrates the cross-section of the human eye. Key labeled parts include: Suspensory ligaments, Conjunctiva, Sclera (white of eye), Choroid, Retina, Fovea, Vitreous humour, Blind Spot, Optic Nerve, Tendon of rectus muscle, Ciliary body (containing ciliary muscle), Posterior chamber, Iris (coloured part of eye), Pupil, Cornea, Lens, Anterior chamber containing aqueous humour, and Ciliary body (containing ciliary muscle).</p>
Retina	Beneath the choroid lies the retina, the innermost membrane of the eye where the light entering the eye is sensed by the receptor cells. The retina has 2 types of photoreceptor cells – rods and cones. These receptor cells respond to light in the 330 to 730 nm wavelength range.	
Fovea	The central portion of the retina at the posterior part is the fovea. It is about 1.5 mm in diameter.	
Rods	There about 100 million rods in the eye. The rods help in the dim-light (scotopic) vision. Their spatial distribution is radially symmetric about the fovea, but varies across the retina. They are distributed over a larger area in the retina. The rods are extremely sensitive and can respond even to a single photon. However they are not involved in color vision. They cannot resolve fine spatial detail despite high number because many rods are connected to a single nerve.	
Cones	There are about 6 million cones in the eye. The cones help in the bright-light (photopic) vision. These are highly sensitive to color. They are located primarily in the fovea where the image is focused by the lens. Each cone cell is connected to its separate nerve ending. Hence they have the ability to resolve fine details.	
	Though the photo-receptors are distributed in radially symmetric manner about the fovea, there is a region near the fovea where	

## Color Images

Photoreceptor cell	Wavelength in nanometers (nm)	Peak response in nanometer (nm)	Interpretation by the human brain
Cones (type L)	[400–680]	564	Red
Cones (type M)	[400–650]	534	Green
Cones (type S)	[370–530]	420	Blue
Rods	[400–600]	498	Shade of gray





*Digital Image Processing, 2nd ed.*

[www.imageprocessingbook.com](http://www.imageprocessingbook.com)

## Image Sensing and Acquisition

- Nowadays most visible and near IR electromagnetic imaging is done with 2-dimensional charged-coupled devices (CCDs).

The diagram shows a 3D perspective of the imaging process. At the top left is a sphere labeled "Illumination (energy) source". Light rays from this source illuminate a "Scene element" (a dark, irregular shape). These rays pass through an "Imaging system" (represented by a small rectangular block) and are projected onto a "Internal image plane" (a grid). To the right of the grid is a square labeled "Output (digitized) image", which contains a smaller version of the scene element. Below the diagram, there is a legend with five boxes labeled a, b, c, d, and e, corresponding to the labels in the text above.

**FIGURE 2.15** An example of the digital image acquisition process. (a) Energy ("illumination") source. (b) An element of a scene. (c) Imaging system. (d) Projection of the scene onto the image plane. (e) Digitized image.  
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*Digital Image Processing, 2nd ed.*

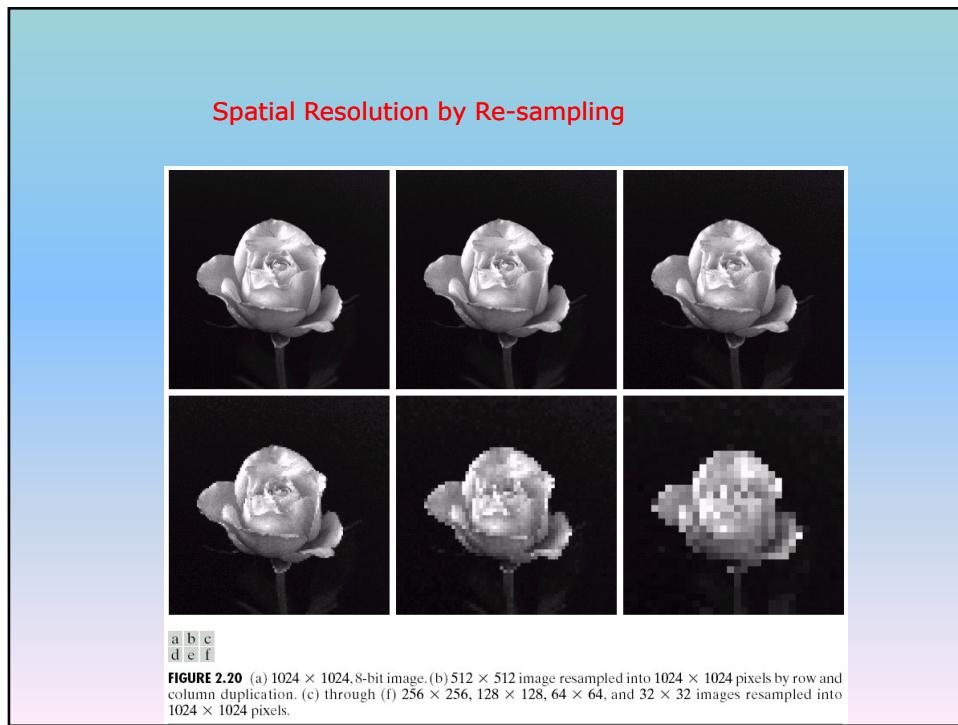
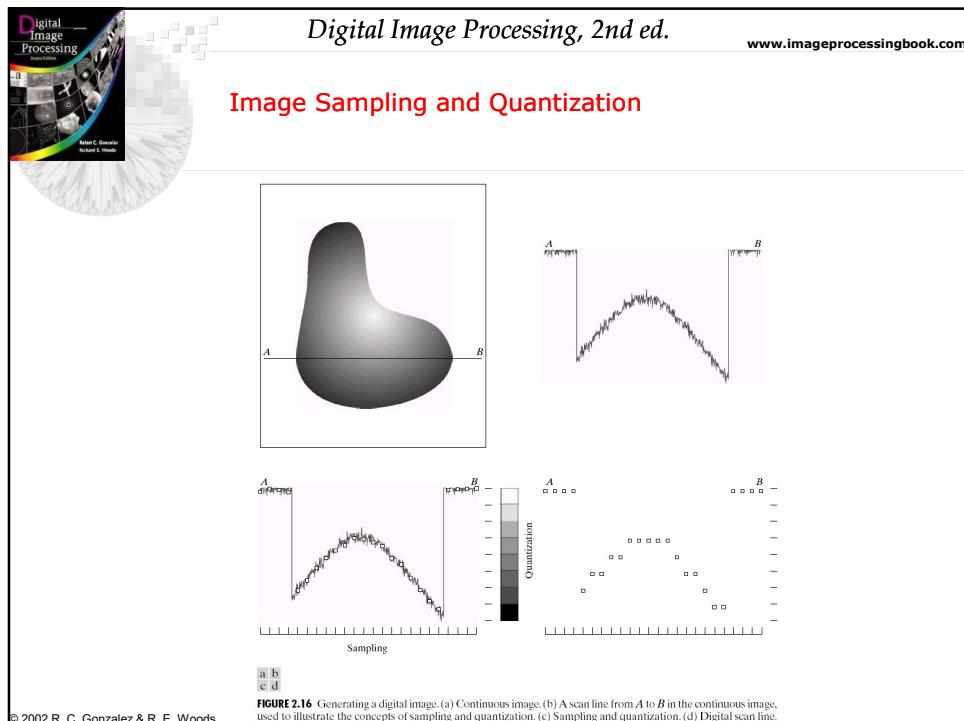
[www.imageprocessingbook.com](http://www.imageprocessingbook.com)

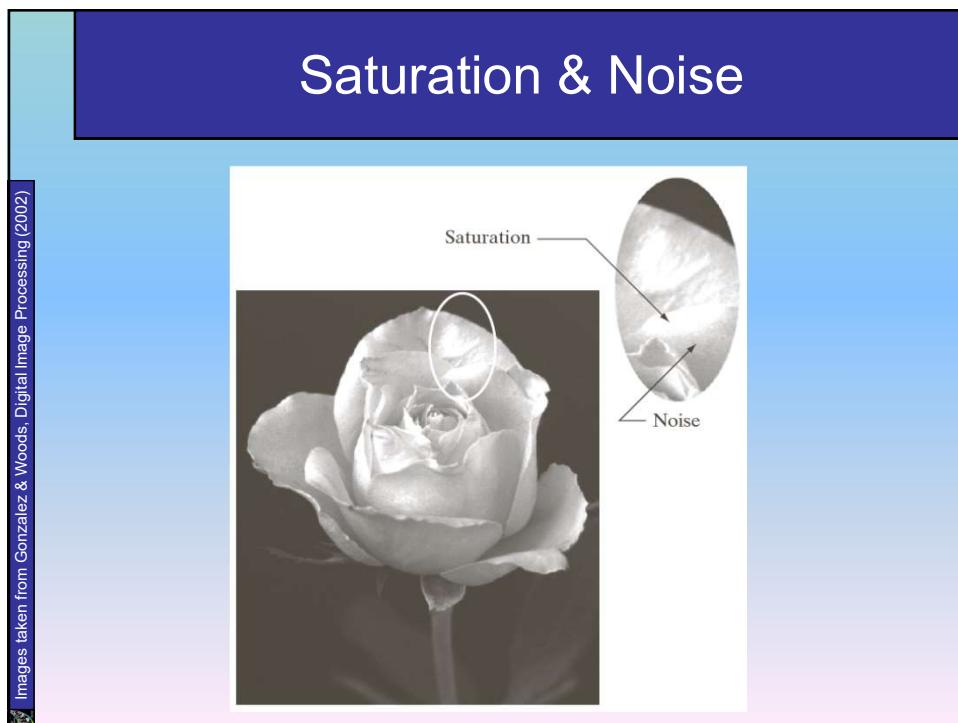
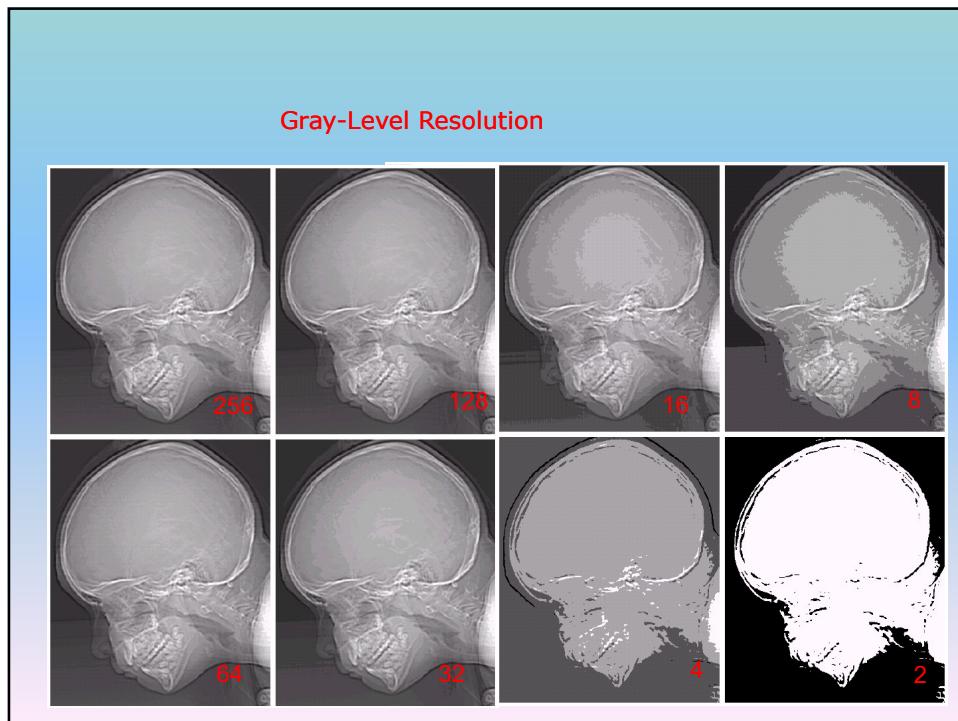
## A Simple Image Formation Model

