====DATSCIW261 ASSIGNMENT #4====

MIDS UC Berkeley, Machine Learning at Scale

DATSCIW261 ASSIGNMENT #4

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W261 - 2, ASSIGNMENT #4

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HW 4.0.

What is MrJob? How is it different to Hadoop MapReduce?

What are the mappint_init, mapper_final(), combiner_final(), reducer_final() methods? When are they called?

Answer

1. MrJob MrJob is a python package that helps us write and run Hadoop streaming jobs. It assists us in submitting job to Hadoop job tracker and in running each individual step under Hadoop streaming.

MapReduce is a framework processing parallelizable problems across huge data sets, using a large number of computers (nodes); cluster or grid. User specify a map fnction that processes a key/value pair to generate intermediate key/value pairs and a reduce function that merges all values associated with the same intermediate key.

Hadoop MapReduce is an implementation of Mapreduce programming framework. This API is implemented in Java. The Hadoop streaming library internally uses this. MrJob supports both local, hadoop and AWS EMR modes. For hadoop mode it internally uses hadoop streaming.

2.

mapper_int(): is used to define an action to be run before the mapper processes any input. mapper_init() is called first if there is function defined.

mapper_final(): is used to define an action to run after the mapper reaches the end of input. mapper_final is called after the mapper function has finished processing but before combiner or reducer is called.

combiner_final(): is used to define an action to run after the combiner reaches the end of input. combiner_final is called after the combiner function has finished processing but before the reducer is called.

reducer_final(): is used to define an action to run after the reducer reaches the end of input.combiner_final is called after the reducer function is finished.

HW 4.1

What is serialization in the context of MrJob or Hadoop?

When it used in these frameworks?

What is the default serialization mode for input and outputs for MrJob?

Answer

What is serialization in the context of MrJob or Hadoop?

Serialization (and deserialization) implies being able to take an object, convert it into bytes and then be able to reconstruct the object back from those bytes. In the context of Hadoop, the mapreduce APIs act upon keys and values. For primitive types serialization would not be a major issue to overcome. However, for complex types, the MR framework needs to know how to take the raw input and convert it into the keys&values for the mappers, then take the keys and values generated by the mapper, serialize them as needed for the shuffle layer to make them available to the reducer and finally write the key-value output generated by the reducer to HDFS/disk in the format needed. This requires the mapreduce framework to understand the serialization format for these keys and values for the framework to function. In the context of MRJob, it uses json for the most part. This can be overridden via use of mrjob custom protocols.

When it used in these frameworks?

- a. De-serialization: Converting raw input to keys and values for the mapper.
- b. Serialize and de-serialize: Write mapper output to disk. Convert bytes received from shuffle layer to keys and values for reducer input.
- c. Serialization: Write reducer output to disk/HDFS.
- What is the default serialization mode for input and outputs for MrJob?

The default input protocol for serialization is RawValueProtocol. The default output and internal protocol are both JSONProtocol.

HW 4.2: Recall the Microsoft logfiles data from the async lecture.

The logfiles are described are located at:

https://kdd.ics.uci.edu/databases/msweb/msweb.html (https://kdd.ics.uci.edu/databases/msweb/msweb.html)

http://archive.ics.uci.edu/ml/machine-learning-databases/anonymous/ (http://archive.ics.uci.edu/ml/machine-learning-databases/anonymous/)

This dataset records which areas (Vroots) of www.microsoft.com each user visited in a one-week timeframe in Feburary 1998.

