

# decrease\_key.R

Preston

2020-05-23

```
# Preston Dunton
# CS320 Honors Option
# May 23, 2020
# pdunton@rams.colostate.edu

# Minimum() in a binomial heap should be  $O(\log n)$ 

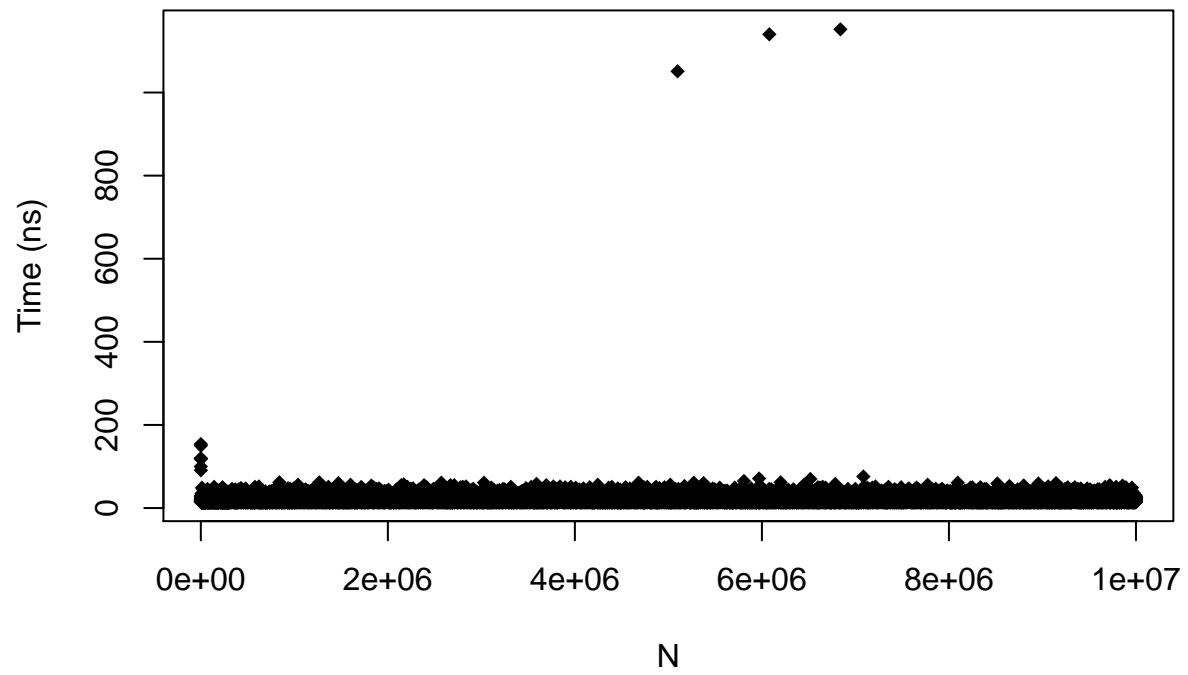
decrease_key_binomial = read.csv("./decrease_key_binomial.csv")
attach(decrease_key_binomial)

## The following object is masked from package:base:
##
##      T
summary(T)

##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
##      14.00   15.00   19.00   19.75   21.00  1152.00

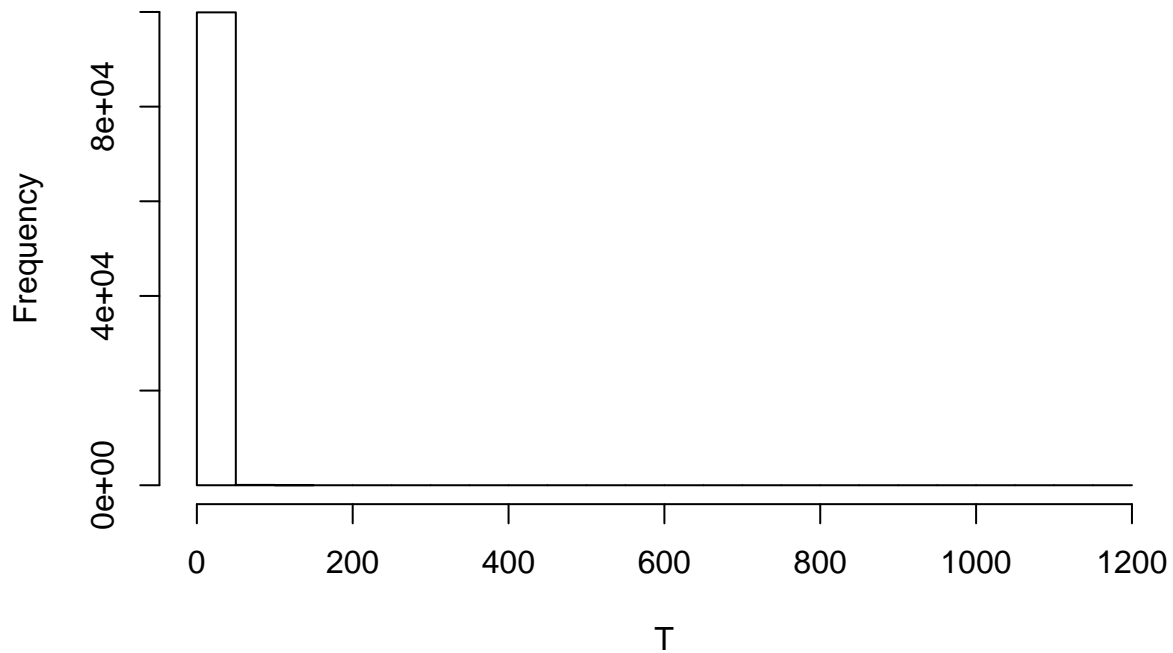
# min 14
# q1 15
# median 19
# mean 19.75
# q3 21
# max 1152
plot(N,T,pch=18,xlab="N",ylab="Time (ns)",main="Binomial_Heap.Decrease_Key()")
```

