

**PROGRAM :** Write a function to find the maximum and minimum elements in an array.

```
import java.util.Scanner;
public class minmax {
    public static int maxx(int[] a, int m) {
        for (int i = 0; i < a.length; i++) {
            if (a[i] > m) {
                m = a[i];
            }
        }
        return m;
    }
    public static int minn(int[] a, int m) {
        for (int i = 0; i < a.length; i++) {
            if (a[i] < m) {
                m = a[i];
            }
        }
        return m;
    }
    public static void main(String[] args) {
        Scanner obj = new Scanner(System.in);
        System.out.println("Enter the size of the array:");
        int size = obj.nextInt();
        int[] a = new int[size];
        for (int i = 0; i < a.length; i++) {
            System.out.println("Enter the elements:" + i);
            a[i] = obj.nextInt();
        }
        int m = Integer.MIN_VALUE;
        int lr = maxx(a, m);
        System.out.println("Max value in arr" + lr);
        m = Integer.MAX_VALUE;
        int sm = minn(a, m);
        System.out.println("Min value in arr " + sm);
    }
}
```

**PROGRAM :** Write a function to reverse an array in place.

**Sourcecode:**

```
import java.util.Scanner;
public class reversearr {
    public void rr(int a[]){
        int i=0;
        int j=a.length-1;
        while (i<j){
            int temp=a[i];
            a[i]=a[j];
            a[j]=temp;

            i++;
            j--;
        }
        for(int k=0;k<a.length;k++){
            System.out.print(a[k]+" ");
        }

    }
    public static void main(String[] args) {
        Scanner obj = new Scanner(System.in);
        System.out.println("Enter the size of the array:");
        int size = obj.nextInt();
        int[] a = new int[size];
        for (int i = 0; i < a.length; i++) {
            System.out.println("Enter the elements:"+i);
            a[i] = obj.nextInt();
        }

        reversearr palat = new reversearr();
        palat.rr(a);
    }
}
```

**PROGRAM : Find the Kth Smallest/Largest Element in an Array: Write a function to find the Kth smallest or largest element in an array.**

PROGRAM :

```
import java.util.Arrays;

public class Main {
    public static int findKthSmallest(int[] arr, int k) {
        Arrays.sort(arr);
        return arr[k - 1];
    }

    public static int findKthLargest(int[] arr, int k) {
        Arrays.sort(arr);
        return arr[arr.length - k];
    }

    public static void main(String[] args) {
        int[] arr = {7, 10, 4, 3, 20, 15};
        int k = 3;

        System.out.println("Kth Smallest Element: " + findKthSmallest(arr, k));
        System.out.println("Kth Largest Element: " + findKthLargest(arr, k));
    }
}
```

**PROGRAM :** Sort an Array of 0s, 1s, and 2s: Given an array containing only 0s, 1s, and 2s, sort the array in linear time.

```
public class Main {
    public static void main(String[] args) {
        int[] nums = {0, 1, 2, 1, 0, 2, 1};
        sortColors(nums);

        System.out.println("Sorted Array:");
        for (int num : nums) {
            System.out.print(num + " ");
        }
    }

    public static void sortColors(int[] nums) {
        int low = 0, mid = 0, high = nums.length - 1;

        while (mid <= high) {
            if (nums[mid] == 0) {
                int temp = nums[low];
                nums[low] = nums[mid];
                nums[mid] = temp;
                low++;
                mid++;
            } else if (nums[mid] == 1) {
                mid++;
            } else {
                int temp = nums[mid];
                nums[mid] = nums[high];
                nums[high] = temp;
                high--;
            }
        }
    }
}
```

**PROGRAM :** Move All Zeroes to End of Array: Write a function to move all zeroes in an array to the end while maintaining the relative order of other elements.

```
public class Main {  
    public static void main(String[] args) {  
        int[] nums = {0, 1, 0, 3, 12};  
        moveZeroes(nums);  
  
        System.out.println("Array After Moving Zeroes:");  
        for (int num : nums) {  
            System.out.print(num + " ");  
        }  
    }  
  
    public static void moveZeroes(int[] nums) {  
        int index = 0;  
  
        for (int num : nums) {  
            if (num != 0) {  
                nums[index++] = num;  
            }  
        }  
  
        while (index < nums.length) {  
            nums[index++] = 0;  
        }  
    }  
}
```



**PROGRAM :** Reverse a Linked List: Write a function to reverse a singly linked list.

```
class ListNode {
    int val;
    ListNode next;

    ListNode(int val) {
        this.val = val;
    }
}

public class Main {
    public static void main(String[] args) {
        ListNode head = new ListNode(1);
        head.next = new ListNode(2);
        head.next.next = new ListNode(3);
        head.next.next.next = new ListNode(4);

        System.out.println("Original Linked List:");
        printList(head);

        head = reverseList(head);

        System.out.println("Reversed Linked List:");
        printList(head);
    }

    public static ListNode reverseList(ListNode head) {
        ListNode prev = null;

        while (head != null) {
```

```
        ListNode nextNode = head.next;
        head.next = prev;
        prev = head;
        head = nextNode;
    }

    return prev;
}

public static void printList(ListNode head) {
    while (head != null) {
        System.out.print(head.val + " ");
        head = head.next;
    }
    System.out.println();
}
}
```



**PROGRAM** : Detect a Cycle in a Linked List: Write a function to detect if a cycle exists in a linked list.

```
public class Main {  
    public static void main(String[] args) {  
        ListNode head = new ListNode(3);  
        head.next = new ListNode(2);  
        head.next.next = new ListNode(0);  
        head.next.next.next = new ListNode(-4);  
        head.next.next.next.next = head.next; // Creates a cycle  
  
        if (hasCycle(head)) {  
            System.out.println("Cycle detected in the linked list.");  
        } else {  
            System.out.println("No cycle detected in the linked list.");  
        }  
    }  
  
    public static boolean hasCycle(ListNode head) {  
        ListNode slow = head, fast = head;  
  
        while (fast != null && fast.next != null) {  
            slow = slow.next;
```

```
fast = fast.next.next;
```

```
if (slow == fast) {
```

```
    return true;
```

```
}
```

```
}
```

```
return false;
```

```
}
```

```
}
```

**PROGRAM :** Find the Middle of a Linked List: Write a function to find the middle element of a linked list.

```
public class Main {  
    public static void main(String[] args) {  
        ListNode head = new ListNode(1);  
        head.next = new ListNode(2);  
        head.next.next = new ListNode(3);  
        head.next.next.next = new ListNode(4);  
        head.next.next.next.next = new ListNode(5);  
  
        ListNode middle = findMiddle(head);  
  
        System.out.println("Middle Element of the Linked List: " + middle.val);  
    }  
  
    public static ListNode findMiddle(ListNode head) {  
        ListNode slow = head, fast = head;  
  
        while (fast != null && fast.next != null) {  
            slow = slow.next;  
            fast = fast.next.next;  
        }  
  
        return slow;  
    }  
}
```



