CM 1110 Fundamentals of Mathematics and Statistics $\,$

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2020-01-31

Contents

C	ourse Syllabus	5					
	Pre-requisites	5					
	Learning Outcomes	5					
	Outline Syllabus	5					
	Method of Assessment	5					
	Lecturer	6					
	Schedule	6					
1	Number Systems	7					
2	Sequence and Series	9					
3	Introduction to Logic	11					
4	Boolean Algebra						
5	Differentiation and Integration						
6	Descriptive Statistics	1					
	6.1 Introduction to Statistics	1					
	6.2 Presentation of Data	7					
7	Sets and Relations	11					
8	Probability	13					
9 Correlation and Regression							

CONTENTS CONTENTS

Course Syllabus

Pre-requisites

None

Learning Outcomes

On successful completion of this module, students will be able to apply fundamental concepts in Mathematics and Statistics for real world problem solving.

Outline Syllabus

- Number Systems
- Sequence and Series
- Introduction to Logic
- Boolean Algebra
- Differentiation and Integration
- Descriptive Statistics
- Sets and Relations
- Probability
- Correlation and Regression

Method of Assessment

- Mid-semester examination
- End-semester examination

CONTENTS CONTENTS

Lecturer

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Schedule

Lectures: TBA

Consultation times: TBA

Number Systems

Sequence and Series

Introduction to Logic

Boolean Algebra

Differentiation and Integration

Descriptive Statistics

6.1 Introduction to Statistics

6.1.1 Some Basic Terminologies Used in Statistics

i Population

• The set of all possible elements in the universe of interest to the researcher

ii Sample

- A Sample is a **subset** (a portion or part) of the population of interest
- The sample must be a representative of the population of interest

iii Element

- Element is an **entity or object** which the information is collected.
- Eg: Student, household, farm, company, tomato plant

iv Variable

- A variable is a feature characteristic which has different 'values' or categories for different elements (items/subjects/individuals)
- Eg: Gender of client, brand of mobile phones, risk level, number of emails received per day, age of client, income of client

v Data

6.1. INTRODUCTION TO STACHEAUCER 6. DESCRIPTIVE STATISTICS

- Data are **measurements or facts** that are collected from a statistical unit/entity of interest
- We collect data on variables
- Data are raw numbers or facts that must be processed (analysed) to get useful information.
- We get information from data.
- *Eg*:

Variable: Age (in years) of client

Data: 21, 45, 18, 32, 30, 22, 23, 27

Information:

The mean age is 27.25 years

The minimum age is 18 years

The range of ages is 18-45

The percentage of clients below 25 years of age: 50%

vi Statistic

- Characteristic of a sample
- The value which calculated based on sample data

vii Parameter

- Characteristic of a population
- The value which calculated based on population data

viii Census

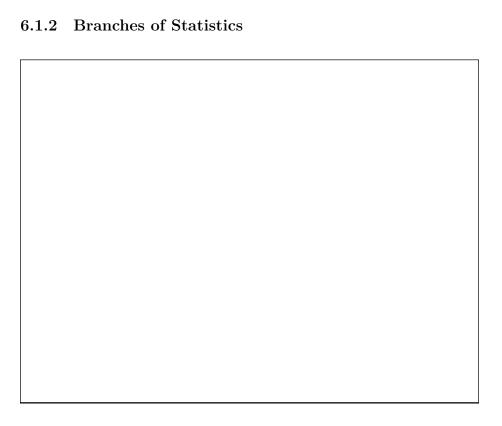
• When a researcher gathers data from the whole population for a given measurement, it is called a census

ix Sampling

- When a researcher gathers data from a sample of the population for a given measurement, it is called sampling
- The process of selecting a sample is also called sampling

Why take a sample instead of studying every member of the population ?

- Prohibitive cost of census
- Destruction of item being studied may be required
- Not possible to test or inspect all members of a population being studied.



i Descriptive Statistics

- Descriptive statistics consists of organizing, summarizing and presenting data in an informative way.
- The main purpose of descriptive statistics is to provide an overview of the data collected.
- Descriptive statistics describes the data collected through frequency tables, graphs and summary measures (mean, variance, quartiles, etc.).

ii Inferential Statistics

- In inferential statistics sample data are used to draw inferences (i.e. derive conclusions) or make predictions about the populations from which the sample has been taken.
- This includes methods used to make decisions, estimates, predictions or generalizations about a population based on a sample.
- This includes point estimations, interval estimation, test of hypotheses, regression analysis, time series analysis, multivariate analysis, etc.

