Team production: a network study of publications in Economics

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Intro

I hope to study

Intro

Motivation

- Is teamwork more productive than solo-work?
- Does team-size alone have an effect?
- Can we empirically study properties of a team production?
 - Additivity?
 - Complementarity?
- Should the planner group workers of similar types? Or should they group workers with very different (high/low) types?

Some challenges

Intro

Motivation

- We only observe team output as Y and a vector of authors as X. Note that the academic production network is different from the trade production network, because economists can usually observe the firm inputs in the the latter case.
- Some authors don't have solo publications. How to infer their contribution?
- Collaboration (network) matrix is very sparse.

Intro

Model of fixed-effects

Preview of conclusion: my paper attempts to give empirical evidence on some properties of team production function

In my model of two-person team production function for paper ℓ ,

$$y_{\ell}^{(2)}(\alpha_1, \alpha_2) = \lambda_2(\alpha_1 + \alpha_2) + f(\alpha_1, \alpha_2) + \epsilon_{\ell}$$

- Linear component $\alpha_1 + \alpha_2$, scaled by team-size effects
- Non-linear component $f(\alpha_1, \alpha_2)$
 - Positive marginal effect: $\lambda_2 + \frac{\partial f}{\partial \alpha_i} > 0$
 - Strong asymmetry in individual marginal effects
 - Supermodularity: $\frac{\partial^2 f}{\partial \alpha_1 \alpha_2} > 0$
 - Potentially right-skewed shock ϵ : a positive shock is more likely than a negative shock

Literature

Intro

Literature

My dissertation is heavily motivated by Bonhomme (2021).

What's similar

- Linear fixed-effects approach
- Use of Moore-Penrose inverse (pseudo-inverse) in the least-square estimation.

What's new

- Bonhomme (2021) focuses on the methodology of estimating fixed-effects model and random-effects model. Based on his fixed-effects model. I use a LS model with stronger but simplifying assumptions. I also explore some interesting properties of team production.
- Bonhomme (2021)'s identification requires variations in the team composition. If two people always work together, their types aren't identified. My identification requires economists to have at least one solo, one 2-person, and one 3-person publications so that their type and the team-size effects can be identified.
- Herkenhoff et al. (2018) uses wage as a proxy of human capital to study team production. My approach does not rely on wage data.

Model of fixed-effects Team-size effect Supermodularity Potentially Right-skewed shock Put it all together 00000

Robustness Check

Intro

Literature

- I tried other choices of dependent variables. This paper quantifies paper quality by journal quality which is then proxied by the (Clarivate) impact factor However, I also tried other dependent variables such as VWL Ranking Deutschland but the results turn out to be very similar.
- In addition to econometricians, I also repeat my estimation on macro and micro theorists. Most results agree.





Additive model of fixed effects

$$\begin{cases} Y_{\ell}^{(1)} = \alpha_i^{(1)} + \epsilon_{\ell}^{(1)} \\ Y_{\ell}^{(2)} = \alpha_i^{(2)} + \alpha_j^{(2)} + \epsilon_{\ell}^{(2)} = \lambda_2(\alpha_i^{(1)} + \alpha_j^{(1)}) + \epsilon_{\ell}^{(2)} \\ Y_{\ell}^{(3)} = \alpha_i^{(3)} + \alpha_j^{(3)} + \alpha_k^{(3)} + \epsilon_{\ell}^{(3)} = \lambda_3(\alpha_i^{(1)} + \alpha_j^{(1)} + \alpha_k^{(1)}) + \epsilon_{\ell}^{(3)} \end{cases}$$

In vector notations,

$$\begin{cases} Y^{(1)} = X_1 \alpha^{(1)} + \epsilon^{(1)} & \text{i j k} \\ Y^{(2)} = \lambda_2 \cdot X_2 \alpha^{(1)} + \epsilon^{(2)} \\ Y^{(3)} = \lambda_3 \cdot X_3 \alpha^{(1)} + \epsilon^{(3)}, \end{cases} \quad X^{(1)} = \begin{cases} \ell_1 & \text{i j k} \\ \ell_1 & \text{i i j k} \\ \ell_1 & \text{i i j k} \\ \ell_2 & \text{i i j k} \\ \ell_2 & \text{i i j k} \\ \ell_3 & \text{i i j k} \\ \ell_3 & \text{i i j k} \\ \ell_3 & \text{i i j k} \\ \ell_1 & \text{i i j k} \\ \ell_1 & \text{i i j k} \\ \ell_1 & \text{i i j k} \\ \ell_2 & \text{i i j k} \\ \ell_2 & \text{i i j k} \\ \ell_3 & \text{i i j k} \\ \ell_3 & \text{i i j k} \\ \ell_1 & \text{i i j k} \\ \ell_2 & \text{i i j k} \\ \ell_3 & \text{i i j k} \\ \ell_4 & \text{i i j k} \\ \ell_3 & \text{i i j k} \\ \ell_4 & \text{i i j k} \\ \ell_4$$

