

size.R

Preston

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```
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# CS320 Honors Option
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# size() can be implemented in an  $O(1)$  and an  $O(\log n)$  way.
# To do it in  $O(1)$  time, keep a size_member in the Binomial_Heap object
# and update it for insertions / deletions. In this case, size() just returns that field.
# To do it in  $O(\log n)$  time, iterate through the linked list of binomial trees
# and use the degree of the head of each tree to calculate how many nodes are in each tree.
# Because the length of that list is at most  $\log n$ , size() is  $O(\log n)$ .
# I implemented the  $O(\log n)$  way because I didn't feel like writing the  $O(1)$  implementation.

size_binomial = read.csv("./size_binomial.csv")
attach(size_binomial)

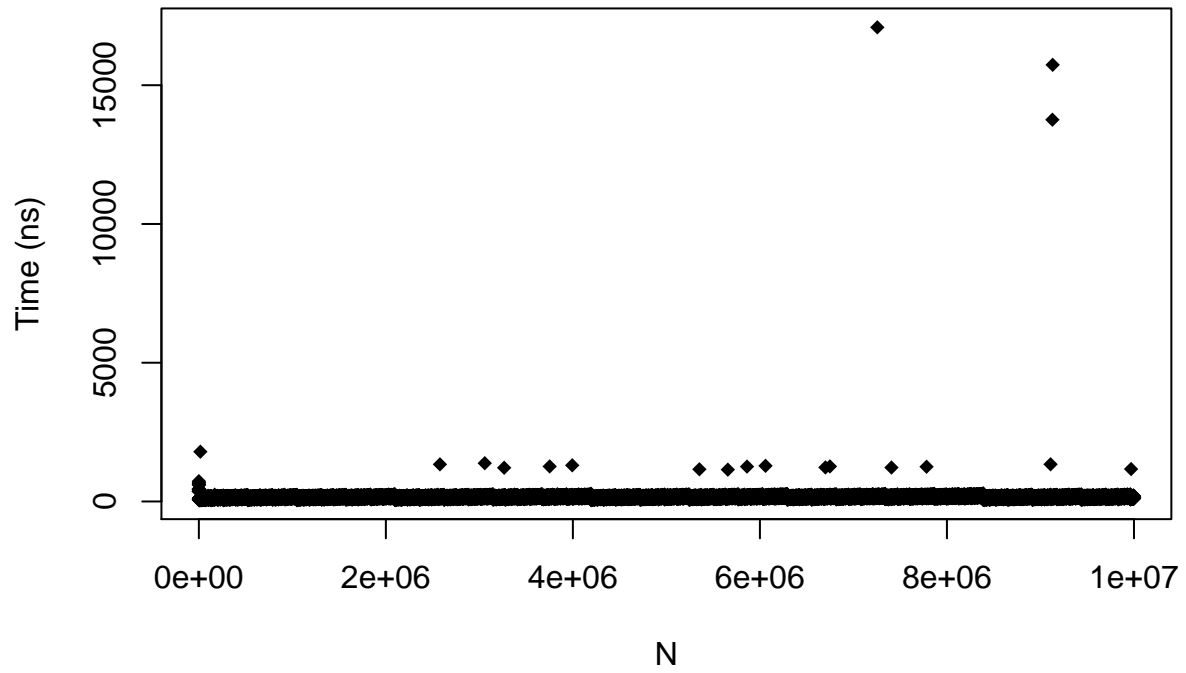
## The following object is masked from package:base:
##
##      T
summary(T)

##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
##      45.0   140.0   157.0   160.6   181.0 17085.0