Here, you must preprocess the data on a single node (i.e., not on a cluster of nodes) from the format:

C,"10001",10001 #Visitor id 10001

V,1000,1 #Visit by Visitor 10001 to page id 1000

V,1001,1 #Visit by Visitor 10001 to page id 1001

V,1002,1 #Visit by Visitor 10001 to page id 1002

C,"10002",10002 #Visitor id 10001

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Note: #denotes comments to the format:

V,1000,1,C, 10001

V,1001,1,C, 10001

V,1002,1,C, 10001

Write the python code to accomplish this.

```
In [3]:
```

```
%%writefile preprocess log.py
#!/usr/bin/python
""" This program process the log file and outputs 2 separate files.
    One for the log information and other is page URLS's.
11 11 11
import sys
import re
inputfile = sys.argv[1]
outputfile = open('processed_anonymous-msweb.data', 'a')
outputfile2 = open('processed urls.data', 'a')
for line in open(inputfile):
    v = line.split(',')
    # If the line is customer information line, save it to customer_info
    if(v[0] == 'C'):
        customer info = v
    # If the line visit information line, concatenate the line with customer info
    elif(v[0]=='V'):
        outputfile.write( line.strip()+','+customer info[0]+','+customer info[1].sti
    # Directly output other lines
    elif(v[0]=='A'):
        outputfile2.write(v[1]+','+ re.sub(r'\"+','',v[4]))
    else:
         continue
```

Writing preprocess log.py

```
In [4]:
!chmod a+x preprocess log.py
! rm processed anonymous-msweb.data
! rm processed_urls.data
!./preprocess log.py anonymous-msweb.data
!wc -l processed anonymous-msweb.data
! head processed anonymous-msweb.data
!wc -l processed_urls.data
! head processed urls.data
rm: processed_anonymous-msweb.data: No such file or directory
rm: processed urls.data: No such file or directory
   98654 processed anonymous-msweb.data
V,1000,1,C,10001
V,1001,1,C,10001
V,1002,1,C,10001
V, 1001, 1, C, 10002
V,1003,1,C,10002
V,1001,1,C,10003
```


1251,/referencesupport

HW 4.3:

1282,/home

1121,/magazine

Find the 5 most frequently visited pages using MrJob from the output of 4.2 (i.e., transfromed log file).

```
In [1]:
%load_ext autoreload
%autoreload 2
```

```
In [5]:
```

```
%%writefile hw4_3.py
'''
Input format:
....
```

```
V,1001,1,C,10001
V,1002,1,C,10001
V,1001,1,C,10002
V,1003,1,C,10002
V,1001,1,C,10003
V,1003,1,C,10003
V,1004,1,C,10003
1 1 1
from mrjob.job import MRJob, MRStep
import csv
import sys
def csv readline(line):
    """Given a sting CSV line, return a list of strings."""
    return csv.reader([line]).next()
class PageVisitHW4 3(MRJob):
    def mapper get visit count(self, line no, line):
        """Extracts the page id and visit count"""
        cell = csv readline(line)
        yield cell[1], 1
    def reducer get visit count(self, pageId, visit counts):
        """Sumarizes the visit counts by adding them together."""
        total = sum(i for i in visit counts)
        yield pageId, total
    def reducer find top5 pages init(self):
        self.printed = 0
    def reducer find top5 pages(self, pageId, visit counts):
        """Print the top 5 pageId's and the counts"""
        if self.printed < 5:</pre>
            yield pageId, visit counts.next()
            self.printed += 1
    def steps(self):
        return [
            MRStep(mapper=self.mapper get visit count,
                   combiner=self.reducer_get_visit_count,
                   reducer=self.reducer get visit count),
            MRStep(reducer init=self.reducer find top5 pages init,
                   reducer=self.reducer find top5 pages,
                   iobconf={
                    "stream.num.map.output.key.fields": "2",
                    "mapreduce.job.output.key.comparator.class":
                         "org.apache.hadoop.mapred.lib.KeyFieldBasedComparator",
                     "mapreduce.partition.keycomparator.options": "-k2,2nr"
                           })]
```