## Binomial\_Heap.Decrease\_Key()



```
hist(T,breaks=30)
```

## Histogram of T



```
# Let's see if we can remove some outliers
```

```
quantile(T,seq(0,1,0.1))
```

```
##    0%   10%   20%   30%   40%   50%   60%   70%   80%   90%  100%
##    14    15    15    16    16    19    20    21    24    26  1152
```

```
quantile(T,seq(0.9,1,0.01))
```

```
##    90%   91%   92%   93%   94%   95%   96%   97%   98%   99%  100%
##    26    27    28    29    30    30    31    32    35    37  1152
```

```
quantile(T,seq(0.99,1,0.001))
```

```
##    99%  99.1%  99.2%  99.3%  99.4%  99.5%  99.6%  99.7%  99.8%  99.9%  100%
##    37    38    39    40    40    41    41    43    46    50   1152
```

```
quantile(T,seq(0.999,1,0.0001))
```

```
##      99.9%      99.91%      99.92%      99.93%      99.94%      99.95%      99.96%      99.97%
##    50.0000    50.0000    50.0000    51.0000    51.0000    53.0000    55.0000    56.0006
##      99.98%      99.99%      100%
##    61.0000    76.0030  1152.0000
```

```
# Let's separate the top 0.01% and analyze
```

```
# Top 0.01%
```

```
sum(T>76) # There are 10 outliers
```

```
## [1] 10
```

```
summary(T[which(T>76)])
```

```
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
##      91.0   118.2   135.0   419.5   826.8  1152.0
```

```
# min 91
```

```
# q1 118.2
```

```
# median 135
```

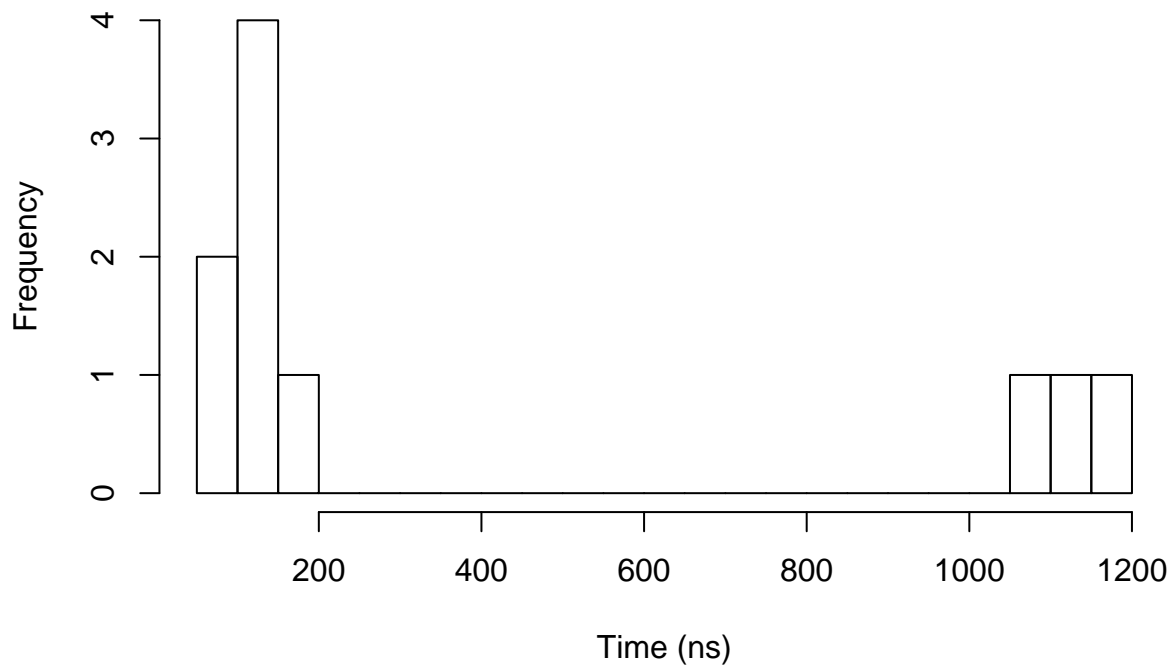
```
# mean 419.5
```

```
# q3 826.8
```

```
# max 1152
```

```
hist(T[which(T>76)],main="Histogram of Top 0.01% of Times",xlab="Time (ns)",breaks=30)
```