**PROGRAM :** Merge Two Sorted Linked Lists: Write a function to merge two sorted linked lists into one sorted linked list.

```
public class Main {  
    public static void main(String[] args) {  
        ListNode l1 = new ListNode(1);  
        l1.next = new ListNode(3);  
        l1.next.next = new ListNode(5);  
  
        ListNode l2 = new ListNode(2);  
        l2.next = new ListNode(4);  
        l2.next.next = new ListNode(6);  
  
        ListNode merged = mergeTwoLists(l1, l2);  
  
        System.out.println("Merged Linked List:");  
        printList(merged);  
    }  
  
    public static ListNode mergeTwoLists(ListNode l1, ListNode l2) {  
        ListNode dummy = new ListNode(-1);  
        ListNode current = dummy;  
  
        while (l1 != null && l2 != null) {
```

```
    if (l1.val <= l2.val) {  
        current.next = l1;  
        l1 = l1.next;  
    } else {  
        current.next = l2;  
        l2 = l2.next;  
    }  
    current = current.next;  
}
```

```
current.next = (l1 != null) ? l1 : l2;
```

```
return dummy.next;  
}
```

```
public static void printList(ListNode head) {  
    while (head != null) {  
        System.out.print(head.val + " ");  
        head = head.next;  
    }  
    System.out.println();  
}  
}
```

**PROGRAM :** Remove Nth Node from End of List: Write a function to remove the Nth node from the start/end of a linked list.

```
public class Main {
    public static void main(String[] args) {
        ListNode head = new ListNode(1);
        head.next = new ListNode(2);
        head.next.next = new ListNode(3);
        head.next.next.next = new ListNode(4);
        head.next.next.next.next = new ListNode(5);

        int n = 2;
        head = removeNthFromEnd(head, n);

        System.out.println("Linked List After Removing " + n + "th Node From End:");
        printList(head);
    }

    public static ListNode removeNthFromEnd(ListNode head, int n) {
        ListNode dummy = new ListNode(0);
        dummy.next = head;
        ListNode first = dummy;
        ListNode second = dummy;

        for (int i = 0; i <= n; i++) {
            first = first.next;
        }

        while (first != null) {
            first = first.next;
            second = second.next;
        }
    }
}
```

```
second.next = second.next.next;
```

```
return dummy.next;
```

```
}
```

```
public static void printList(ListNode head) {
```

```
    while (head != null) {
```

```
        System.out.print(head.val + " ");
```

```
        head = head.next;
```

```
    }
```

```
    System.out.println();
```

```
}
```

```
}
```



**PROGRAM :** Implement a Stack Using Arrays/Lists: Write a function to implement a stack using an array or list with basic operations: push, pop, peek, and isEmpty.

```
class Stack {
    private int[] stack;
    private int top;

    public Stack(int size) {
        stack = new int[size];
        top = -1;
    }

    public void push(int x) {
        if (top == stack.length - 1) {
            System.out.println("Stack Overflow");
            return;
        }
        stack[++top] = x;
    }

    public int pop() {
        if (top == -1) {
            System.out.println("Stack Underflow");
            return -1;
        }
        return stack[top--];
    }

    public int peek() {
        if (top == -1) {
            System.out.println("Stack is Empty");
            return -1;
        }
        return stack[top];
    }
}
```

```
}

public boolean isEmpty() {
    return top == -1;
}

}

public class Main {
    public static void main(String[] args) {
        Stack stack = new Stack(5);

        stack.push(10);
        stack.push(20);
        stack.push(30);

        System.out.println("Top Element: " + stack.peek());

        System.out.println("Popped: " + stack.pop());
        System.out.println("Popped: " + stack.pop());

        System.out.println("Is Stack Empty? " + stack.isEmpty());
    }
}
```

**PROGRAM :** Implement a Stack Using Linked List: Write a function to implement a stack using a linked list with basic operations: push, pop, peek, and isEmpty.

```
#include <iostream>
using namespace std;
struct Node {
    int data;
    Node* next;
};
class Stack {
private:
    Node* top;
public:
    Stack() {
        top = nullptr;
    }
    void push(int x) {
        Node* newNode = new Node();
        newNode->data = x;
        newNode->next = top;
        top = newNode;
    }
    int pop() {
        if (isEmpty()) {
            cout << "Stack Underflow!" << endl;
            return -1;
        }
        int poppedValue = top->data;
        Node* temp = top;
        top = top->next;
        delete temp;
    }
};
```

```

return poppedValue;
}
int peek() {
if (isEmpty()) {
cout << "Stack is empty!" << endl;
return -1;
}
return top->data;
}
bool isEmpty() {
return top == nullptr;
}
};

```

**PROGRAM :** Check for Balanced Parentheses: Write a function to check if a string containing parentheses is balanced.

```

#include <iostream>
#include <stack>
using namespace std;
bool isBalanced(string expr) {
stack<char> s;
for (char ch : expr) {
if (ch == '(' || ch == '{' || ch == '[') {
s.push(ch);
} else if (ch == ')' || ch == '}' || ch == ']') {
if (s.empty() || (ch == ')' && s.top() != '(') || (ch == '}' && s.top() != '{') || (ch == ']' && s.top() != '[')) {
return false;
}
s.pop();
}
}
return s.empty();}

```

**PROGRAM :** Evaluate Postfix Expression: Write a function to evaluate a given postfix expression.

```
#include <iostream>
#include <stack>
#include <cctype>
using namespace std;
int evaluatePostfix(string expr) {
    stack<int> s;
    for (char ch : expr) {
        if (isdigit(ch)) {
            s.push(ch - '0');
        } else {
            int b = s.top(); s.pop();
            int a = s.top(); s.pop();
            switch (ch) {
                case '+': s.push(a + b); break;
                case '-': s.push(a - b); break;
                case '*': s.push(a * b); break;
                case '/': s.push(a / b); break;
            }
        }
    }
    return s.top();
}
```

**PROGRAM :** Next Greater Element: Write a function to find the next greater element for each element.

```
#include <iostream>
#include <vector>
#include <stack>
using namespace std;
vector<int> nextGreaterElement(vector<int>& nums) {
    vector<int> result(nums.size(), -1);
    stack<int> s;
    for (int i = 0; i < nums.size(); ++i) {
        while (!s.empty() && nums[s.top()] < nums[i]) {
            result[s.top()] = nums[i];
            s.pop();
        }
        s.push(i);
    }
    return result;
}
```

**PROGRAM :** Implement a Queue Using Arrays/Lists: Write a function to implement a queue using an array or list with basic operations: enqueue, dequeue, front, and isEmpty.

```
#include <iostream>
#include <vector>
using namespace std;
class Queue {
private:
vector<int> arr;
public:
void enqueue(int x) {
arr.push_back(x);
}
int dequeue() {
if (isEmpty()) {
cout << "Queue Underflow!" << endl;
return -1;
}
int frontElement = arr[0];
arr.erase(arr.begin());
return frontElement;
}
int front() {
if (isEmpty()) {
cout << "Queue is empty!" << endl;
return -1;
}
return arr[0];
}
bool isEmpty() {
return arr.empty();
}
};
```

