MLR Model

Preston Dunton, Trevor Overton, Jasmine DeMeyer

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Imports and Constants

```
library("tidyverse")
source('./gibbs_util.R')

RANDOM_SEED = 440
```

Data Loading / Cleaning

```
load('./burritodata.Rda')
head(burrito)
```

```
##
                   Location Cost Hunger Length Circum Volume Tortilla Temp Meat
## 1
       Donato's taco shop 6.49
                                      3.0
                                               NA
                                                       NA
                                                               NA
                                                                          3
                                                                             5.0
                                                                                   3.0
## 2 Oscar's Mexican food 5.45
                                      3.5
                                               NA
                                                       NA
                                                               NA
                                                                          2
                                                                             3.5
                                                                                   2.5
## 3 Oscar's Mexican food 4.85
                                      1.5
                                                                             2.0
                                               NA
                                                      NA
                                                               NA
                                                                                   2.5
                                                                             2.0
## 4 Oscar's Mexican food 5.25
                                      2.0
                                               NA
                                                       NA
                                                               NA
                                                                          3
                                                                                   3.5
              Pollos Maria 6.59
## 5
                                      4.0
                                               NA
                                                      NA
                                                               NA
                                                                             5.0
                                                                                   4.0
## 6
              Pollos Maria 6.99
                                      4.0
                                               NA
                                                      NA
                                                               NA
                                                                             4.0
##
     Fillings Meat_filling Uniformity Salsa Synergy Wrap Reviewer overall Beef
           3.5
## 1
                         4.0
                                      4.0
                                             4.0
                                                      4.0
                                                             4
                                                                   Scott
                                                                             3.80
                                                                   Scott
## 2
           2.5
                         2.0
                                      4.0
                                             3.5
                                                      2.5
                                                             5
                                                                             3.00
                                                                                      1
## 3
           3.0
                         4.5
                                      4.0
                                             3.0
                                                      3.0
                                                                   Emily
                                                                             3.00
## 4
           3.0
                         4.0
                                      5.0
                                             4.0
                                                      4.0
                                                                Ricardo
                                                                             3.75
                                                             5
                                                                                      1
## 5
           3.5
                         4.5
                                      5.0
                                             2.5
                                                      4.5
                                                             4
                                                                   Scott
                                                                             4.20
## 6
           3.5
                         2.5
                                      2.5
                                             2.5
                                                      4.0
                                                             1
                                                                   Emily
                                                                             3.20
##
     Pico Guac Cheese Fries Sour_cream Pork Chicken Shrimp Fish Rice Beans Lettuce
                                                        0
                                                                0
                                                                     0
                                                                                  0
## 1
              1
                      1
                             1
                                         0
                                               0
                                                                           0
         1
## 2
         1
              1
                      1
                             1
                                         0
                                               0
                                                        0
                                                                0
                                                                     0
                                                                           0
                                                                                  0
                             0
## 3
         1
              1
                      0
                                         0
                                               1
                                                        0
                                                                0
                                                                     0
                                                                           0
                                                                                  0
                                                                                           0
## 4
                             0
                                         0
                                                        0
                                                                0
                                                                                           0
         1
              1
                                         0
                                               0
                                                        0
                                                                                  0
                                                                                          0
## 5
         1
              0
                      1
                             1
                                                                0
                                                                     0
                                                                           0
## 6
                      1
                                         1
                                                        1
     Tomato Bell_peper Carrots Cabbage Sauce Cilantro Onion Taquito Pineapple Ham
##
                                                0
## 1
           0
                       0
                                0
                                         0
                                                          0
                                                                 0
                                                                          0
## 2
           0
                       0
                                0
                                         0
                                                0
                                                          0
                                                                 0
                                                                          0
                                                                                     0
                                                                                         0
```

```
## 3
                        0
                                  0
                                                  0
                                                                                             0
## 4
                        0
                                  0
                                           0
                                                  0
           0
                                                             0
                                                                    0
                                                                             0
                                                                                             0
## 5
                        0
                                  0
                                           0
                                                  0
                                  0
                                           0
                                                  0
## 6
                        Ω
                                                             0
                                                                    0
                                                                             0
                                                                                         0
                                                                                             0
           1
##
     Chile_relleno Nopales Lobster Egg Mushroom Bacon Sushi Avocado Corn Zucchini
                             0
                                      0
                                           0
                                                     0
                                                             0
                                                                    0
## 1
                   0
                                                                             0
                                                                                   0
## 2
                   0
                             0
                                      0
                                           0
                                                     0
                                                                    0
                                                                                   0
                                                             0
                                                                             0
                                                                                              0
## 3
                                           0
                   0
                             0
                                      0
                                                     0
                                                             0
                                                                    0
                                                                             0
                                                                                   0
                                                                                              0
## 4
                   0
                             0
                                      0
                                           0
                                                     0
                                                             0
                                                                    0
                                                                             0
                                                                                   0
                                                                                              0
## 5
                    0
                             0
                                      0
                                           0
                                                                    0
                                                                                   0
                                                                                              0
                                                     0
                                                             0
                                                                             0
## 6
                    0
                             0
                                      0
                                           0
                                                      0
                                                                    0
                                                                                   0
                                                                                              0
```

```
# Count Remove NA Cost rows
which(is.na(burrito$Cost))
```