- Binary images:** images having only two possible brightness levels (black and white)
- Gray scale images :** “black and white” images
- Color images:** can be described mathematically as three gray scale images
- Let  $f(x,y)$  be an image function, then  

$$f(x,y) = i(x,y) r(x,y),$$
 where  $i(x,y)$ : the illumination function  
 $r(x,y)$ : the reflection function  
 Note:  $0 < i(x,y) < \infty$  and  $0 < r(x,y) < 1$ .
- For digital images the minimum gray level is usually 0, but the maximum depends on number of quantization levels used to digitize an image. The most common is 256 levels, so that the maximum level is 255.

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## Resolution: How Much Is Enough?

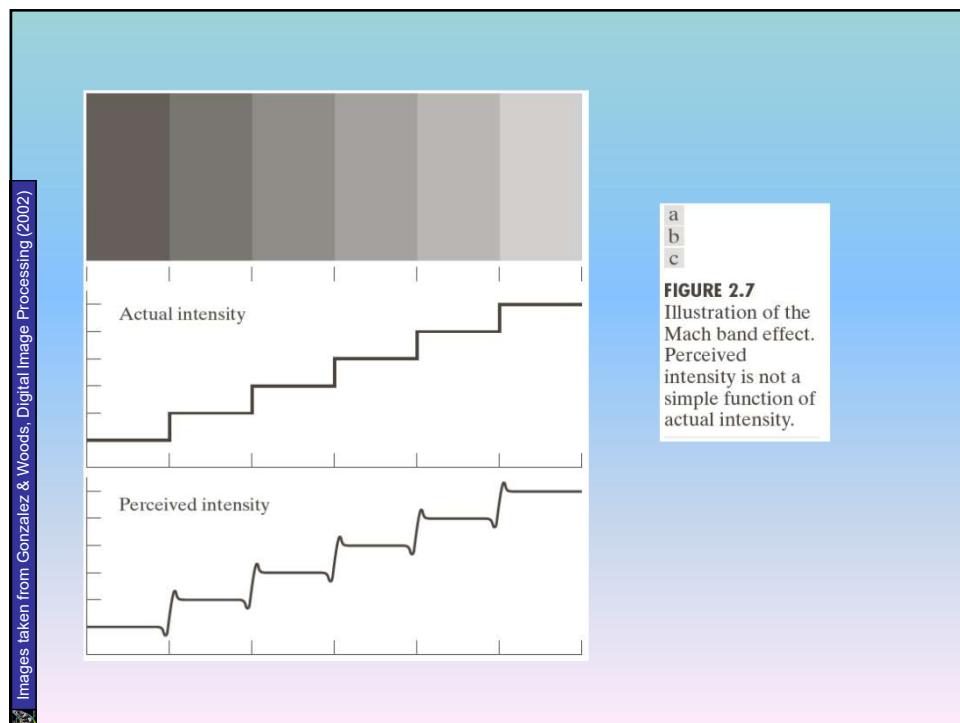
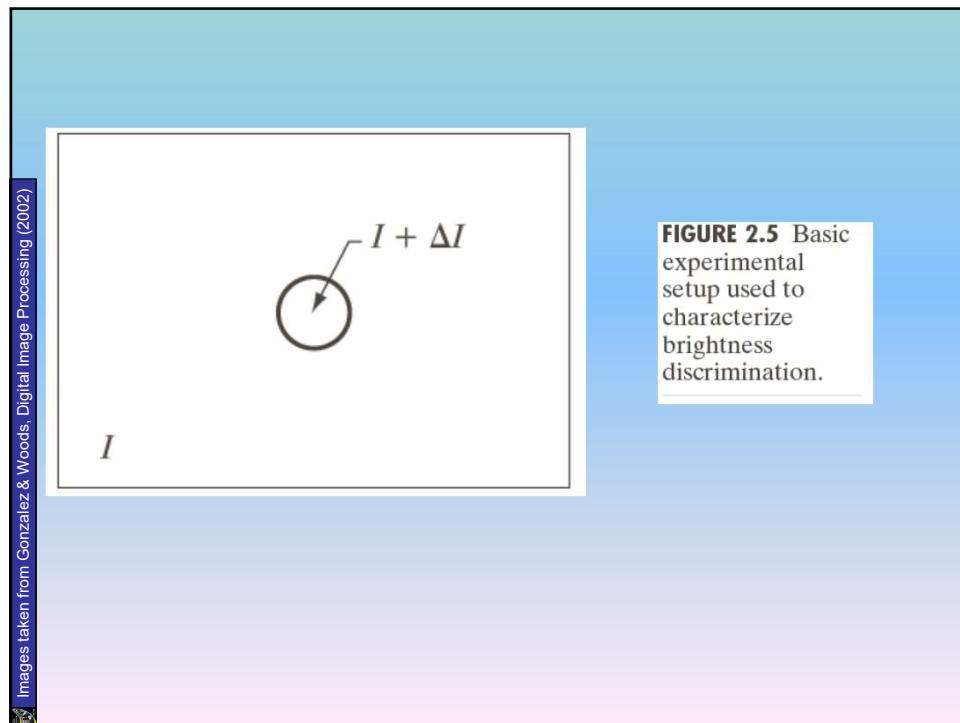
The big question with resolution is always *how much is enough?*

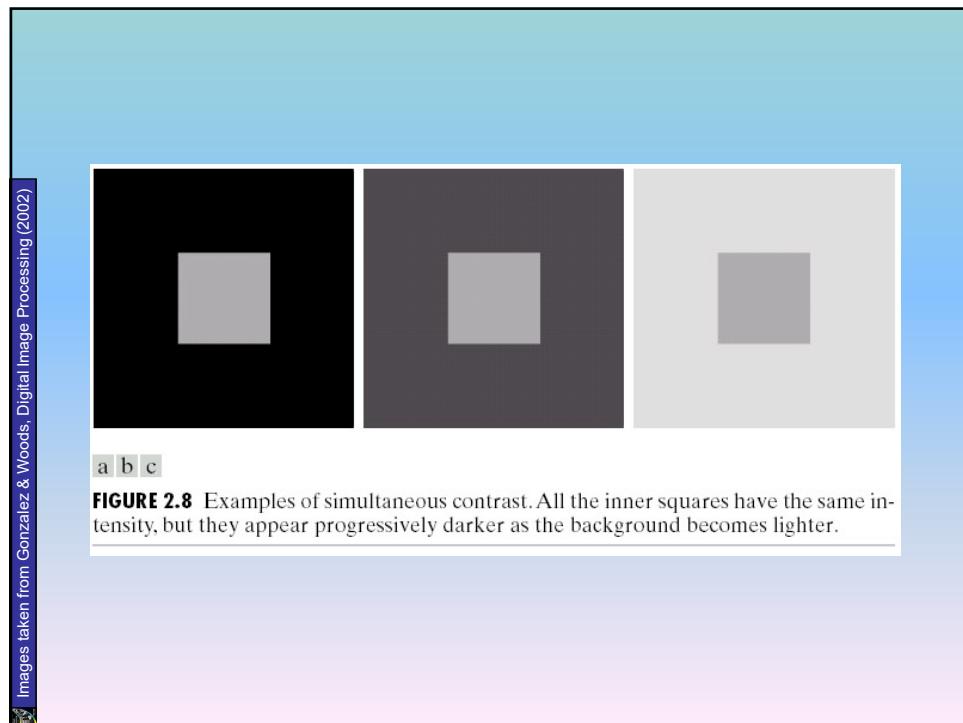
- This all depends on what is in the image and what you would like to do with it
- Key questions include
  - Does the image look aesthetically pleasing?
  - Can you see what you need to see within the image?

