

assignment_operator.R

Preston

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```
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# CS320 Honors Option
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# The assignment operator = of a binomial heap should be O(n+m)
# where the assignment is heap_of_size_n = heap_of_size_m;

assignment_operator_binomial = read.csv("./assignment_operator_binomial.csv")
attach(assignment_operator_binomial)

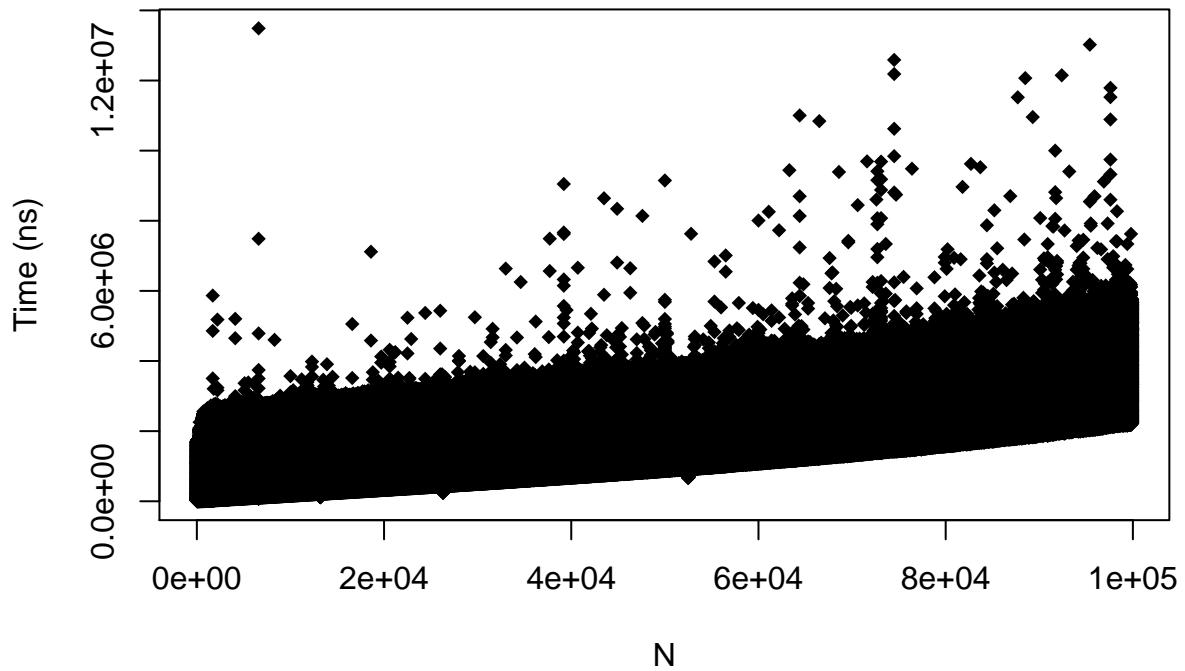
## The following object is masked from package:base:
##
##      T
# Note: this dataset is larger because it records for all combinations of n and m
length(T)

## [1] 1000000
# We will also need a variable for n+m
NplusM = N+M

summary(T)

