

heap_union.R

Preston

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# CS320 Honors Option
# May 23, 2020
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# Heap_Union() in a binomial heap should be O(log(n+m))
# where the two heaps have a size of n and m respectively

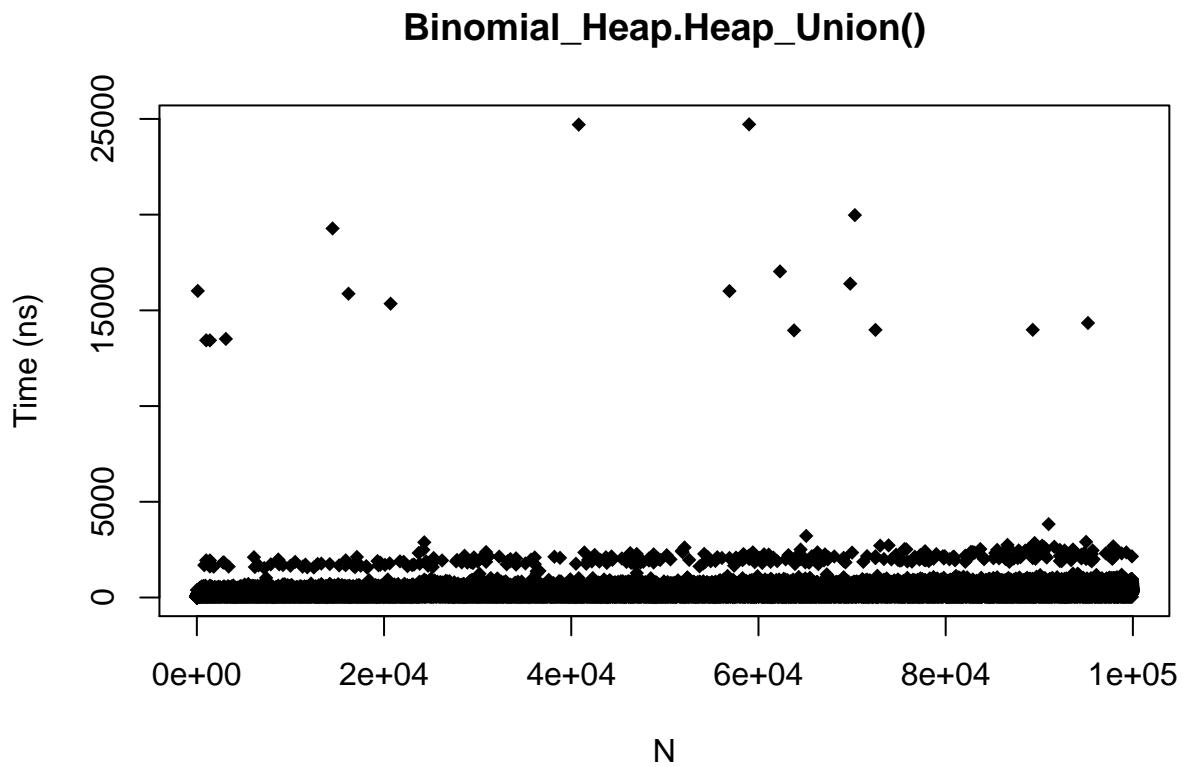
heap_union_binomial = read.csv("./heap_union_binomial.csv")
attach(heap_union_binomial)

## The following object is masked from package:base:
## 
##      T
# Note: this dataset is larger because it records for all combinations of n and m
length(T)

## [1] 1000000
# We will also need a variable for n+m
NplusM = N+M

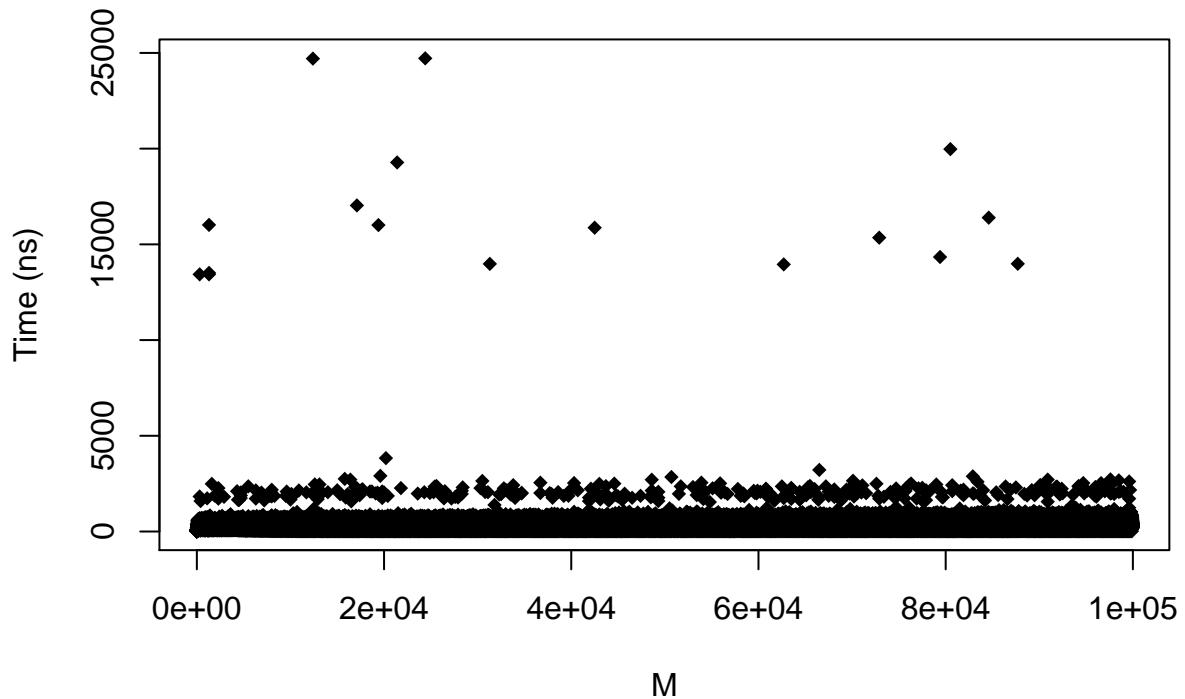
summary(T)