[1] 113 135

```
burrito = burrito[!is.na(burrito$Cost),]
nrow(burrito)
```

[1] 237

```
##
                 Location Cost Hunger Length Circum Volume Tortilla Temp Meat
## 1
       Donato's taco shop 6.49
                                   3.0
                                            NA
                                                                     3 5.0
                                                   NA
                                                           NA
                                                                              3.0
## 2 Oscar's Mexican food 5.45
                                   3.5
                                            NA
                                                   NA
                                                           NA
                                                                     2
                                                                        3.5
                                                                              2.5
## 3 Oscar's Mexican food 4.85
                                   1.5
                                            NA
                                                   NA
                                                           NA
                                                                     3
                                                                        2.0
                                                                              2.5
## 4 Oscar's Mexican food 5.25
                                   2.0
                                            NA
                                                   NA
                                                           NA
                                                                     3
                                                                        2.0
                                                                              3.5
## 5
             Pollos Maria 6.59
                                   4.0
                                            NA
                                                   NA
                                                           NA
                                                                        5.0
                                                                     4
                                                                              4.0
## 6
             Pollos Maria 6.99
                                   4.0
                                            NΑ
                                                   NA
                                                           NA
                                                                     3 4.0 5.0
     Fillings Meat_filling Uniformity Salsa Synergy Wrap Reviewer overall Beef
## 1
          3.5
                        4.0
                                                  4.0
                                                               Scott
                                                                         3.80
                                   4.0
                                          4.0
                                                          4
                                                                                 1
## 2
          2.5
                        2.0
                                   4.0
                                          3.5
                                                  2.5
                                                          5
                                                               Scott
                                                                         3.00
                                                                                 1
## 3
          3.0
                        4.5
                                   4.0
                                          3.0
                                                                         3.00
                                                  3.0
                                                          5
                                                               Emily
                                                                                 0
## 4
          3.0
                        4.0
                                   5.0
                                          4.0
                                                  4.0
                                                          5 Ricardo
                                                                         3.75
## 5
          3.5
                        4.5
                                   5.0
                                          2.5
                                                  4.5
                                                                         4.20
                                                          4
                                                               Scott
                                                                                 1
## 6
          3.5
                        2.5
                                   2.5
                                          2.5
                                                  4.0
                                                          1
                                                               Emily
                                                                         3.20
     Pico Guac Cheese Fries Sour_cream Pork Chicken Shrimp Rice Beans Lettuce
                                      0
                                            0
                                                    0
                                                                 0
                                                                       0
## 1
             1
                    1
                           1
                                                            0
## 2
                     1
                                       0
                                            0
                                                    0
                                                                 0
                                                                       0
                                                                                0
        1
             1
                           1
                                                            0
```

```
0
## 3
                                                               0
                                                                                    0
## 4
        1
              1
                      0
                            0
                                         0
                                              0
                                                       0
                                                               0
                                                                           0
                                              0
                                                       0
                                                                           0
                                                                                    0
## 5
              0
                      1
                            1
                                                               0
## 6
        0
                            0
                                         1
                                              0
                                                       1
                                                               0
                                                                           1
                                                                                    1
              1
                      1
##
     Sauce Cilantro Onion Avocado Vegetable Breakfast Other
## 1
         0
                   0
                                              0
                          0
                                   0
## 2
         0
                   0
                          0
                                   0
                                              0
                                                         0
                                                                0
## 3
         0
                   0
                                   0
                                              0
                                                         0
                                                                0
                          0
## 4
         0
                   0
                          0
                                   0
                                              0
                                                         0
                                                                0
## 5
         0
                   0
                          0
                                   0
                                              0
                                                         0
                                                                0
## 6
                   0
                          0
                                   0
                                              1
                                                                0
ingredient_cols = colnames(burrito)[18:36]
ingredient_X = as.matrix(burrito[ingredient_cols])
dim(ingredient_X); head(ingredient_X)
## [1] 237 19
        Beef Pico Guac Cheese Fries Sour_cream Pork Chicken Shrimp Rice Beans
##
## [1,]
                              1
                                     1
                                                 0
                 1
                       1
## [2,]
                                                       0
                                                                                    0
            1
                 1
                       1
                              1
                                     1
                                                 0
                                                                0
                                                                        0
                                                                             0
## [3,]
            0
                       1
                              0
                                     0
                                                 0
                                                       1
                                                                0
                                                                        0
                                                                                    0
## [4,]
                              0
                                     0
                                                 0
                                                       0
                                                                0
                                                                        0
                                                                             0
                                                                                    0
            1
                       1
                 1
                                                       0
## [5,]
            1
                       0
                               1
                                     1
                                                 0
                                                                0
                                                                        0
                                                                             0
                                                                                    0
## [6,]
            0
                 0
                       1
                                     0
                                                 1
                                                       0
                                                                1
                                                                        0
                                                                             1
                                                                                    1
                              1
        Lettuce Sauce Cilantro Onion Avocado Vegetable Breakfast Other
## [1,]
               0
                      0
                                0
                                      0
                                               0
## [2,]
               0
                      0
                                0
                                      0
                                               0
                                                          0
                                                                     0
                                                                            0
## [3,]
                      0
                                               0
                                                          0
                                                                            0
               0
                                0
                                      0
                                                                     0
## [4,]
               0
                                0
                                      0
                                               0
                                                          0
                                                                     0
                                                          0
               0
                      0
                                0
                                      0
                                               0
                                                                            0
## [5,]
                                                                     0
## [6,]
                                      0
                                               0
cost_y = burrito$Cost
length(cost_y); head(cost_y)
## [1] 237
## [1] 6.49 5.45 4.85 5.25 6.59 6.99
```