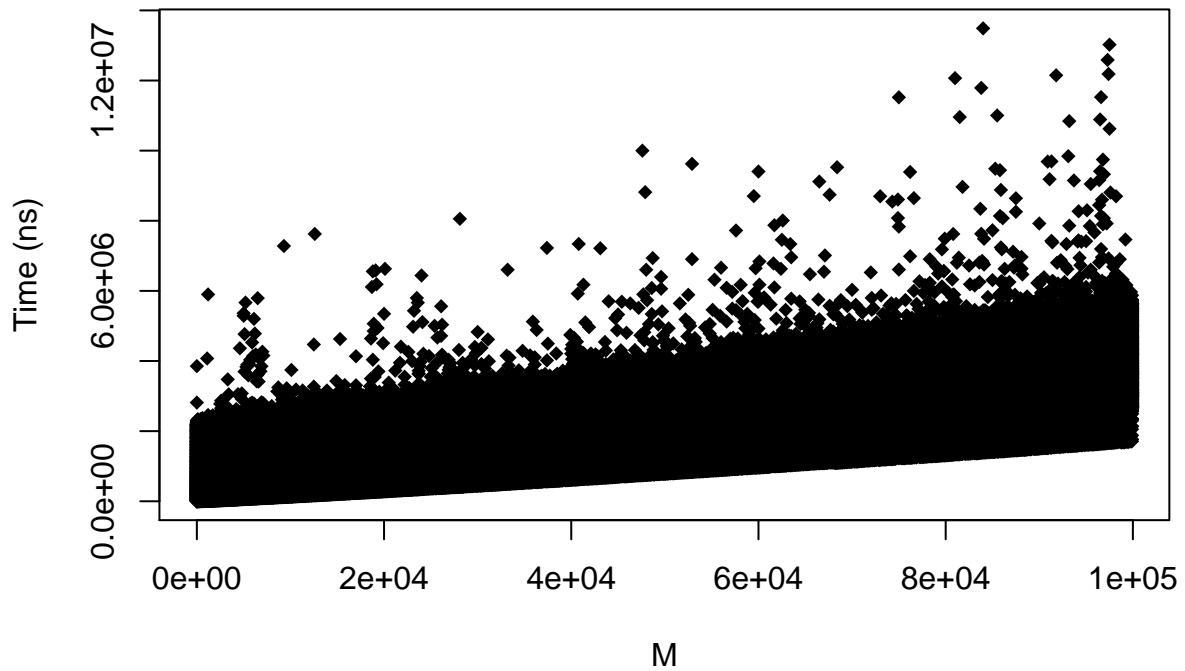
##      Min.    1st Qu.     Median      Mean    3rd Qu.      Max.
##      767    1528234   2331850   2399332   3171077  13487930
# min 767
# q1 1528234
# median 2331850
# mean 2399332
# q3 3171077
# max 13487930
plot(N,T,pch=18,xlab="N",ylab="Time (ns)",main="Binomial_Heap Assignment Operator")
```

Binomial_Heap Assignment Operator



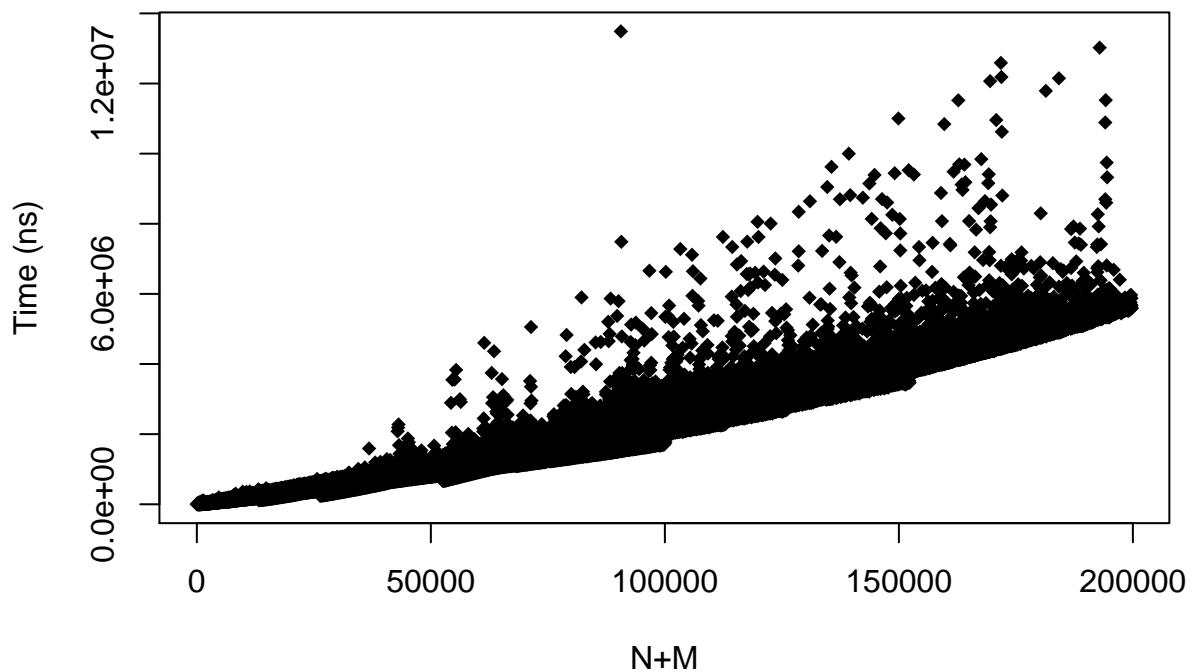
```
plot(M,T,pch=18,xlab="M",ylab="Time (ns)",main="Binomial_Heap Assignment Operator")
```

Binomial_Heap Assignment Operator