##      Min. 1st Qu. Median    Mean 3rd Qu.    Max.
##      14.0   220.0   274.0   292.3   341.0 24717.0
# min 14
# q1 220
# median 274
# mean 292
# q3 341
# max 24717
plot(N,T,pch=18,xlab="N",ylab="Time (ns)",main="Binomial_Heap.Heap_Union()")
```



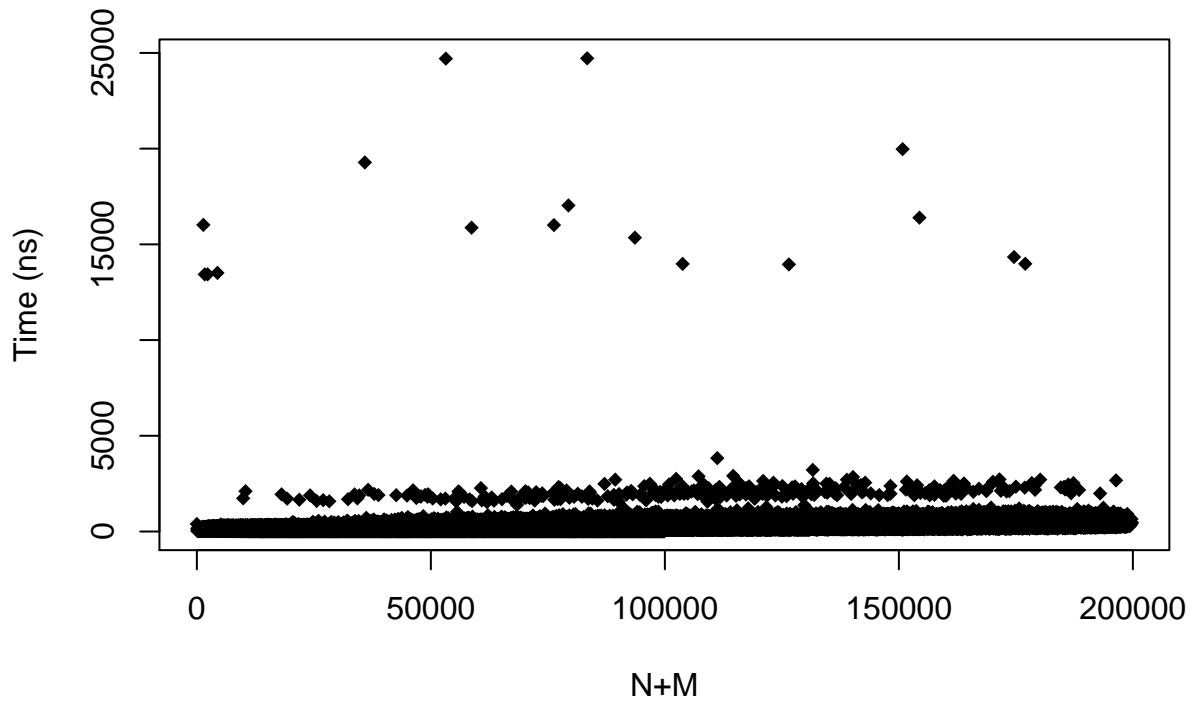
```
plot(M,T,pch=18,xlab="M",ylab="Time (ns)",main="Binomial_Heap.Heap_Union()")
```

Binomial_Heap.Heap_Union()



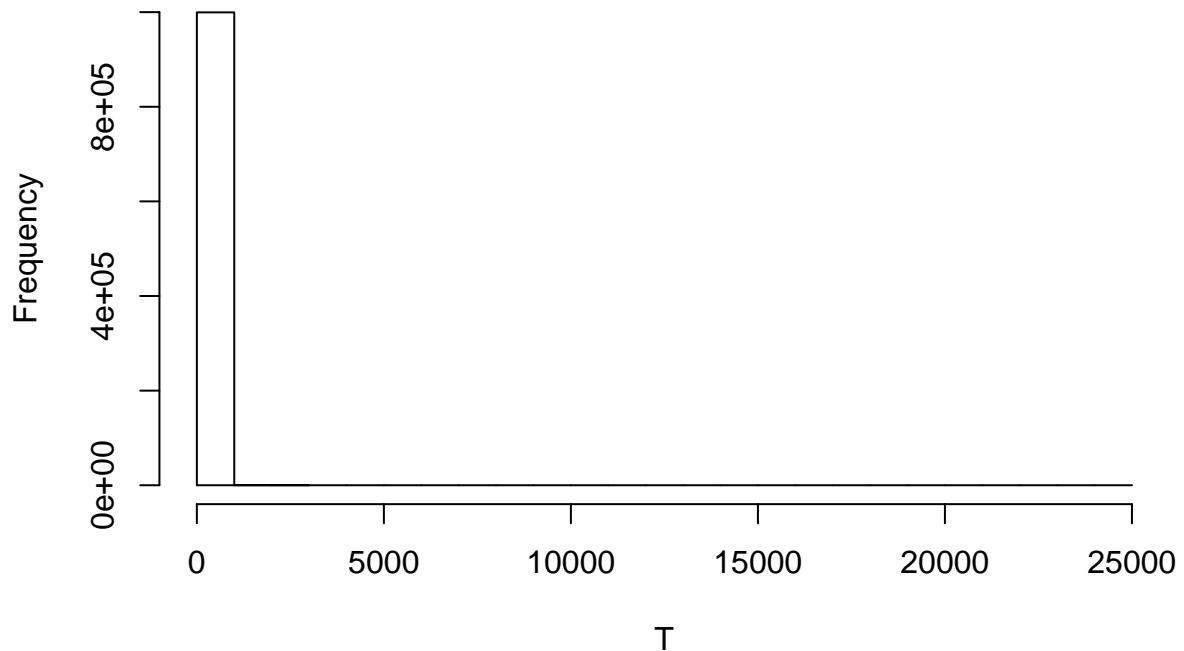
```
plot(NplusM,T,pch=18,xlab="N+M",ylab="Time (ns)",main="Binomial_Heap.Heap_Union()")
```

Binomial_Heap.Heap_Union()