## Resolution: How Much Is Enough? (cont...)

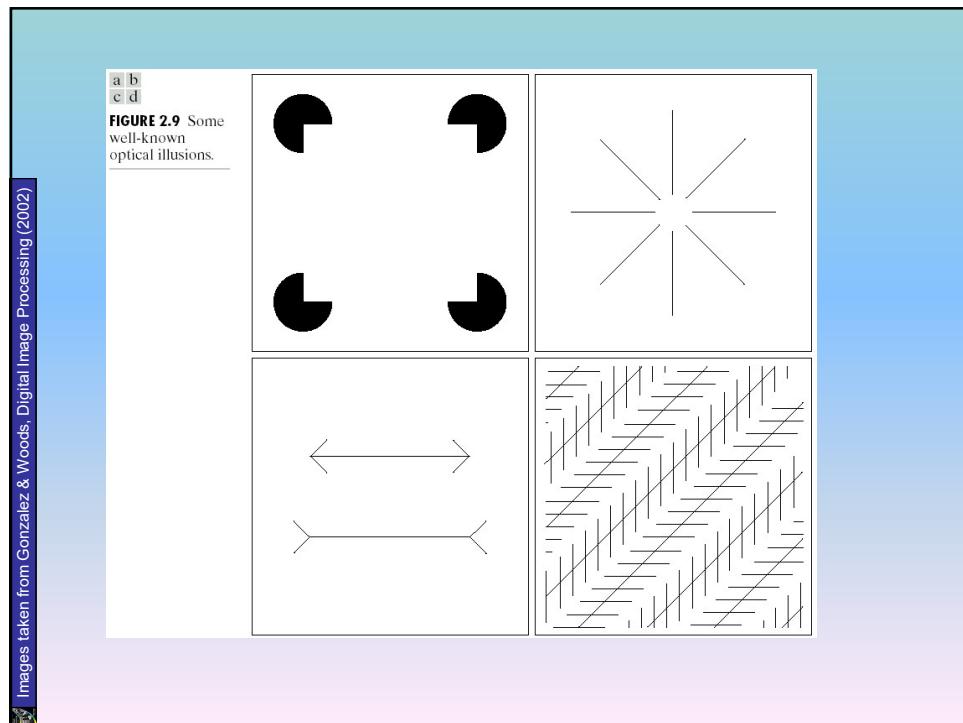


The picture on the right is fine for counting the number of cars, but not for reading the number plate





**FIGURE 2.8** Examples of simultaneous contrast. All the inner squares have the same intensity, but they appear progressively darker as the background becomes lighter.



**FIGURE 2.9** Some well-known optical illusions.

## What is Digital Image Processing?

Digital image processing focuses on two major tasks

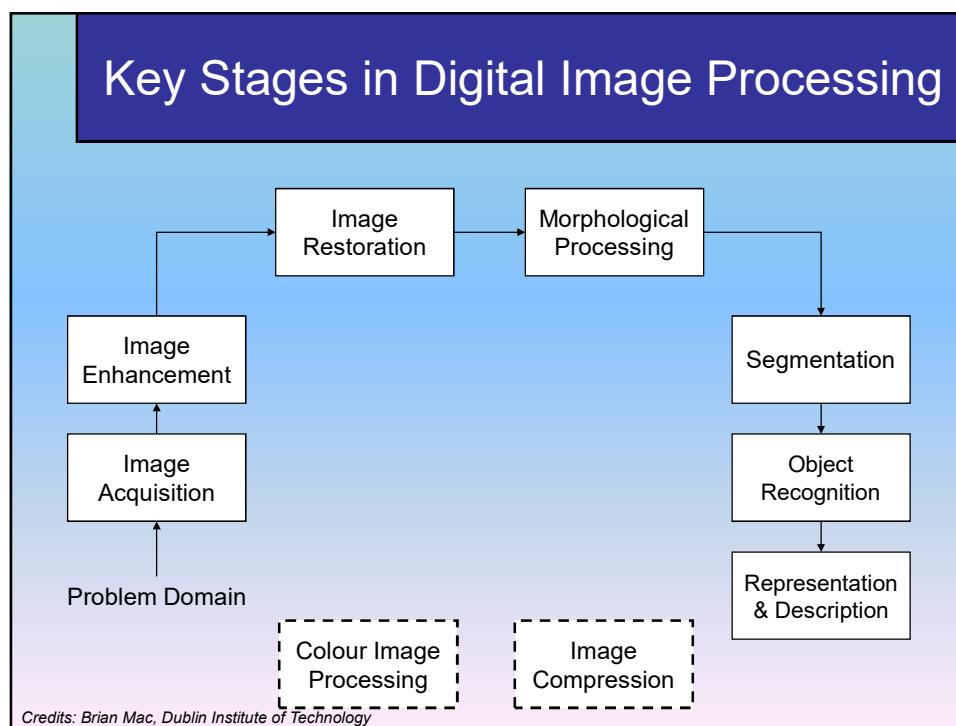
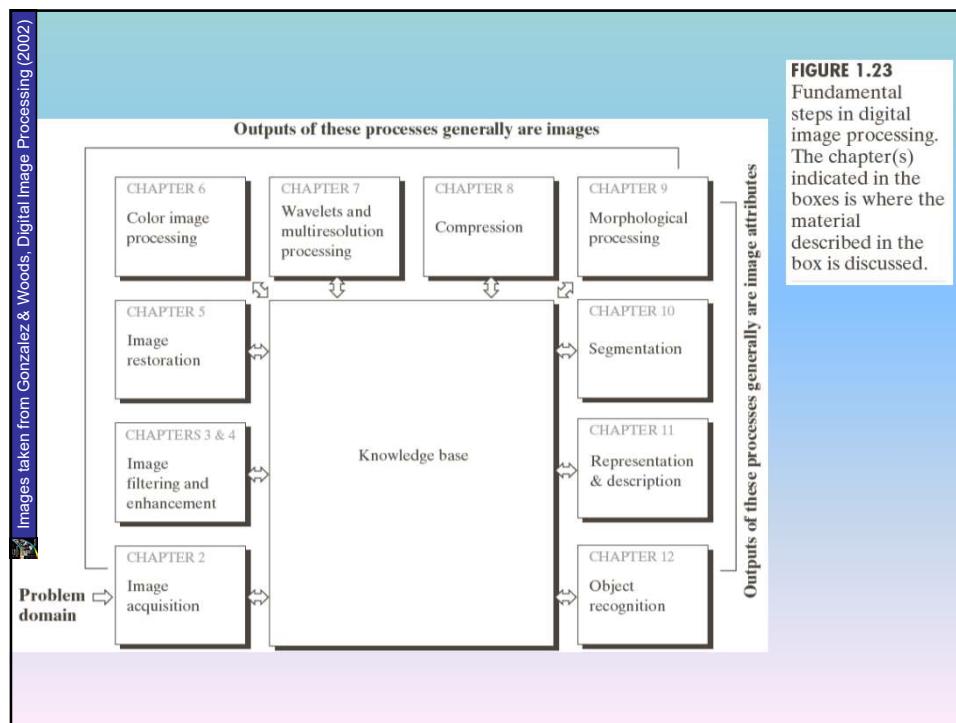
- Improvement of pictorial information for human interpretation
- Processing of image data for storage, transmission and representation for autonomous machine perception

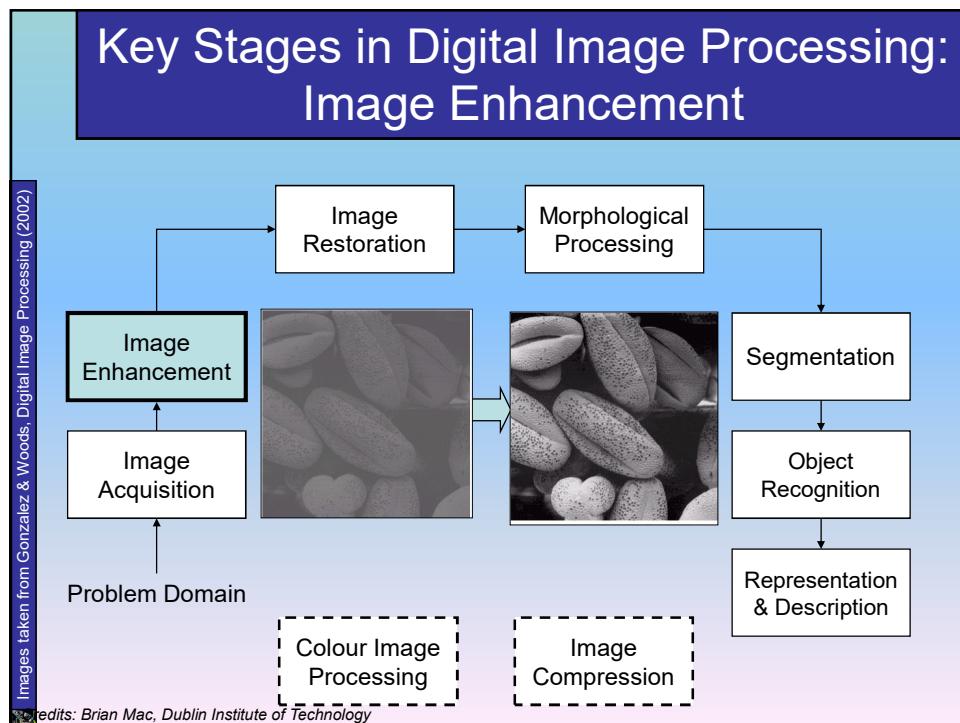
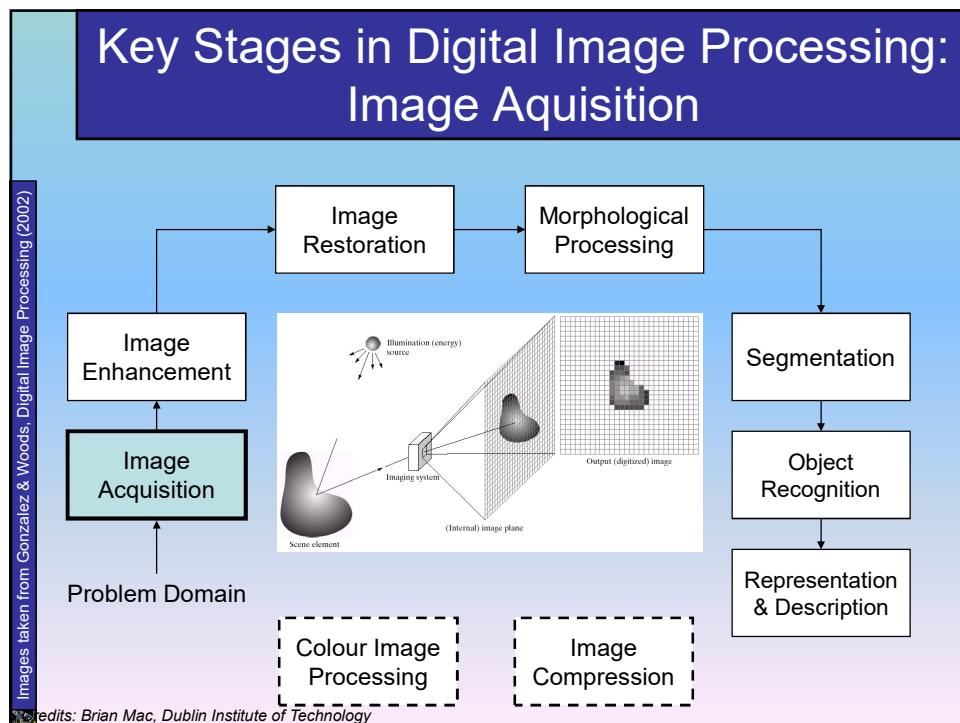
Some argument about where image processing ends and fields such as computer vision start

