### MLR Model

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#### Imports and Constants

```
library("tidyverse")
## -- Attaching packages --
## v ggplot2 3.3.2 v purrr
## v tibble 3.0.3 v dplyr
                              0.3.4
                             1.0.2
## v tidyr 1.1.2 v stringr 1.4.0
          1.3.1
                   v forcats 0.5.0
## v readr
## -- Conflicts ------ tidyver
## x dplyr::filter() masks stats::filter()
## x dplyr::lag()
                 masks stats::lag()
source('./gibbs_util.R')
## Attaching package: 'pracma'
## The following object is masked from 'package:purrr':
##
##
      cross
## Loading required package: reshape2
## Attaching package: 'reshape2'
## The following object is masked from 'package:tidyr':
##
##
      smiths
RANDOM\_SEED = 440
```

# Data Loading / Cleaning

```
load('./burritodata.Rda')
head(burrito)
##
                   Location Cost Hunger Length Circum Volume Tortilla Temp Meat
## 1
       Donato's taco shop 6.49
                                      3.0
                                               NA
                                                                            5.0 3.0
                                                       NA
                                                               NA
## 2 Oscar's Mexican food 5.45
                                      3.5
                                                                             3.5
                                                                                   2.5
                                               NA
                                                       NA
                                                                             2.0
## 3 Oscar's Mexican food 4.85
                                      1.5
                                               NA
                                                       NA
                                                               NA
                                                                          3
                                                                                   2.5
## 4 Oscar's Mexican food 5.25
                                      2.0
                                               NA
                                                       NA
                                                               NA
                                                                             2.0
                                                                                   3.5
## 5
              Pollos Maria 6.59
                                      4.0
                                               NA
                                                                             5.0
                                                       NA
                                                               NA
                                                                                   4.0
## 6
              Pollos Maria 6.99
                                      4.0
                                                                          3 4.0
                                               NA
                                                       NA
                                                               NA
                                                                                   5.0
##
     Fillings Meat_filling Uniformity Salsa Synergy Wrap Reviewer overall Beef
           3.5
## 1
                         4.0
                                      4.0
                                             4.0
                                                      4.0
                                                             4
                                                                   Scott
                                                                             3.80
## 2
           2.5
                         2.0
                                      4.0
                                             3.5
                                                      2.5
                                                                   Scott
                                                                             3.00
## 3
           3.0
                         4.5
                                      4.0
                                             3.0
                                                      3.0
                                                             5
                                                                   Emily
                                                                             3.00
                                                                                      0
## 4
           3.0
                         4.0
                                      5.0
                                             4.0
                                                      4.0
                                                             5
                                                                Ricardo
                                                                             3.75
                                                                                      1
## 5
           3.5
                         4.5
                                      5.0
                                             2.5
                                                      4.5
                                                             4
                                                                   Scott
                                                                             4.20
                                                                                      1
## 6
           3.5
                         2.5
                                      2.5
                                             2.5
                                                      4.0
                                                             1
                                                                             3.20
                                                                   Emily
     Pico Guac Cheese Fries Sour_cream Pork Chicken Shrimp Fish Rice Beans Lettuce
## 1
                             1
                                                        0
                                                                0
## 2
         1
              1
                      1
                             1
                                         0
                                               0
                                                        0
                                                                0
                                                                     0
                                                                           0
                                                                                  0
                                                                                           0
## 3
                      0
                             0
                                         0
                                                        0
                                                                0
                                                                                  0
                                                                                           0
                                         0
                                                        0
                                                                                  0
## 4
                      0
                             0
                                               0
                                                                0
                                                                     0
                                                                           0
                                                                                           0
         1
              1
## 5
              0
                      1
                             1
                                         0
                                               0
                                                        0
                                                                0
                                                                     0
                                                                                  0
## 6
         0
                      1
                             0
                                         1
                                                        1
                                                                0
                                                                     0
                                                                                  1
              1
                                               0
                                                                           1
     Tomato Bell_peper Carrots Cabbage Sauce Cilantro Onion Taquito Pineapple
## 1
                                0
           0
                       0
                                         0
                                                0
                                                          0
                                                                 0
                                                                          0
## 2
                                                                 0
                                                                                          0
           0
                       0
                                0
                                         0
                                                0
                                                          0
                                                                          0
                                                                                     0
## 3
                                                0
                                                                                          0
           0
                       0
                                0
                                         0
                                                          0
                                                                 0
                                                                          0
                                                                                     0
## 4
           0
                       0
                                0
                                         0
                                                0
                                                          0
                                                                 0
                                                                          0
                                                                                     0
                                                                                          0
## 5
                       0
                                0
                                         0
                                                0
                                                          0
                                                                 0
                                                                                     0
           0
                                                                          0
                                                                                          0
## 6
           1
                       0
                                0
                                         0
                                                0
                                                          0
                                                                 0
                                                                          0
                                                                                          0
     Chile_relleno Nopales Lobster Egg Mushroom Bacon Sushi Avocado
## 1
                   0
                            0
                                     0
                                         0
                                                   0
                                                          0
                                                                 0
                                                                          0
                                                                               0
                                                                                          0
## 2
                   0
                            0
                                     0
                                         0
                                                   0
                                                          0
                                                                 0
                                                                          0
                                                                               0
                                                                                          0
## 3
                   0
                            0
                                     0
                                         0
                                                   0
                                                          0
                                                                 0
                                                                          0
                                                                               0
                                                                                          0
## 4
                   0
                            0
                                     0
                                         0
                                                   0
                                                          0
                                                                 0
                                                                               0
                                                                                          0
## 5
                   0
                            0
                                     0
                                         0
                                                   0
                                                          0
                                                                 0
                                                                          0
                                                                               0
                                                                                          0
## 6
                            0
                                     0
                                                          0
                                                                 0
                                                                               0
                                                                                          0
# Count Remove NA Cost rows
which(is.na(burrito$Cost))
## [1] 113 135
```

```
burrito = burrito[!is.na(burrito$Cost),]
nrow(burrito)
```