```
hist(T,breaks=30)
```

Histogram of T

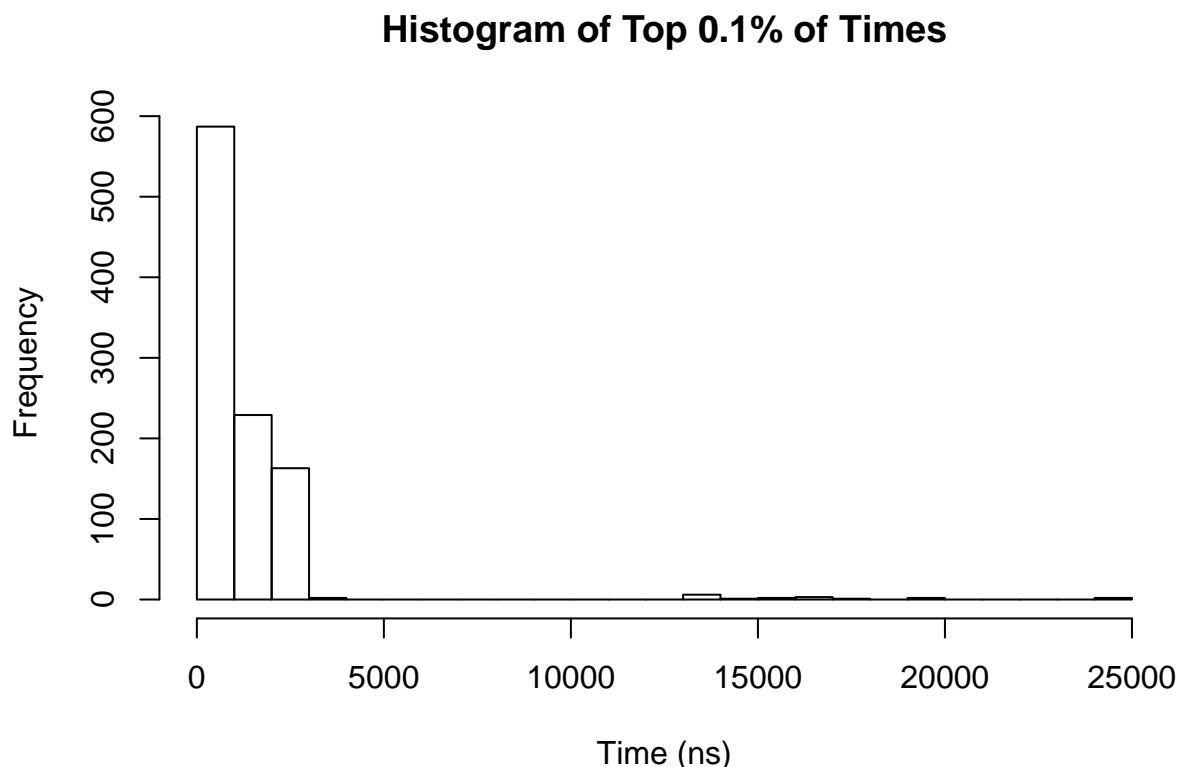


```
# Let's try and remove some outliers
quantile(T,seq(0,1,0.1))
##    0%    10%    20%    30%    40%    50%    60%    70%    80%    90%   100%
##   14    178    208    231    252    274    297    324    362    425  24717
quantile(T,seq(0.9,1,0.01))
##   90%   91%   92%   93%   94%   95%   96%   97%   98%   99%  100%
##  425   434   446   458   472   488   510   540   586   665  24717
quantile(T,seq(0.99,1,0.001))
##  99% 99.1% 99.2% 99.3% 99.4% 99.5% 99.6% 99.7% 99.8% 99.9% 100%
## 665   676   687   701   716   733   753   778   813   872  24717
# Let's separate the top 0.1% and analyze
# Top 0.1%
sum(T>872) # There are 998 outliers
## [1] 998
summary(T[which(T>872)])
##    Min. 1st Qu. Median      Mean 3rd Qu.      Max.
##  873.0   904.0   950.5  1545.3  1861.8 24717.0
```

```

# min 873
# q1 904
# median 950.5
# mean 1545.3
# q3 1861.8
# max 24717
hist(T[which(T>872)],main="Histogram of Top 0.1% of Times",xlab="Time (ns)",breaks=30)

```