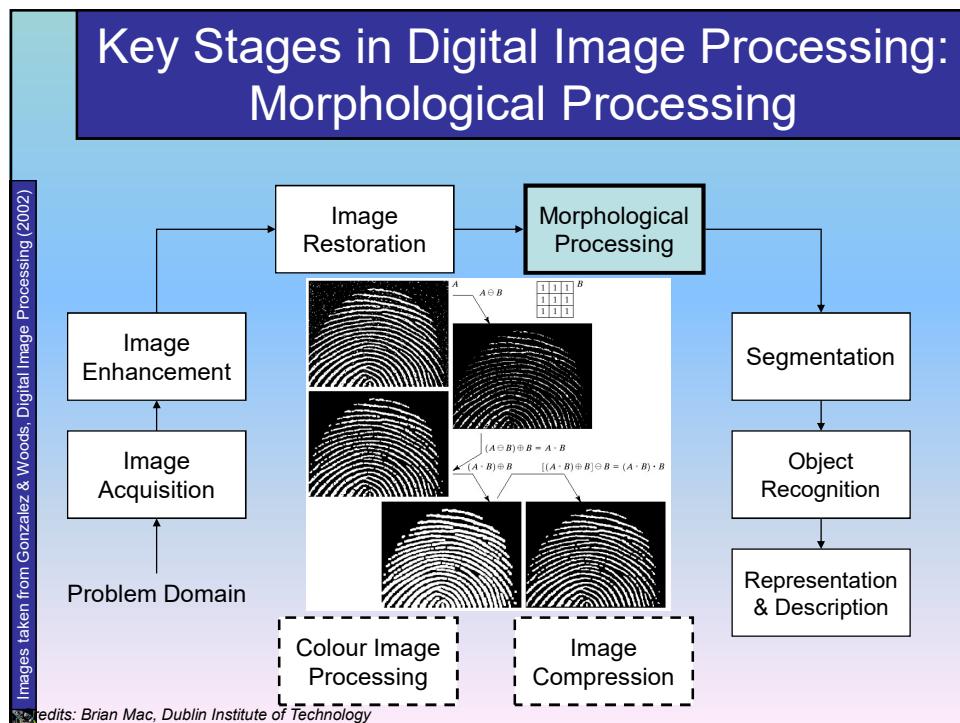
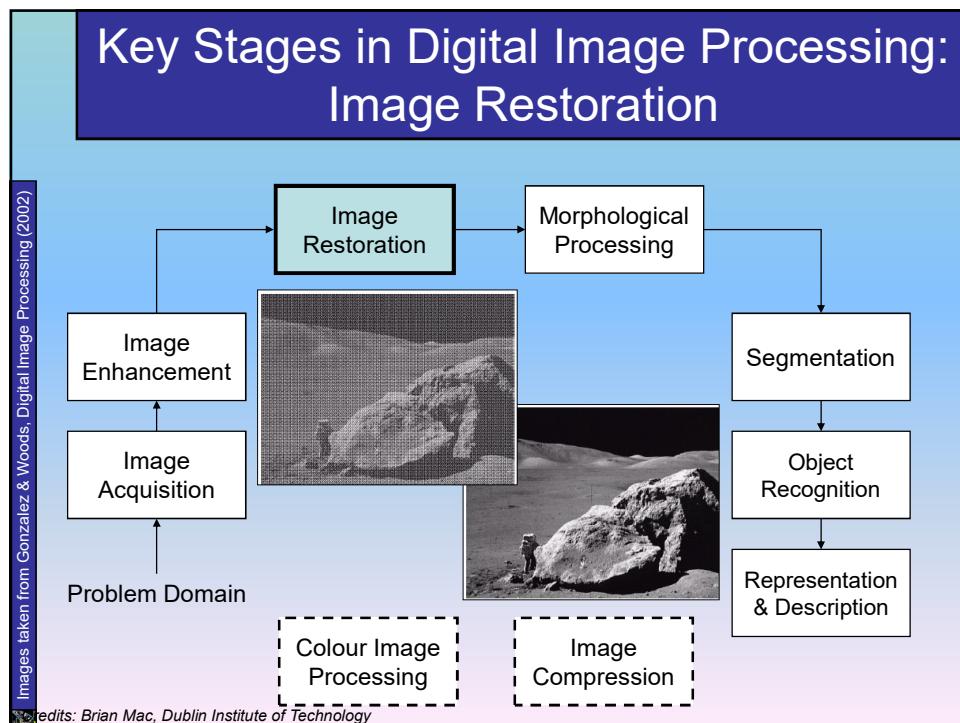
## DIP and Computer Vision

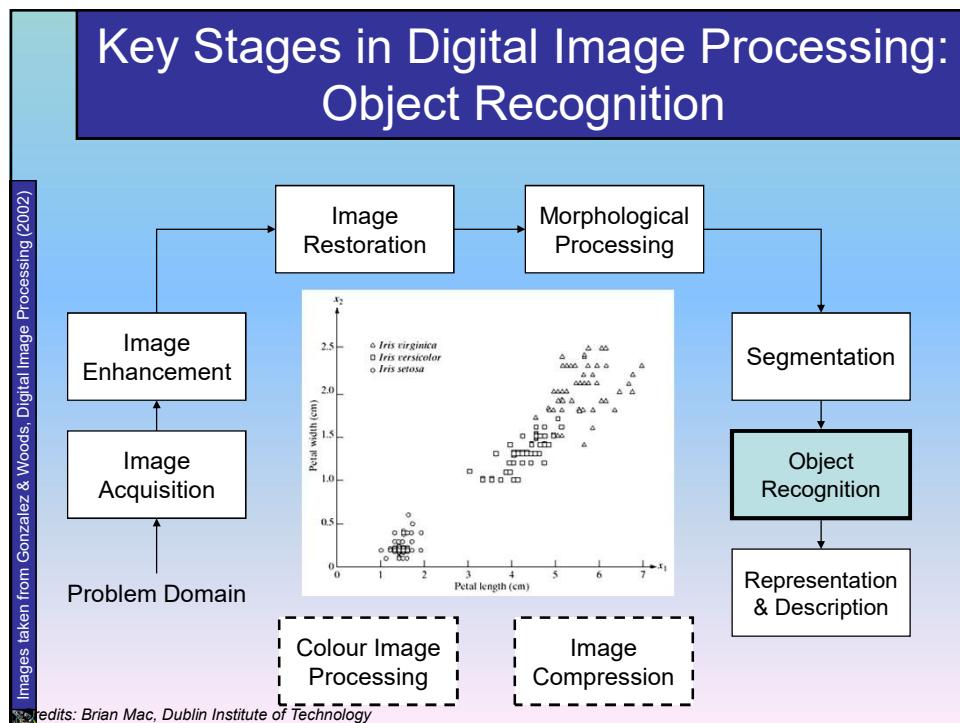
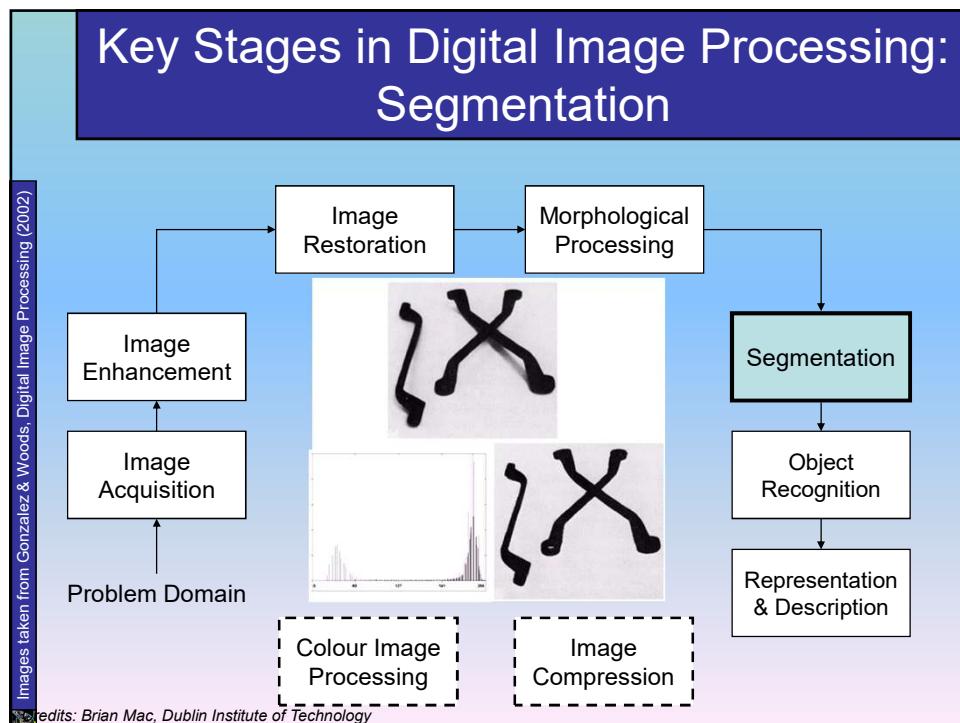
The continuum from image processing to computer vision can be broken up into low-, mid- and high-level processes