```
plot(NplusM,T,pch=18,xlab="N+M",ylab="Time (ns)",main="Binomial_Heap Assignment Operator")
```

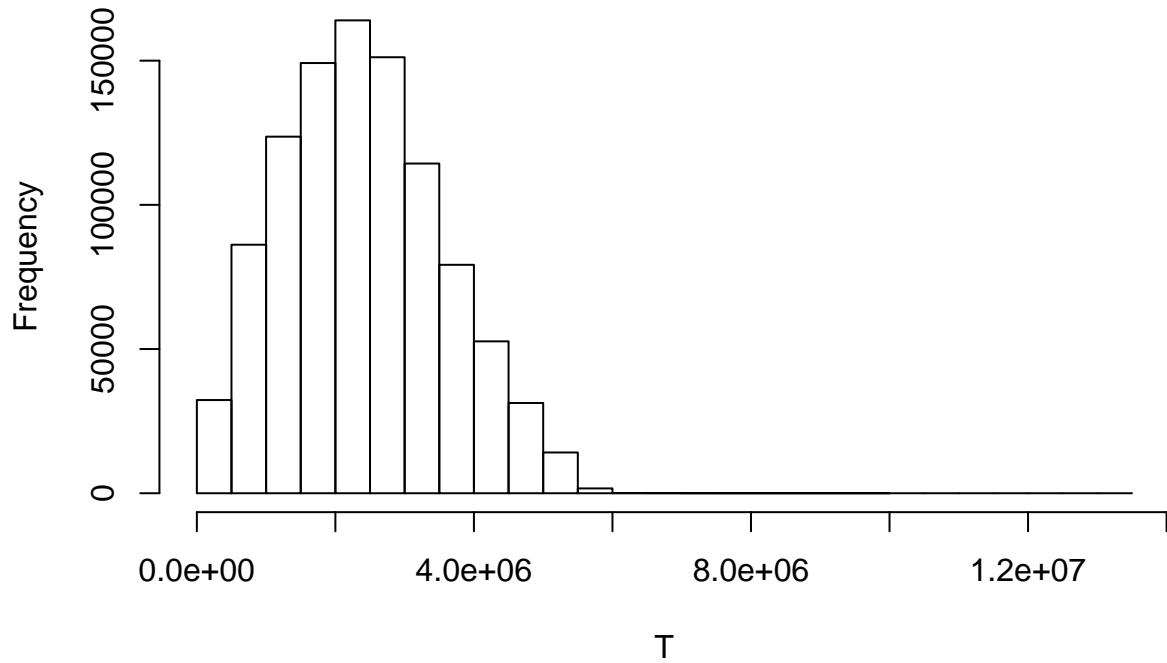
Binomial_Heap Assignment Operator



```
# It's interesting to see how this last chart clusters the data closer than the others.  
# There is also some strange edges at the bottom of trend curve.  
# This could maybe be the same patterns observed in the clear().  
# Both the assignment operator and clear() make use of the delete_tree() internal function,  
# which could be the cause of this pattern.
```