**PROGRAM :** Implement a Queue Using Linked List: Write a function to implement a queue using a linked list with basic operations: enqueue, dequeue, front, and isEmpty.

```
#include <iostream>
using namespace std;
struct Node {
    int data;
    Node* next;
};
class Queue {
private:
    Node* frontNode;
    Node* rearNode;
public:
    Queue() {
        frontNode = rearNode = nullptr;
    }
    void enqueue(int x) {
        Node* newNode = new Node();
        newNode->data = x;
        newNode->next = nullptr;
        if (rearNode) {
            rearNode->next = newNode;
        }
        rearNode = newNode;
        if (!frontNode) {
            frontNode = rearNode;
        }
    }
    int dequeue() {
        if (isEmpty()) {
            cout << "Queue Underflow!" << endl;
            return -1;
        }
        int frontValue = frontNode->data;
        Node* temp = frontNode;
        frontNode = frontNode->next;
        delete temp;
        if (!frontNode) {
            rearNode = nullptr;
        }
        return frontValue;
    }
    int front() {
        if (isEmpty()) {
            cout << "Queue is empty!" << endl;
            return -1;
        }
        return frontNode->data;
    }
};
```



```
}  
bool isEmpty() {  
    return frontNode == nullptr;  
}  
};
```

**PROGRAM :** Implement a Circular Queue: Write a function to implement a circular queue with basic operations: enqueue, dequeue, front, rear, and isEmpty.

```
#include <iostream>
using namespace std;
class CircularQueue {
private:
int* arr;
int size, front, rear, count;
public:
CircularQueue(int n) {
size = n;
arr = new int[n];
front = rear = count = 0;
}
void enqueue(int x) {
if (count == size) {
cout << "Queue Overflow!" << endl;
return;
}
arr[rear] = x;
rear = (rear + 1) % size;
count++;
}
int dequeue() {
if (isEmpty()) {
cout << "Queue Underflow!" << endl;
return -1;
}
int frontValue = arr[front];
front = (front + 1) % size;
count--;
return frontValue;
}
int frontElement() {
if (isEmpty()) {
cout << "Queue is empty!" << endl;
return -1;
}
return arr[front];
}
bool isEmpty() {
return count == 0;
}
};
```

**PROGRAM :** Generate Binary Numbers from 1 to N: Write a function to generate binary numbers from 1 to N using a queue.

```
#include <iostream>
#include <queue>
using namespace std;
void generateBinary(int n) {
    queue<string> q;
    q.push("1");
    while (n-->0) {
        string curr = q.front();
        q.pop();
        cout << curr << " ";
        q.push(curr + "0");
        q.push(curr + "1");
    }
}
```

**PROGRAM :** Implement a Queue Using Stacks: Write a function to implement a queue using two stacks.

```
#include <iostream>
#include <stack>
using namespace std;
class QueueUsingStacks {
private:
    stack<int> s1, s2;
public:
    void enqueue(int x) {
        s1.push(x);
    }
    int dequeue() {
        if (isEmpty()) {
            cout << "Queue Underflow!" << endl;
            return -1;
        }
        if (s2.empty()) {
            while (!s1.empty()) {
                s2.push(s1.top());
                s1.pop();
            }
        }
        int frontValue = s2.top();
        s2.pop();
        return frontValue;
    }
    bool isEmpty() {
        return s1.empty() && s2.empty();
    }
};
```

**PROGRAM:** Implement a Binary Tree: Write a class to implement a basic binary tree with insert, delete.

```
class BinaryTree {  
    class Node {  
        int key;  
        Node left, right;  
  
        public Node(int item) {  
            key = item;  
            left = right = null;  
        }  
    }  
}  
  
Node root;  
  
public BinaryTree() {  
    root = null;  
}  
  
// Insert a node  
void insert(int key) {  
    root = insertRec(root, key);  
}  
  
Node insertRec(Node root, int key) {  
    if (root == null) {  
        root = new Node(key);  
        return root;  
    }  
    if (key < root.key)  
        root.left = insertRec(root.left, key);
```

```

    else if (key > root.key)
        root.right = insertRec(root.right, key);
    return root;
}

```

// Delete a node

```

void delete(int key) {
    root = deleteRec(root, key);
}

```

```

Node deleteRec(Node root, int key) {

```

```

    if (root == null) return root;

```

```

    if (key < root.key)

```

```

        root.left = deleteRec(root.left, key);

```

```

    else if (key > root.key)

```

```

        root.right = deleteRec(root.right, key);

```

```

    else {

```

```

        // Node with only one child or no child

```

```

        if (root.left == null)

```

```

            return root.right;

```

```

        else if (root.right == null)

```

```

            return root.left;

```

```

        // Node with two children: Get the inorder successor (smallest in the right subtree)

```

```

        root.key = minValue(root.right);

```

```

        root.right = deleteRec(root.right, root.key);

```

```

    }

```

```

    return root;

```

```

}

```

```

int minValue(Node root) {

```

```

    int minValue = root.key;
    while (root.left != null) {
        minValue = root.left.key;
        root = root.left;
    }
    return minValue;
}

// Inorder traversal
void inorder() {
    inorderRec(root);
}

void inorderRec(Node root) {
    if (root != null) {
        inorderRec(root.left);
        System.out.print(root.key + " ");
        inorderRec(root.right);
    }
}

// Main method to test the tree
public static void main(String[] args) {
    BinaryTree tree = new BinaryTree();

    // Insert nodes
    tree.insert(50);
    tree.insert(30);
    tree.insert(20);
    tree.insert(40);

    System.out.println("Inorder traversal:");

```

```
tree.inorder();
```

```
System.out.println("\n\nDelete 20");
```

```
tree.delete(20);
```

```
System.out.println("Inorder traversal:");
```

```
tree.inorder();
```

```
System.out.println("\n\nDelete 30");
```

```
tree.delete(30);
```

```
System.out.println("Inorder traversal:");
```

```
tree.inorder();
```

```
}
```

```
}
```



**PROGRAM:** Implement a Binary Tree: Write a class to implement a basic binary tree with insert, delete.

```
class InorderTraversal {  
    class Node {  
        int key;  
        Node left, right;  
  
        Node(int item) {  
            key = item;  
            left = right = null;  
        }  
    }  
  
    Node root;  
  
    void insert(int key) {  
        root = insertRec(root, key);  
    }  
  
    Node insertRec(Node root, int key) {  
        if (root == null) {  
            root = new Node(key);  
            return root;  
        }  
        if (key < root.key) root.left = insertRec(root.left, key);  
        else if (key > root.key) root.right = insertRec(root.right, key);  
        return root;  
    }  
  
    void inorder() {  
        System.out.print("Inorder Traversal: ");  
    }  
}
```

```
        inorderRec(root);  
        System.out.println();  
    }
```

```
void inorderRec(Node root) {  
    if (root != null) {  
        inorderRec(root.left);  
        System.out.print(root.key + " ");  
        inorderRec(root.right);  
    }  
}
```

```
public static void main(String[] args) {  
    InorderTraversal tree = new InorderTraversal();  
    tree.insert(50);  
    tree.insert(30);  
    tree.insert(20);  
    tree.insert(40);  
    tree.inorder();  
}
```