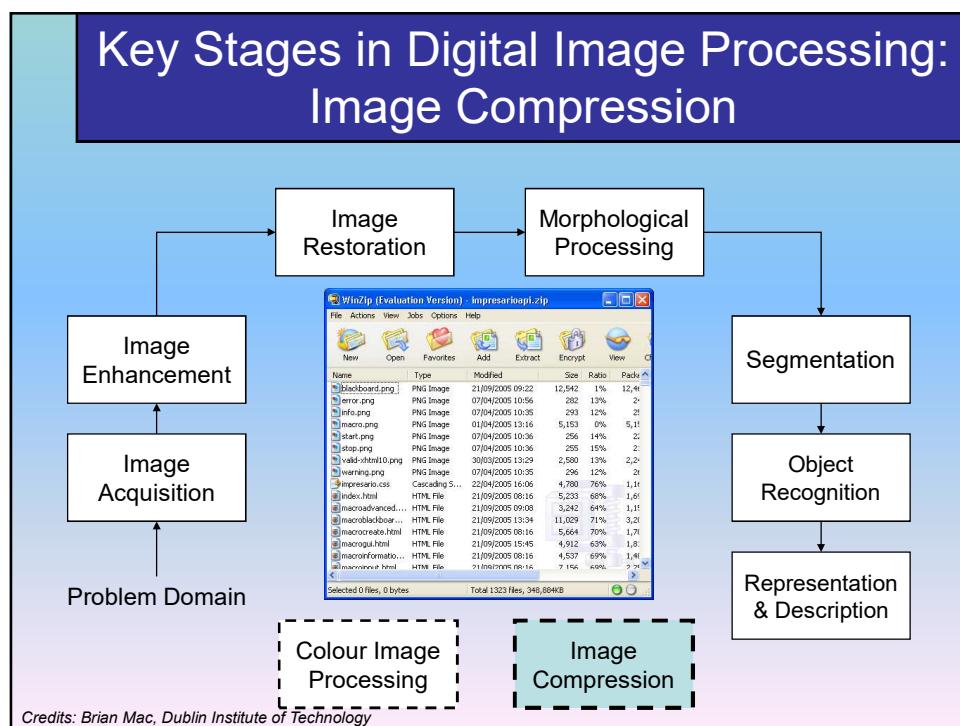
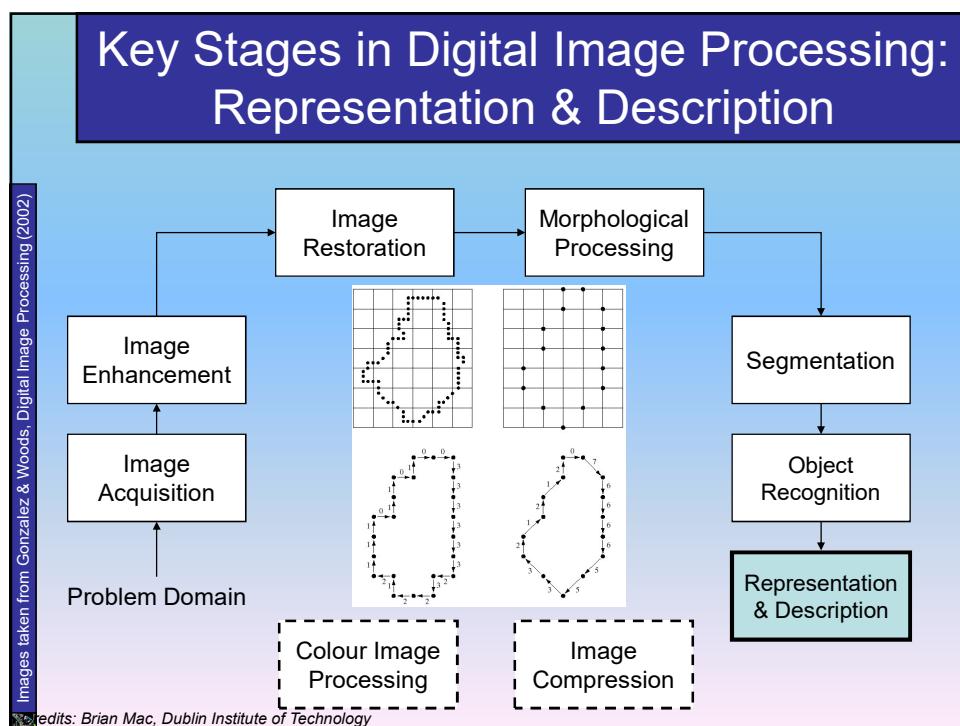
Low Level Process	Mid Level Process	High Level Process
<b>Input:</b> Image <b>Output:</b> Image	<b>Input:</b> Image <b>Output:</b> Attributes	<b>Input:</b> Attributes <b>Output:</b> Understanding
<b>Examples:</b> Noise removal, image sharpening	<b>Examples:</b> Object recognition, segmentation	<b>Examples:</b> Scene understanding, autonomous navigation



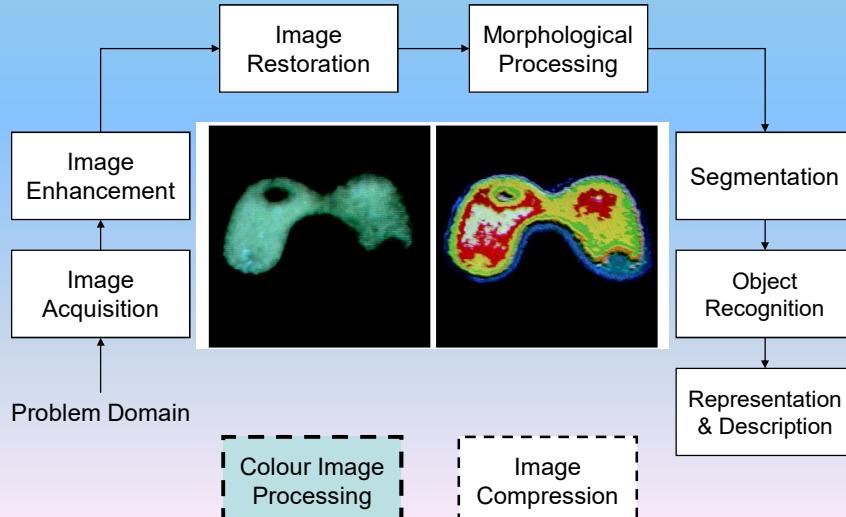








## Key Stages in Digital Image Processing: Colour Image Processing

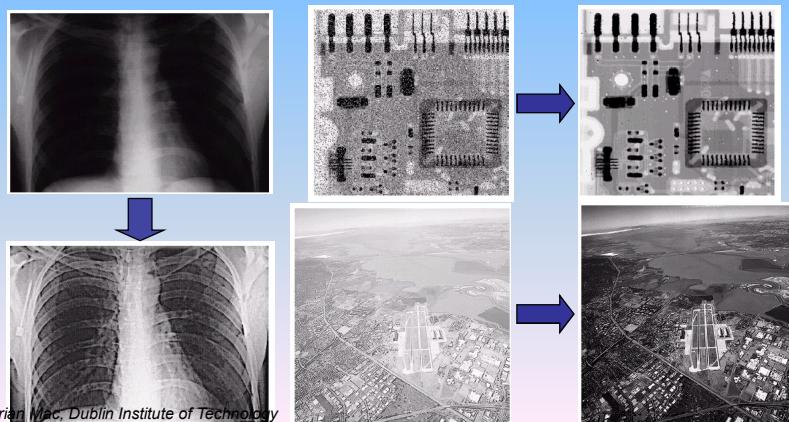


Credits: Brian Mac, Dublin Institute of Technology

## Examples: Image Enhancement

One of the most common uses of DIP techniques: improve quality, remove noise etc

Images taken from Gonzalez & Woods, Digital Image Processing (2002)



Credits: Brian Mac, Dublin Institute of Technology

*Digital Image Processing, 2nd ed.*

[www.imageprocessingbook.com](http://www.imageprocessingbook.com)

### How to Decide Spatial and Gray-Level Resolution?



a b c

**FIGURE 2.22** (a) Image with a low level of detail. (b) Image with a medium level of detail. (c) Image with a relatively large amount of detail. (Image (b) courtesy of the Massachusetts Institute of Technology.)

- Figure 2.22 (a): The woman's face; Image with low level of detail.
- Figure 2.22 (b): The cameraman; Image with medium level of detail.
- Figure 2.22 (c): The crowd picture; Image with a relatively large amount of detail.

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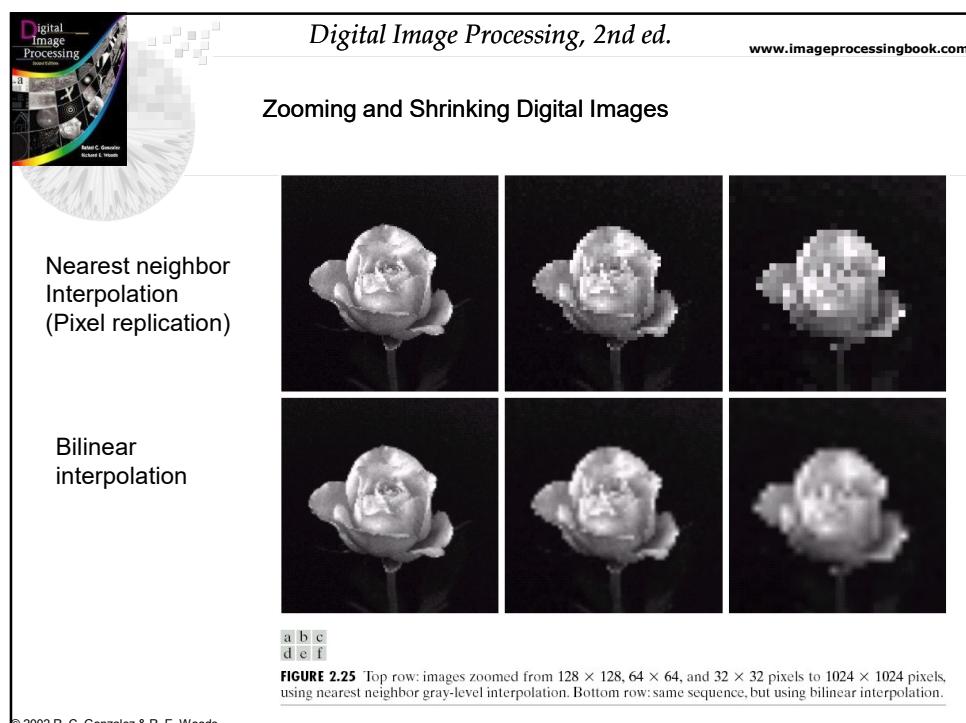
*Digital Image Processing, 2nd ed.*

[www.imageprocessingbook.com](http://www.imageprocessingbook.com)

### Zooming and Shrinking Digital Images

- **Zooming:** increasing the number of pixels in an image so that the image appears larger
  - **Nearest neighbor interpolation**
    - For example: pixel replication--to repeat rows and columns of an image
  - **Bilinear interpolation**
    - Smoother
  - Higher order interpolation
- **Image shrinking:** subsampling

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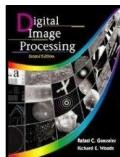


*Digital Image Processing, 2nd ed.* [www.imageprocessingbook.com](http://www.imageprocessingbook.com)

Some Basic Relationships Between Pixels

- Neighbors of a pixel
  - There are three kinds of neighbors of a pixel:
    - $N_4(p)$  4-neighbors: the set of horizontal and vertical neighbors
    - $N_D(p)$  diagonal neighbors: the set of 4 diagonal neighbors
    - $N_8(p)$  8-neighbors: union of 4-neighbors and diagonal neighbors

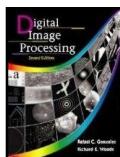
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## Some Basic Relationships Between Pixels

- **Adjacency:**
  - Two pixels that are neighbors and have the same grey-level (or some other specified similarity criterion) are adjacent
  - Pixels can be 4-adjacent, diagonally adjacent, 8-adjacent, or m-adjacent.
- **m-adjacency (mixed adjacency):**
  - Two pixels  $p$  and  $q$  of the same value (or specified similarity) are  $m$ -adjacent if either
    - (i)  $q$  and  $p$  are 4-adjacent, or
    - (ii)  $p$  and  $q$  are diagonally adjacent and do not have any common 4-adjacent neighbors.
    - They cannot be both (i) and (ii).