```

# Bottom 99.9%
summary(T[which(T<=872)])

```

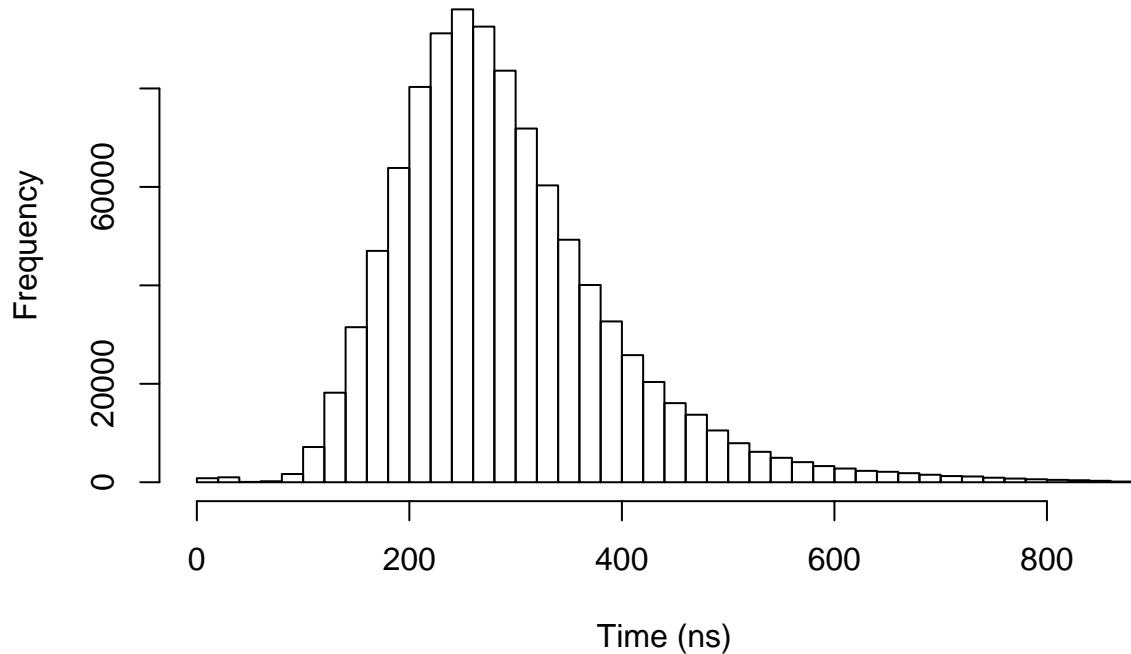
	Min.	1st Qu.	Median	Mean	3rd Qu.	Max.
##	14	220	273	291	341	872

```

# min 14
# q1 220
# median 273
# mean 291
# q3 341
# max 872
hist(T[which(T<=872)],main="Histogram of Bottom 99.9% of Times",xlab="Time (ns)",breaks=40)

```

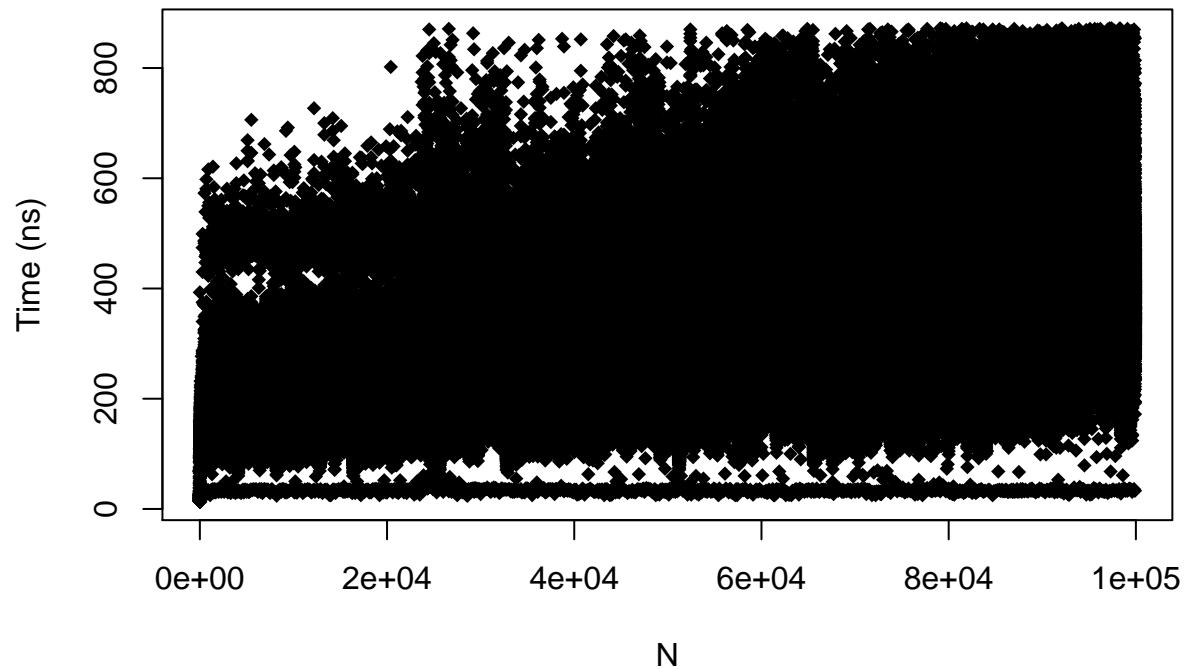
Histogram of Bottom 99.9% of Times