**PROGRAM:** Preorder Traversal: Write a function to perform preorder traversal of a binary tree.

```
class PreorderTraversal {  
  
    class Node {  
  
        int key;  
  
        Node left, right;  
  
        Node(int item) {  
            key = item;  
            left = right = null;  
        }  
    }  
  
    Node root;  
  
    void insert(int key) {  
        root = insertRec(root, key);  
    }  
  
    Node insertRec(Node root, int key) {  
        if (root == null) {  
            root = new Node(key);  
            return root;  
        }  
        if (key < root.key) root.left = insertRec(root.left, key);  
        else if (key > root.key) root.right = insertRec(root.right, key);  
        return root;  
    }  
  
    void preorder() {  
        System.out.print("Preorder Traversal: ");  
    }  
}
```

```
    preorderRec(root);  
    System.out.println();  
}
```

```
void preorderRec(Node root) {  
    if (root != null) {  
        System.out.print(root.key + " ");  
        preorderRec(root.left);  
        preorderRec(root.right);  
    }  
}
```

```
public static void main(String[] args) {  
    PreorderTraversal tree = new PreorderTraversal();  
    tree.insert(50); tree.insert(30); tree.insert(20);  
    tree.insert(40); tree.insert(70); tree.insert(60); tree.insert(80);  
    tree.preorder();  
}
```

**PROGRAM:** Postorder Traversal: Write a function to perform postorder traversal of a binary tree.

```
class PostorderTraversal {  
    class Node {  
        int key;  
        Node left, right;  
  
        Node(int item) {  
            key = item;  
            left = right = null;  
        }  
    }  
  
    Node root;  
  
    void insert(int key) {  
        root = insertRec(root, key);  
    }  
  
    Node insertRec(Node root, int key) {  
        if (root == null) {  
            root = new Node(key);  
            return root;  
        }  
        if (key < root.key) root.left = insertRec(root.left, key);  
        else if (key > root.key) root.right = insertRec(root.right, key);  
        return root;  
    }  
  
    void postorder() {  
        System.out.print("Postorder Traversal: ");  
    }  
}
```

```
    postorderRec(root);  
    System.out.println();  
}
```

```
void postorderRec(Node root) {  
    if (root != null) {  
        postorderRec(root.left);  
        postorderRec(root.right);  
        System.out.print(root.key + " ");  
    }  
}
```

```
public static void main(String[] args) {  
    PostorderTraversal tree = new PostorderTraversal();  
    tree.insert(50); tree.insert(30); tree.insert(20);  
    tree.insert(40); tree.insert(70); tree.insert(60); tree.insert(80);  
    tree.postorder();  
}
```

**PROGRAM:** Level Order Traversal: Write a function to perform level order traversal of a binary tree.

```
import java.util.LinkedList;
```

```
import java.util.Queue;
```

```
class LevelOrderTraversal {
```

```
    class Node {
```

```
        int key;
```

```
        Node left, right;
```

```
        Node(int item) {
```

```
            key = item;
```

```
            left = right = null;
```

```
        }
```

```
    }
```

```
    Node root;
```

```
    void insert(int key) {
```

```
        root = insertRec(root, key);
```

```
    }
```

```
    Node insertRec(Node root, int key) {
```

```
        if (root == null) {
```

```
            root = new Node(key);
```

```
            return root;
```

```
        }
```

```
        if (key < root.key) root.left = insertRec(root.left, key);
```

```
        else if (key > root.key) root.right = insertRec(root.right, key);
```

```
        return root;
```

```
}
```

```
void levelOrder() {
```

```
    System.out.print("Level Order Traversal: ");
```

```
    if (root == null) return;
```

```
    Queue<Node> queue = new LinkedList<>();
```

```
    queue.add(root);
```

```
    while (!queue.isEmpty()) {
```

```
        Node tempNode = queue.poll();
```

```
        System.out.print(tempNode.key + " ");
```

```
        if (tempNode.left != null) queue.add(tempNode.left);
```

```
        if (tempNode.right != null) queue.add(tempNode.right);
```

```
    }
```

```
    System.out.println();
```

```
}
```

```
public static void main(String[] args) {
```

```
    LevelOrderTraversal tree = new LevelOrderTraversal();
```

```
    tree.insert(50); tree.insert(30); tree.insert(20);
```

```
    tree.insert(40); tree.insert(70); tree.insert(60); tree.insert(80);
```

```
    tree.levelOrder();
```

```
}
```

```
}
```



**PROGRAM:** Height of a Binary Tree: Write a function to find the height of a binary tree.

```
class BinaryTreeHeight {  
    class Node {  
        int key;  
        Node left, right;  
  
        public Node(int item) {  
            key = item;  
            left = right = null;  
        }  
    }  
  
    Node root;  
  
    // Function to insert nodes in the binary tree  
    void insert(int key) {  
        root = insertRec(root, key);  
    }  
  
    Node insertRec(Node root, int key) {  
        if (root == null) {  
            root = new Node(key);  
            return root;  
        }  
        if (key < root.key)  
            root.left = insertRec(root.left, key);  
        else if (key > root.key)  
            root.right = insertRec(root.right, key);  
        return root;  
    }  
}
```

```

    }

    // Function to calculate the height of the binary tree
    int height(Node node) {
        if (node == null) {
            return 0; // Base case: height of an empty tree is 0
        }

        // Recursively find the height of left and right subtrees
        int leftHeight = height(node.left);
        int rightHeight = height(node.right);

        // Height of the tree is the maximum of the two subtree heights + 1
        return Math.max(leftHeight, rightHeight) + 1;
    }

    public static void main(String[] args) {
        BinaryTreeHeight tree = new BinaryTreeHeight();

        // Insert nodes into the binary tree
        tree.insert(50);
        tree.insert(30);
        tree.insert(20);
        tree.insert(40);

        // Calculate and print the height of the binary tree
        int treeHeight = tree.height(tree.root);
        System.out.println("Height of the Binary Tree: " + treeHeight);
    }
}

```

**PROGRAM:** Diameter of a Binary Tree: Write a function to find the diameter of a binary tree.

```
class DiameterBinaryTree {  
    class Node {  
        int key;  
        Node left, right;  
  
        public Node(int item) {  
            key = item;  
            left = right = null;  
        }  
    }  
  
    Node root;  
  
    int diameter(Node root) {  
        int[] diameter = new int[1]; // To store the result  
        height(root, diameter);  
        return diameter[0];  
    }  
  
    int height(Node node, int[] diameter) {  
        if (node == null) {  
            return 0;  
        }  
  
        int leftHeight = height(node.left, diameter);  
        int rightHeight = height(node.right, diameter);  
        diameter[0] = Math.max(diameter[0], leftHeight + rightHeight);  
        return Math.max(leftHeight, rightHeight) + 1;  
    }  
}
```

```
public static void main(String[] args) {  
    DiameterBinaryTree tree = new DiameterBinaryTree();  
    tree.root = tree.new Node(1);  
    tree.root.left = tree.new Node(2);  
    tree.root.right = tree.new Node(3);  
    tree.root.left.left = tree.new Node(4);  
    tree.root.left.right = tree.new Node(5);  
  
    System.out.println("Diameter of the tree: " + tree.diameter(tree.root));  
}  
}
```