```
hist(T,breaks=30)
```

Histogram of T

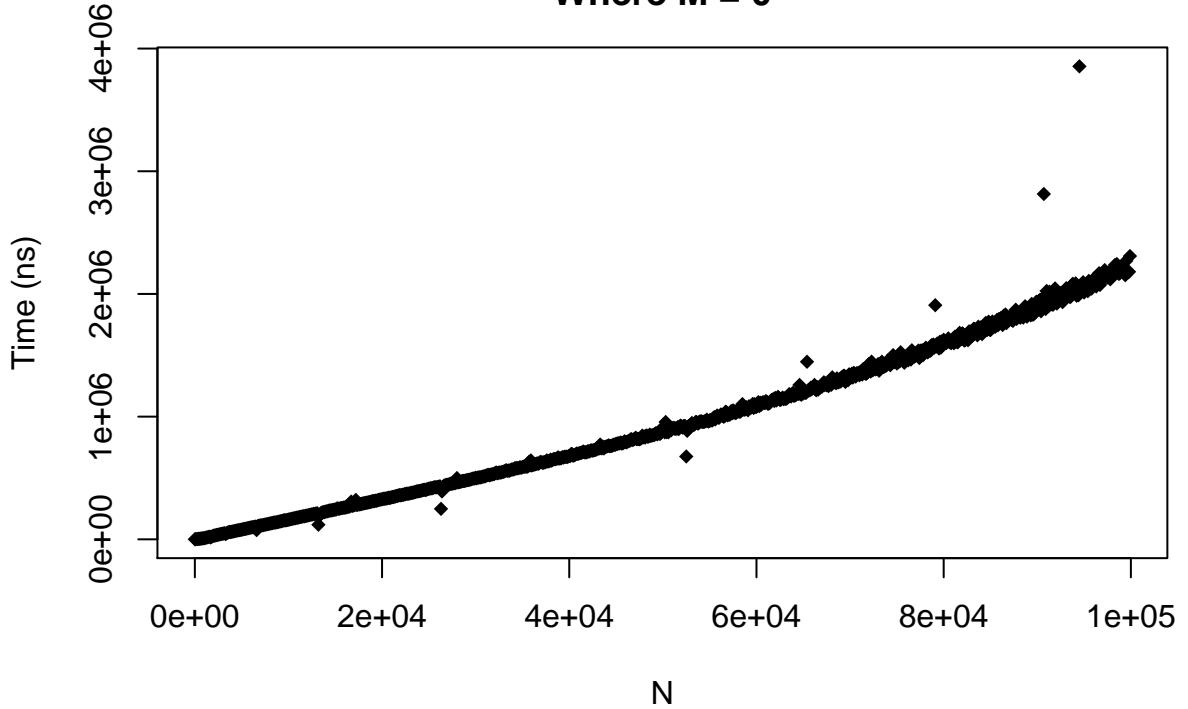


```
# A normal distribution. Something unexpected for an O(n+m) function. Other linear functions
# we have seen, such as the copy constructor and clear() demonstrate a near uniform distribution.

# These scatterplots are a mess! This is because there are multiple T values for a single N or M value
# Let's hold N and M constant and retry.
# N and M take on the same uniform distribution between 0 and 100000.
# Let's use the start, middle, and end of that range to create scatterplots