V,1000,1,C,10001

```
if __name__ == '__main__':
    PageVisitHW4 3.run()
Overwriting hw4 3.py
In [12]:
from hw4 3 import PageVisitHW4 3
mr job = PageVisitHW4 3(args=['processed anonymous-msweb.data', '-r', 'hadoop', '
with mr job.make runner() as runner:
    runner.run()
    # stream_output: get access of the output
    print "5 most frequently visited pages:"
    for line in runner.stream output():
        print mr_job.parse_output_line(line)
5 most frequently visited pages:
('1008', 10836)
ERROR:mrjob.fs.hadoop:STDERR: 16/02/11 11:57:19 WARN util.NativeCodeLo
ader: Unable to load native-hadoop library for your platform... using
builtin-java classes where applicable
('1034', 9383)
('1004', 8463)
('1018', 5330)
('1017', 5108)
HW 4.4:
Find the most frequent visitor of each page using MrJob and the output of 4.2 (i.e., transfromed log file). In this
output please include the webpage URL, webpageID and Visitor ID.
In [8]:
%%writefile hw4_4.py
from mrjob.job import MRJob, MRStep
import mrjob
import csv
import sys
def csv readline(line):
    """Given a sting CSV line, return a list of strings."""
    return csv.reader([line]).next()
class PageVisitHW4 4(MRJob):
```

BASE URL = "http://www.microsoft.com"

```
# Have to use Raw Protocol in order to get sorting (using 3rd key) to work.
    INTERNAL PROTOCOL = mrjob.protocol.RawProtocol
    OUTPUT PROTOCOL = mrjob.protocol.RawProtocol
    def mapper1(self, line no, line):
        cell = csv readline(line)
        # page, visitor \t count
        yield ",".join([cell[1], cell[4]]), "1"
    def reducer1(self, key, values):
        """Sum up the visit count per (page, visitor) pair."""
        total = sum([int(v) for v in values])
        fields = key.split(",")
        # page \t visitor \t total
        yield fields[0], "\t".join([fields[1], str(total)])
    def reducer2 init(self):
        # Build the dictionary of pageId:url
        self.urls = {}
        with open("processed urls.data", "r") as f:
            for fields in csv.reader(f):
                self.urls[fields[0]] = fields[1]
    def reducer2(self, key, values):
        # url \t pageId \t visitor \t total
        yield self.BASE_URL + self.urls[key] + "\t" + key, values.next()
    def steps(self):
        return [
            MRStep(mapper=self.mapper1,
                   reducer=self.reducer1,
            MRStep(reducer init=self.reducer2 init,
                   reducer=self.reducer2,
                   jobconf={
                    "stream.num.map.output.key.fields": "3",
                    "mapreduce.job.output.key.comparator.class":
                        "org.apache.hadoop.mapred.lib.KeyFieldBasedComparator",
                    "mapreduce.partition.keycomparator.options": "-k3,3nr"
                          }) ]
if name == ' main ':
    PageVisitHW4 4.run()
```

```
In [13]:
!python ./hw4 4.py \
-r hadoop \
--file processed urls.data \
--strict-protocols \
processed anonymous-msweb.data > most visitors.out
no configs found; falling back on auto-configuration
no configs found; falling back on auto-configuration
creating tmp directory /var/folders/dm/nsw7wjf91f1c74hgl17ldw040000gn/
T/hw4 4.patrickng.20160211.035741.553883
writing wrapper script to /var/folders/dm/nsw7wjf91f1c74hgl17ldw040000
gn/T/hw4 4.patrickng.20160211.035741.553883/setup-wrapper.sh
Using Hadoop version 2.7.1
Copying local files into hdfs:///user/patrickng/tmp/mrjob/hw4 4.patric
kng.20160211.035741.553883/files/
HADOOP: Unable to load native-hadoop library for your platform... usin
```

g builtin-java classes where applicable
HADOOP: packageJobJar: [/var/folders/dm/nsw7wjf91f1c74hgl17ldw040000gn/T/hadoop-unjar9199386722825397230/] [] /var/folders/dm/nsw7wjf91f1c74hgl17ldw040000gn/T/streamjob4861490282259515716.jar tmpDir=null

Counters from step 1:

(no counters found)

HADOOP: Unable to load native-hadoop library for your platform... usin g builtin-java classes where applicable