## [1] 237

burrito<-burrito%>%mutate(Vegetable=as.logical(Pineapple+Bell\_peper+Tomato+Cabbage+Mushroom+Corn+Carrot burrito<-burrito%>%mutate(Breakfast=as.logical(Egg+Bacon+Ham))

```
burrito<-burrito%>%mutate(Other=as.logical(Fish+Taquito+Chile_relleno+Nopales+Sushi+Lobster))
burrito<-select(burrito, -c('Pineapple','Bell_peper','Tomato','Cabbage','Mushroom','Corn','Carrots','Zu
burrito<-burrito%>%mutate_at(c('Vegetable','Other','Breakfast'),as.double)
head(burrito)
```

```
##
                  Location Cost Hunger Length Circum Volume Tortilla Temp Meat
                                     3.0
## 1
       Donato's taco shop 6.49
                                                                            5.0
                                                                                 3.0
                                              NA
                                                      NA
                                                              NA
## 2 Oscar's Mexican food 5.45
                                     3.5
                                              NA
                                                      NA
                                                              NA
                                                                         2
                                                                            3.5
                                                                                 2.5
## 3 Oscar's Mexican food 4.85
                                     1.5
                                              NA
                                                      NA
                                                              NA
                                                                            2.0
                                                                                 2.5
                                                                         3
## 4 Oscar's Mexican food 5.25
                                     2.0
                                              NA
                                                      NA
                                                             NA
                                                                         3
                                                                            2.0
                                                                                 3.5
                                     4.0
                                                                            5.0
## 5
              Pollos Maria 6.59
                                              NA
                                                      NA
                                                              NA
                                                                                4.0
                                                                         4
## 6
              Pollos Maria 6.99
                                     4.0
                                              NA
                                                      NA
                                                             NA
                                                                         3
                                                                            4.0 5.0
##
     Fillings Meat_filling Uniformity Salsa Synergy Wrap Reviewer overall Beef
## 1
          3.5
                         4.0
                                     4.0
                                            4.0
                                                     4.0
                                                            4
                                                                  Scott
                                                                            3.80
## 2
           2.5
                         2.0
                                     4.0
                                            3.5
                                                     2.5
                                                            5
                                                                  Scott
                                                                            3.00
                                                                                     1
## 3
           3.0
                         4.5
                                     4.0
                                            3.0
                                                     3.0
                                                            5
                                                                  Emily
                                                                            3.00
                                                                                     0
## 4
          3.0
                         4.0
                                     5.0
                                            4.0
                                                                            3.75
                                                     4.0
                                                            5 Ricardo
                                                                                     1
## 5
          3.5
                         4.5
                                     5.0
                                            2.5
                                                     4.5
                                                            4
                                                                  Scott
                                                                            4.20
                                                                                     1
## 6
           3.5
                         2.5
                                     2.5
                                            2.5
                                                     4.0
                                                            1
                                                                  Emily
                                                                            3.20
                                                                                     0
##
     Pico Guac Cheese Fries Sour_cream Pork Chicken Shrimp Rice Beans Lettuce
## 1
              1
                            1
                                        0
                                              0
                                                       0
                                                               0
                                                                    0
                                                                           0
## 2
                                        0
                                              0
                                                       0
                                                               0
                                                                    0
                                                                           0
                                                                                    0
        1
              1
                      1
                            1
## 3
        1
              1
                      0
                            0
                                        0
                                              1
                                                       0
                                                               0
                                                                    0
                                                                           0
                                                                                    0
## 4
                      0
                            0
                                        0
                                              0
                                                       0
                                                               0
                                                                    0
                                                                           0
                                                                                    0
              1
        1
## 5
        1
                      1
                            1
                                        0
                                              0
                                                       0
                                                               0
                                                                    0
                                                                           0
                                                                                    0
## 6
        0
              1
                      1
                            0
                                        1
                                              0
                                                       1
                                                               0
                                                                    1
                                                                           1
                                                                                    1
     Sauce Cilantro Onion Bacon Avocado Vegetable Breakfast
##
## 1
         0
                   0
                                          0
                                                     0
                          0
                                 0
                                                                      0
         0
                   0
                                                                      0
## 2
                          0
                                 0
                                          0
                                                     0
                                                                0
## 3
         0
                                                     0
                                                                0
                                                                      0
                   0
                          0
                                 0
                                          0
## 4
         0
                   0
                          0
                                 0
                                          0
                                                     0
                                                                0
                                                                      0
## 5
         0
                   0
                                 0
                                          0
                                                     0
                                                                0
                                                                      0
                          0
## 6
         0
                   0
                          0
                                 0
                                          0
                                                     1
                                                                0
                                                                      0
```

```
ingredient_cols = colnames(burrito)[18:37]
ingredient_X = as.matrix(burrito[ingredient_cols])
dim(ingredient_X); head(ingredient_X)
```

```
## [1] 237 20
```

