

# Hierarchical Discrete Lattice Assembly: An Approach for the Digital Fabrication of Mesoscale Structures

1 Miana Smith\*

2 Center for Bits and Atoms

3 Massachusetts Institute of Technology

4 Cambridge, Massachusetts, USA

5 miana@mit.edu

6 Alexander Htet Kyaw

7 School of Architecture and Planning  
8 Massachusetts Institute of Technology  
9 Cambridge, Massachusetts, USA

10 checkemail

11 Paul Arthur Richard\*

12 École Polytechnique Fédérale de Lausanne

13 Lausanne, Switzerland

14 paul.richard@epfl.ch

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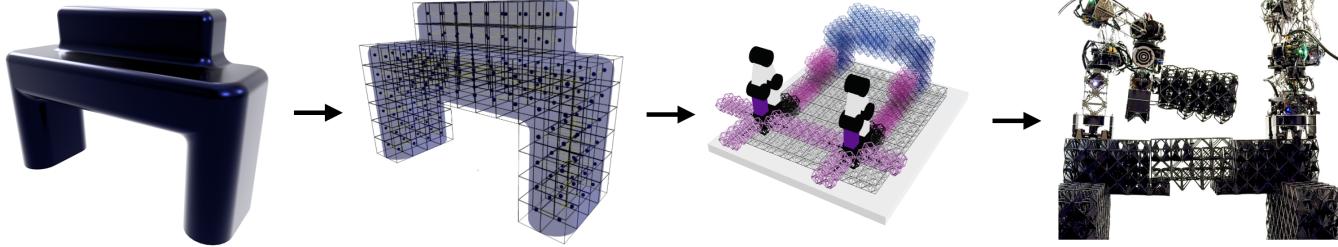


Figure 1: Pipeline from STL Mesh → Voxelization → Simulation → Robotic Assembly

## ABSTRACT

Although digital fabrication processes at the desktop scale have become proficient and prolific, systems aimed at producing larger-scale structures are still typically complex, expensive, and unreliable. In this work, we present an approach for the fabrication of mesoscale structures using simple robots and interlocking lattice building blocks. A target structure is first voxelized so that it can be populated with an architected lattice. These voxels are then grouped into larger interconnected blocks, which are produced using standard digital fabrication processes, leveraging their capability to produce highly complex geometries at a small scale. These blocks, on the size scale of tens of centimeters, are then fed to mobile relative robots that are able to traverse over the structure and place new blocks to form structures on the meter scale. Using this system, we demonstrate the voxelization, hierarchical blocking, path planning, and robotic implementation for a series of meter-scale objects.

\*Both authors contributed equally to this research.

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<https://doi.org/XXXXXXX.XXXXXXX>

## CCS CONCEPTS

- Computer systems organization → External interfaces for robotics; Robotic components;
- Human-centered computing → User interface toolkits.

## KEYWORDS

Large-Scale Fabrication, Digital Fabrication, Modular Assembly, Robotics, Cellular Materials

## ACM Reference Format:

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## 1 INTRODUCTION

Text text

## 2 BACKGROUND

## 3 SYSTEM OVERVIEW

## 4 SOFTWARE IMPLEMENTATION

## 5 HARDWARE IMPLEMENTATION

### 5.1 Robots

### 5.2 Voxels

#### 5.2.1 Mechanical Performance.

117 **6 DEMONSTRATIONS**

118 **7 DISCUSSION, FUTURE WORK, AND**

119 **LIMITATIONS**

120 **8 CONCLUSION**

121 **9 TEMPLATE OVERVIEW**

122 As noted in the introduction, the “*acmart*” document class can be  
 123 used to prepare many different kinds of documentation — a double-  
 124 anonymous initial submission of a full-length technical paper, a two-page SIGGRAPH Emerging Technologies abstract, a “camera-  
 125 ready” journal article, a SIGCHI Extended Abstract, and more — all  
 126 by selecting the appropriate *template style* and *template parameters*.

127 This document will explain the major features of the document  
 128 class. For further information, the *LaTeX User’s Guide* is available  
 129 from <https://www.acm.org/publications/proceedings-template>.