HADOOP: packageJobJar: [/var/folders/dm/nsw7wjf91f1c74hgl17ldw040000gn/T/hadoop-unjar4574631163935162190/] [] /var/folders/dm/nsw7wjf91f1c74hgl17ldw04000gn/T/streamjob2516918319451535318.jar tmpDir=null

Counters from step 2:

(no counters found)

Streaming final output from hdfs://user/patrickng/tmp/mrjob/hw4_4.patrickng.20160211.035741.553883/output

STDERR: 16/02/11 11:59:01 WARN util.NativeCodeLoader: Unable to load n ative-hadoop library for your platform... using builtin-java classes w here applicable

removing tmp directory /var/folders/dm/nsw7wjf91f1c74hgl17ldw040000gn/T/hw4_4.patrickng.20160211.035741.553883 deleting hdfs://user/patrickng/tmp/mrjob/hw4_4.patrickng.20160211.035

741.553883 from HDFS

```
In [14]:
```

```
Webpage URL, Page Id, Customer Id, Visit Count
http://www.microsoft.com/train cert
(http://www.microsoft.com/train cert)
                                         1295
                                                 42616
http://www.microsoft.com/partner (http://www.microsoft.com/partner)
1284
        41108
http://www.microsoft.com/cinemania
(http://www.microsoft.com/cinemania)
                                         1283
                                                 41033
                                                         1
http://www.microsoft.com/home (http://www.microsoft.com/home)
                                                                 1282
41244
http://www.microsoft.com/intellimouse
(http://www.microsoft.com/intellimouse) 1281
                                                 37099
                                                         1
http://www.microsoft.com/music (http://www.microsoft.com/music) 1280
41643
http://www.microsoft.com/msgolf (http://www.microsoft.com/msgolf)
1279
        31062
http://www.microsoft.com/hed (http://www.microsoft.com/hed)
                                                                 1278
41317
http://www.microsoft.com/stream (http://www.microsoft.com/stream)
1277
        30111
http://www.microsoft.com/vtestsupport
```

print "Webpage URL, Page Id, Customer Id, Visit Count"

!head most visitors.out | sed s/\"//g

HW 4.5

Here you will use a different dataset consisting of word-frequency distributions for 1,000 Twitter users. These Twitter users use language in very different ways, and were classified by hand according to the criteria:

1

40810

0: Human, where only basic human-human communication is observed.

(http://www.microsoft.com/vtestsupport) 1276

- 1: Cyborg, where language is primarily borrowed from other sources (e.g., jobs listings, classifieds postings, advertisements, etc...).
- 2: Robot, where language is formulaically derived from unrelated sources (e.g., weather/seismology, police/fire event logs, etc...).
- 3: Spammer, where language is replicated to high multiplicity (e.g., celebrity obsessions, personal promotion, etc...)

Check out the preprints of our recent research, which spawned this dataset:

http://arxiv.org/abs/1505.04342 (http://arxiv.org/abs/1505.04342)

http://arxiv.org/abs/1508.01843 (http://arxiv.org/abs/1508.01843)

The main data lie in the accompanying file:

topUsers_Apr-Jul_2014_1000-words.txt

and are of the form:

USERID,CODE,TOTAL,WORD1_COUNT,WORD2_COUNT,....

where

USERID = unique user identifier CODE = 0/1/2/3 class code TOTAL = sum of the word counts

Using this data, you will implement a 1000-dimensional K-means algorithm in MrJob on the users by their 1000-dimensional word stripes/vectors using several centroid initializations and values of K.