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## Some Basic Relationships Between Pixels

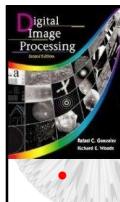
- **An example of adjacency:**

$\begin{matrix} 0 & 1 & 1 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{matrix}$	$\begin{matrix} 0 & 1 \cdots 1 \\ 0 & 1 \cdots 0 \\ 0 & 0 \cdots 1 \end{matrix}$	$\begin{matrix} 0 & 1 \cdots 1 \\ 0 & 1 \cdots 0 \\ 0 & 0 \cdots 1 \end{matrix}$
---	--	--

a   b   c

**FIGURE 2.26** (a) Arrangement of pixels; (b) pixels that are 8-adjacent (shown dashed) to the center pixel; (c)  $m$ -adjacency.

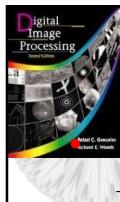
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## Some Basic Relationships Between Pixels

- **Path:**
  - The length of the path
  - Closed path
- **Connectivity** in a subset  $S$  of an image
  - Two pixels are connected if there is a path between them that lies completely within  $S$ .
- **Connected component** of  $S$ :
  - The set of all pixels in  $S$  that are connected to a given pixel in  $S$ .
- **Region** of an image
- Boundary, border or **contour** of a region  $R$ 
  - The set of points that are adjacent to points in the complement of  $R$ .
- **Edge**: a path of one or more pixels that separate two regions of significantly different gray levels.

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## Some Basic Relationships Between Pixels

### Distance measures

- Distance function: a function of two points,  $p$  and  $q$ , in space that satisfies three criteria
  - (a)  $D(p, q) \geq 0$
  - (b)  $D(p, q) = D(q, p)$ , and
  - (c)  $D(p, z) \leq D(p, q) + D(q, z)$
- The Euclidean distance  $D_e(p, q)$   

$$D_e(p, q) = \sqrt{(x-s)^2 + (y-t)^2}$$
- The city-block (Manhattan) distance  $D_4(p, q)$   

$$D_4(p, q) = |x-s| + |y-t|$$
- The chessboard distance  $D_8(p, q)$   

$$D_8(p, q) = \max(|x-s|, |y-t|)$$
- $D_m(p, q)$  = Shortest  $m$ -path between  $p$  and  $q$ .  
 In this case, distance depends also on the value of pixels along the path and their neighbours

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## A Note About Grey Levels

So far when we have spoken about image grey level values we have said they are in the range [0, 255]

- Where 0 is black and 255 is white

There is no reason why we have to use this range

- The range [0,255] stems from display technologies

For many of the image processing operations in this lecture grey levels are assumed to be given in the range [0.0, 1.0]

## What Is Image Enhancement?

Image enhancement is the process of making images more useful

The reasons for doing this include:

- Highlighting interesting detail in images
- Removing noise from images
- Making images more visually appealing

## Image Enhancement Examples

Images taken from Gonzalez & Woods, Digital Image Processing (2002)



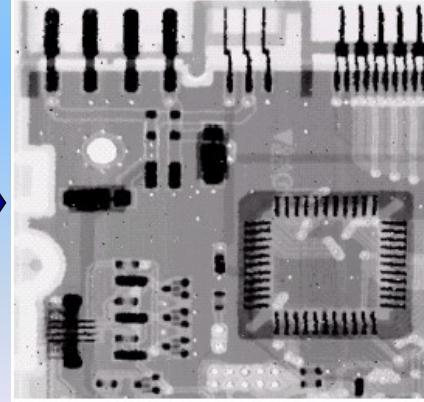
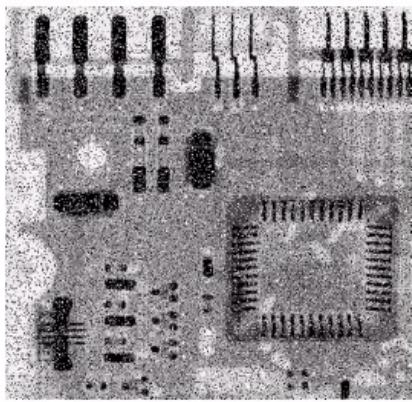
Images taken from Gonzalez & Woods, Digital Image Processing (2002)

## Image Enhancement Examples (cont...)



## Image Enhancement Examples (cont...)

Images taken from Gonzalez & Woods, Digital Image Processing (2002)



## Image Enhancement Examples (cont...)

Images taken from Gonzalez & Woods, Digital Image Processing (2002)

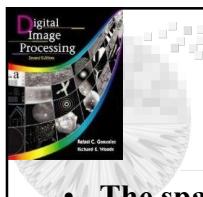


## Spatial & Frequency Domains

There are two broad categories of image enhancement techniques

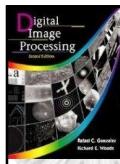
- Spatial domain techniques
  - Direct manipulation of image pixels
- Frequency domain techniques
  - Manipulation of Fourier transform or wavelet transform of an image

For the moment we will concentrate on techniques that operate in the spatial domain



### Digital Image Processing, 2nd ed. Image Enhancement in the Spatial Domain

- **The spatial domain:**
  - The image plane
  - For a digital image is a Cartesian coordinate system of discrete rows and columns. At the intersection of each row and column is a pixel. Each pixel has a value, which we will call intensity.
- **The frequency domain :**
  - A (2-dimensional) discrete Fourier transform of the spatial domain
  - We will discuss it later (Book chapter 4)
- **Enhancement :**
  - To “improve” the usefulness of an image by using some transformation on the image.
  - Often the improvement is to help make the image “better” looking, such as increasing the intensity or contrast.



## Background

- A mathematical representation of **spatial domain enhancement**:

$$g(x, y) = T[f(x, y)]$$

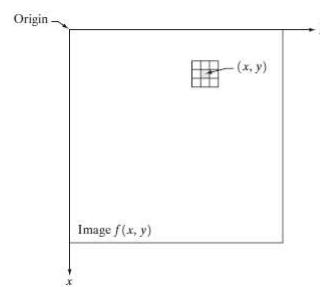
where  $f(x, y)$ : the input image

$g(x, y)$ : the processed image

$T$ : an operator on  $f$ , defined over some neighborhood of  $(x, y)$

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**FIGURE 3.1** A  $3 \times 3$  neighborhood about a point  $(x, y)$  in an image.



- The simplest form of  $T$ , is when the neighborhood of size  $1 \times 1$  (that is a single pixel). In this case,  $g$  depends only on the value of  $f$  at  $(x, y)$ , and  $T$  becomes a *grey-level* (also called *intensity* or *mapping*) *transformation function* of the form:

$$s = T(r)$$

Where, for simplicity in notation,  $r$  and  $s$  are variables denoting, respectively, the grey level of  $f(x, y)$  and  $g(x, y)$  at any point  $(x, y)$

# Examples of Enhancement Techniques

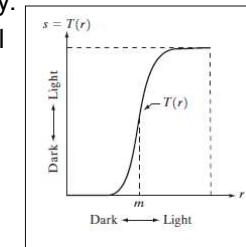
- **Contrast Stretching:**

If  $T(r)$  has the form as shown in the figure below, the effect of applying the transformation to every pixel of  $f$  to generate the corresponding pixels in  $g$  would:

Produce higher contrast than the original image, by:

- Darkening the levels below  $m$  in the original image
- Brightening the levels above  $m$  in the original image

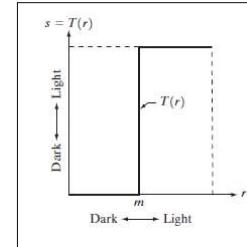
So, Contrast Stretching: is a simple image enhancement technique that improves the contrast in an image by ‘stretching’ the range of intensity values it contains to span a desired range of values. Typically, it uses a linear function



# Examples of Enhancement Techniques

- **Thresholding**

Is a limited case of contrast stretching, it produces a two-level (binary) image.



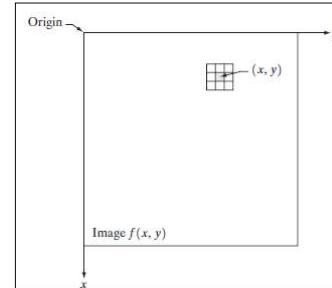
Some fairly simple, yet powerful, processing approaches can be formulated with grey-level transformations. Because enhancement at any point in an image depends only on the gray level at that point, techniques in this category often are referred to as *point processing*.

## Examples of Enhancement Techniques

Larger neighborhoods allow considerable more flexibility. The general approach is to use a function of the values of  $f$  in a predefined neighborhood of  $(x,y)$  to determine the value of  $g$  at  $(x,y)$ .

One of the principal approaches in this formulation is based on the use of so-called *masks* (also referred to as *filters*)

So, a **mask/filter**: is a small (say 3X3) 2-D array, such as the one shown in the figure, in which the values of the mask coefficients determine the nature of the process, such as *image sharpening*. Enhancement techniques based on this type of approach often are referred to as *mask processing* or *filtering*.



