# Chapter 18

# Multi Party Computation Using Infinite Product Series Over Distributed Data

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**Abstract**. The potency of data mining tools to discover useful rules among large data inspires the companies to share their data to be mined. The big problem of these companies is trusting to a third party miner. Currently, the issue of Multi Party Computation (MPC) tries to solve this conflict using cryptographic tool. In this paper, we propose a secure summation algorithm for online transactions, where the users will send the data to the miner, stepwise. The algorithm emerges the excessively useful response time, so the execution time of summation for 1000 users' data is only 0.9s.

**Keywords.** Multi Party Computation, Privacy Preserving, Secure Counting Algorithm, Distributed Data

#### 1.1 Introduction

Today, the large amount of data will be used among the large number of companies. There exist a lot of valuable patterns and roles which are hided between wooded data. Data mining tools has been developed to discover these worth facts. It is sophisticated where the data has been distributed among number of parties because of privacy of their sensitive data. Each company leans to gain the advantage of data mining tools, but he does not propend to share his sensitive data. Multi Party Computation (MPS) has been solved this conflict. MPC ensures the privacy preserving of data us-

ing cryptographic tools as well as precious aggregation over the distributed data.

In this paper, we propose a cryptographic method that allows a Miner system to compute aggregation of respondents' data. As we mentioned before, it is important that content of data should not be revealed. In this algorithm, each client only sends a message to Miner system and there is no need to any inner interaction between clients. The algorithm ensures that no extra information is revealed to Miner System except the summation of respondents' data.

Our algorithm could be used as basic fundamental for data mining tools. It is also useful for implementing an E-Voting system or calculation of web pages poll result.

First, we will briefly introduce some related work and basic cryptographic method in section 1.2, respectively and then we will fully explain the base algorithm in section 1.3. We explain the problem and proposed algorithm in section 1.4 and we represent our result in section 1.5. The paper will ends with a discussion about the earned result and precise conclusion in section 1.6.

# 1.2 Background and Related Work

The secure multi-party computation also known as (MPC) is one of the main results of the theory of cryptography. First, Yao's [2] introduced the multi-party computation and nowadays many authors have attend many optimizations and extensions to the basic concept, for two main branch; the two-party (2PC) and the multi-party (MPC) [6,7,9,10,14,15]. Most of recently papers on secure multi-party computation area have been focused on theory of multi-party computation and there is no much applicable implementing of MPC, although, in the few last year some practical implementation of multi-party computation has been appeared [1,3,11,12,21].

There exist many algorithm and techniques for secure multi-party computation. We have focused on more practical and high speed algorithms which have been published.

Secure multi-party computation essentially comes in two flavors [16]. The first approach is typically based upon secret sharing and operates on an arithmetic circuit representation of the computed function, such as in the BGW (Ben-Or, Goldwasser and Wigderson) or CCD (Chaum, Crepeau and Damg°ard) protocols [5,13]. This approach is usually applied when there is an honest majority among the participants (which can only exist if more than two parties participate in the protocol). An alternative approach represents the function as a binary circuit. This approach was used in the

original two-party garbled circuit construction of Yao [2], and in the GMW (Goldreich, Micali and Wigderson) multi-party protocol [7].

Our proposed algorithm is secure within the semi-honest model. The algorithm is secure under Diffie-Hillman DDH assumption and uses El-Gamal encryption for increasing robustness and speed.

### 1.2.1 ElGamal Cryptosystem

The ElGamal cryptosystem is a part of public encryption systems. The public key is (h, G, q, g) where G is a cyclic group of order q with the generator g,  $h=g^x$  and x is the private key which is randomly chosen from [1, q]. All computation in the ElGamal scheme is done in the group G.

Under the public key (h, G, q, g), the ciphertext of a message m (which is the representation of an element of G) is encrypted as  $E(m)=(c_1, c_2)$  where  $c_1=m.h^r$ ,  $c_2=g^r$  and r is randomly chosen from [1, q]. To decrypt the ciphertext  $(c_1, c_2)$  with the private key x, the plaintext message m can be decrypted as  $m=c_1(c_2^x)^{-1}$ . It clearly is true because

$$c_1(c_2^x)^{-1} = m.h^r(g^{rx})^{-1} = m.h^r(h^r)^{-1} = m$$
 (1)

ElGamal encryption is semantically secure under the Decisional Diffie-Hellman (DDH) assumption [4]. One family in which DDH is believed to be intractable is the quadratic residue subgroup  $Q_p$  of  $Z_p^*$  where p, q are two primes and p=2q+1.