```
# Let's look at the scatterplots again without the outliers
```

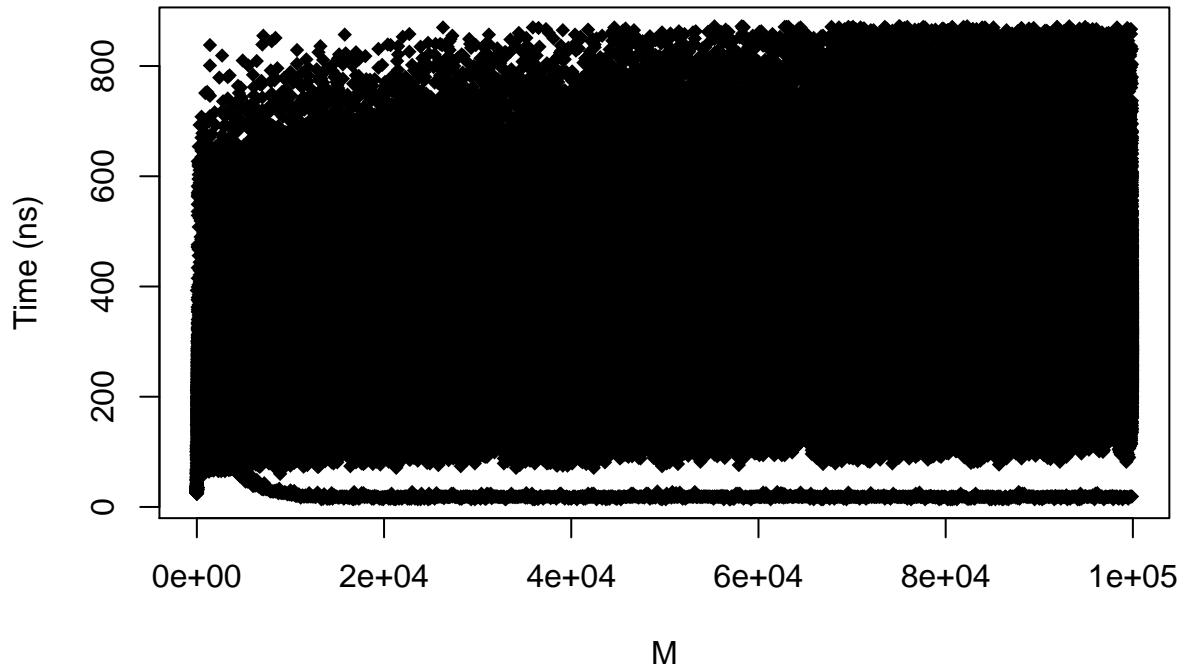
```
plot(N[which(T<=872)],T[which(T<=872)],pch=18,xlab="N",ylab="Time (ns)",main="Binomial_Heap.Heap_Union(
```

Binomial_Heap.Heap_Union() for Bottom 99.9% of Times



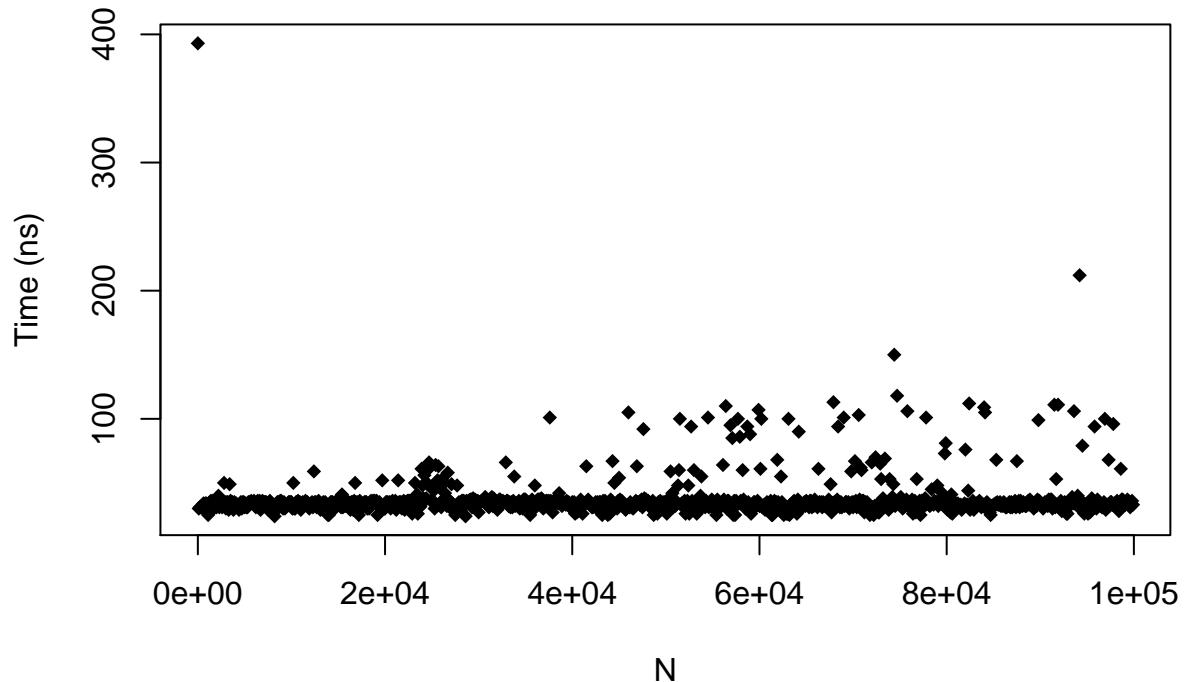
```
plot(M[which(T<=872)],T[which(T<=872)],pch=18,xlab="M",ylab="Time (ns)",main="Binomial_Heap.Heap_Union()")
```

Binomial_Heap.Heap_Union() for Bottom 99.9% of Times



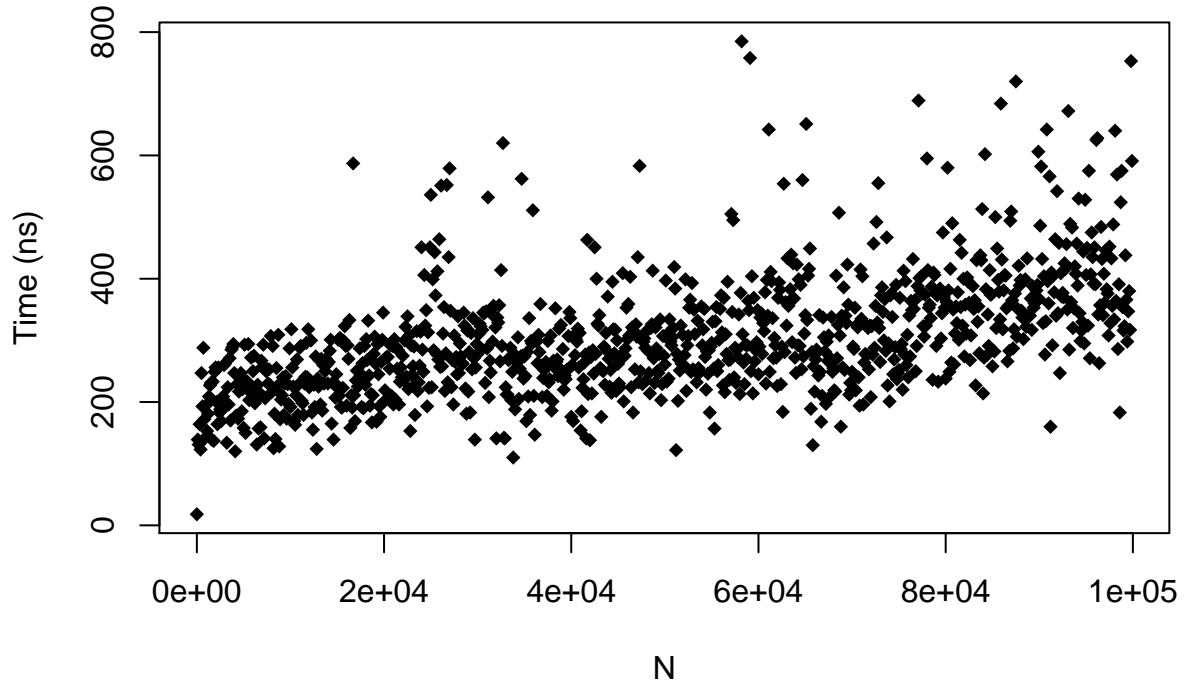
```
# These are a mess! This is because there are multiple T values for a single N or M value.  
# Let's hold N and M constant and retry.  
# N and M take on the same uniform distribution between 0 and 100000.  
# Let's use the start, middle, and end of that range to create scatterplots  
  