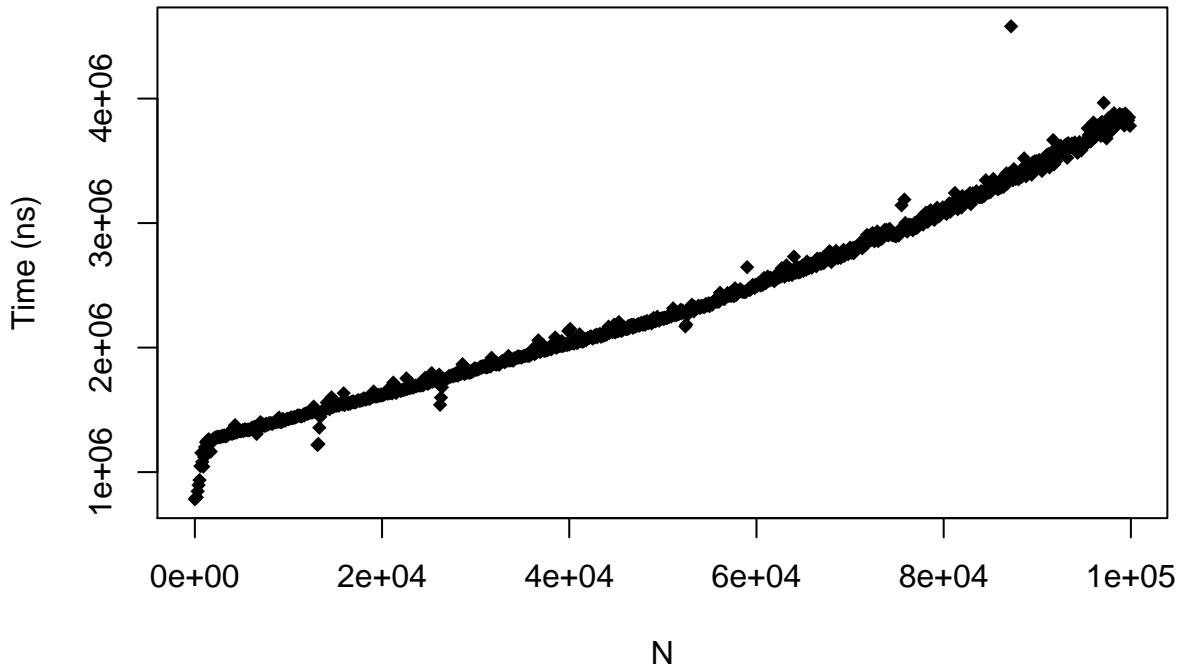
plot(N[which(M==0)],T[which(M==0)],pch=18,xlab="N",ylab="Time (ns)",main="Binomial_Heap Assignment Operator")
```

Binomial_Heap Assignment Operator Where M = 0



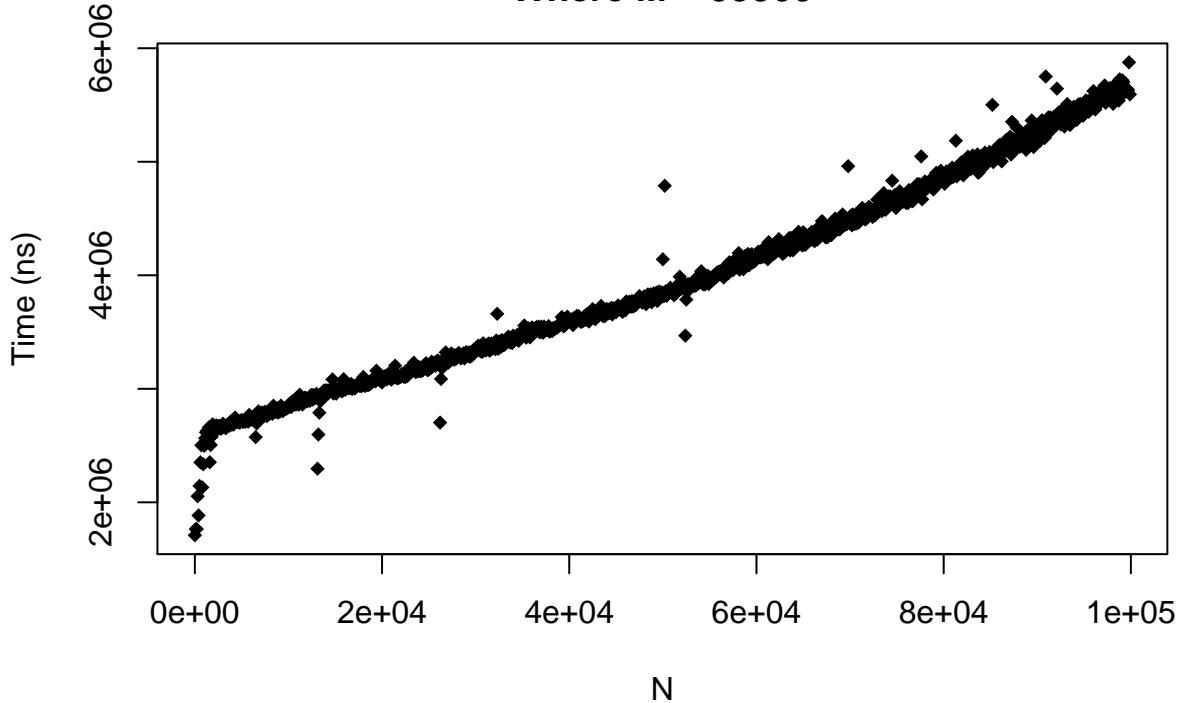
```
plot(N[which(M==49900)],T[which(M==49900)],pch=18,xlab="N",ylab="Time (ns)",main="Binomial_Heap Assignment Operator Where M = 0")
```

Binomial_Heap Assignment Operator Where M = 49900



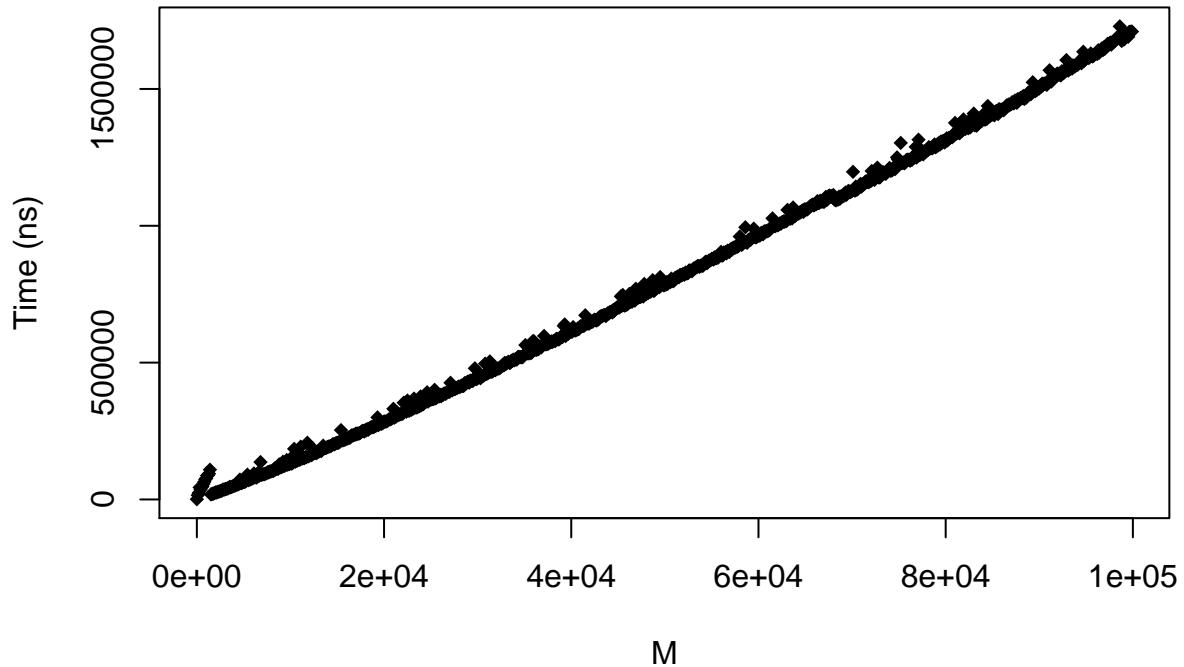
```
plot(N[which(M==99900)],T[which(M==99900)],pch=18,xlab="N",ylab="Time (ns)",main="Binomial_Heap Assignment Operator Where M = 49900")