133 **9.1 Template Styles**

134 The primary parameter given to the “*acmart*” document class is the  
 135 *template style* which corresponds to the kind of publication or SIG  
 136 publishing the work. This parameter is enclosed in square brackets  
 137 and is a part of the *documentclass* command:

138 \documentclass[STYLE]{acmart}

139 Journals use one of three template styles. All but three ACM  
 140 journals use the *acmsmall* template style:

- *acmsmall*: The default journal template style.
- *acmlarge*: Used by JOCCH and TAP.
- *acmtog*: Used by TOG.

141 The majority of conference proceedings documentation will use  
 142 the *acmconf* template style.

- *sigconf*: The default proceedings template style.
- *sigchi*: Used for SIGCHI conference articles.
- *sigplan*: Used for SIGPLAN conference articles.

143 **9.2 Template Parameters**

144 In addition to specifying the *template style* to be used in formatting  
 145 your work, there are a number of *template parameters* which modify  
 146 some part of the applied template style. A complete list of these  
 147 parameters can be found in the *LaTeX User’s Guide*.

148 Frequently-used parameters, or combinations of parameters, in-  
 149 clude:

- *anonymous, review*: Suitable for a “double-anonymous” conference submission. Anonymizes the work and includes line numbers. Use with the *\acmSubmissionID* command to print the submission’s unique ID on each page of the work.
- *authorversion*: Produces a version of the work suitable for posting by the author.
- *screen*: Produces colored hyperlinks.

150 This document uses the following string as the first command  
 151 in the source file:

152 \documentclass[sigconf, authordraft]{acmart}

153 **10 MODIFICATIONS**

154 Modifying the template — including but not limited to: adjusting  
 155 margins, typeface sizes, line spacing, paragraph and list definitions,  
 156 and the use of the *\vspace* command to manually adjust the vertical  
 157 spacing between elements of your work — is not allowed.

158 Your document will be returned to you for revision if mod-  
 159 ifications are discovered.

160 **11 TYPEFACES**

161 The “*acmart*” document class requires the use of the “Libertine”  
 162 typeface family. Your *T<sub>E</sub>X* installation should include this set of  
 163 packages. Please do not substitute other typefaces. The “*lmodern*”  
 164 and “*ltimes*” packages should not be used, as they will override  
 165 the built-in typeface families.

166 **12 TITLE INFORMATION**

167 The title of your work should use capital letters appropriately —  
 168 <https://capitalizemytitle.com/> has useful rules for capitalization.  
 169 Use the *title* command to define the title of your work. If your  
 170 work has a subtitle, define it with the *subtitle* command. Do not  
 171 insert line breaks in your title.

172 If your title is lengthy, you must define a short version to be  
 173 used in the page headers, to prevent overlapping text. The *title*  
 174 command has a “short title” parameter:

175 \title[short title]{full title}

176 **13 AUTHORS AND AFFILIATIONS**

177 Each author must be defined separately for accurate metadata iden-  
 178 tification. As an exception, multiple authors may share one affiliation.  
 179 Authors’ names should not be abbreviated; use full first names  
 180 wherever possible. Include authors’ e-mail addresses whenever  
 181 possible.

182 Grouping authors’ names or e-mail addresses, or providing an  
 183 “e-mail alias,” as shown below, is not acceptable:

184 \author{Brooke Aster, David Mehldau}  
 185 \email{dave, judy, steve@university.edu}  
 186 \email{firstname.lastname@phillips.org}

187 The *authornote* and *authortotemark* commands allow a note  
 188 to apply to multiple authors — for example, if the first two authors  
 189 of an article contributed equally to the work.

190 If your author list is lengthy, you must define a shortened version  
 191 of the list of authors to be used in the page headers, to prevent  
 192 overlapping text. The following command should be placed just  
 193 after the last *\author{}* definition:

194 \renewcommand{\shortauthors}{McCartney, et al.}

195 Omitting this command will force the use of a concatenated list of  
 196 all of the authors’ names, which may result in overlapping text in  
 197 the page headers.

198 The article template’s documentation, available at <https://www.acm.org/publications/proceedings-template>, has a complete expla-  
 199 nation of these commands and tips for their effective use.

200 Note that authors’ addresses are mandatory for journal articles.

## 233 14 RIGHTS INFORMATION

234 Authors of any work published by ACM will need to complete a  
 235 rights form. Depending on the kind of work, and the rights man-  
 236 agement choice made by the author, this may be copyright transfer,  
 237 permission, license, or an OA (open access) agreement.