## Some Basic Intensity (Gray-level) Transformation Functions

- Grey-level transformation functions (also called, intensity functions), are considered the simplest of all image enhancement techniques.
- The value of pixels, before and after processing, will be denoted by  $r$  and  $s$ , respectively. These values are related by the expression of the form:

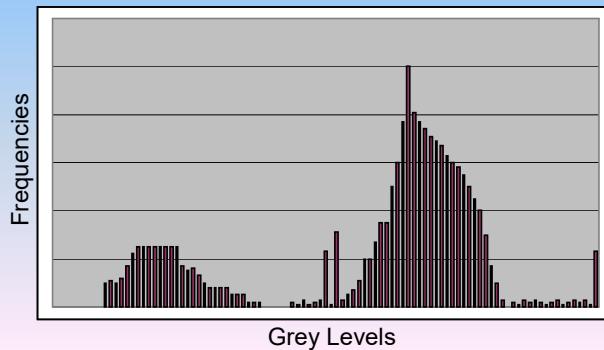
$$s = T(r)$$

where  $T$  is a transformation that maps a pixel value  $r$  into a pixel value  $s$ .

# Image Histograms

The histogram of an image shows us the distribution of grey levels in the image

Massively useful in image processing,  
especially in segmentation



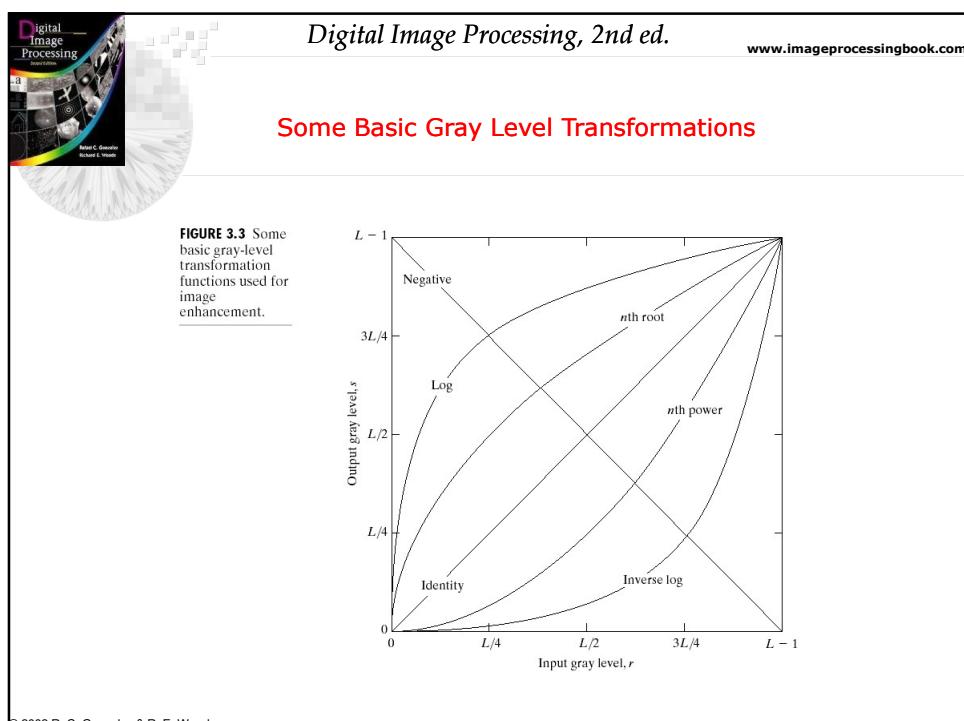
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**Gray-level Transformation**

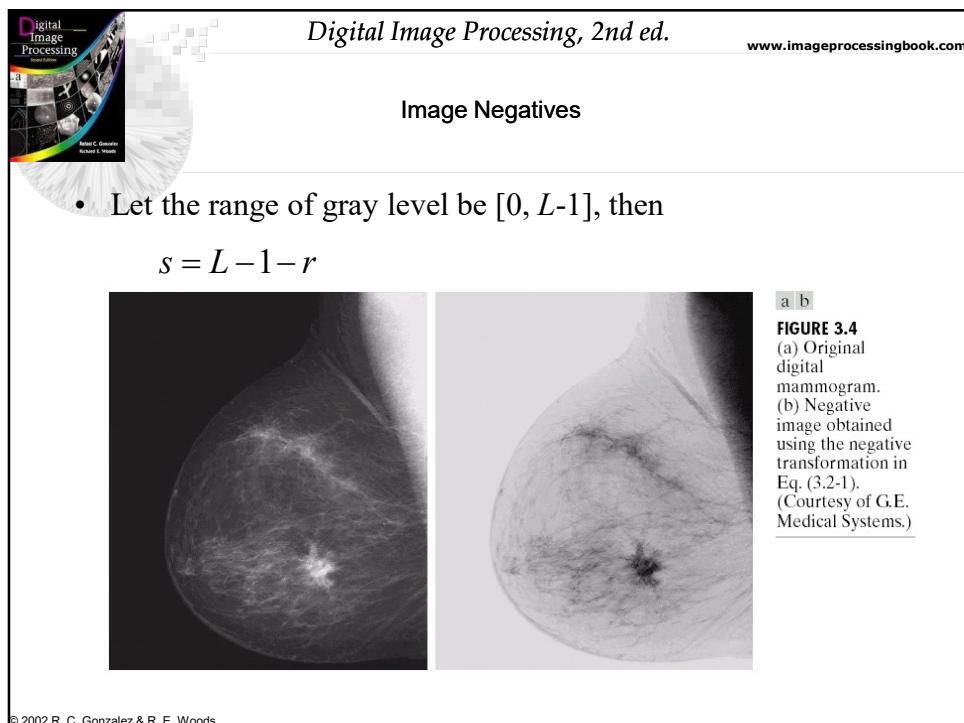
**a** **b**

**FIGURE 3.2** Gray-level transformation functions for contrast enhancement.

The figure illustrates two gray-level transformation functions.   
**a:** A sigmoidal curve representing a non-linear transformation. The vertical axis is labeled  $s = T(r)$  with 'Light' at the top and 'Dark' at the bottom. The horizontal axis is labeled  $r$  with 'Dark' on the left and 'Light' on the right. A point  $m$  is marked on the horizontal axis. The curve starts near zero for small  $r$ , passes through  $(m, 0.5)$ , and approaches 1 for large  $r$ .   
**b:** A step function representing a linear transformation. The vertical axis is labeled  $s = T(r)$  with 'Light' at the top and 'Dark' at the bottom. The horizontal axis is labeled  $r$  with 'Dark' on the left and 'Light' on the right. A point  $m$  is marked on the horizontal axis. The function is 0 for  $r < m$  and 1 for  $r \geq m$ .   
Below the graphs are three grayscale images of sunflowers. The first image is the original. The second image shows the result of applying the sigmoidal transformation (a.  $T(r)$ ). The third image shows the result of applying the step transformation (b.  $T(r)$ ).



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## Log Transformations

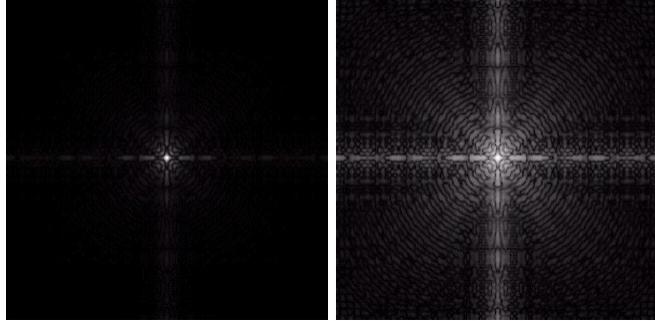
$$s = c \log(1 + r)$$

where  $c$  : constant

$$r \geq 0$$

a b

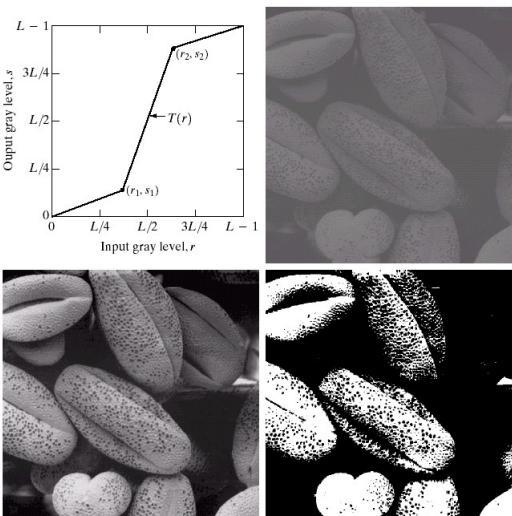
**FIGURE 3.5**  
 (a) Fourier spectrum.  
 (b) Result of applying the log transformation given in Eq. (3.2-2) with  $c = 1$ .



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## Piecewise-Linear Transformation Functions Contrast Stretching

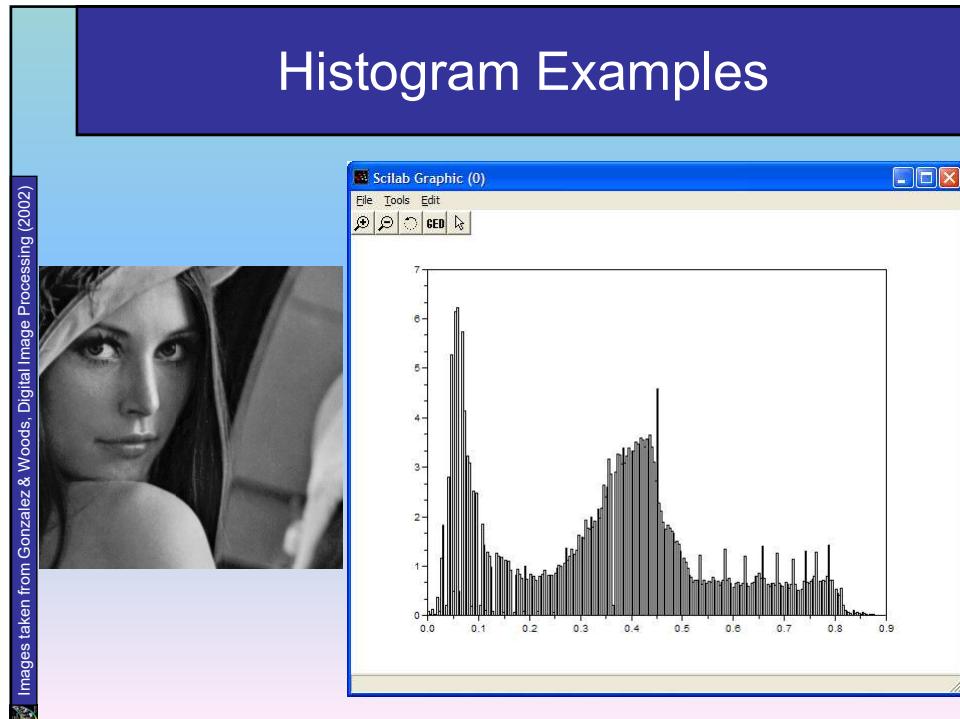


a b  
c d

**FIGURE 3.10**  
 Contrast stretching.  
 (a) Form of transformation function. (b) A low-contrast image. (c) Result of contrast stretching. (d) Result of thresholding. (Original image courtesy of Dr. Roger Heady, Research School of Biological Sciences, Australian National University, Canberra, Australia.)