## Histogram of Top 0.01% of Times



```
# Bottom 99.99%
```

```
summary(T[which(T<=76)])
```

```
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
##      14.00   15.00   19.00   19.71   21.00   76.00
```

```
# min 14
```

```
# q1 15
```

```
# median 19
```

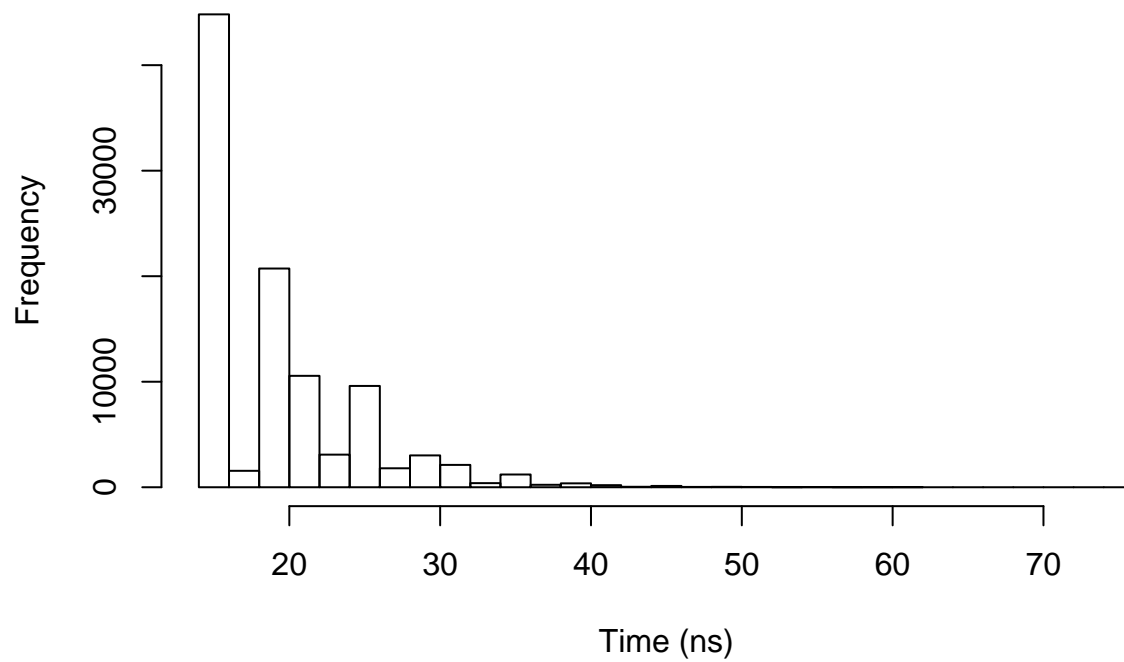
```
# mean 19.71
```

```
# q3 21
```

```
# max 76
```

```
hist(T[which(T<=76)],main="Histogram of Bottom 99.99% of Times",xlab="Time (ns)",breaks=30)
```

## Histogram of Bottom 99.99% of Times



*# 99.99% of deletions take less than 76 ns*  
*# There also appears to be no large correlation between  $N$  and insertion time*  
*# The implementation must be correct for an  $O(\log n)$  time*

```
detach(decrease_key_binomial)
```