238 Regardless of the rights management choice, the author will  
 239 receive a copy of the completed rights form once it has been sub-  
 240 mitted. This form contains  $\text{\LaTeX}$  commands that must be copied  
 241 into the source document. When the document source is compiled,  
 242 these commands and their parameters add formatted text to several  
 243 areas of the final document:

- 244 • the “ACM Reference Format” text on the first page.
- 245 • the “rights management” text on the first page.
- 246 • the conference information in the page header(s).

247 Rights information is unique to the work; if you are preparing  
 248 several works for an event, make sure to use the correct set of  
 249 commands with each of the works.

250 The ACM Reference Format text is required for all articles over  
 251 one page in length, and is optional for one-page articles (abstracts).

## 255 15 CCS CONCEPTS AND USER-DEFINED 256 KEYWORDS

257 Two elements of the “acmart” document class provide powerful  
 258 taxonomic tools for you to help readers find your work in an online  
 259 search.

260 The ACM Computing Classification System — <https://www.acm.org/publications/class-2012> — is a set of classifiers and concepts  
 261 that describe the computing discipline. Authors can select entries  
 262 from this classification system, via <https://dl.acm.org/ccs/ccs.cfm>,  
 263 and generate the commands to be included in the  $\text{\LaTeX}$  source.

264 User-defined keywords are a comma-separated list of words and  
 265 phrases of the authors’ choosing, providing a more flexible way of  
 266 describing the research being presented.

267 CCS concepts and user-defined keywords are required for for  
 268 all articles over two pages in length, and are optional for one- and  
 269 two-page articles (or abstracts).

## 273 16 SECTIONING COMMANDS

274 Your work should use standard  $\text{\LaTeX}$  sectioning commands: `\section`,  
 275 `\subsection`, `\subsubsection`, `\paragraph`, and `\ subparagraph`. The sectioning levels up to `\subsubsection` should be numbered;  
 276 do not remove the numbering from the commands.

277 Simulating a sectioning command by setting the first word or  
 278 words of a paragraph in boldface or italicized text is **not allowed**.

279 Below are examples of sectioning commands.

### 283 16.1 Subsection

284 This is a subsection.

286 16.1.1 Subsubsection. This is a subsubsection.

288 Paragraph. This is a paragraph.

289 Subparagraph This is a subparagraph.

291 **Table 1: Frequency of Special Characters**

292 Non-English or Math	293 Frequency	294 Comments
295 $\emptyset$	296 1 in 1,000	297 For Swedish names
298 $\pi$	299 1 in 5	300 Common in math
301 $$$	302 4 in 5	303 Used in business
304 $\Psi_1^2$	305 1 in 40,000	306 Unexplained usage

## 301 17 TABLES

302 The “acmart” document class includes the “booktabs” package —  
<https://ctan.org/pkg/booktabs> — for preparing high-quality tables.

303 Table captions are placed *above* the table.

304 Because tables cannot be split across pages, the best placement  
 305 for them is typically the top of the page nearest their initial cite.  
 306 To ensure this proper “floating” placement of tables, use the envi-  
 307 ronment `table` to enclose the table’s contents and the table caption.  
 308 The contents of the table itself must go in the `tabular` environment,  
 309 to be aligned properly in rows and columns, with the desired hori-  
 310 zontal and vertical rules. Again, detailed instructions on `tabular`  
 311 material are found in the  *$\text{\LaTeX}$  User’s Guide*.

312 Immediately following this sentence is the point at which Table 1  
 313 is included in the input file; compare the placement of the table  
 314 here with the table in the printed output of this document.

315 To set a wider table, which takes up the whole width of the page’s  
 316 live area, use the environment `table*` to enclose the table’s contents  
 317 and the table caption. As with a single-column table, this wide  
 318 table will “float” to a location deemed more desirable. Immediately  
 319 following this sentence is the point at which Table 2 is included in  
 320 the input file; again, it is instructive to compare the placement of  
 321 the table here with the table in the printed output of this document.

322 Always use midrule to separate table header rows from data rows,  
 323 and use it only for this purpose. This enables assistive technologies  
 324 to recognise table headers and support their users in navigating  
 325 tables more easily.