##		Beef	Pico	Guac	Cheese	Fries	Sour_c	ream	${\tt Pork}$	Chicken	${\tt Shrimp}$	${\tt Rice}$	Beans
##	[1,]	1	1	1	1	1		0	0	0	0	0	0
##	[2,]	1	1	1	1	1		0	0	0	0	0	0
##	[3,]	0	1	1	0	0		0	1	0	0	0	0
##	[4,]	1	1	1	0	0		0	0	0	0	0	0
##	[5,]	1	1	0	1	1		0	0	0	0	0	0
##	[6,]	0	0	1	1	0		1	0	1	0	1	1
##		Lettu	ce S	auce (	Cilantro	Onion	Bacon	Avoc	cado V	/egetable	e Breakt	fast (	Other
##	[1,]		0	0	C	) (	0		0	(	)	0	0
##	[2,]		0	0	C	) (	0		0	(	)	0	0
##	[3,]		0	0	C	) (	0		0	(	)	0	0

#### Model Fit with Gibbs Sampler

```
set.seed(RANDOM_SEED)

p = ncol(ingredient_X) + 1

tau_2 = 4

prior_sigma = 1.5

a = 1 / (prior_sigma^4)
b = 1 / (prior_sigma^2)

post_dist = mlr_gibbs(ingredient_X, cost_y, mu=rep(0, p), tau_2, a, b)
post_dist = post_dist[5001:1000, ]
head(post_dist)
```