**PROGRAM:** Check if a Binary Tree is Balanced: Write a function to check if a binary tree is height.

```
class BalancedBinaryTree {  
    class Node {  
        int key;  
        Node left, right;  
  
        public Node(int item) {  
            key = item;  
            left = right = null;  
        }  
    }  
    Node root;  
  
    boolean isBalanced(Node root) {  
        return checkHeight(root) != -1;  
    }  
  
    int checkHeight(Node node) {  
        if (node == null) return 0;  
  
        int leftHeight = checkHeight(node.left);  
        if (leftHeight == -1) return -1;  
  
        int rightHeight = checkHeight(node.right);  
        if (rightHeight == -1) return -1;  
  
        if (Math.abs(leftHeight - rightHeight) > 1) return -1;  
  
        return Math.max(leftHeight, rightHeight) + 1;  
    }  
}
```

```
}
```

```
public static void main(String[] args) {
```

```
    BalancedBinaryTree tree = new BalancedBinaryTree();
```

```
    tree.root = tree.new Node(1);
```

```
    tree.root.left = tree.new Node(2);
```

```
    tree.root.right = tree.new Node(3);
```

```
    tree.root.left.left = tree.new Node(4);
```

```
    tree.root.left.right = tree.new Node(5);
```

```
    System.out.println("Is the tree balanced? " + tree.isBalanced(tree.root));
```

```
}
```

```
}
```

**PROGRAM:** Lowest Common Ancestor: Write a function to find the lowest common ancestor of two nodes in a binary tree.

```
class LCABinaryTree {  
    class Node {  
        int key;  
        Node left, right;  
  
        public Node(int item) {  
            key = item;  
            left = right = null;  
        }  
    }  
  
    Node root;  
  
    Node findLCA(Node root, int n1, int n2) {  
        if (root == null) return null;  
  
        if (root.key == n1 || root.key == n2) return root;  
  
        Node leftLCA = findLCA(root.left, n1, n2);  
        Node rightLCA = findLCA(root.right, n1, n2);  
  
        if (leftLCA != null && rightLCA != null) return root;  
  
        return (leftLCA != null) ? leftLCA : rightLCA;  
    }  
  
    public static void main(String[] args) {  
        LCABinaryTree tree = new LCABinaryTree();  
    }  
}
```

```
tree.root = tree.new Node(3);
tree.root.left = tree.new Node(5);
tree.root.right = tree.new Node(1);
tree.root.left.left = tree.new Node(6);
tree.root.left.right = tree.new Node(2);

System.out.println("LCA of 5 and 1: " + tree.findLCA(tree.root, 5, 1).key);
System.out.println("LCA of 6 and 2: " + tree.findLCA(tree.root, 6, 2).key);
}
}
```



**PROGRAM:** Implement Graph Using Adjacency List: Write a class to implement a basic graph using an adjacency list with methods to add vertices and edges.

```
import java.util.*;

class Graph {

    private Map<Integer, List<Integer>> adjList;

    public Graph() {
        adjList = new HashMap<>();
    }

    // Add a vertex
    void addVertex(int v) {
        adjList.putIfAbsent(v, new ArrayList<>());
    }

    // Add an edge
    void addEdge(int src, int dest) {
        adjList.putIfAbsent(src, new ArrayList<>());
        adjList.putIfAbsent(dest, new ArrayList<>());
        adjList.get(src).add(dest);
        adjList.get(dest).add(src); // For undirected graph
    }

    // Print the graph
    void printGraph() {
        for (var entry : adjList.entrySet()) {
            System.out.print(entry.getKey() + " -> ");
            for (int neighbor : entry.getValue()) {
```

```
        System.out.print(neighbor + " ");  
    }  
    System.out.println();  
}  
}
```

```
public static void main(String[] args) {  
    Graph graph = new Graph();  
  
    graph.addVertex(1);  
    graph.addVertex(2);  
    graph.addVertex(3);  
    graph.addVertex(4);  
  
    graph.addEdge(1, 2);  
    graph.addEdge(1, 3);  
    graph.addEdge(2, 4);  
  
    graph.printGraph();  
}  
}
```

**PROGRAM:** Breadth-First Search (BFS): Write a function to perform BFS on a graph from a given start vertex.

```
import java.util.*;

class GraphBFS {

    private Map<Integer, List<Integer>> adjList = new HashMap<>();

    void addEdge(int src, int dest) {
        adjList.putIfAbsent(src, new ArrayList<>());
        adjList.putIfAbsent(dest, new ArrayList<>());
        adjList.get(src).add(dest);
        adjList.get(dest).add(src); // For undirected graph
    }

    void bfs(int startVertex) {
        Set<Integer> visited = new HashSet<>();
        Queue<Integer> queue = new LinkedList<>();

        queue.add(startVertex);
        visited.add(startVertex);

        while (!queue.isEmpty()) {
            int vertex = queue.poll();
            System.out.print(vertex + " ");

            for (int neighbor : adjList.get(vertex)) {
                if (!visited.contains(neighbor)) {
                    queue.add(neighbor);
                    visited.add(neighbor);
                }
            }
        }
    }
}
```

```
    }  
    }  
}
```

```
public static void main(String[] args) {  
    GraphBFS graph = new GraphBFS();  
    graph.addEdge(1, 2);  
    graph.addEdge(1, 3);  
    graph.addEdge(2, 4);  
    graph.addEdge(3, 5);  
  
    System.out.print("BFS starting from vertex 1: ");  
    graph.bfs(1);  
}  
}
```

**PROGRAM:** Depth-First Search (DFS): Write a function to perform DFS on a graph from a given start vertex.

```
import java.util.*;

class GraphDFS {

    private Map<Integer, List<Integer>> adjList = new HashMap<>();

    void addEdge(int src, int dest) {
        adjList.putIfAbsent(src, new ArrayList<>());
        adjList.putIfAbsent(dest, new ArrayList<>());
        adjList.get(src).add(dest);
        adjList.get(dest).add(src); // For undirected graph
    }

    void dfs(int startVertex) {
        Set<Integer> visited = new HashSet<>();
        dfsHelper(startVertex, visited);
    }

    private void dfsHelper(int vertex, Set<Integer> visited) {
        visited.add(vertex);
        System.out.print(vertex + " ");

        for (int neighbor : adjList.get(vertex)) {
            if (!visited.contains(neighbor)) {
                dfsHelper(neighbor, visited);
            }
        }
    }
}
```

```
public static void main(String[] args) {  
    GraphDFS graph = new GraphDFS();  
    graph.addEdge(1, 2);  
    graph.addEdge(1, 3);  
    graph.addEdge(2, 4);  
    graph.addEdge(3, 5);  
  
    System.out.print("DFS starting from vertex 1: ");  
    graph.dfs(1);  
}  
}
```