Assumptions (Would be great if future theory work can relax the strong assumptions)

- Individual type α_i is fixed.
- Team-size effects λ are unobserved scalars. Normalize $\lambda_1 = 1$.
- Shocks are mutually independent
- Shocks are independent of team formation
- Shocks are independent of types
- Shocks are independent of team formation, conditional on types

Sample selection (Metric)

Data

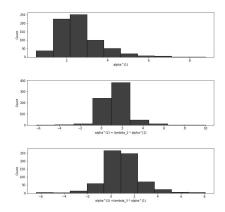
- Econometricians economists who have published at least 3 articles in Journal of Econometrics, Journal of Business Economic Statistics, Journal of Applied Econometrics, Econometric Theory, Journal of Financial Econometrics, Journal of Time Series Econometrics, Journal of Time Series Analysis and Econometrics Journal.
- Find all articles written by the econometricians defined above, including those in non-metric journals
- Measure paper quality by journal quality which is proxied by the (Clarivate) impact factor (I also tried other dependent variables such as VWL Ranking Deutschland but the results turn out to be similar)

		Sample	_	_	Subsam		_
		1	2	3	1	2	3
Article Count	Number of Papers	11555.0	9616.0	3327.0	5732.0	6281.0	2561.0
	mean	6.11	5.09	1.76	8.14	8.92	3.64
	std	9.73	7.22	3.29	11.79	9.88	4.29
	min	0.0	0.0	0.0	1.0	1.0	1.0
	q10	0.0	0.0	0.0	1.0	1.0	1.0
	q30	1.0	1.0	0.0	2.0	3.0	1.0
	median	3.0	3.0	1.0	4.0	6.0	2.0
	q70	6.0	5.0	2.0	8.0	10.0	4.0
	q90	15.0	13.0	5.0	18.0	20.0	7.0
	max	145.0	130.0	48.0	145.0	130.0	48.0
Journal Quality	Number of Authors	11555.0	4808.0	1109.0	5732.0	4053.0	1087.0
•	mean	3.0	2.75	2.73	2.83	2.77	2.73
	std	2.93	1.89	1.4	2.2	1.94	1.4
	min	0.11	0.5	0.51	0.38	0.51	0.51
	q10	1.16	1.37	1.39	1.18	1.37	1.37
	q30	1.82	2.1	2.1	1.85	2.1	2.1
	median	2.37	2.39	2.39	2.35	2.39	2.39
	q70	2.9	2.44	2.42	2.68	2.44	2.42
	q90	5.62	5.03	5.03	5.33	5.03	5.03
	max	53.24	53.24	15.56	53.24	53.24	15.56

Table: Descriptive statistics

Data

Empirical distribution of fixed-effects



Some observations

- Individual types are very heterogeneous.
- Estimated distributions are roughly shape-preserving.

Model of fixed-effects

Team-size effect

Complementarity

Supermodularity

Potentially Right-skewed shock

Put it all togethe

Team-size effect



Why care about λ ?

Fixing the heterogeneity parameter Δ , the collaboration gain is $2\lambda_2-1$. For example, $\lambda_2=0.55$ implies 10% gain, if you coauthor with someone of your type instead of working alone.

- In two-person teams, suppose economist i has type α_i and coauthor j has type $\alpha_j = \alpha_i + \Delta$ for some $\Delta \in \mathbb{R}$.
- Solo output = α_i
- Two-person output = $\lambda_2 (\alpha_i + \alpha_j)$
- Difference in output = $\lambda_2 (\alpha_i + (\alpha_i + \Delta)) \alpha_i = (2\lambda_2 1)\alpha_i + \lambda_2 \Delta$

Fixing the heterogeneity parameter Δ , the collaboration gain is $2\lambda_2-1$. For example, $\lambda_2=0.55$ implies 10% gain, if you coauthor with someone of your type instead of working alone.