## 328 18 MATH EQUATIONS

329 You may want to display math equations in three distinct styles:  
 330 inline, numbered or non-numbered display. Each of the three are  
 331 discussed in the next sections.

### 334 18.1 Inline (In-text) Equations

335 A formula that appears in the running text is called an inline or  
 336 in-text formula. It is produced by the `math` environment, which  
 337 can be invoked with the usual `\begin{math} \dots \end{math}` construction or  
 338 with the short form `$ \dots $`. You can use any of the symbols and  
 339 structures, from  $\alpha$  to  $\omega$ , available in  $\text{\LaTeX}$  [?]; this section will  
 340 simply show a few examples of in-text equations in context. Notice  
 341 how this equation:  $\lim_{n \rightarrow \infty} x = 0$ , set here in in-line math style,  
 342 looks slightly different when set in display style. (See next section).

### 344 18.2 Display Equations

345 A numbered display equation—one set off by vertical space from  
 346 the text and centered horizontally—is produced by the `equation`

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**Table 2: Some Typical Commands**

Command	A Number	Comments
\author	100	Author
\table	300	For tables
\table*	400	For wider tables

environment. An unnumbered display equation is produced by the **displaymath** environment.

Again, in either environment, you can use any of the symbols and structures available in L<sup>A</sup>T<sub>E</sub>X; this section will just give a couple of examples of display equations in context. First, consider the equation, shown as an inline equation above:

$$\lim_{n \rightarrow \infty} x = 0 \quad (1)$$

Notice how it is formatted somewhat differently in the **displaymath** environment. Now, we'll enter an unnumbered equation:

$$\sum_{i=0}^{\infty} x + 1$$

and follow it with another numbered equation:

$$\sum_{i=0}^{\infty} x_i = \int_0^{\pi+2} f \quad (2)$$

just to demonstrate L<sup>A</sup>T<sub>E</sub>X's able handling of numbering.

## 19 FIGURES

The “figure” environment should be used for figures. One or more images can be placed within a figure. If your figure contains third-party material, you must clearly identify it as such, as shown in the example below.

**Figure 2: 1907 Franklin Model D roadster. Photograph by Harris & Ewing, Inc. [Public domain], via Wikimedia Commons. (<https://goo.gl/VLCRBB>).**

Your figures should contain a caption which describes the figure to the reader.

Figure captions are placed *below* the figure.

Every figure should also have a figure description unless it is purely decorative. These descriptions convey what's in the image to someone who cannot see it. They are also used by search engine crawlers for indexing images, and when images cannot be loaded.

A figure description must be unformatted plain text less than 2000 characters long (including spaces). **Figure descriptions should not repeat the figure caption – their purpose is to capture important information that is not already provided in the caption or the main text of the paper.** For figures that convey important and complex new information, a short text description may not be adequate. More complex alternative descriptions can be placed in an appendix and referenced in a short figure description. For example, provide a data table capturing the information in a bar chart, or a structured list representing a graph.

For additional information regarding how best to write figure descriptions and why doing this is so important, please see <https://www.acm.org/publications/taps/describing-figures/>.

### 19.1 The “Teaser Figure”

A “teaser figure” is an image, or set of images in one figure, that are placed after all author and affiliation information, and before the body of the article, spanning the page. If you wish to have such a figure in your article, place the command immediately before the `\maketitle` command:

```
\begin{teaserfigure}
\includegraphics[width=\textwidth]{sampleteaser}
\caption{figure caption}
\Description{figure description}
\end{teaserfigure}
```

## 20 CITATIONS AND BIBLIOGRAPHIES

The use of BibT<sub>E</sub>X for the preparation and formatting of one's references is strongly recommended. Authors' names should be complete — use full first names (“Donald E. Knuth”) not initials (“D. E. Knuth”) — and the salient identifying features of a reference should be included: title, year, volume, number, pages, article DOI, etc.

The bibliography is included in your source document with these two commands, placed just before the `\end{document}` command:

```
\bibliographystyle{ACM-Reference-Format}
\bibliography{bibfile}
```

where “bibfile” is the name, without the “.bib” suffix, of the BibT<sub>E</sub>X file.