# min 45
# q1 140
# median 157
# mean 160
# q3 181
# max 17085

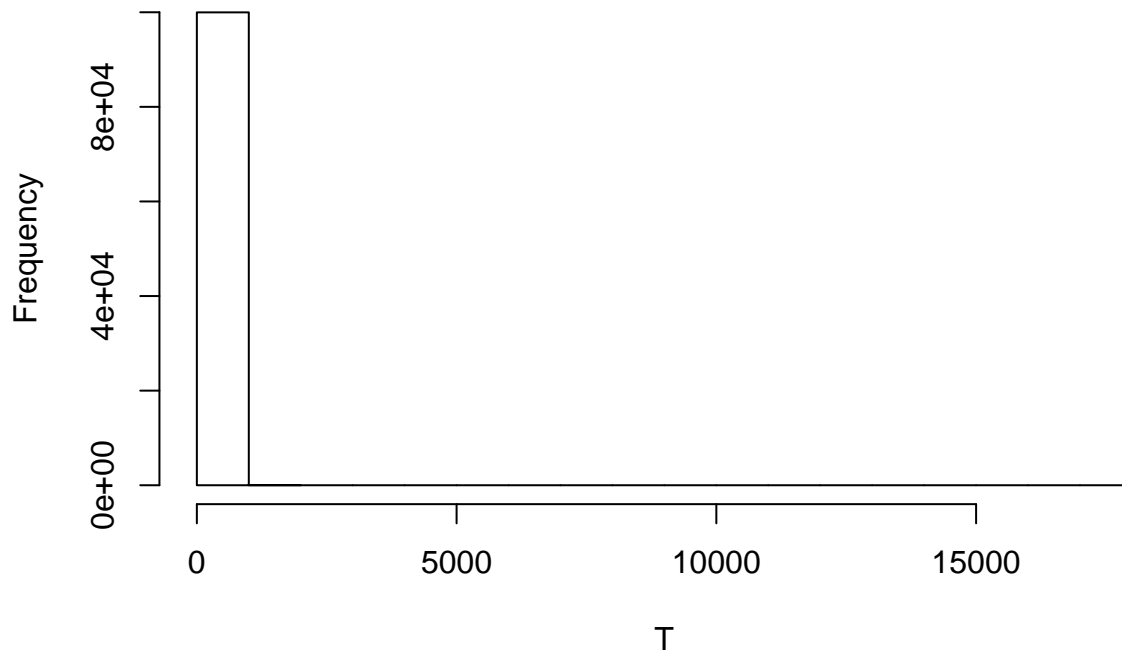
plot(N,T,pch=18,xlab="N",ylab="Time (ns)",main="Binomial Heap.Size()")
```

Binomial Heap.Size()



```
hist(T,breaks=20)
```

Histogram of T



```
# Let's see if we can remove some outliers
```

```
quantile(T,seq(0,1,0.1))
```

```
##      0%      10%      20%      30%      40%      50%      60%      70%      80%      90%     100%
##      45      124      137      142      153      157      167      179      183      196    17085
```

```
quantile(T,seq(0.9,1,0.01))
```

```
##      90%      91%      92%      93%      94%      95%      96%      97%      98%      99%     100%
##      196      198      205      206      207      208      210      219      221      232    17085
```

```
# Let's separate the top 1% and analyze
```

```
# Top 1%
```

```
sum(T>232) # There are 986 outliers
```

```
## [1] 986
```

```
summary(T[which(T>232)])
```

```
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
##      233.0  234.0   236.0   307.4   246.0 17085.0
```