Two ways to estimate λ

Estimation

By assumption, individuals has fixed types. We then have two moment conditions.

$$\alpha_i^{(2)} = \lambda_2 \alpha_i^{(1)}$$

$$\alpha_i^{(3)} = \lambda_3 \alpha_i^{(1)}$$

One straightforward way to estimate λ is to simply regress $\alpha_i^{(2)}$ on $\alpha_i^{(1)}$ and $\alpha_i^{(3)}$ on $\alpha_i^{(1)}$.

But we do *not* know the true $\alpha_i^{(1)}$. Instead, we have plug-in estimates $\hat{\alpha}_i^{(1)}$.

Least square regression on $\hat{\alpha}_i^{(1)}$ leads to regression attenuation because of the noisy regressors.

	Two-person team	Three-person team
Scaling factor	0.47	0.32
Collaboration gain	-5.2%	-2.8%
Number of metric-economists	704	704

Table: Attenuated Metric team-size effects

Generalized method of moments

■ Because λ_2 and λ_3 are scalars, by manipulating our moment conditions, we get

$$\mathbb{E}[\alpha_i^{(2)} - \lambda_2 \alpha_i^{(1)}] = 0$$

$$\mathbb{E}[\alpha_i^{(3)} - \lambda_2 \alpha_i^{(1)}] = 0$$

Because least-squared estimation is unbiased,

$$\mathbb{E}[\hat{\alpha}_i^{(1)}] = \alpha_i^{(1)}, \quad \mathbb{E}[\hat{\alpha}_i^{(2)}] = \alpha_i^{(2)}, \text{ and } \mathbb{E}[\hat{\alpha}_i^{(3)}] = \alpha_i^{(3)}$$

So the sample analog is

$$\begin{cases} \frac{1}{l} \sum_{i} \hat{\alpha}_{i}^{(2)} - \lambda_{2} \frac{1}{l} \sum_{i} \hat{\alpha}_{i}^{(1)} = 0\\ \frac{1}{l} \sum_{i} \hat{\alpha}_{i}^{(3)} - \lambda_{3} \frac{1}{l} \sum_{i} \hat{\alpha}_{i}^{(1)} = 0 \end{cases}$$

So,

Estimation

$$\hat{\lambda}^{\text{GMM}}(\hat{\alpha}) = \begin{bmatrix} 1 \\ \frac{1}{7} \sum_{i} \hat{\alpha}_{i}^{(2)} / \frac{1}{7} \sum_{i} \hat{\alpha}_{i}^{(1)} \\ \frac{1}{7} \sum_{i} \hat{\alpha}_{i}^{(3)} / \frac{1}{7} \sum_{i} \hat{\alpha}_{i}^{(1)} \end{bmatrix}$$

GMM results

iwo-person team i nree-person i	
Scaling factor 0.51 0.36	
Collaboration gain 2.5% 7.8%	
Number of econometricians 737 737	

Table: GMM estimates of Metric team-size effects

Iwo-person team	Inree-person team
0.52	0.37
4.8%	12.2%
396	396
	4.8%

Table: GMM estimates of Macro team-size effects

	Two-person team	Three-person team
Scaling factor	0.47	0.28
Collaboration gain	-5.9%	-14.6%
Number of micro-economists	859	859

Table: GMM estimates of Micro team-size effects





Regressions of $Y^{(2)}$, impact factor of two-author papers

To reduce the noise in $\hat{\alpha}_i^{(1)}$, I only look at economists with more than 3 solo publications.

	(1)	(2)
$Min(\hat{\alpha}_1, \hat{\alpha}_2)$	0.677***	0.597***
	(0.066)	(0.038)
$Max(\hat{\alpha}_1, \hat{\alpha}_2)$	0.357***	0.437***
	(0.047)	(0.021)
$\hat{\sigma}(\hat{\alpha}_1, \hat{\alpha}_2)$		-0.113***
		(0.040)
Observations	1,885	1,885
R^2	0.636	0.636
Adjusted R ²	0.636	0.636
Residual Std. Error	2.234(df = 1883)	2.234(df = 1883
Note:	*p<0.1: **	n<0.05: ***p<0.01

- 1. The marginal effect of the lowest-type is significantly higher than that of the highest-type. Consistent with other empirical literature such as Ahmadpoora and Jones (2016).
- 2. Does the spread of types play a role in the asymmetric marginal effects?

