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Lab 2

EE141, Digital Signal Processing, Fall 2025

Problem 1: Reviewing and verifying properties of the DTFT

In this problem, we consider the discrete time Fourier transform given by

$$X(e^{j\omega}) = \sum_{n=-\infty}^{\infty} x[n]e^{-j\omega n}.$$

We also consider that if x[n] is a causal sequence, this sum reduces to

$$X(e^{j\omega}) = \sum_{n=0}^{\infty} x[n]e^{-j\omega n},$$
(1)

and we can further truncate the above sum to

$$X(e^{j\omega}) \approx \tilde{X}(e^{j\omega}) \triangleq \sum_{n=0}^{\infty} x[n]e^{-j\omega n}$$
 (2)

if x[n] decays to zero as $n \to \infty$. For this problem, we let $x[n] = 0.8^n u[n]$ and $y[n] = 0.7^n \cos(\frac{\pi n}{6}) u[n]$.

a) Solving analytically for x[n], we observe

$$X(e^{j\omega}) = \sum_{n=0}^{\infty} 0.8^n e^{-j\omega n}$$

as x[n] is a causal signal, shown in (1). We can further simplify to

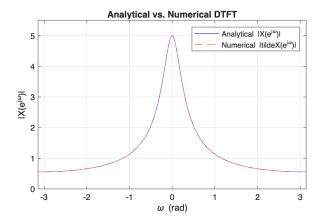
$$X(e^{j\omega}) = \sum_{n=0}^{\infty} (0.8e^{-j\omega})^n,$$

where we observe this as a converging sum, as $a = 0.8 < \infty$. Continuing with our idea of infinite geometric series, we can simplify this even further to

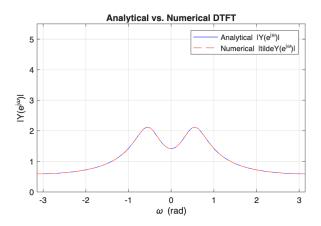
$$X(e^{j\omega}) = \frac{1}{1 - 0.8e^{-j\omega}}.$$

We can then use this in MATLAB to solve for $X(e^{j\omega})$ in an analytical manner, using our w = linspace(-pi, pi, K) where K = 500.

- **b)** Picking a large enough N s.t. $0.9^N \approx 0$ (ended up choosing N = 10000), we use MATLAB to numerically compute $X(e^{j\omega_k})$ using (2).
- c) Plotting the analytical and numerical solutions, we observe the following:



d) Doing the same for y[n], we observe the following plot:



e)