Note that each "point" is a user as represented by 1000 words, and that word-frequency distributions are generally heavy-tailed power-laws (often called Zipf distributions), and are very rare in the larger class of discrete, random distributions. For each user you will have to normalize by its "TOTAL" column. Try several parameterizations and initializations:

- (A) K=4 uniform random centroid-distributions over the 1000 words
- (B) K=2 perturbation-centroids, randomly perturbed from the aggregated (user-wide) distribution
- (C) K=4 perturbation-centroids, randomly perturbed from the aggregated (user-wide) distribution
- (D) K=4 "trained" centroids, determined by the sums across the classes.

and iterate until a threshold (try 0.001) is reached. After convergence, print out a summary of the classes present in each cluster. In particular, report the composition as measured by the total portion of each class type (0-3) contained in each cluster, and discuss your findings and any differences in outcomes across parts A-D.

Note that you do not have to compute the aggregated distribution or the class-aggregated distributions, which are rows in the auxiliary file:

topUsers_Apr-Jul_2014_1000-words_summaries.txt

```
In [262]:
%%writefile custom func.py
# function to calculate purity of cluster and print it. Its a generic function that
def calc purity(cluster dist):
    #calculate purity and print class distribution
    print 'Cluster distribution'
    print '-'*100
    user class = { 0:'Human', 1:'Cyborg', 2:'Robot', 3:'Spammer' }
    human = sum([cluster_dist[k].get('0',0) for k in cluster_dist.keys()])
    cyborg = sum([cluster dist[k].get('1',0) for k in cluster dist.keys()])
    robot = sum([cluster_dist[k].get('2',0) for k in cluster_dist.keys()])
    spammer = sum([cluster_dist[k].get('3',0) for k in cluster_dist.keys()])
    print "{0:>5} |{1:>15} |{2:>15} |{3:>15} |{4:>15}".format(
        "k", "Human"+':'+str(human), "Cyborg"+':'+str(cyborg), "Robot"+':'+str(robot
    print '-'*100
    max cl={}
    total = 0
    for cid, cvalue in cluster_dist.iteritems():
        total += sum(cvalue.values())
        print "{0:>5} |{1:>15} |{2:>15} |{3:>15} |{4:>15}".format(
        cid, cvalue.get('0',0), cvalue.get('1',0), cvalue.get('2',0), cvalue.get('1',0)
        max cl[cid]=max(cvalue.values())
    print '-'*100
    print 'purity : %3.3f' %(100*sum(max cl.values())*1.0/total)
    print '-'*100
Overwriting custom func.py
In [263]:
%%writefile Kmeans.py
from numpy import argmin, array, random
from mrjob.job import MRJob
from mrjob.step import MRJobStep
from itertools import chain
import numpy as np
#Calculate find the nearest centroid for data point
def MinDist(datapoint, centroid points):
    datapoint = array(datapoint)
    centroid points = array(centroid points)
    diff = datapoint - centroid points
    diffsq = diff*diff
    # Get the nearest centroid for each instance
    minidx = argmin(list(diffsq.sum(axis = 1)))
    return minidx
#Check whether centroids converge
def stop criterion(centroid points old, centroid points new,T):
  return np.alltrue(abs(np.array(centroid points new) - np.array(centroid points
```

```
oldvalue = list(chain(*centroid points old))
    newvalue = list(chain(*centroid points new))
    Diff = [abs(x-y) \text{ for } x, y \text{ in } zip(oldvalue, newvalue)]
    Flag = True
    for i in Diff:
        if(i>T):
            Flag = False
            break
    return Flag
class MRKmeans(MRJob):
    centroid points=[]
    def steps(self):
        return [
            MRJobStep(mapper init=self.mapper init,mapper=self.mapper,combiner=self)
    #load centroids info from file
    def mapper init(self):
        self.centroid_points = [map(float,s.split('\n')[0].split(',')) for s in oper
    #load data and output the nearest centroid index and data point
    def mapper(self, , line):
        D = line.split(',')
        total = int(D[2])
        code=int(D[1])
        #normalise the input data
        data=map(float,D[3:])
        normalise data=map(lambda x:((1.0 * x) / total),data)
        #sending the class composition along with the mapper output
        yield int(MinDist(normalise data, self.centroid points)),(list(normalise data)
    #Combine sum of data points locally
    def combiner(self, idx, inputdata):
        code = {} #for class composition
        sum features= None
        num = 0 #for count
        for features,n,codes in inputdata:
            features = array(features) #convert to array first
            if sum features is None: #if looping through first, initialise array of
                sum features = np.zeros(features.size)
            sum features += features #add features
            num += n #increment count
            #count codes
            for k,v in codes.iteritems(): #increment class composition
                code[k] = code.get(k,0) + v
        yield idx,(list(sum features),num,code)
    #Aggregate sum for each cluster and then calculate the new centroids
    def reducer(self, idx, inputdata):
        centroids = None
```