plot(N[which(T<=872 & M==0)],T[which(T<=872 & M==0)],pch=18,xlab="N",ylab="Time (ns)",main="Binomial_Hea
```

Binomial_Heap.Heap_Union() for Bottom 99.9% of Times Where M = 0



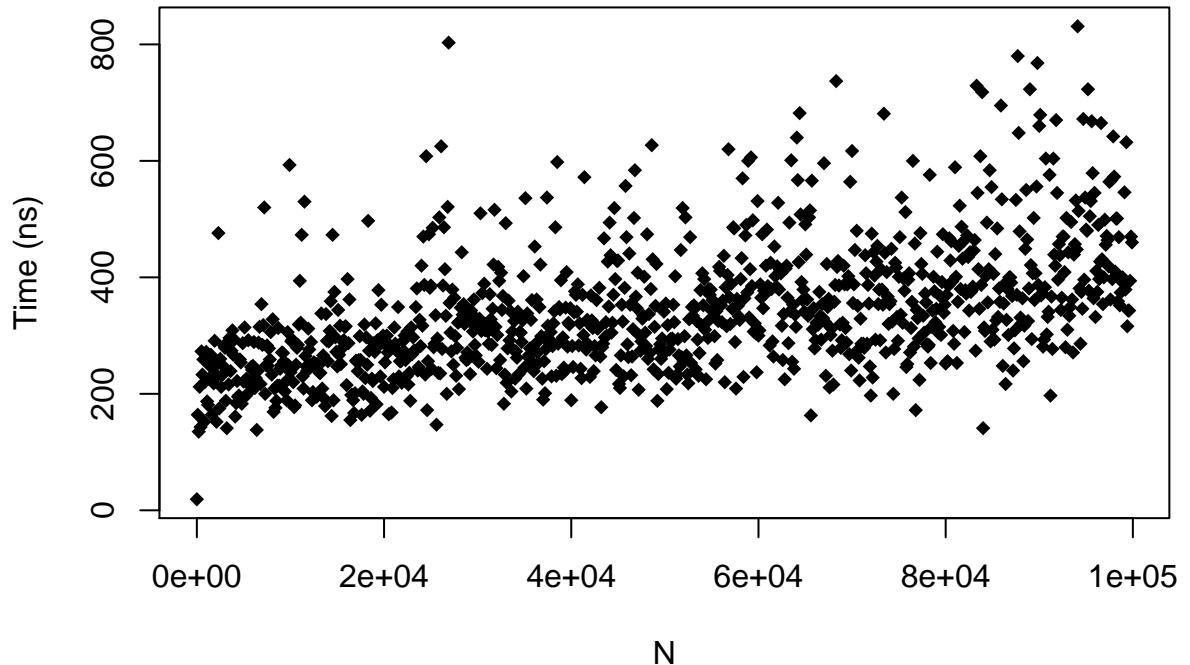
```
plot(N[which(T<=872 & M==49900)],T[which(T<=872 & M==49900)],pch=18,xlab="N",ylab="Time (ns)",main="Binomial_Heap.Heap_Union() for Bottom 99.9% of Times Where M = 0")
```

**Binomial_Heap.Heap_Union() for Bottom 99.9% of Times
Where M = 49900**



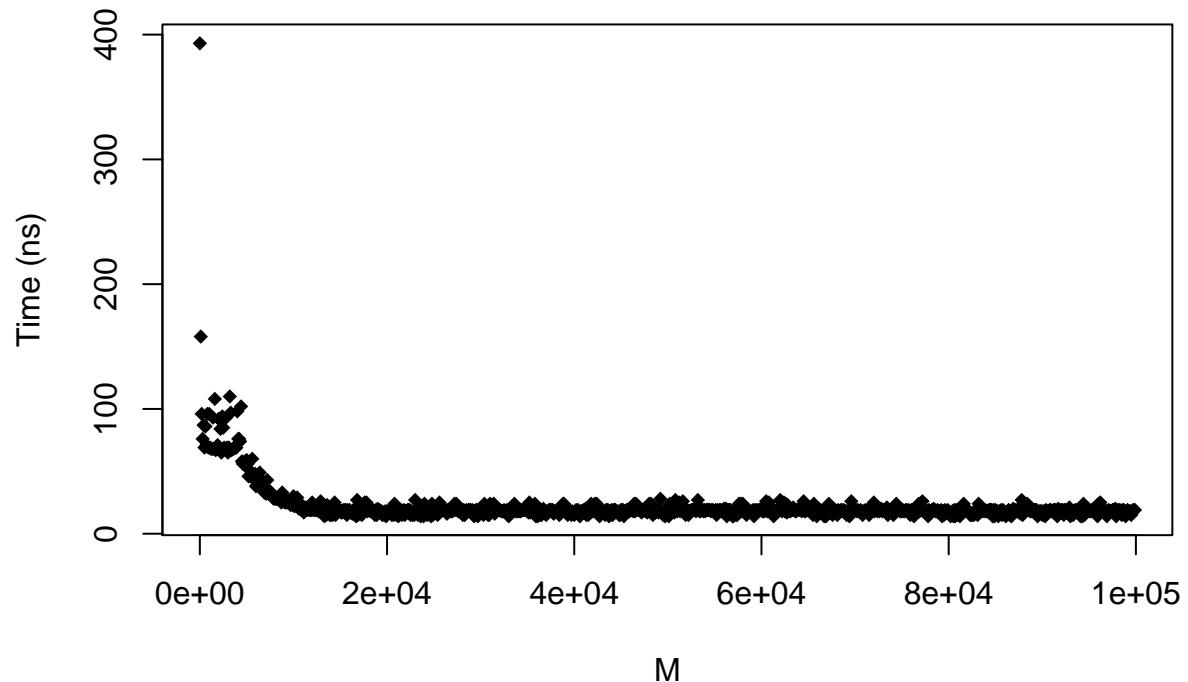
```
plot(N[which(T<=872 & M==99900)],T[which(T<=872 & M==99900)],pch=18,xlab="N",ylab="Time (ns)",main="Binomial_Heap.Heap_Union() for Bottom 99.9% of Times Where M = 49900")
```

Binomial_Heap.Heap_Union() for Bottom 99.9% of Times Where M = 99900