Model Fit with Gibbs Sampler

```
set.seed(RANDOM_SEED)

p = ncol(ingredient_X) + 1
tau_2 = 4
prior_sigma = 1.5
a = 1 / (prior_sigma^4)
```

```
b = 1 / (prior_sigma^2)
mlr_post_dist = mlr_gibbs(ingredient_X, cost_y, mu=rep(0, p), tau_2, a, b)
mlr_post_dist = mlr_post_dist[5001:1000, ]
summarize_dist(mlr_post_dist, colnames(mlr_post_dist), round_places=2)
```

Parameter Post	. Mean	Post. Sd	95% CI Low	95% CI High
Intercept	6.41	0.20	6.02	6.80
Beef	0.16	0.30	-0.42	0.75
Pico	-0.09	0.20	-0.47	0.31
Guac	0.19	0.20	-0.20	0.57
Cheese	-0.17	0.25	-0.66	0.31
Fries	0.29	0.24	-0.19	0.75
Sour_cream	0.34	0.21	-0.06	0.75
Pork	0.16	0.33	-0.49	0.81
Chicken	0.47	0.38	-0.27	1.24
Shrimp	1.60	0.46	0.69	2.50
Rice	0.00	0.28	-0.55	0.54
Beans	-0.45	0.28	-0.99	0.11
Lettuce	0.18	0.41	-0.60	0.98
Sauce	0.17	0.31	-0.44	0.77
Cilantro	-0.17	0.82	-1.77	1.39
Onion	-0.05	0.78	-1.58	1.47
Avocado	-0.03	0.56	-1.12	1.09
Vegetable	0.21	0.28	-0.35	0.75
Breakfast	-0.32	0.54	-1.36	0.75
Other	1.30	0.31	0.69	1.91
sigma	1.15	0.05	1.05	1.26

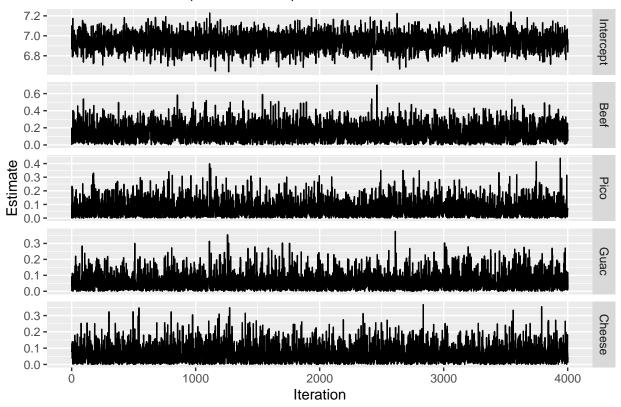
This model won't work for us because it fits prices to be negative. Instead, why don't we use a truncated Gibbs sampler.