In the ElGamal encryption, one cleartext has many possible ciphertexts because of the random value r. ElGamal supports rerandomization: a new ciphertext E'(m) of m can be computed from a ciphertext  $E(m)=(c_1, c_2)$  as  $E'(m)=(c_1,h^{r'},c_2,g^{r'})$  where r' is randomly chosen from [1, q].

#### 1.2.2 Secret Sharing

Secret sharing is the method of sharing a secret by multiple parties, so that no one and no party know the secret, but the secret could be constructed by combing some parties' shares.

For example, in a two-party case, Alice and Bob share a value x modulo some appropriate value N, in such a way that Alice holds a, Bob holds b, and x is equal to  $(a+b) \mod N$ . This is called additive secret sharing. An important property of this kind of secret sharing is that if Alice and Bob have shares of a and b, then they can each locally add their shares modulo N to obtain shares of a+b.

Shamir secret sharing is a threshold scheme [19]. In Shamir secret sharing, there are N parties and a polynomial P of degree k-l such that P(0)=x where x is a secret. Each of the N parties holds a point in the polynomial P.

Because k points  $(x_i, y_i)$   $(1 \le i \le k)$  uniquely define a polynomial P of degree k-I, a subset of at least k parties can reconstruct the secret x. But, fewer than k parties cannot construct the secret x. This scheme is also called (N, k) *Shamir secret sharing*.

## 1.3 Aggregation Algorithm

In our scenario, there are n clients, so we call them  $C_1, \ldots, C_n$ ; respectively. Each client owns his private data  $d_i$ . The aim of the Miner System is to calculate the sum  $d = \sum_{i=1}^{n} d_i$  with ensuring the privacy of  $d_i$ .

In our model, because of its practicability, the clients do not need to know about other clients and they never communicate themselves. So there is no communication channel between different clients. Moreover, each client only sends one encrypted message to the Miner. So, they do not need multi round interaction between clients and the Miner System.

The implemented algorithm [17] is based on the homomorphism property of mentioned ElGamal encryption [8,20]. The DDH assumption and the ElGamal cryptosystem ensure the privacy of the algorithm. The algorithm also uses the exponentiation's mathematical properties for converting multiplication to desired sums. We also use modular arithmetic operation to speed up the computing time of big prime numbers. It is surely affect on algorithm time.

Let G be a group where (/G/=q for a large prime q), and let g be a generator of G. The group G is assumed for all computations in this paper. Suppose that each respondent  $C_i$  has two pairs of keys:  $((x_i \mod_q), (X_i \mod_q = (g^x_i \mod_q)), ((y_i \mod_q), (Y_i \mod_q = (g^y_i \mod_q)))$ . We also define

$$(X \, mod_q) = \prod_{i=1}^n (X_i mod_q) \tag{2}$$

$$(Y \, mod_q) = \prod_{i=1}^n (Y_i \, mod_q) \tag{3}$$

The values  $x_i$  and  $y_i$  are private keys;  $X_i$  and  $Y_i$  are public keys. All respondents need to calculate the values of X and Y from public keys.

First, each respondent  $C_i$  try to encrypt his value  $d_i$  using his private key  $x_i$ ,  $y_i$  and shared public key X, Y in ElGamal encryption system as described below

$$E(d_i) = \begin{cases} \left(m_i \, mod_q\right) = \left(g^{d_i} \, mod_q\right) \cdot \left(X^{y_i} \, mod_q\right) \\ \left(h_i \, mod_q\right) = \left(Y^{x_i} \, mod_q\right) \end{cases}$$
(4)

Then all clients send their encrypted message to Miner. The Miner System gathers all encrypted data together and computes m, h as:

$$m = \prod_{i=1}^{n} (m_i \ mod_a) , h = \prod_{i=1}^{n} (h_i \ mod_a)$$
 (5)

The Miner will use m, h for decrypting the d as sum of  $d_i$ . Then the Miner tries to find correct d between all possible values. It means that the miner tries to calculate  $(g^d \ mod_p)$  for all possible of d values. This stage is more time consuming step and will continue until there exist any d as

$$(m \, mod_q) = (g^d \, mod_q).(h \, mod_q) \tag{6}$$

This value is the desired summation of respondents' votes. Mathematic demonstration is shown in [18]. The Miner cannot take discrete logarithms; the Miner must use trial and error to learn d. The time consumption parameter of algorithm returns to the range of possible values of d. In case of Boolean votes the range of d is the number of respondent's n.