code = 11

```
num = 0
        for features, n, codes in inputdata:
            features = array(features)
            if centroids is None:
                centroids = np.zeros(features.size)
            centroids += features
            num += n #increment predicted cluster count
            #count codes
            for k,v in codes.iteritems(): #increment class composition
                code[k] = code.get(k,0)+v
        centroids new = centroids / num #compute new centroid
        yield idx, (list(centroids new),code)
if name == ' main ':
    MRKmeans.run()
Overwriting Kmeans.py
In [264]:
%%writefile run_kmeans.py
from numpy import random
import numpy as np
from Kmeans import MRKmeans, stop criterion
import sys
from custom func import calc purity
mr job = MRKmeans(args=['topUsers Apr-Jul 2014 1000-words.txt'])
random.seed(0)
#number of features
n = 1000
#get centroid type and number of clusters from user
if len(sys.argv) >2: k = int(sys.argv[2])
cen type = sys.argv[1]
#Geneate initial centroids
centroid points = []
#based on the centroid type generate centroids
if(cen_type=='Uniform'):
    rand int = random.uniform(size=[k,n])
    total = np.sum(rand int,axis=1)
    centroid_points = (rand_int.T/total).T
    with open('Centroids.txt', 'w+') as f:
        f.writelines(','.join(str(j) for j in i) + '\n' for i in centroid points)
    f.close()
```

```
elif(cen type=='Perturbation'):
    data = [s.split('\n')[0].split(',') for s in
                   open("topUsers Apr-Jul 2014 1000-words summaries.txt").readlines
    #get the total count of words
    total = int(data[2])
    feature = map(lambda x:((1.0 * float(x)) / total), data[3:]) #normalise
    pertubation = feature + random.sample(size=(k,n)) #generate random sample and ad
    sum per = np.sum(pertubation,axis=1) # calculate the sum to be used for normalia
    centroid points = (pertubation.T/sum per).T
    with open('Centroids.txt', 'w+') as f:
        f.writelines(','.join(str(j) for j in i) + '\n' for i in centroid points)
    f.close()
else:
    data = [s.split('\n')[0].split(',') for s in
                   open("topUsers Apr-Jul 2014 1000-words summaries.txt").readlines
    for cluster in data:
        total = 0
        total = int(cluster[2])#get the total count of words
        feature = map(lambda x:((1.0 * float(x)) / total), cluster[3:]) #normalise
        centroid points.append(feature)
    with open('Centroids.txt', 'w+') as f:
        f.writelines(','.join(str(j) for j in i) + '\n' for i in centroid_points)
    f.close()
print 'Centroid Type: %s' %cen type
# Update centroids iteratively
i = 0
while(1):
    # save previous centoids to check convergency
    centroid points old = centroid points[:]
    print "iteration"+str(i)+":"
    with mr job.make runner() as runner:
        centroid points = []
        cluster dist ={}
        runner.run()
        # stream output: get access of the output
        for line in runner.stream output():
            key,value = mr job.parse output line(line)
            centroid, codes = value
            centroid points.append(centroid)
            cluster dist[key]=codes
    i = i + 1
    #check if we have convergence
    if(stop criterion(centroid points old,centroid points,0.001)):
        break
    #write new centroids back to file
    with open('Centroids.txt', 'w') as f:
        for centroid in centroid points:
            f.writelines(','.join(map(str, centroid)) + '\n')
        f.close()
```

```
calc_purity(cluster_dist)
Overwriting run kmeans.py
In [248]:
!python run kmeans.py Uniform 4
Centroid Type: Uniform
iteration0:
iteration1:
iteration2:
iteration3:
iteration4:
iteration5:
Cluster distribution
   k | Human:752 | Cyborg:91 | Robot:54 | Spammer:
103
             0 |
   0
                           0
                                   11
         0 | 51 |
                                          0
   1 |
             1 |
                            37 |
   2
                                         38
           751 |
                      3 |
   3 |
                                           5
99
purity : 85.100
```