```
plot(M[which(T<=872 & N==0)],T[which(T<=872 & N==0)],pch=18,xlab="M",ylab="Time (ns)",main="Binomial_He")
```

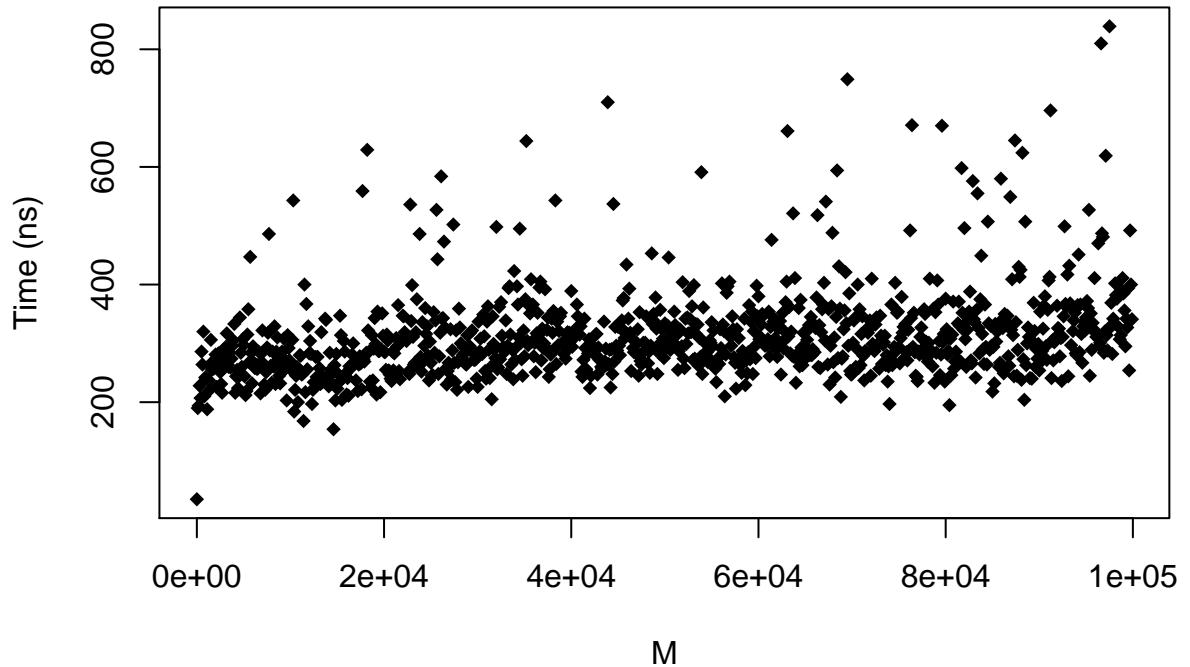
Binomial_Heap.Heap_Union() for Bottom 99.9% of Times Where N = 0



Interesting trend here. The times start high and decrease.

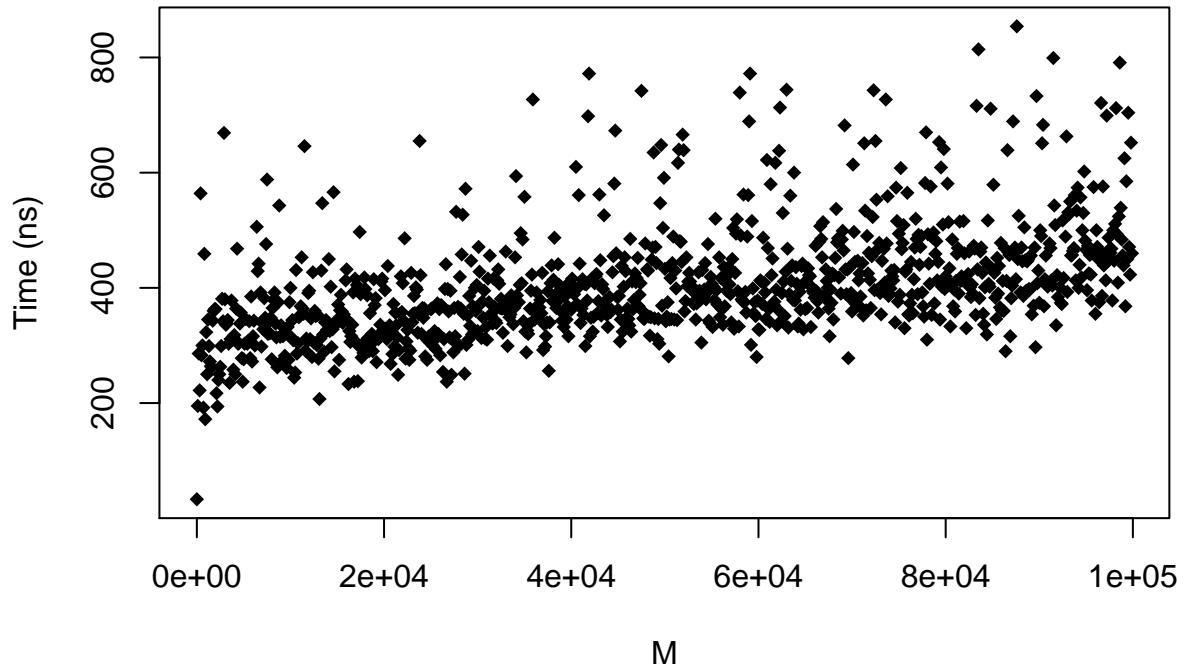
```
plot(M[which(T<=872 & N==49900)],T[which(T<=872 & N==49900)],pch=18,xlab="M",ylab="Time (ns)",main="Bin")
```

Binomial_Heap.Heap_Union() for Bottom 99.9% of Times Where N = 49900