### 1.4 Problem Explanation

Base on the mentioned algorithm, before the process starts, the miner should ensure that all clients are ready to send their data and the Miner knows the number of clients. It means that the system is semi-offline system. This condition avoids us to use the algorithm in real world online problems like as E-Voting or web page's poll result. Because in this cases, the clients are not ready at the beginning time and the time of user's appearance is optional. The miner does not have any knowledge which how many clients could join to system and when they will appear. So the Miner could not able to compute the secret shared between the clients. As we mentioned before, the secret shared between the users is the product of their public keys as we called *X*, *Y*. All clients should be present their public keys to compute the shared secret key *X*, *Y* before aggregation started. Moreover, all users should send their data; therefore the Miner could compute the summation.

So, in most online cases the algorithm will fail and is inapplicable. Due to the Miner, likewise, clients cannot assess the product of user's public keys that do not join yet.

In this paper, infinite product series have been used as shared secret key instead of X, Y. The final amounts of these series do not change with increasing the number of elements. An infinite product series define as

$$A = \prod_{i=1}^{\infty} \alpha_i \text{ like as } \prod_{i=1}^{\infty} \frac{1}{e} \left( \frac{1}{3i+1} \right)^{3i+\frac{1}{2}} = 1.0123785$$
 (7)

#### 1.4.1 Proposed Algorithm

The proposed algorithm also is based on the homomorphism property of mentioned ElGamal encryption. We note that the security of ElGamal encryption depends on new random values being used for each encryption. Same as before, each client  $C_i$  has two pairs of keys:  $((x_i \mod_q), (X_i \mod_q = (g^{x_i} \mod_q)), ((y_i \mod_q), (Y_i \mod_q = (g^{y_i} \mod_q)))$  as private and public keys, respectively. Remember that the  $x_i$  and  $y_i$  values cannot be reused in different uses of the running algorithm. Here, we are not able to compute the  $X_i$ ,  $Y_i$ . So we use two infinite series  $Q_i$ ,  $Y_i$  instead of  $X_i$ ,  $Y_i$ .

$$(\Omega_i mod_g) = (g^{\omega_i} mod_g), \ (\Omega \ mod_g) = \prod_{i=1}^n (\Omega_i mod_g)$$
(8)

$$(\Psi_i mod_q) = (g^{\psi_i} mod_q), \ (\Psi mod_q) = \prod_{i=1}^n (\Psi_i mod_q)$$
 (9)

The client  $C_i$  encrypt his value  $d_i$  in ElGamal encryption system using  $\Omega$ ,  $\Psi$  as described below

$$E(d_i) = \begin{cases} \left(m_i \ mod_q\right) = (g^{d_i} \ mod_q). (\Omega^{y_i} \ mod_q) \\ (h_i \ mod_q) = (\Psi^{x_i} \ mod_q) \end{cases}$$
(10)

and send his encrypted message in assition to his public keys  $X_i$ ,  $Y_i$  to the Miner. The Miner System computes m, h, X, Y as before:

$$m = \prod_{i=1}^{n} (m_i \ mod_a) , h = \prod_{i=1}^{n} (h_i \ mod_a)$$
 (11)

$$X = \prod_{i=1}^{n} (X_i \ mod_q) \ , Y = \prod_{i=1}^{n} (Y_i \ mod_q)$$
 (12)

The Miner tries to find desired d to satisfy below

$$(m \, mod_a). (X^{\sum_{i=1}^n \psi_i}) = (g^d \, mod_a). (h \, mod_a). (Y^{\sum_{i=1}^n \omega_i})$$

$$(13)$$

The desired d is the summation of clients' data.

#### 1.4.2 Algorithm Demonstration

In this section, we prove that the algorithm represented in 4.1 correctly computes the summation of respondents' data. Suppose that the Miner finds a d so

$$(m \, mod_q). \, (X^{\sum_{i=1}^n \psi_i}) = (g^d \, mod_q). \, (h \, mod_q). \, (Y^{\sum_{i=1}^n \omega_i})$$
 (13\*)

We will show that  $d = \sum_{i=1}^{n} d_i$ .