In [249]:
!python run_kmeans.py Perturbation 2

Centroid Type: Perturbation
iteration0:
iteration1:
iteration2:
iteration3:

Cluster distribution

k | Human:752 | Cyborg:91 | Robot:54 | Spammer:

103

0 | 751 | 3 | 16 | 99 1 | 1 | 88 | 38 |

purity : 83.900

In [250]:

 k							
)3	Human:752	 	 Cyborg:91		Robot:54		Spammer
0	0	<u>-</u>	0		5		
1	0		51		0	1	
2	1		37		38	1	
3	751		3		11		

```
In [247]:
!python run kmeans.py Trained
Centroid Type: Trained
iteration0:
iteration1:
iteration2:
iteration3:
iteration4:
Cluster distribution
  k | Human:752 | Cyborg:91 | Robot:54 | Spammer:
103
  0
             749
                           3
                                       14
38
        0 | 51 |
  1 |
                                       0
0
                     37 |
  2
            1 |
                                       40
                     0 |
          2
                                        0
  3
61
```

purity : 90.100

In []:

HW4.6 (OPTIONAL) Scaleable K-MEANS++

Read the following paper entitled "Scaleable K-MEANS++" located at:

http://theory.stanford.edu/~sergei/papers/vldb12-kmpar.pdf

In MrJob, implement $K-MEANS \mid \mid$ and compare with a random initialization when used in

conjunction with the kmeans algorithm as an initialization step for the 2D dataset

generated using code in the following notebook:

https://www.dropbox.com/s/lbzwmyv0d8rocfq/MrJobKmeans.ipynb?dl=0

Plot the initialization centroids and the centroid trajectory as the K-MEANS $\mid \mid$ algorithms iterates.

Repeat this for a random initalization (i.e., pick a training vector at random for each inital centroid) of the kmeans algorithm. Comment on the trajectories of both

algorithms.

Report on the number of passes over the training data, and time required to run both clustering algorithms.

Also report the rand index score for both algorithms and comment on your findings.

Using the kmeans | Algorithm

Note to grader: we did not complete 4.6 but did read the paper and provide our interpretation and initial study in the following cells.

Algorithm Summary

- 1. Sample one point c1 uniformly from the dataset X. The set C of candidate centroids has its first member, c1.
- 2. Compute phi(X, c1) = sum of squared distances from c1 to all points in dataset
- 3. Calculate log(phi(X, c1)) to determine number of times NN to perform Step 4.
- 4. for i in range(NN): sample x in dataset with probability: $L * d^2(x, C) / phi(X, C)$
- 5. Add the points discovered in Step 4 to the set of candidate centroids C.
- 6. Complete the for loop; collect all candidate centroids.
- 7. For each ci in C, let wi be the number of points in X closest to ci. The wi are weights for ci.
- 8. The cardinality of C is typically > k. Use kmeans on weighted ci in C to find k candidate centroids.

where:

- L is an oversampling factor (we will use 2k, or 6)
- d²(x, C) is the squared distance of x from the set of centroids C (it is the minimum distance of x to any point ci in C).
- phi(X, C) is the sum of minimum squared distances from all x in X to C.

Parallelized Implementation

Steps 1, 2, and 3 above are initial setup steps. Steps 4 and 7 can be parallelized. Step 8, reducing the set of weighted centroids, can be done quickly with Lloyd kmeans clustering, given that there is a reduced set of points, and centroids can easily be recomputed using the weights.