**PROGRAM:** Detect Cycle in an Undirected Graph: Write a function to detect if there is a cycle in an undirected graph.

```
import java.util.*;

class GraphCycleDetection {

    private Map<Integer, List<Integer>> adjList = new HashMap<>();

    void addEdge(int src, int dest) {
        adjList.putIfAbsent(src, new ArrayList<>());
        adjList.putIfAbsent(dest, new ArrayList<>());
        adjList.get(src).add(dest);
        adjList.get(dest).add(src);
    }

    boolean hasCycle() {
        Set<Integer> visited = new HashSet<>();
        for (int vertex : adjList.keySet()) {
            if (!visited.contains(vertex)) {
                if (detectCycle(vertex, -1, visited)) {
                    return true;
                }
            }
        }
        return false;
    }

    private boolean detectCycle(int current, int parent, Set<Integer> visited) {
        visited.add(current);

        for (int neighbor : adjList.get(current)) {
            if (neighbor == parent) continue;
            if (visited.contains(neighbor)) return true;
            if (detectCycle(neighbor, current, visited)) return true;
        }
        return false;
    }
}
```

```
        if (!visited.contains(neighbor)) {  
            if (detectCycle(neighbor, current, visited)) {  
                return true;  
            }  
        } else if (neighbor != parent) {  
            return true;  
        }  
    }  
    return false;  
}
```

```
public static void main(String[] args) {  
    GraphCycleDetection graph = new GraphCycleDetection();  
    graph.addEdge(1, 2);  
    graph.addEdge(1, 3);  
    graph.addEdge(2, 3);  
  
    System.out.println("Does the graph have a cycle? " + graph.hasCycle());  
}  
}
```



**PROGRAM:** Connected Components in an Undirected Graph: Write a function to find the number of connected components in an undirected graph.

```
import java.util.*;

class GraphConnectedComponents {

    private Map<Integer, List<Integer>> adjList = new HashMap<>();

    void addEdge(int src, int dest) {
        adjList.putIfAbsent(src, new ArrayList<>());
        adjList.putIfAbsent(dest, new ArrayList<>());
        adjList.get(src).add(dest);
        adjList.get(dest).add(src);
    }

    int countConnectedComponents() {
        Set<Integer> visited = new HashSet<>();
        int count = 0;

        for (int vertex : adjList.keySet()) {
            if (!visited.contains(vertex)) {
                dfs(vertex, visited);
                count++;
            }
        }
        return count;
    }

    private void dfs(int vertex, Set<Integer> visited) {
        visited.add(vertex);
```

```
    for (int neighbor : adjList.get(vertex)) {  
        if (!visited.contains(neighbor)) {  
            dfs(neighbor, visited);  
        }  
    }  
}
```

```
public static void main(String[] args) {  
    GraphConnectedComponents graph = new GraphConnectedComponents();  
    graph.addEdge(1, 2);  
    graph.addEdge(3, 4);  
    graph.addEdge(5, 6);  
  
    System.out.println("Number of connected components: " +  
graph.countConnectedComponents());  
}
```

**PROGRAM:** Find MST Using Kruskal's Algorithm: Write a function to find the Minimum Spanning Tree of a graph using Kruskal's algorithm.

```
import java.util.*;

class KruskalMST {

    class Edge implements Comparable<Edge> {

        int src, dest, weight;

        Edge(int src, int dest, int weight) {

            this.src = src;
            this.dest = dest;
            this.weight = weight;
        }

        public int compareTo(Edge other) {

            return this.weight - other.weight;
        }
    }

    class Subset {

        int parent, rank;
    }

    int vertices;

    List<Edge> edges = new ArrayList<>();

    KruskalMST(int vertices) {

        this.vertices = vertices;
    }
}
```

```
void addEdge(int src, int dest, int weight) {  
    edges.add(new Edge(src, dest, weight));  
}
```

```
int find(Subset[] subsets, int i) {  
    if (subsets[i].parent != i) {  
        subsets[i].parent = find(subsets, subsets[i].parent);  
    }  
    return subsets[i].parent;  
}
```

```
void union(Subset[] subsets, int x, int y) {  
    int xRoot = find(subsets, x);  
    int yRoot = find(subsets, y);  
  
    if (subsets[xRoot].rank < subsets[yRoot].rank) {  
        subsets[xRoot].parent = yRoot;  
    } else if (subsets[xRoot].rank > subsets[yRoot].rank) {  
        subsets[yRoot].parent = xRoot;  
    } else {  
        subsets[yRoot].parent = xRoot;  
        subsets[xRoot].rank++;  
    }  
}
```

```
void kruskalMST() {  
    List<Edge> result = new ArrayList<>();  
    Collections.sort(edges);  
  
    Subset[] subsets = new Subset[vertices];  
    for (int i = 0; i < vertices; i++) {
```

```

        subsets[i] = new Subset();
        subsets[i].parent = i;
        subsets[i].rank = 0;
    }

    for (Edge edge : edges) {
        int x = find(subsets, edge.src);
        int y = find(subsets, edge.dest);

        if (x != y) {
            result.add(edge);
            union(subsets, x, y);
        }
    }

    System.out.println("Edges in MST:");
    for (Edge edge : result) {
        System.out.println(edge.src + " - " + edge.dest + ": " + edge.weight);
    }
}

public static void main(String[] args) {
    KruskalMST graph = new KruskalMST(4);

    graph.addEdge(0, 1, 10);
    graph.addEdge(0, 2, 6);
    graph.addEdge(0, 3, 5);
    graph.kruskalMST();
}
}

```

**PROGRAM:** Find MST Using Prim's Algorithm: Write a function to find the Minimum Spanning Tree of a graph using Prim's algorithm.

```
import java.util.*;

class PrimMST {
    int vertices;

    PrimMST(int vertices) {
        this.vertices = vertices;
    }

    void primMST(int[][] graph) {
        int[] parent = new int[vertices];
        int[] key = new int[vertices];
        boolean[] mstSet = new boolean[vertices];

        Arrays.fill(key, Integer.MAX_VALUE);
        key[0] = 0;
        parent[0] = -1;

        for (int count = 0; count < vertices - 1; count++) {
            int u = minKey(key, mstSet);
            mstSet[u] = true;

            for (int v = 0; v < vertices; v++) {
                if (graph[u][v] != 0 && !mstSet[v] && graph[u][v] < key[v]) {
                    parent[v] = u;
                    key[v] = graph[u][v];
                }
            }
        }
    }
}
```

```
    printMST(parent, graph);  
}
```

```
int minKey(int[] key, boolean[] mstSet) {  
    int min = Integer.MAX_VALUE, minIndex = -1;  
  
    for (int v = 0; v < vertices; v++) {  
        if (!mstSet[v] && key[v] < min) {  
            min = key[v];  
            minIndex = v;  
        }  
    }  
  
    return minIndex;  
}
```

```
void printMST(int[] parent, int[][] graph) {  
    System.out.println("Edge \tWeight");  
    for (int i = 1; i < vertices; i++) {  
        System.out.println(parent[i] + " - " + i + "\t" + graph[i][parent[i]]);  
    }  
}
```

```
public static void main(String[] args) {  
    PrimMST graph = new PrimMST(5);  
    int[][] matrix = {  
        {0, 2, 0, 6, 0},  
        {2, 0, 3, 8, 5},  
        {0, 3, 0, 0, 7},  
    };  
    graph.primMST(matrix);  
} }
```