Citations and references are numbered by default. A small number of ACM publications have citations and references formatted in the “author year” style; for these exceptions, please include this command in the **preamble** (before the command “`\begin{document}`”) of your L<sup>A</sup>T<sub>E</sub>X source:

```
\citestyle{acmauthoryear}
```

Some examples. A paginated journal article [? ], an enumerated journal article [? ], a reference to an entire issue [? ], a monograph (whole book) [? ], a monograph/whole book in a series (see 2a in spec. document) [? ], a divisible-book such as an anthology or compilation [? ] followed by the same example, however we only output the series if the volume number is given [? ] (so Editor00a's series should NOT be present since it has no vol. no.), a chapter in a divisible book [? ], a chapter in a divisible book in a series [? ], a multi-volume work as book [? ], a couple of articles in a proceedings (of a conference, symposium, workshop for example) (paginated proceedings article) [? ? ], a proceedings article with all possible elements [? ], an example of an enumerated proceedings

465 article [? ], an informally published work [? ], a couple of preprints  
 466 [? ? ], a doctoral dissertation [? ], a master's thesis: [? ], an online  
 467 document / world wide web resource [? ? ? ], a video game (Case  
 468 1) [? ] and (Case 2) [? ] and [? ] and (Case 3) a patent [? ], work  
 469 accepted for publication [? ], 'YYYYb'-test for prolific author [? ]  
 470 and [? ]. Other cites might contain 'duplicate' DOI and URLs (some  
 471 SIAM articles) [? ]. Boris / Barbara Beeton: multi-volume works as  
 472 books [? ] and [? ]. A presentation [? ]. An article under review [? ].  
 473 A couple of citations with DOIs: [? ? ]. Online citations: [? ? ? ].  
 474 Artifacts: [? ] and [? ].

## 475 21 ACKNOWLEDGMENTS

477 Identification of funding sources and other support, and thanks  
 478 to individuals and groups that assisted in the research and the  
 479 preparation of the work should be included in an acknowledgment  
 480 section, which is placed just before the reference section in your  
 481 document.

482 This section has a special environment:

```
483 \begin{acks}  

  484 ...  

  485 \end{acks}
```

487 so that the information contained therein can be more easily col-  
 488 lected during the article metadata extraction phase, and to ensure  
 489 consistency in the spelling of the section heading.

490 Authors should not prepare this section as a numbered or un-  
 491 numbered \section; please use the "acks" environment.

## 492 22 APPENDICES

494 If your work needs an appendix, add it before the "\end{document}"  
 495 command at the conclusion of your source document.

496 Start the appendix with the "appendix" command:

```
497 \appendix
```

499 and note that in the appendix, sections are lettered, not numbered.  
 500 This document has two appendices, demonstrating the section and  
 501 subsection identification method.

## 502 23 MULTI-LANGUAGE PAPERS

504 Papers may be written in languages other than English or include  
 505 titles, subtitles, keywords and abstracts in different languages (as  
 506 a rule, a paper in a language other than English should include  
 507 an English title and an English abstract). Use language=... for  
 508 every language used in the paper. The last language indicated is  
 509 the main language of the paper. For example, a French paper with  
 510 additional titles and abstracts in English and German may start  
 511 with the following command

```
512 \documentclass[sigconf, language=english, language=german,  

  513 language=french]{acmart}
```

514 The title, subtitle, keywords and abstract will be typeset in the  
 515 main language of the paper. The commands \translatedXXX, XXX  
 516 begin title, subtitle and keywords, can be used to set these elements  
 517 in the other languages. The environment translatedabstract  
 518 is used to set the translation of the abstract. These commands  
 519 and environment have a mandatory first argument: the language  
 520 of the second argument. See sample-sigconf-i13n.tex file for  
 521 examples of their usage.

## 24 SIGCHI EXTENDED ABSTRACTS

The "sigchi-a" template style (available only in L<sup>A</sup>T<sub>E</sub>X and not in Word) produces a landscape-orientation formatted article, with a wide left margin. Three environments are available for use with the "sigchi-a" template style, and produce formatted output in the margin:

**sidebar:** Place formatted text in the margin.

**marginfigure:** Place a figure in the margin.

**margintable:** Place a table in the margin.

## ACKNOWLEDGMENTS

Left blank for anonymity.

## REFERENCES

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