Steps 1, 2, 3:

First, as in MrJobKmeans notebook, we generate data by generating noise around three clusters with true centroids (4,0), (6,6), (0,4).

```
In [3]:
%matplotlib inline
import numpy as np
import pylab
size1 = size2 = size3 = 10000
samples1 = np.random.multivariate_normal([4, 0], [[1, 0], [0, 1]], size1)
data = samples1
samples2 = np.random.multivariate_normal([6, 6], [[1, 0],[0, 1]], size2)
data = np.append(data,samples2, axis=0)
samples3 = np.random.multivariate_normal([0, 4], [[1, 0], [0, 1]], size3)
data = np.append(data,samples3, axis=0)
# Randomlize data
data = data[np.random.permutation(size1+size2+size3),]
np.savetxt('Kmeandata.csv',data,delimiter = ",")
In [12]:
data.shape
Out[12]:
(30000, 2)
In [20]:
#Calculate first value of phi (phi(X,c1):
def steps123(n):
    a = np.random.choice(30000)
    c1 = data[a,:2]
    diff = data - c1
    nn = diff*diff
    tot = sum(nn)[0] + sum(nn)[1]
    NN = int(np.log(tot))
    return c1, tot, np.log(tot)
c1, tot, num rounds = steps123(30000)
print "Step 1: c1 = ", c1
print "Step 2: psi(X, c1) = ", tot
```

```
Depending on c1, the value of np.log(tot) varies from 13 to 14. We will assume a value of 14. (In ten trials of
```

2.89458932]

print "Step 3: log(psi(X,c1)) = ", num rounds

Step 1: c1 = [0.0624622]

Step 2: psi(X, c1) = 760009.162248

computing np.log(tot), the mean was 13.6).

Step 3: log(psi(X,c1)) = 13.5410857678

```
In [22]:

trial_list = []

for i in range(10):
    c1, tot, num_rounds = steps123(30000)
    trial_list.append(num_rounds)
num_trials = sum(trial_list)/10.0
```

13.6122647212

print num_trials

KMeans|| step 4: sampling

```
In [23]:
```

```
from numpy import argmin, array
from collections import namedtuple
from random import random, choice
from copy import copy
def MinDist(datapoint, centroid points):
    datapoint = array(datapoint)
    centroid points = array(centroid points)
    diff = datapoint - centroid points
    diffsq = diff*diff
    # Get the nearest centroid for each instance
    minidx = argmin(list(diffsq.sum(axis = 1)))
    mindistsq = min(list(diffsq.sum(axis = 1)))
    return minidx, mindistsq
def sampler(points, cluster centers, ell, num trials): #ell is oversampling factor
    This function returns ell sampled points from the distribution with
    probability ell*d^2(x,C)/phi(X,C) for cluster centers C and points X.
    cluster centers[0] = copy(choice(points)) #first random choice of cluster point
    d = [0.0 for in xrange(len(points))]
    for i in xrange(1, num trials):
        sum = 0
        for j, p in enumerate(points):
            d[j] = MinDist(p, cluster centers)[1] #min dist of p to clusterpts i
            sum += d[j]
        sum *= random() #generate random number and scale sum
        jj = 0
        while jj*ell < len(d):</pre>
            for m in range(ell):
                sum -= d[j*ell+m] #subtract ell chunks from sum
            jj += 1
            if sum > 0:
                continue
            for mm in range(ell):
                indx = (jj-1)*ell + mm
                cluster centers.append(points[mm]) ##ell points sampled
```

Discussion of 4.6 going forward:

The above function sampler could be parallelized in MrJob to calculate samplings of "ell" points. All mappers would have to have a copy of the dataset and write centroids to a file.

Then another mapReduce job could compute the weights of all the centroids computed in Step 4. Finally a third mapReduce could perform Lloyd Kmeans on the weighted centroids of Step 7 to produce k centroids.							
In []:							