**PROGRAM:** Fibonacci Sequence: Write a function to compute the nth Fibonacci number using dynamic programming.

```
class FibonacciDP {  
    int fibonacci(int n) {  
        if (n <= 1) return n;  
  
        int[] dp = new int[n + 1];  
        dp[0] = 0;  
        dp[1] = 1;  
  
        for (int i = 2; i <= n; i++) {  
            dp[i] = dp[i - 1] + dp[i - 2];  
        }  
  
        return dp[n];  
    }  
  
    public static void main(String[] args) {  
        FibonacciDP fib = new FibonacciDP();  
        int n = 10;  
        System.out.println("Fibonacci number at position " + n + ": " +  
fib.fibonacci(n));  
    }  
}
```



**PROGRAM:** Climbing Stairs: Write a function to determine how many distinct ways there are to climb a staircase with n steps if you can climb either 1 or 2 steps at a time.

```
class ClimbingStairs {  
    int countWays(int n) {  
        if (n <= 1) return 1;  
  
        int[] dp = new int[n + 1];  
        dp[0] = 1;  
        dp[1] = 1;  
  
        for (int i = 2; i <= n; i++) {  
            dp[i] = dp[i - 1] + dp[i - 2];  
        }  
  
        return dp[n];  
    }  
  
    public static void main(String[] args) {  
        ClimbingStairs stairs = new ClimbingStairs();  
        int n = 5; // Example: 5 steps  
        System.out.println("Number of ways to climb " + n + " steps: " +  
            stairs.countWays(n));  
    }  
}
```

**PROGRAM:** Min Cost Climbing Stairs: Write a function to determine the minimum cost to reach the top of a staircase given a list of costs associated with each step.

```
class MinCostClimbingStairs {  
    int minCost(int[] cost) {  
        int n = cost.length;  
        if (n == 0) return 0;  
        if (n == 1) return cost[0];  
  
        int[] dp = new int[n];  
        dp[0] = cost[0];  
        dp[1] = cost[1];  
  
        for (int i = 2; i < n; i++) {  
            dp[i] = cost[i] + Math.min(dp[i - 1], dp[i - 2]);  
        }  
  
        return Math.min(dp[n - 1], dp[n - 2]);  
    }  
  
    public static void main(String[] args) {  
        MinCostClimbingStairs stairs = new MinCostClimbingStairs();  
        int[] cost = {10, 15, 20}; // Example: Costs at each step  
        System.out.println("Minimum cost to reach the top: " +  
            stairs.minCost(cost));  
    }  
}
```

**PROGRAM:** House Robber: Write a function to determine the maximum amount of money you can rob from a row of houses without robbing two adjacent houses.

```
class HouseRobber {  
    int rob(int[] nums) {  
        if (nums.length == 0) return 0;  
        if (nums.length == 1) return nums[0];  
  
        int prev2 = 0, prev1 = 0;  
        for (int num : nums) {  
            int temp = prev1;  
            prev1 = Math.max(prev1, prev2 + num);  
            prev2 = temp;  
        }  
  
        return prev1;  
    }  
  
    public static void main(String[] args) {  
        HouseRobber robber = new HouseRobber();  
        int[] nums = {2, 7, 9, 3, 1}; // Example: Amounts of money in houses  
        System.out.println("Maximum money that can be robbed: " +  
            robber.rob(nums));  
    }  
}
```

**PROGRAM:** Maximum Subarray Sum (Kadane's Algorithm): Write a function to find the contiguous subarray with the maximum sum.

```
class MaximumSubarraySum {  
    int maxSubArray(int[] nums) {  
        int maxSoFar = nums[0];  
        int maxEndingHere = nums[0];  
  
        for (int i = 1; i < nums.length; i++) {  
            maxEndingHere = Math.max(nums[i], maxEndingHere + nums[i]);  
            maxSoFar = Math.max(maxSoFar, maxEndingHere);  
        }  
  
        return maxSoFar;  
    }  
  
    public static void main(String[] args) {  
        MaximumSubarraySum maxSum = new MaximumSubarraySum();  
        int[] nums = {-2, 1, -3, 4, -1, 2, 1, -5, 4}; // Example array  
        System.out.println("Maximum subarray sum: " +  
maxSum.maxSubArray(nums));  
    }  
}
```

**PROGRAM:** Activity Selection: Given a set of activities with start and end times, select the maximum number of activities that do not overlap.

```
import java.util.*;

class ActivitySelection {
    static class Activity {
        int start, end;

        Activity(int start, int end) {
            this.start = start;
            this.end = end;
        }
    }

    void selectActivities(Activity[] activities) {
        Arrays.sort(activities, Comparator.comparingInt(a -> a.end)); // Sort by
end time

        List<Activity> selected = new ArrayList<>();
        selected.add(activities[0]);

        int lastEndTime = activities[0].end;

        for (int i = 1; i < activities.length; i++) {
            if (activities[i].start >= lastEndTime) {
                selected.add(activities[i]);
            }
        }
    }
}
```

```
        lastEndTime = activities[i].end;
    }
}
```

```
System.out.println("Selected activities:");
for (Activity activity : selected) {
    System.out.println("Start: " + activity.start + ", End: " + activity.end);
}
}
```

```
public static void main(String[] args) {
    ActivitySelection selection = new ActivitySelection();
    Activity[] activities = {
        new Activity(1, 3),
        new Activity(2, 5),
        new Activity(4, 7),
        new Activity(6, 8),
        new Activity(5, 9)
    };

    selection.selectActivities(activities);
}
}
```

**PROGRAM:** Fractional Knapsack Problem: Given weights and values of items and the maximum capacity of a knapsack, determine the maximum value that can be obtained by including fractions of items.

```
import java.util.*;
```

```
class FractionalKnapsack {
```

```
    static class Item {
```

```
        int weight, value;
```

```
        Item(int weight, int value) {
```

```
            this.weight = weight;
```

```
            this.value = value;
```

```
        }
```

```
    }
```

```
    double knapSack(int W, Item[] items) {
```

```
        Arrays.sort(items, (a, b) -> Double.compare(b.value * 1.0 / b.weight,  
a.value * 1.0 / a.weight));
```

```
        double totalValue = 0;
```

```
        for (Item item : items) {
```

```
            if (W == 0) break;
```

```
            if (item.weight <= W) {
```

```
                totalValue += item.value;
```

```
                W -= item.weight;
```

```
        } else {  
            totalValue += item.value * ((double) W / item.weight);  
            break;  
        }  
    }  
}  
  
return totalValue;  
}
```

```
public static void main(String[] args) {  
    FractionalKnapsack knapsack = new FractionalKnapsack();  
    Item[] items = {  
        new Item(60, 100),  
        new Item(100, 120),  
        new Item(120, 150)  
    };  
  
    int W = 50; // Maximum weight capacity of the knapsack  
    System.out.println("Maximum value we can obtain: " +  
        knapsack.knapSack(W, items));  
}  
}
```



