

Q3) $\frac{dy}{dx} + 4xy = e^{-2x^2}$, $y(0) = -4.3$

$$\text{I.F} = e^{\int 4x dx} = e^{4 \cdot \frac{x^2}{2}} = e^{2x^2}$$

$$y(e^{2x^2}) = \int e^{-2x^2} \cdot e^{2x^2} dx$$

$$y(e^{2x^2}) = \int dx \Rightarrow y(e^{2x^2}) = x + c$$

If $x = 0$, $y = -4.3$

$$-4.3 (e^0) = c$$

$$c = -4.3$$

$$y(e^{2x^2}) = x - 4.3$$

$$\Rightarrow e^{-2x^2} (x - 4.3)$$

$$y = e^{-2x^2} (x - 4.3)$$