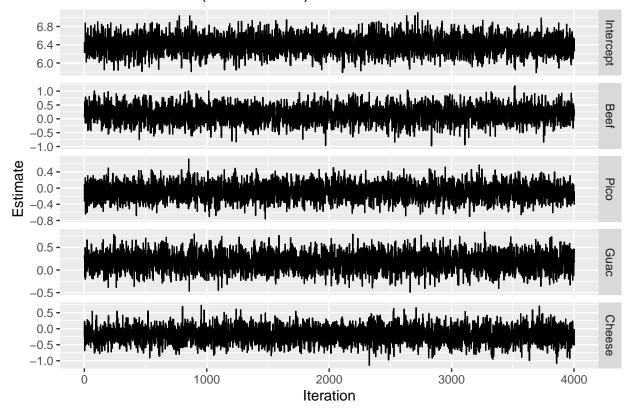
```
##
       Intercept
                      Beef
                                 Pico
                                            Guac
                                                    Cheese
                                                               Fries
## [1,] 6.457323 0.14732084 0.10498064 0.3292975 -0.2687287 0.07278756
       6.230226 0.06600002 -0.32106258 0.2469540 0.2267794 0.30107685
## [2,]
       6.337929 0.32886158 -0.12912433 0.2607176 -0.6843773 0.72381129
## [3,]
       6.270581 0.61552338 -0.11429203 0.1452726 -0.3716379 0.15098337
        6.382961 0.38377479 0.03512385 -0.1591162 -0.1348034 0.14152734
## [5,]
## [6,]
       6.409782 0.16454399 -0.22361254 0.4933260 0.1153033 0.17706473
##
       Sour cream
                                Chicken
                                           Shrimp
                        Pork
                                                        Rice
## [1,] 0.6005529 0.10435494 0.38171132 1.3362527 -0.30623467 -0.3977458
## [2,] 0.3924969 0.65234797 0.32672399 1.5144784 -0.03185142 -0.5693427
## [3,] 0.1409256 -0.02688308 0.95340142 1.3045827 0.14504859 -0.2310543
## [4,]
       0.5427439 0.17205256 -0.07227909 0.6228603 0.22285072 -0.2981898
## [5,]
       0.2447920 0.67862036 -0.03876074 1.3723927 0.30107326 -1.1899112
## [6,] -0.1505483 -0.07035614 0.15116520 0.5530529 0.31118019 -0.4697745
##
          Lettuce
                       Sauce
                              Cilantro
                                            Onion
                                                       Bacon
                                                                Avocado
## [1,]
       0.0514829 -0.02662257 -1.2774799 1.02905652 0.3399074 0.83556669
## [2,]
       0.4711304 -0.23048708 0.2321436 -0.46798069
                                                  0.2205063 0.80705995
## [3,]
       0.2266287 0.17267496 0.1164244 0.09069149
                                                   1.0152561
                                                            0.07163328
0.9923300 0.42192685 -0.2755737 -0.31124968 -0.1375917 -0.17809750
## [6,] 0.5618469 -0.21932279 -1.5656351 1.44070028 1.7297049 1.26642241
         Vegetable Breakfast
##
                                Other
                                         sigma
## [1,] -0.29091587 -0.5525855 0.8586459 1.171498
## [2,] 0.53883107 -0.9508692 1.4629677 1.054488
## [3,] 0.24809310 0.1382003 1.0314996 1.066971
```

```
## [4,] 0.17801284 -0.4203790 1.0541865 1.158596
## [5,] 0.34353953 -0.4983536 1.2487876 1.218173
## [6,] 0.04511161 -1.9742351 0.9298518 1.156093
```

## **Model Diagnostics**

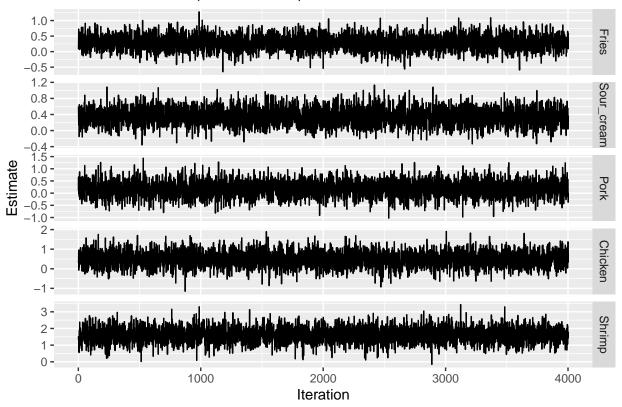
```
plot_traces(post_dist[,1:5], 'Parameter Traces (After Burn In)')
```

#### Parameter Traces (After Burn In)

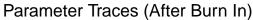


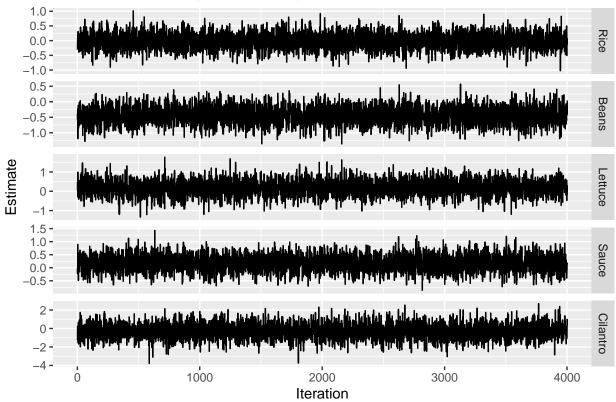
plot\_traces(post\_dist[,6:10], 'Parameter Traces (After Burn In)')