Truncated Gibbs

Model Diagnostics

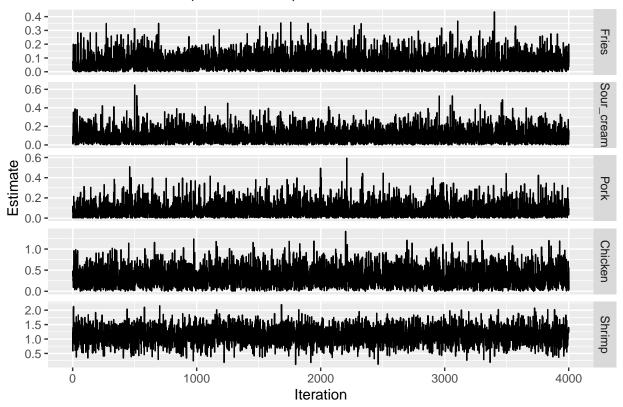
```
plot_traces(truncated_post_dist[,1:5], 'Parameter Traces (After Burn In)')
```

Parameter Traces (After Burn In)



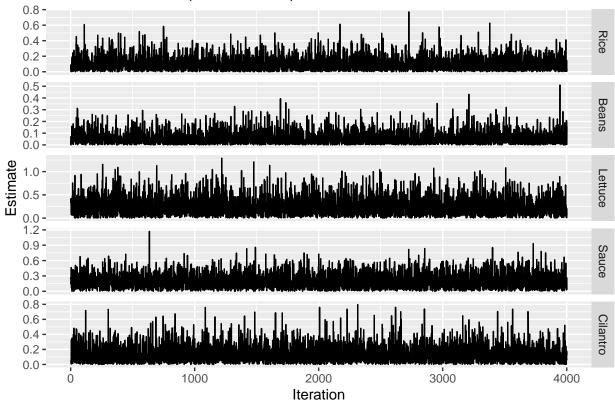
plot_traces(truncated_post_dist[,6:10], 'Parameter Traces (After Burn In)')

Parameter Traces (After Burn In)



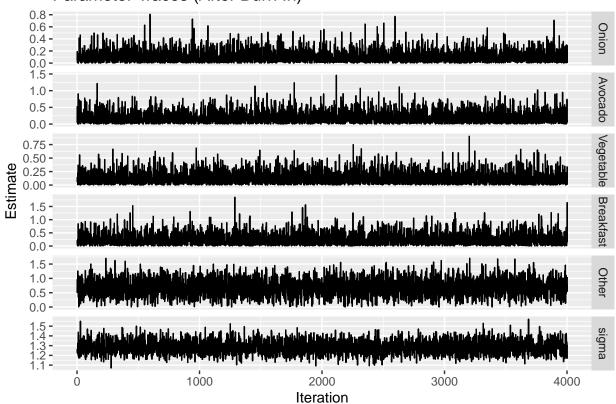
plot_traces(truncated_post_dist[,11:15], 'Parameter Traces (After Burn In)')

Parameter Traces (After Burn In)

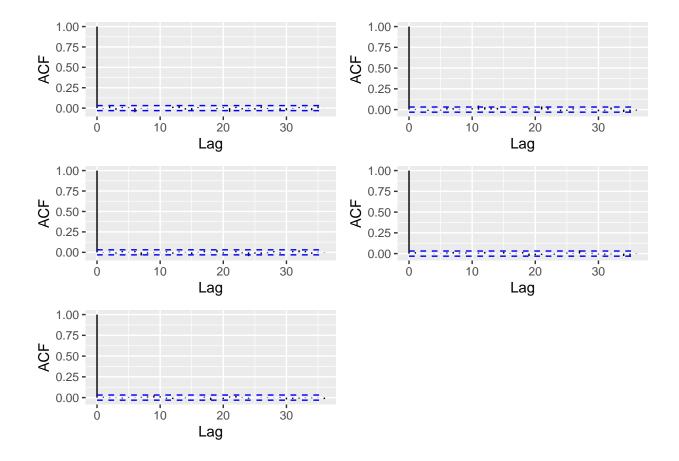


plot_traces(truncated_post_dist[,16:21], 'Parameter Traces (After Burn In)')