```
# min 233
```

```
# q1 234
```

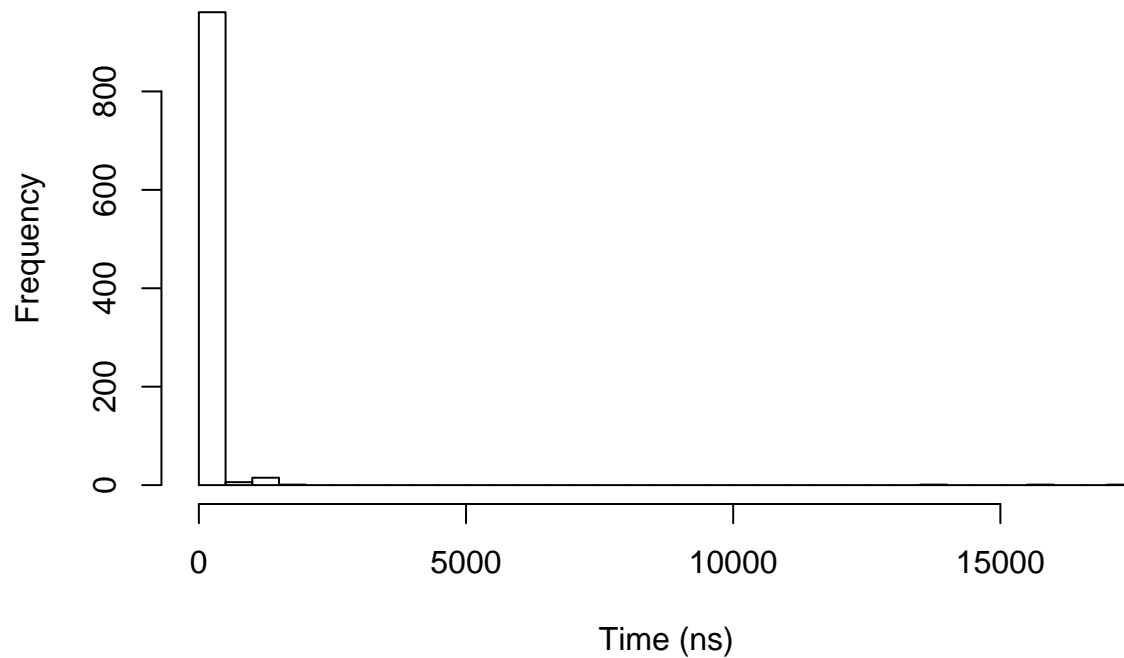
```
# median 236
```

```
# mean 307.4
```

```
# q3 246
```

```
# max 17085
hist(T[which(T>232)],main="Histogram of Top 1% of Times",xlab="Time (ns)",breaks=30)
```

Histogram of Top 1% of Times



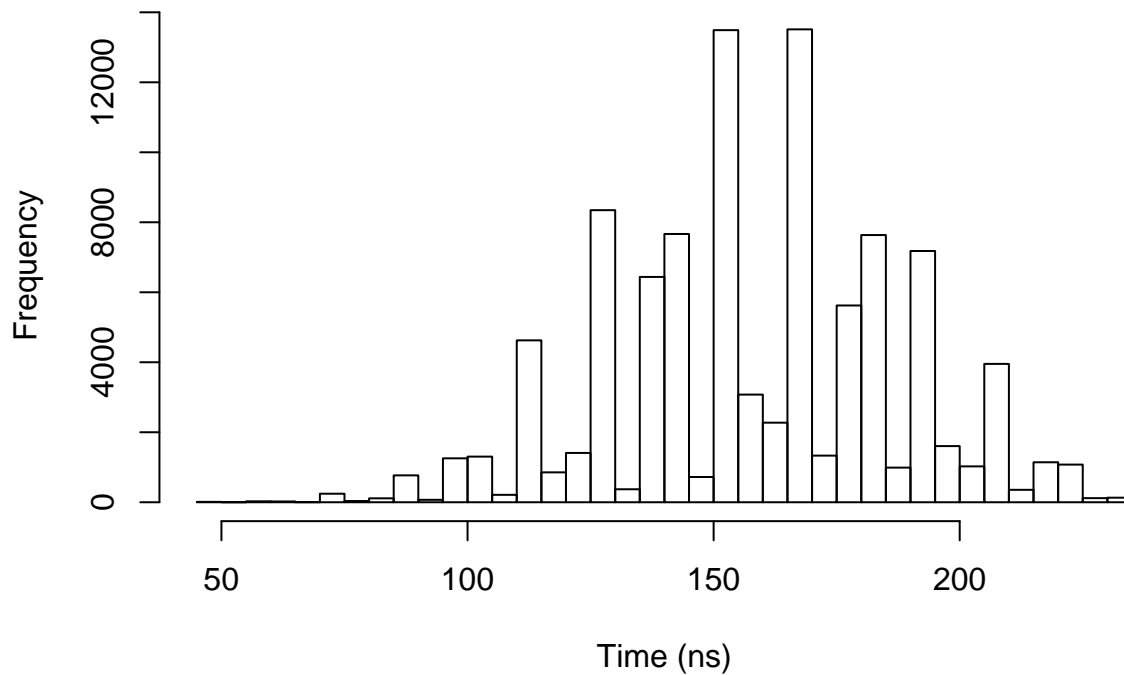
```
# Bottom 99%
summary(T[which(T<=232)])
```

```
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
##      45.0   140.0   156.0   159.1   181.0   232.0
```

```
# min 45
# q1 140
# median 156
# mean 159.1
# q3 181
# max 232
```

```
hist(T[which(T<=232)],main="Histogram of Bottom 99% of Times",xlab="Time (ns)",breaks=30)
```

Histogram of Bottom 99% of Times



```
# Looks like most calls to size() take under 232 ns.  
# There also doesn't appear to be a large correlation between T and N  
# The implementation appears to be O(logn) time like the other operations that have this trend.  
# An O(1) implementation could be achieved by implementing a size_member, but I don't want to  
# bother with that.
```

```
detach(size_binomial)
```