#### Parameter Traces (After Burn In)



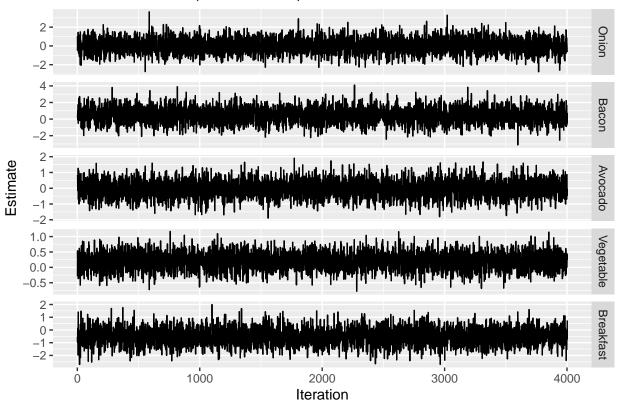
plot\_traces(post\_dist[,11:15], 'Parameter Traces (After Burn In)')





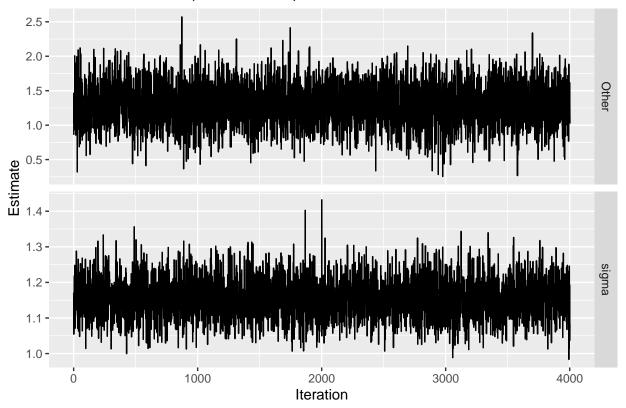
plot\_traces(post\_dist[,16:20], 'Parameter Traces (After Burn In)')

#### Parameter Traces (After Burn In)



plot\_traces(post\_dist[,21:22], 'Parameter Traces (After Burn In)')

## Parameter Traces (After Burn In)



summarize\_dist(post\_dist, colnames(post\_dist))

Parameter	Post. Mean	Post. Sd	95% CI Low	95% CI High
Intercept	6.4018019	0.1925394	6.0300919	6.7802210
Beef	0.1713374	0.2965908	-0.4084506	0.7565898
Pico	-0.0889503	0.1993238	-0.4712776	0.3023580
Guac	0.1828112	0.1987330	-0.2011067	0.5706622
Cheese	-0.1873992	0.2489841	-0.6794948	0.3112114
Fries	0.2930892	0.2370922	-0.1668237	0.7594959
Sour_cream	0.3467485	0.2143117	-0.0616446	0.7803448
Pork	0.1820559	0.3296050	-0.4748285	0.8220752
Chicken	0.4931122	0.3919773	-0.2858897	1.2553760
Shrimp	1.6144664	0.4566544	0.7128927	2.5349351
Rice	-0.0138185	0.2738275	-0.5461606	0.5160242
Beans	-0.4423016	0.2832106	-0.9958315	0.1122606
Lettuce	0.1806142	0.4030846	-0.6082863	0.9632470
Sauce	0.1749063	0.3140238	-0.4469121	0.7862746
Cilantro	-0.2735357	0.8311912	-1.9075545	1.3902547
Onion	0.0417970	0.7897053	-1.5060108	1.5679840
Bacon	0.4852320	0.9353513	-1.3491983	2.2827975
Avocado	-0.0375106	0.5550635	-1.1247251	1.0443457
Vegetable	0.2003486	0.2795536	-0.3587789	0.7429298
Breakfast	-0.5281622	0.6648215	-1.8195506	0.8246326
Other	1.3065765	0.3052995	0.7141348	1.8949340

Parameter	Post. Mean	Post. Sd	95% CI Low	95% CI High
sigma	1.1542459	0.0556615	1.0497315	1.2689966

# Model Interpretations