```

Binomial_Heap Assignment Operator Where M = 99900



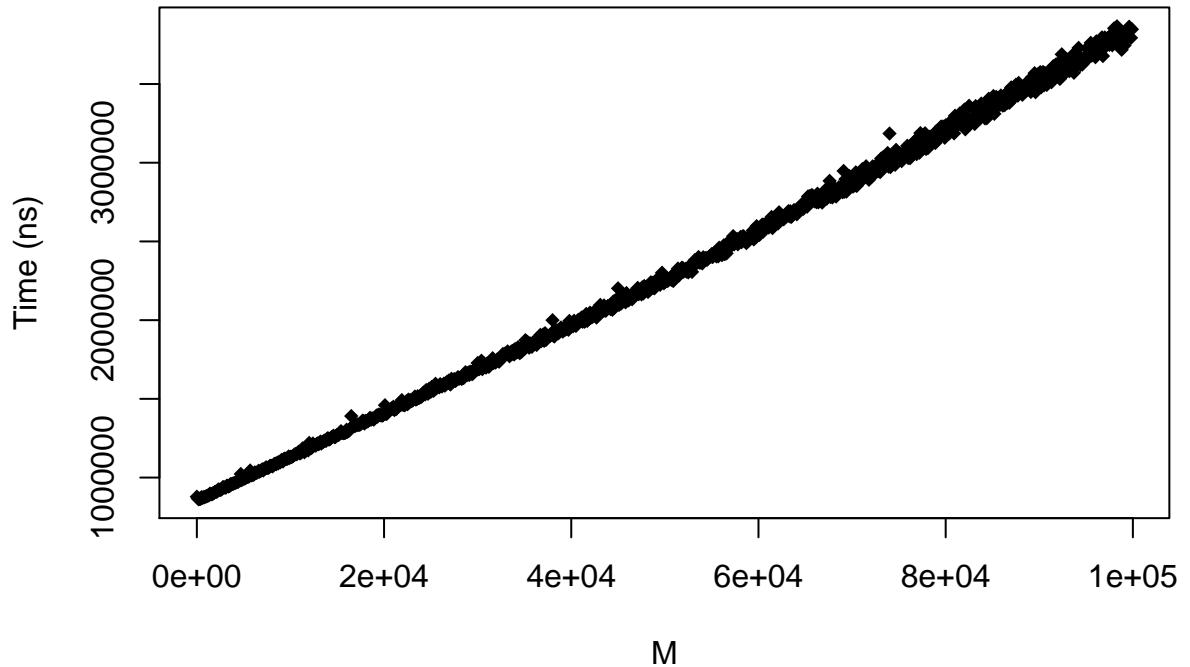
```
plot(M[which(N==0)],T[which(N==0)],pch=18,xlab="M",ylab="Time (ns)",main="Binomial_Heap Assignment Operator")
```

Binomial_Heap Assignment Operator Where N = 0



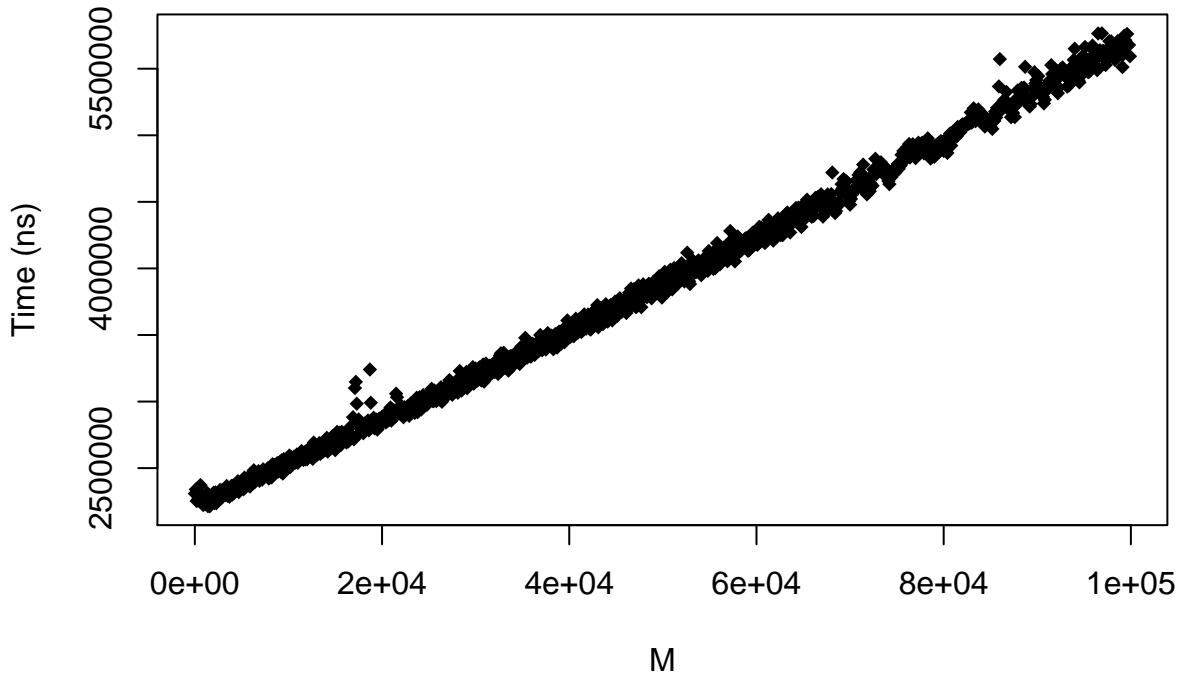
```
# This is extremely linear. Wow!
plot(M[which(N==49900)],T[which(N==49900)],pch=18,xlab="M",ylab="Time (ns)",main="Binomial_Heap Assignment Operator Where N = 0")
```

**Binomial_Heap Assignment Operator
Where N = 49900**