**PROGRAM:** Huffman Coding: Given a set of characters and their frequencies, construct the Huffman Tree to encode the characters.

```
import java.util.*;

class HuffmanCoding {

    static class Node {

        char ch;

        int freq;

        Node left, right;

        Node(char ch, int freq) {

            this.ch = ch;

            this.freq = freq;

            this.left = this.right = null;

        }

    }

    static class MinHeap {

        List<Node> heap;

        MinHeap() {

            heap = new ArrayList<>();

        }

        void insert(Node node) {

            heap.add(node);

            int i = heap.size() - 1;

            while (i > 0 && heap.get(i).freq < heap.get((i - 1) / 2).freq) {

                Collections.swap(heap, i, (i - 1) / 2);

                i = (i - 1) / 2;

            }

        }

    }

}
```

```

    }
}

Node extractMin() {
    Node min = heap.get(0);
    heap.set(0, heap.get(heap.size() - 1));
    heap.remove(heap.size() - 1);
    minHeapify(0);
    return min;
}

void minHeapify(int i) {
    int left = 2 * i + 1, right = 2 * i + 2;
    int smallest = i;

    if (left < heap.size() && heap.get(left).freq < heap.get(smallest).freq) {
        smallest = left;
    }

    if (right < heap.size() && heap.get(right).freq < heap.get(smallest).freq) {
        smallest = right;
    }

    if (smallest != i) {
        Collections.swap(heap, i, smallest);
        minHeapify(smallest);
    }
}

void buildHuffmanTree(Map<Character, Integer> freqMap) {

```

```

MinHeap minHeap = new MinHeap();
for (Map.Entry<Character, Integer> entry : freqMap.entrySet()) {
    minHeap.insert(new Node(entry.getKey(), entry.getValue()));
}

while (minHeap.heap.size() > 1) {
    Node left = minHeap.extractMin();
    Node right = minHeap.extractMin();
    Node merged = new Node('$', left.freq + right.freq);
    merged.left = left;
    merged.right = right;
    minHeap.insert(merged);
}

Node root = minHeap.extractMin();
printCodes(root, "");
}

void printCodes(Node root, String code) {
    if (root == null) return;
    if (root.ch != '$') {
        System.out.println(root.ch + ": " + code);
    }
    printCodes(root.left, code + "0");
    printCodes(root.right, code + "1");
}

public static void main(String[] args) {
    HuffmanCoding huffman = new HuffmanCoding();
    Map<Character, Integer> freqMap = new HashMap<>();
    freqMap.put('a', 5);

```

```
freqMap.put('b', 9);  
freqMap.put('c', 12);  
freqMap.put('d', 13);  
freqMap.put('e', 16);  
freqMap.put('f', 45);  
  
huffman.buildHuffmanTree(freqMap);  
}  
}
```

**PROGRAM:** Job Sequencing Problem: Given a set of jobs, each with a deadline and profit, maximize the total profit by scheduling the jobs to be done before their deadlines.

```
import java.util.*;
```

```
class JobSequencing {
```

```
    static class Job {
```

```
        int id, deadline, profit;
```

```
        Job(int id, int deadline, int profit) {
```

```
            this.id = id;
```

```
            this.deadline = deadline;
```

```
            this.profit = profit;
```

```
        }
```

```
    }
```

```
    void jobScheduling(Job[] jobs, int n) {
```

```
        Arrays.sort(jobs, (a, b) -> b.profit - a.profit); // Sort jobs by profit in  
        descending order
```

```
        boolean[] slots = new boolean[n];
```

```
        Arrays.fill(slots, false);
```

```
        int maxProfit = 0;
```

```
        List<Integer> jobSequence = new ArrayList<>();
```

```
        for (Job job : jobs) {
```

```

        for (int j = job.deadline - 1; j >= 0; j--) {
            if (!slots[j]) {
                slots[j] = true;
                maxProfit += job.profit;
                jobSequence.add(job.id);
                break;
            }
        }
    }

    System.out.println("Job sequence: " + jobSequence);
    System.out.println("Total profit: " + maxProfit);
}

```

```

public static void main(String[] args) {
    JobSequencing scheduling = new JobSequencing();
    Job[] jobs = {
        new Job(1, 4, 20),
        new Job(2, 1, 10),
        new Job(3, 1, 40),
        new Job(4, 1, 30)
    };
    int n = 4;
    scheduling.jobScheduling(jobs, n);
}
}

```

**PROGRAM:** Minimum Number of Coins: Given different denominations of coins and an amount, find the minimum number of coins needed to make up that amount.

```
import java.util.*;

class MinimumCoins {

    int minCoins(int[] coins, int amount) {

        int[] dp = new int[amount + 1];

        Arrays.fill(dp, Integer.MAX_VALUE);

        dp[0] = 0;

        for (int i = 1; i <= amount; i++) {

            for (int coin : coins) {

                if (i - coin >= 0 && dp[i - coin] != Integer.MAX_VALUE) {

                    dp[i] = Math.min(dp[i], dp[i - coin] + 1);

                }

            }

        }

        return dp[amount] == Integer.MAX_VALUE ? -1 : dp[amount];

    }

    public static void main(String[] args) {

        MinimumCoins coins = new MinimumCoins();

        int[] coinDenominations = {1, 2, 5}; // Coin denominations

        int amount = 11;

        System.out.println("Minimum coins required: " + coins.minCoins(coinDenominations, amount));

    }

}
```

**PROGRAM:** N-Queens Problem: Place N queens on an N×N chessboard so that no two queens threaten each other.

```
class NQueens {  
    static final int N = 4;  
  
    boolean isSafe(int[][] board, int row, int col) {  
        for (int i = 0; i < col; i++) {  
            if (board[row][i] == 1) return false;  
        }  
  
        for (int i = row, j = col; i >= 0 && j >= 0; i--, j--) {  
            if (board[i][j] == 1) return false;  
        }  
  
        for (int i = row, j = col; j >= 0 && i < N; i++, j--) {  
            if (board[i][j] == 1) return false;  
        }  
  
        return true;  
    }  
  
    boolean solveNQueens(int[][] board, int col) {  
        if (col >= N) return true;  
  
        for (int i = 0; i < N; i++) {
```



```

        if (isSafe(board, i, col)) {
            board[i][col] = 1;
            if (solveNQueens(board, col + 1)) return true;
            board[i][col] = 0;
        }
    }

    return false;
}

void printSolution(int[][] board) {
    for (int i = 0; i < N; i++) {
        for (int j = 0; j < N; j++) {
            System.out.print(board[i][j] + " ");
        }
        System.out.println();
    }
}

public static void main(String[] args) {
    NQueens queens = new NQueens();
    int[][] board = new int[N][N];

    if (queens.solveNQueens(board, 0)) {
        queens.printSolution(board);
    } else {

```

```
        System.out.println("Solution does not exist");  
    }  
}  
}
```