$$(m \, mod_q). (X^{\sum_{i=1}^n \psi_i}) = (g^d \, mod_q). (h \, mod_q). (Y^{\sum_{i=1}^n \omega_i})$$

$$\Rightarrow (\prod_{i=1}^n (m_i \, mod_q)). (X^{\sum_{i=1}^n \psi_i}) = (g^d \, mod_q). (\prod_{i=1}^n (h_i \, mod_q)). (Y^{\sum_{i=1}^n \omega_i})$$

$$\begin{split} &\Rightarrow \left(g^d \ mod_q\right) = \frac{(\prod_{i=1}^n(m_i \ mod_q)).(x^{\sum_{i=1}^n \psi_i})}{(\prod_{i=1}^n(h_i \ mod_q)).(x^{\sum_{i=1}^n \psi_i})} = \frac{(\prod_{i=1}^n(g^d \ mod_q).(\alpha^{y_i} \ mod_q)).(x^{\sum_{i=1}^n \psi_i})}{(\prod_{i=1}^n(g^{y_i} \ mod_q)).(x^{\sum_{i=1}^n \psi_i})} \\ &= \frac{(\prod_{i=1}^n(g^{d_i} \ mod_q).\prod_{i=1}^n(\alpha^{y_i} \ mod_q)).(x^{\sum_{i=1}^n \psi_i})}{(\prod_{i=1}^n(\psi^{x_i} \ mod_q)).(x^{\sum_{i=1}^n \psi_i})} = \frac{\prod_{i=1}^n(g^{d_i} \ mod_q).\prod_{i=1}^n(\alpha^{y_i} \ mod_q)}{(\prod_{i=1}^n(\psi^{x_i} \ mod_q)).(x^{\sum_{i=1}^n \psi_i})} \\ &= g^{\sum_{i=1}^n(d_i \ mod_q)} \cdot \frac{\alpha^{\sum_{j=1}^n(y_j \ mod_q)}}{(y^{\sum_{j=1}^n(x_j \ mod_q)})} \cdot \frac{(x^{\sum_{i=1}^n \psi_i})}{(y^{\sum_{i=1}^n \psi_i})} \\ &= g^{\sum_{i=1}^n(d_i \ mod_q)} \cdot \frac{(\prod_{i=1}^n(a_i \ mod_q))^{\sum_{j=1}^n(y_j \ mod_q)}}{(\prod_{i=1}^n(\psi \ mod_q))^{\sum_{j=1}^n(y_j \ mod_q)}} \cdot \frac{(x^{\sum_{i=1}^n \psi_i})}{(y^{\sum_{i=1}^n \psi_i})} \\ &= g^{\sum_{i=1}^n(d_i \ mod_q)} \cdot \frac{(\prod_{i=1}^n(g^{\omega_i \ mod_q}))^{\sum_{j=1}^n(y_j \ mod_q)}}{(\prod_{i=1}^n(g^{\omega_i \ mod_q}))^{\sum_{j=1}^n(y_j \ mod_q)}} \cdot \frac{(x^{\sum_{i=1}^n \psi_i})}{(x^{\sum_{i=1}^n \psi_i})} \\ &= g^{\sum_{i=1}^n(d_i \ mod_q)} \cdot \frac{g^{\sum_{i=1}^n(\omega_i \ mod_q)} \sum_{j=1}^n(y_j \ mod_q)}{g^{\sum_{j=1}^n(y_j \ mod_q)} \cdot \frac{(x^{\sum_{i=1}^n \psi_i})}{(x^{\sum_{i=1}^n \psi_i})}} \\ &= g^{\sum_{i=1}^n(d_i \ mod_q)} \cdot \frac{g^{\sum_{j=1}^n(y_j \ mod_q)} \sum_{j=1}^n(y_j \ mod_q)} \cdot \frac{(x^{\sum_{i=1}^n \psi_i})}{(x^{\sum_{i=1}^n \psi_i})} \\ &= g^{\sum_{i=1}^n(d_i \ mod_q)} \cdot \frac{g^{\sum_{j=1}^n(y_j \ mod_q)} \sum_{j=1}^n(\omega_i \ mod_q)} \cdot \frac{(x^{\sum_{i=1}^n \psi_i})}{(x^{\sum_{i=1}^n \psi_i})} \\ &= g^{\sum_{i=1}^n(d_i \ mod_q)} \cdot \frac{(\prod_{i=1}^n(g^{\omega_i \ mod_q}))^{\sum_{i=1}^n(\omega_i \ mod_q)}}{(\prod_{i=1}^n(g^{\omega_i \ mod_q}))^{\sum_{i=1}^n(\omega_i \ mod_q)}} \cdot \frac{(x^{\sum_{i=1}^n \psi_i})}{(x^{\sum_{i=1}^n \psi_i})} \\ &= g^{\sum_{i=1}^n(d_i \ mod_q)} \cdot \frac{(\prod_{i=1}^n(y_i \ mod_q))^{\sum_{i=1}^n(\omega_i \ mod_q)}}{(\prod_{i=1}^n(y_i \ mod_q))^{\sum_{i=1}^n(\omega_i \ mod_q)}} \cdot \frac{(x^{\sum_{i=1}^n \psi_i})}{(x^{\sum_{i=1}^n \psi_i})} \\ &= g^{\sum_{i=1}^n(d_i \ mod_q)} \cdot \frac{(\prod_{i=1}^n(y_i \ mod_q))^{\sum_{i=1}^n(\omega_i \ mod_q)}}{(\prod_{i=1}^n(y_i \ mod_q)} \cdot \frac{(x^{\sum_{i=1}^n \psi_i})}{(x^{\sum_{i=1}^n \psi_i})} \\ &= g^{\sum_{i=1}^n(d_i \ mod_q)} \cdot \frac{(\prod_{i=1}^n(y_i \ mod_q))^{\sum_{i=1}^n(\omega_i \ mod_q)}}{(\prod_{$$