```
plot(M[which(N==99900)],T[which(N==99900)],pch=18,xlab="M",ylab="Time (ns)",main="Binomial_Heap Assignment Operator Where N = 49900")
```

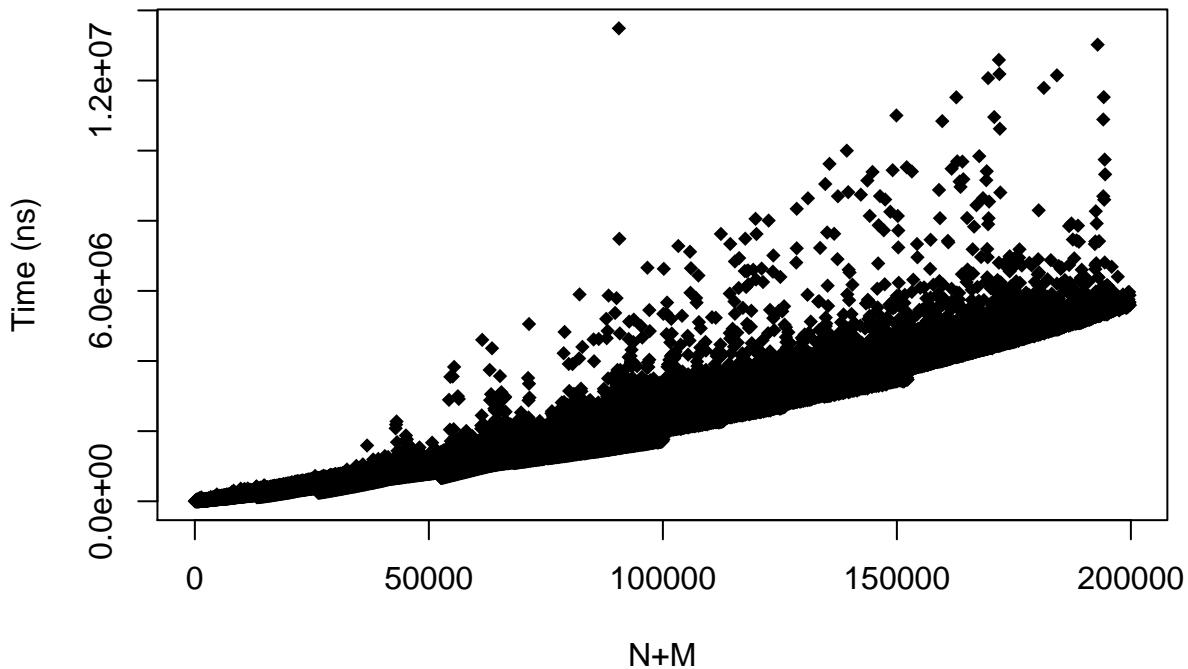
Binomial_Heap Assignment Operator Where N = 99900