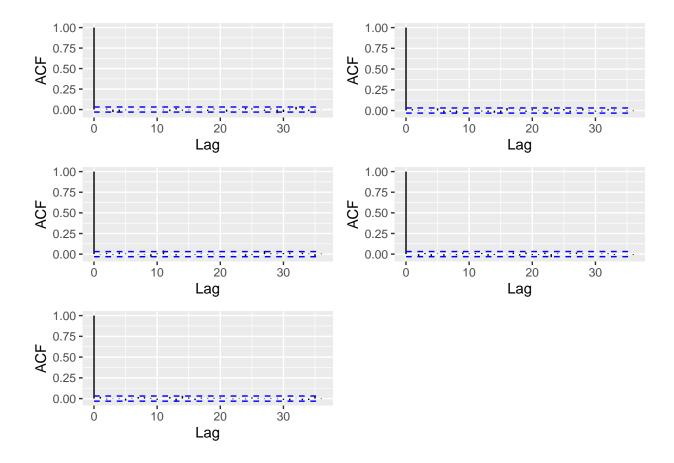




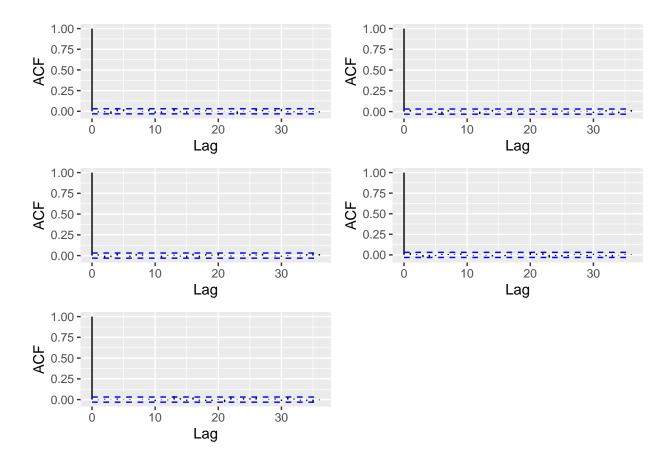
acf_plots(truncated_post_dist[,1:5])



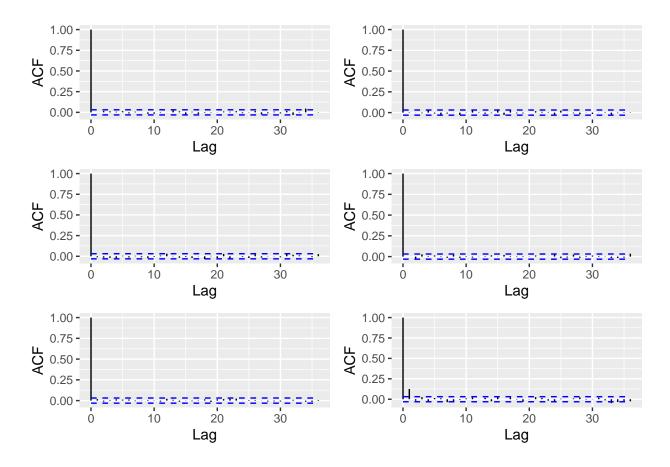
acf_plots(truncated_post_dist[,6:10])



acf_plots(truncated_post_dist[,11:15])



acf_plots(truncated_post_dist[,16:21])



summarize_dist(truncated_post_dist, colnames(truncated_post_dist), round_places=2)

Parameter	Post. Mean	Post. Sd	95% CI Low	95% CI High
Intercept	6.94	0.08	6.78	7.11
Beef	0.15	0.10	0.01	0.37
Pico	0.07	0.06	0.00	0.23
Guac	0.06	0.05	0.00	0.20
Cheese	0.06	0.06	0.00	0.21
Fries	0.07	0.06	0.00	0.22
Sour_cream	0.10	0.08	0.00	0.30
Pork	0.08	0.07	0.00	0.28
Chicken	0.35	0.23	0.02	0.87
Shrimp	1.14	0.30	0.55	1.73
Rice	0.10	0.09	0.00	0.33
Beans	0.06	0.06	0.00	0.21
Lettuce	0.25	0.20	0.01	0.77
Sauce	0.20	0.15	0.01	0.57
Cilantro	0.14	0.12	0.00	0.44
Onion	0.11	0.10	0.00	0.37
Avocado	0.20	0.18	0.01	0.65
Vegetable	0.13	0.11	0.00	0.42
Breakfast	0.25	0.22	0.01	0.83
Other	0.69	0.30	0.13	1.28
sigma	1.28	0.07	1.16	1.42

Model Interpretations