# 1.5 Experimental Result

We implemented our algorithm in Delphi. All cryptographic operations use the OpenSSL and FGBigInt libraries. The OpenSSL library is accessible at www.openssl.org website. The IIS HTTP Server has been used for network simulation under windows Vista on a PC with a 2.4GHz processor and 2GB memory. We choose the 512 bits as the length of each cryptographic key. The main parameters of experiment are: Number of Clients and the range of d. Moreover, the time of computing  $d_i$  in each respondent will affect on final time. The key generation also is time consuming process, but these parameters are ignored in our experimental result. Because, as we mentioned before, these values can be precomputed offline before the protocol starts.

In our result, we propose the time consumption of algorithm as the main factor. The algorithm's stages are:

- Sending Encrypted message to Miner
- Computing m, h, X, Y on Miner
- Finding desired d across its' possible values

We define two different phase of result. In first phase, each client owns a Boolean data. In sooth, we are counting the users' data. This case is similar to E-Voting systems that each client is free to select an option and the Miner aims to know how many users do vote the idea. The final result of phase 1 is shown in Fig. 1.1. In this experiment, the respondents send the Boolean data to Miner. In this condition, the range of d is equal to number of clients. We use 50, 100, 200, 500 and 1000 users in our experiment and the earned time is base on the average of five algorithm runs. As you can see, the time offers a linear behavior related to number of users. For example, Miner computation takes 952 milliseconds for 1000 voters.

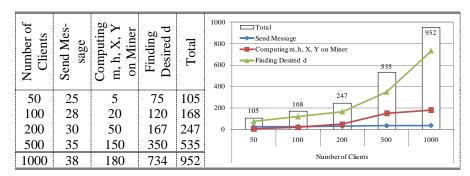


Fig. 1.1. Total time of Protocol related to Number of respondents

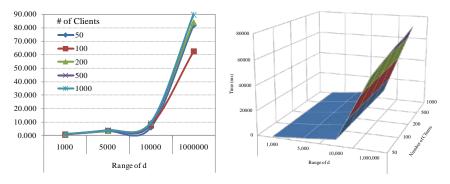


Fig. 1.2. a) Total time related to Number of Voters and Range of d-b) 3d view

In second phase, we have focused on non Boolean cases. In this case, the time is highly related to range of d. The range of d is not a simple parameter and return to many conditions. The Fig. 1.2 shows the time of al-

gorithm execution related to number of clients and range of d. We earn the algorithm takes less than 0.5 second for 1000 voters with d in range of 1 to 1,000,000.

#### 1.6 Discussion and Conclusion

In this paper, we proposed a secure aggregation algorithm. Our proposed algorithm ensures the confidentially of sensitive respondents' data. Furthermore, it does not need communication channels between different respondents or multi round interaction between any respondent and the Miner Systems.

The mathematical demonstration ensures the accuracy of data's aggregation. On the other hand, The DDH assumption and the ElGamal cryptosystem ensure the privacy of the algorithm and respondents' data, so the Miner system can not reveal respondents' data. Our experimental results also show significantly desirable response time. The time increasing is derived from high security of algorithm, because the Miner could not able to decrypt the message, so the Miner should use trial and error to find the result. The algorithm can also be used for any model enabled by counting values. Our both theoretical analysis and proof in addition to experimental results show that the algorithm is very efficient and runs in desirable time.