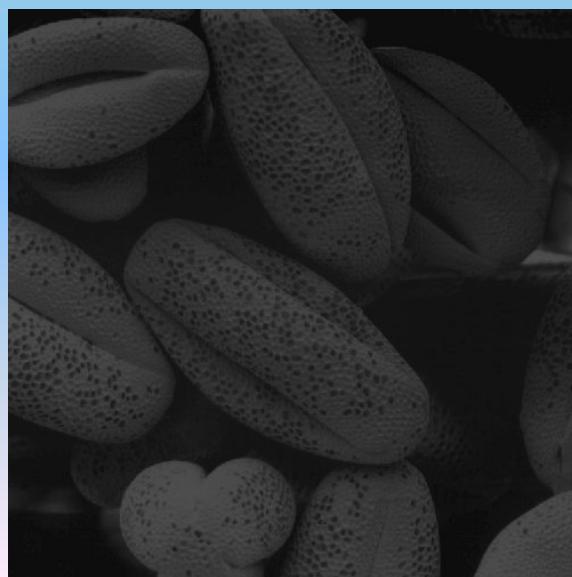
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## Histogram Examples



Images taken from Gonzalez & Woods, Digital Image Processing (2002)

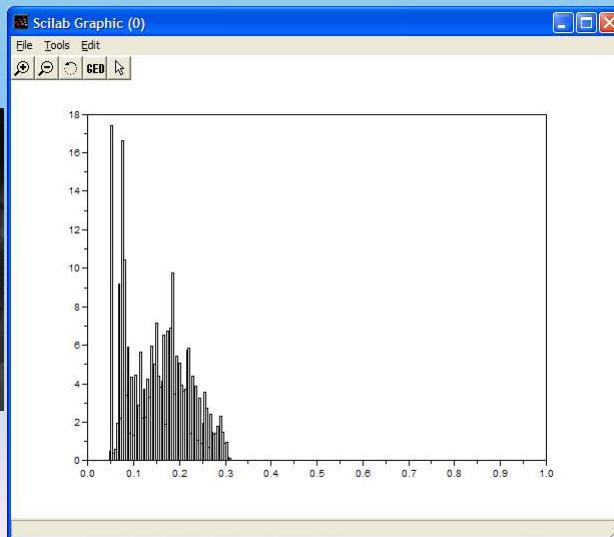
## Histogram Examples (cont...)



Images taken from Gonzalez & Woods, Digital Image Processing (2002)

## Histogram Examples (cont...)

Images taken from Gonzalez & Woods, Digital Image Processing (2002)

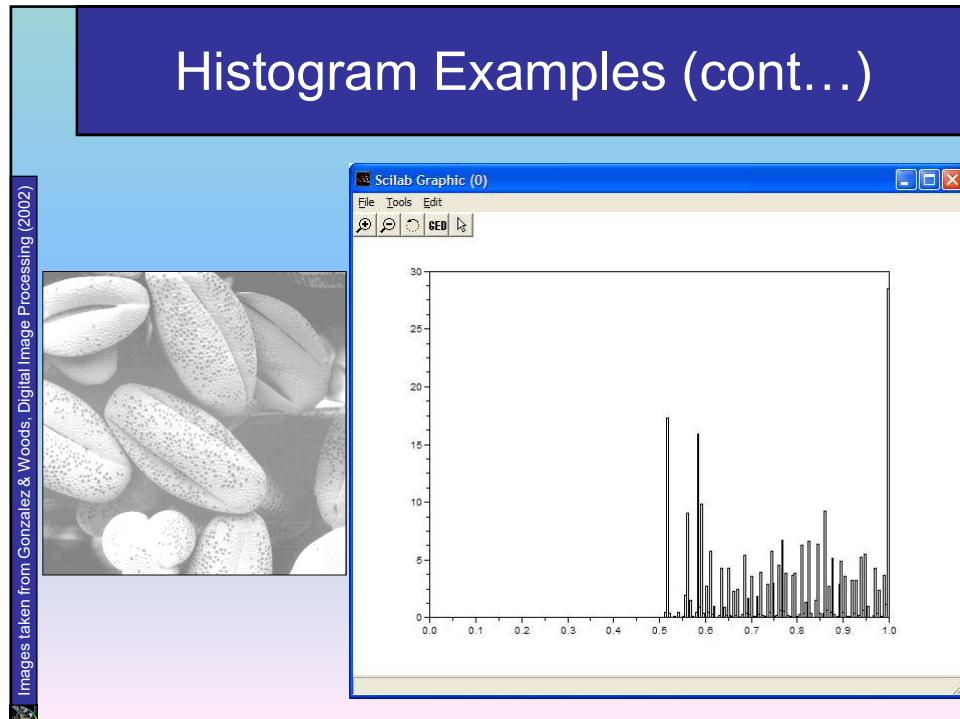


Images taken from Gonzalez & Woods, Digital Image Processing (2002)

## Histogram Examples (cont...)



## Histogram Examples (cont...)

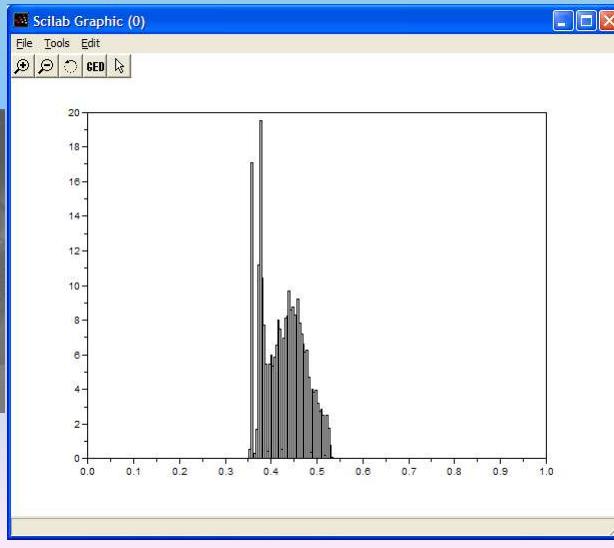
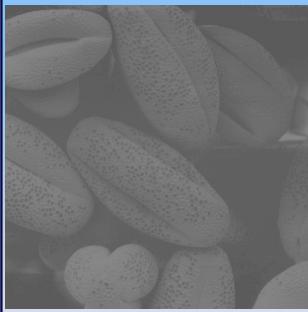


## Histogram Examples (cont...)



## Histogram Examples (cont...)

Images taken from Gonzalez & Woods, Digital Image Processing (2002)

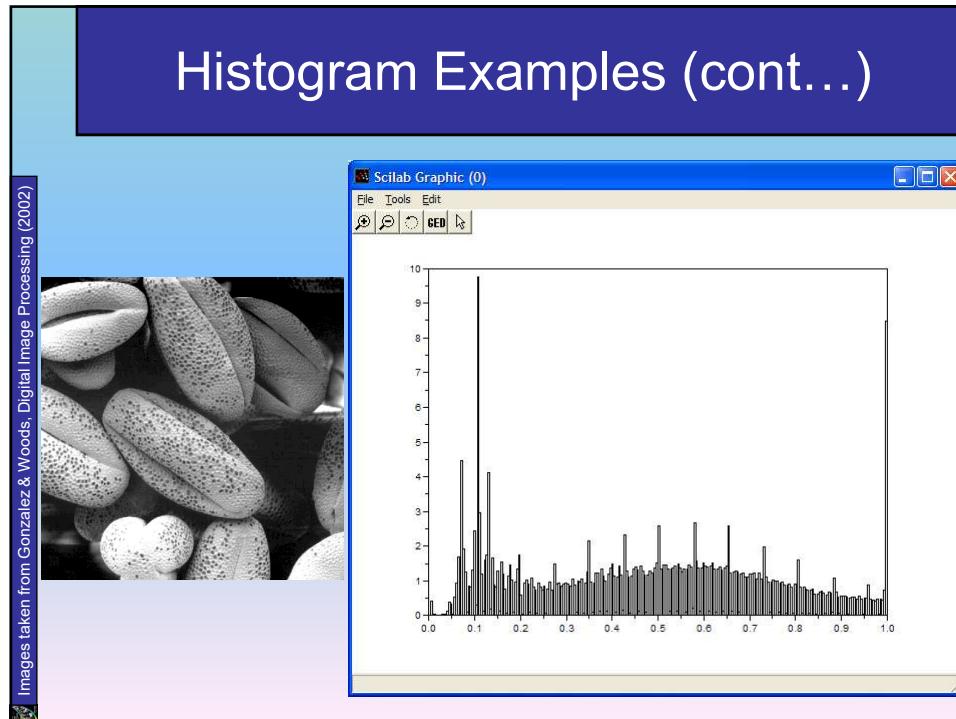


## Histogram Examples (cont...)

Images taken from Gonzalez & Woods, Digital Image Processing (2002)



## Histogram Examples (cont...)



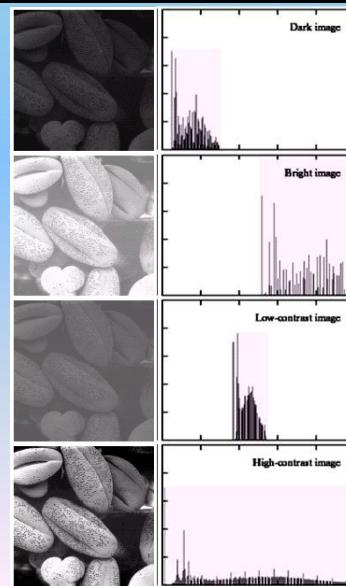
Images taken from Gonzalez & Woods, Digital Image Processing (2002)

## Histogram Examples (cont...)

A selection of images and their histograms

Notice the relationships between the images and their histograms

Note that the high contrast image has the most evenly spaced histogram



Images taken from Gonzalez & Woods, Digital Image Processing (2002)