```
# Since we know that the times should be based on N+M, let's stop all these scatterplots
# and use our N+M variable

plot(NplusM,T,pch=18,xlab="N+M",ylab="Time (ns)",main="Binomial_Heap Assignment Operator")
```

Binomial_Heap Assignment Operator



```
# We've already seen this. Let's do multiple regression to take a look  
# at the relationship between N+M and T using numbers.
```

```
cor(NplusM,T) # Higher correlation of 0.9891723. A sign that we are probably seeing O(n+m), as we expe
```

```
## [1] 0.9891723
```

```
lm(T~N+M)
```

```
##
```

```
## Call:
```

```
## lm(formula = T ~ N + M)
```

```
##
```

```
## Coefficients:
```

	N	M
(Intercept)	25.74	30.18
-394063.94		

```
lm(T~NplusM)
```

```
##
```

```
## Call:
```

```
## lm(formula = T ~ NplusM)
```

```
##
```

```
## Coefficients:
```

	NplusM
(Intercept)	27.96
-394063.94	

```
# Using our N and M variables separately in multiple regression,  
# we see that as N increases by 1, T increases by 25.74ns
```

```
# and as M increases by 1, T increases by 30.18ns.  
# Using our N+M variable, we see that as N or M increases by 1,  
# T increases by 27.96ns.  
# The coefficient for our N+M variable is the average of the  
# coefficients for each variable seperate.  
  
# Because the coefficients are high and we have a strong correlation  
# between N+M and T, we can assume that the assignment operator  
# does in fact have a time complexity of O(n+m)  
  
detach(assignment_operator_binomial)
```