

Question 1: Coins.java

Output for question one Coins.java

enter an amount in cents:

```
17
This amount can be changed in the following ways:
1 dime 1 nickel 2 pennies
1 dime 7 pennies
3 nickels 2 pennies
2 nickels 7 pennies
1 nickel 12 pennies
17 pennies
```

enter an amount in cents:

```
20
This amount can be changed in the following ways:
2 dimes
1 dime 2 nickels
1 dime 1 nickel 5 pennies
1 dime 10 pennies
4 nickels
3 nickels 5 pennies
2 nickels 10 pennies
1 nickel 15 pennies
20 pennies
```

This program prints all the different ways change can be made while checking the plurals/singular noun depending on the number of coins. In its recursive function it starts from the condition check at step 0 and then add 1 to quarter and keep on repeating the step till the amount is either 0 or goes less than 0 and at that point it moves to the next condition check step 1 provided amount became negative in the previous step. and then again repeats the same step with rest of the coins and condition check increases by 1 at every coin change.

Question 2 Hypercube.java

running time of part b:

```
public void recursiveWalk() {
    int len = numOfDimensions;
    Corner createCorner = new Corner();
    recursiveWalk(createCorner.coordinates, len);
}

public static void reverseRecursiveWalk(String coordinates, int n) {
    if (n == 0) {
        System.out.println(coordinates);
    } else {
        recursiveWalk(coordinates + "1", n - 1);
        reverseRecursiveWalk(coordinates + "0", n - 1);
    }
}

// append order n binary numbers to end of prefix string, and print it
public static void recursiveWalk(String coordinates, int n) {
    if (n == 0) {
        System.out.println(coordinates);
    } else {
        recursiveWalk(coordinates + "0", n - 1);
        reverseRecursiveWalk(coordinates + "1", n - 1);
    }
}
```

Time taken on my computer to run recursive algorithm for 3D hyper cube = 0 milli second

no. of corners generated $= 2^n$

when $n=1$, $T(1) = \{0,1\}$

$$T(n) = C + T(n-1) + T(n+1)$$

BY INDUCTION

$$T(n) = \begin{cases} T(n-1) + C & \text{if } n > 0 \\ C & \text{if } n = 0 \end{cases}$$

$$\begin{aligned} T(n) &= T(n-1) + C \\ &= T(n-1-1) + C + C \\ &= T(n-3) + 3C \\ &= T(n-4) + 4C \end{aligned}$$

⋮

$$\begin{aligned} &= T(n-k) + kC \\ &= T(n-k) + C \end{aligned}$$

$$T(n) = T(n-k) + C$$

$$\approx O(n)$$

So, it is $O(n)$ for the recursive solution.

running time of part c:

```

public void iterativeWalk()
{
    int len = this.numOfDimensions;
    iterativeWalkHelper(this, len);
    for(Corner c : this.walk) {
        System.out.println(c.coordinates);
    }
}

private static void iterativeWalkHelper(Hypercube h, int n)
{
    Queue<Integer> Cornerqueue = new LinkedList<Integer>();
    int num = 0;
    Cornerqueue.add(0);
    for (int i = 0; i < n; i++)
    {
        int size = Cornerqueue.size();
        for (int j = size - 1; j >= 0; j--)
        {
            int k = -1;
            if(k != j)
            {
                Iterator<Integer> it = Cornerqueue.iterator();
                for(; k!= j; k++) {
                    num = it.next();
                }
                Cornerqueue.add(num + size);
            }
        }
    }
    for(int cor : Cornerqueue)
    {
        Corner c = new Corner();
        c.coordinates = "";
        for(int k = 0; k < n; k++) {
            c.coordinates = c.coordinates + "0";
        }
        Corner newCorner = new Corner();
        newCorner.coordinates = (c.coordinates + Integer.toBinaryString(cor)).substring(Integer.toBinaryString(cor).length());
        h.walk.push(newCorner);
    }
}

```

Handwritten annotations for time complexity analysis:

- $O(n)$ (green) next to `iterativeWalk()`
- $O(n)$ (green) next to `iterativeWalkHelper`
- $O(1)$ (green) next to `Cornerqueue.add(0);`
- $O(n)$ (blue) next to the inner loop `for (int j = size - 1; j >= 0; j--)`
- $O(n^2)$ (blue) next to the inner loop `for (int j = size - 1; j >= 0; j--)`
- $O(n)$ (green) next to the inner loop `for(; k!= j; k++)`
- $O(1)$ (green) next to `Cornerqueue.add(num + size);`
- $O(n)$ (blue) next to the outer loop `for (int i = 0; i < n; i++)`
- $O(\log(n)) (blue) next to the inner loop `for(int k = 0; k < n; k++)`$

From the above analysis of the iterative function and other functions being used in it it turns out to be $O(n) = n^3$

Result I/O of question 2 :

Iterative walk on 3D cube is :

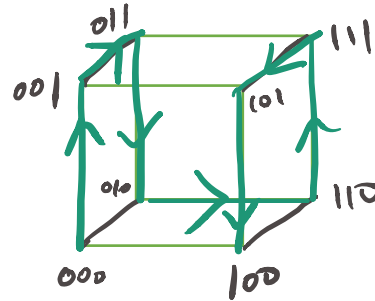
```
000
001
011
010
110
111
101
100
```

iterative walk on 3D cube time elapsed IS...3

recursive walk on 3D cube:

```
000
001
011
010
110
111
101
100
```

recursive walk on 3D cube time elapsed IS...0



Every corner visited as per requirement.

Iterative walk on 4D cube:[0000, 1000, 1001, 1011, 1010, 1110, 1111, 1101, 1100, 0100, 0101, 0111, 0110, 0010, 0011, 0001]

recursive walk on 4D cube:

```
0000
0001
0011
0010
0110
0111
0101
0100
1100
1101
1111
1110
1010
1011
1001
1000
```

Iterative walk on 5D cube:[00000, 10000, 10001, 10011, 10010, 10110, 10111, 10101, 10100, 11100, 11101, 11111, 11110, 11010, 11011, 11001, 11000, 01000, 01001, 01011, 01010, 01110, 01111, 01101, 01100, 00100, 00101, 00111, 00110, 00010, 00011, 00001]

recursive walk on 5D cube:

```
0000
0001
```

0011
0010
0110
0111
0101
0100
1100
1101
1111
1110
1010
1011
1001
1000

Question 3 : ADT Stack. AugStack.java

I/O of ADT is :

Top = 26
Min = 6
Top = 26
Min = 6
Top = 35
Min = 3

] Solution of Question 3.