Estimation

Evidence of complementarity (Macro)

	(1)	(2)
$Min(\hat{\alpha}_1, \hat{\alpha}_2)$	0.941***	0.749***
	(0.096)	(0.056)
$Max(\hat{\alpha}_1, \hat{\alpha}_2)$	0.173**	0.365***
	(0.068)	(0.029)
$\hat{\sigma}(\hat{\alpha}_1, \hat{\alpha}_2)$		-0.272***
		(0.057)
Observations	1,043	1,043
R^2	0.610	0.610
Adjusted R ²	0.609	0.609
Residual Std. Error	2.938(df = 1041)	2.938(df = 1041)
Note:	*p<0.1; **	p<0.05; ***p<0.01

Evidence of complementarity (Micro)

	(1)	(2)	
$Min(\hat{\alpha}_1, \hat{\alpha}_2)$	1.059***	0.813***	
	(0.049)	(0.031)	
$Max(\hat{\alpha}_1, \hat{\alpha}_2)$	0.074***	0.320***	
	(0.025)	(0.011)	
$\hat{\sigma}(\hat{\alpha}_1, \hat{\alpha}_2)$		-0.348***	
(1/ 2/		(0.025)	
Observations	2,466	2,466	
R^2	0.453	0.453	
Adjusted R ²	0.452	0.452	
Residual Std. Error	3.159(df = 2464)	3.159(df = 2464)	
Note:	*p<0.1; **p<0.05; ***p<0.01		





Empirical evidence of supermodularity

Supermodularity

If f is twice differentiable, f is strictly supermodular is equivalent to

$$\frac{\partial f}{\partial \alpha_i \partial \alpha_j} > 0$$

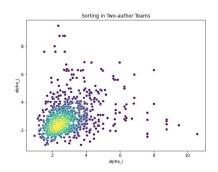
I assign quartiles (Q1, Q2, Q3, Q4) to Researcher 2 based on their estimated $\hat{\alpha}_2^{(1)}$. Then, I create three interaction terms between $\hat{\alpha}_4^{(1)}$ and the dummy variables

Then, I create three interaction terms between $\alpha_1^{r,r}$ and the dummy variables corresponding to the quartiles.

	(1)	(2)
$\hat{\alpha}_1$	0.918***	
	(0.017)	
$\hat{\alpha}_1 \times$ Dummy for coauthor belonging to Q2		0.847***
		(0.039)
$\hat{\alpha}_1 \times$ Dummy for coauthor belonging to Q3		0.933***
		(0.038)
$\hat{\alpha}_1 \times$ Dummy for coauthor belonging to Q4		1.002***
		(0.033)
Observations	1,885	1,885
R^2	0.600	0.516
Adjusted R ²	0.600	0.515
Residual Std. Error	2.342(df = 1884)	2.578(df = 1882)
Note:	*p<0.1; **p<0.05; ***p<0.01	

Model of fixed-effects Team-size effect Complementarity Supermodularity Potentially Right-skewed shock Put it all together 00000 0000 0000 0000 0000

Positive assortive sorting and Supermodularity



Chade, Eeckhout, and Smith (2017)

Match output function is supermodular if and only if positive assortive matching (PSM) is optimal, assuming

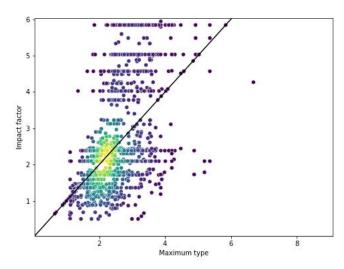
- Transferable utility
- Frictionless searching

Sorting





What's in it for the higher types to work with the lower-type?







Put it all together

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In my model of two-person team production function for paper ℓ ,

$$y_{\ell}^{(2)}(\alpha_1, \alpha_2) = \lambda_2(\alpha_1 + \alpha_2) + f(\alpha_1, \alpha_2) + \epsilon_{\ell}$$

- Linear component $\alpha_1 + \alpha_2$, scaled by team-size effects
- Non-linear component $f(\alpha_1, \alpha_2)$
 - Positive marginal effect: $\lambda_2 + \frac{\partial f}{\partial \alpha_i} > 0$
 - Strong asymmetry in individual marginal effects: Is $\frac{\partial f}{\partial \alpha_j}$ related to cardinal value of α_i or its ordinal rank in the team? Or is it related to how big the gap is between team members' types.
 - \blacksquare Supermodularity: $\frac{\partial^2 f}{\partial \alpha_1 \alpha_2} > 0$
 - lacktriangle Potentially right-skewed shock ϵ : a positive shock is more likely than a negative shock

Model of fixed-effects Team-size effect Complementarity Supermodularity Potentially Right-skewed shock Put it all together 000 000 000 000 000 000 000 000

Thank you!

Any questions?