```
plot(M[which(T<=872 & N==99900)],T[which(T<=872 & N==99900)],pch=18,xlab="M",ylab="Time (ns)",main="Binomial_Heap.Heap_Union() for Bottom 99.9% of Times Where N = 49900")
```

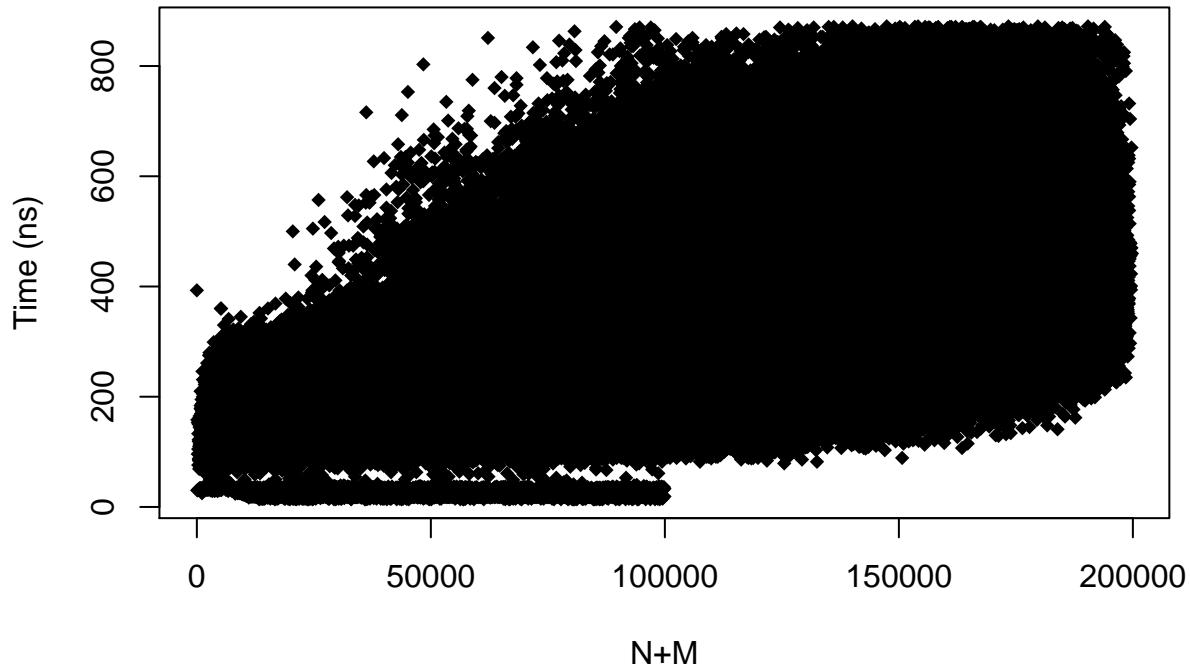
Binomial_Heap.Heap_Union() for Bottom 99.9% of Times Where N = 99900



```
# Since we know that the times should be based on N+M, let's stop all these scatterplots
# and use our N+M variable

plot(NplusM[which(T<=872)],T[which(T<=872)],pch=18,xlab="N+M",ylab="Time (ns)",main="Binomial_Heap.
```

Binomial_Heap.Heap_Union() for Bottom 99.9% of Times



```
# This is also a mess. Let's do multiple regression to take a look
# at the relationship between N+M and T using numbers.

cor(NplusM,T) # Lower correlation of 0.4497216. Good sign for O(log(N+M))

## [1] 0.4497216
lm(T~N+M)

##
## Call:
## lm(formula = T ~ N + M)
##
## Coefficients:
## (Intercept)          N            M
## 1.482e+02   1.969e-03   9.156e-04

lm(T~NplusM)

##
## Call:
## lm(formula = T ~ NplusM)
##
## Coefficients:
## (Intercept)      NplusM
## 1.482e+02   1.442e-03

# All coefficients are very small, which suggests that the relationship is not linear
# as we have seen in operations we know to be linear in time.
```

```
# Because we see positive coefficients and a general increase in time as N and M increase,  
# we can assume that our implementation is correct for O(log(n+m))
```

```
detach(heap_union_binomial)
```