# References

- 1. Amirbekyan A, Estivil-Castro V (2007) Privacy-Preserving Regression Algorithms. In: Proceedings of the 7th WSEAS International Conference on Simulation, Modelling and Optimization, vol., Beijing, China
- 2. Andrew Chi-Chih Y (1986) How to generate and exchange secrets. In: Proceedings of the 27th Annual Symposium on Foundations of Computer Science, vol. IEEE Computer Society,
- 3. Bogetoft P, Damgård I, Jakobsen T, Nielsen K, Pagter J, Toft T (2006) A Practical Implementation of Secure Auctions Based on Multiparty Integer Computation. In: Financial Cryptography and Data Security, vol., pp 142-147
- 4. Boneh D (1998) The decision Diffie-Hellman problem. Lecture Notes in Computer Science
- 5. David C, Claude C, peau, Ivan D (1988) Multiparty unconditionally secure protocols. In: Proceedings of the twentieth annual ACM symposium on Theory of computing, vol. ACM, Chicago, Illinois, United States
- 6. Goldreich O (2004) Foundations of Cryptography, vol 2. Cambridge Univ. Press,
- 7. Goldreich O, Micali S, Wigderson A (1987) How to play ANY mental game.

- In: Proceedings of the nineteenth annual ACM symposium on Theory of computing, vol. ACM, New York, New York, United States
- 8. Hirt M, Sako K (2000) Efficient receipt-free voting based on homomorphic encryption. In Advances in Cryptology Proceedings of EUROCRYPT volume 1807 of Lecture Notes in Computer Science
- 9. Jarecki S, Shmatikov V (2007) Efficient Two-Party Secure Computation on Committed Inputs. EUROCRYPT
- 10. Lindell Y, Pinkas B (2007) An Efficient Protocol for Secure Two-Party Computation in the Presence of Malicious Adversaries. EUROCRYPT 52-79
- 11. Ma J, Sivakumar K (2005) Privacy-Preserving Bayesian Network Parameter Learning. In: 4th WSEAS Int. Conf. on Computational Intelligence, Man-Machine Systems and Cybernetics, vol., Miami, Florida, USA, pp 46-51
- 12. Ma J, Sivakumar K (2006) A Framework of Privacy-Preserving Bayesian Network Parameter Learning using Post Randomization. WSEAS Transaction of Information Science and Applications 3(1)
- 13. Michael B-O, Shafi G, Avi W (1988) Completeness theorems for non-cryptographic fault-tolerant distributed computation. In: Proceedings of the twentieth annual ACM symposium on Theory of computing, vol. ACM, Chicago, Illinois, United States
- 14. Mishra DK, Chandwani M (2007) Extended Protocol for Secure Multiparty Computation using Ambiguous Identity. WSEAS Transaction on Computer Research 2(2)
- 15. Mohassel P, Franklin M (2006) Efficiency Tradeoffs for Malicious Two-Party Computation. In: Public Key Cryptography PKC 2006, vol., pp 458-473
- Pinkas B, Schneider T, Smart N, Williams S (2009) Secure Two-Party Computation Is Practical. In: Advances in Cryptology – ASIACRYPT 2009, vol., pp 250-267
- 17. Rasouli A, Hosseinkhani J, Shamsi M, Harouni M (2010) A Robust and High Speed E-Voting Algorithm Using ElGammel CryptoSystem. In: The 2nd International Conference on Computer and Automation Engineering, vol., Singapore
- 18. Rasouli A, Maarof MAB, Shamsi M (2010) A New Multi Party Aggregation Algorithm Using Infinite Product Series. In: The 9th WSEAS International Conference on Applications of Computer Engineering, vol., Penang, Malaysia
- 19. Shamir A (1979) How to share a secret. Communications of the ACM:22(11) 612–613
- 20. Wang M-N, Yen S-M, Wu C-D, Lin C-T (2006) Cryptanalysis on an Elgamallike cryptosystem for encrypting large messages. In: Proceedings of the 6th WSEAS International Conference on Applied Informatics and Communications, vol., Elounda, Greece
- 21. Yehuda L, Benny P, Nigel PS (2008) Implementing Two-Party Computation Efficiently with Security Against Malicious Adversaries. In: Proceedings of the 6th international conference on Security and Cryptography for Networks, vol. Springer-Verlag, Amalfi, Italy