6.1. INTRODU	UCTION TO STACHSAIHCER 6.	DESCRIPTIVE STATISTIC
6.1.3 Type	s of Variables	
6.1.3.1 Quali	tative / Quantitative Varia	bles
i Qualitative v	variable (Categorical variab	le)
• The chara	cteristic is a quality.	
• The data a	are categories.	
	not be given numerical values. it may be given a numerical lab	el
• Qualitativ	e variables are sometimes referr	
• <i>Eg</i> :		
Gender:		
Age group:		
Education level:		
A/L stream:		
Degree type:		
Hair colour:		
4	Prepared by Dr. Priyanga	D. Talagala

CHAPTER 6. DESCRIPTIVE STAGISTINGSRODUCTION TO STATISTICS

FIT student batch:

Undergraduate level:

Grade that you can obtain for CM 1110/ CM1130

ii Quantitative variable

- The characteristic is a quantity
- The data are numbers
- Quantitative data require numeric values that indicate how much or how many.
- They are obtained by counting or measuring with some scale
- *Eg*:

Number of family members:

Number of emails received per day:

Weight of a student:

Age:

Credit balance in the SIM card:

Time remaining in class:

Temperature:

Marks

6.1.3.2 Discrete/ Continuous Variables

• Quantitative variables can be classified as either discrete or continuous.

i Discrete Variables

- Quantitative
- Usually the data are obtained by counting
- There are impossible values between any two possible values
- *Eg:*

Number of family members:

Number of emails received per day:

ii Continuous Variables

- Quantitative
- Usually, the data are obtained by measuring with a scale

6.1. INTRODUCTION TO STACHEAUCER 6. DESCRIPTIVE STATISTICS

 There are no impossible values between any two possible values.(any value between any two possible values is also a possible value) i.e a continuous variable can take any value within a specified range. Eg:
Weight of a student:
Age:
Credit balance in the SIM card:
Time remaining in class:
Temperature:
Marks
3.1.4 Scales of Measurements
 There are four levels of measurements called, nominal, ordinal, interval and ratio. Each levels has its own rules and restrictions Different levels of measurement contains different amount of information

with respect to whatever the data are measuring

i Nominal Scale

- Qualitative
- No order or ranking in categories.
- These categories have to be mutually exclusive, i.e. it should not be possible to place an individual or object in more than one category
- A name of a category can be substituted by a number, but it will be mere label and have no numerical meaning

ii Ordinal Scale

- Qualitative
- Categories can be ordered or ranked
- A name of a category can be substituted by a number, but such a sequence does not indicate absolute quantities.
- Difference between any two numbers on the scale does not have a numerical meaningful.
- It cannot be assumed that the differences between adjacent numbers on the scale are equal.

iii Interval Scale

- Quantitative
- Data can be ordered or ranked
- There is no absolute zero point. Zero is only an arbitrary point with which other values can compare
- Difference between two numbers is a meaningful numerical value
- Ration of two numbers is not a meaningful numerical value.

iv Ratio Scale

- Quantitative
- Highest level of measurement
- There exist an absolute zero point (It has a true zero point)
- Ratio between different measurements is meaningful

6.2 Presentation of Data

The sinking of the Titanic is one of the most infamous shipwrecks in history.

On April 15, 1912, during her maiden voyage, the widely considered "unsinkable" RMS Titanic sank after colliding with an iceberg. Unfortunately, there

6.2. PRESENTATION OF DATCHAPTER 6. DESCRIPTIVE STATISTICS

weren't enough lifeboats for everyone onboard, resulting in the death of 1502 out of 2224 passengers and crew

1

Here's a quick summary of our variables:

Variable Name	Description			
PassengerID	Passenger ID (just a row number,			
	so obviously not useful for			
	prediction)			
Survived	Survived (1) or died (0)			
Pclass	Passenger class (first, second or			
	third)			
Name	Passenger name			
Gender	Passenger Gender			
Age	Passenger age			
SibSp	Number of siblings/spouses aboard			
Parch	Number of parents/children aboard			
Ticket	Ticket number			
Fare	Fare			
Cabin	Cabin			
Embarked	Port of embarkation ($S =$			
	Southampton, $C = Cherbourg$, Q			
	= Queenstown)			

6.2.1 Tabular Presentations of Data

Raw Data

- Raw data are collected data that have not been organized numerically
- Eg: Passenger age

##		PassengerId	Pclass					Name	Sex	Age
##	1	892	3				Kelly, Mr	. James	male	34.5
##	2	893	3		Wil	lkes, Mrs.	James (Ellen	Needs)	${\tt female}$	47.0
##	3	894	2			Myles,	Mr. Thomas	Francis	male	62.0
##	4	895	3				Wirz, Mr.	Albert	male	27.0
##	5	896	3	Hirvonen	Mrs.	Alexander	(Helga E Lin	dqvist)	${\tt female}$	22.0
##	6	897	3			Svensso	on, Mr. Johan	Cervin	male	14.0
##		SibSp Parch	Ticket	t Fare	${\tt Cabin}$	Embarked				
##	1	0 0	33091	1 7.8292		Q				

 $^{^{1}} Data\ source:\ https://www.kaggle.com/varimp/a-mostly-tidyverse-tour-of-the-titanic$

CHAPTER 6. DESCRIPTIVE STATISTICS2. PRESENTATION OF DATA

```
## 2
        1
              0
                 363272 7.0000
                                             S
## 3
        0
              0
                 240276 9.6875
                                             Q
                                             S
        0
              0 315154 8.6625
              1 3101298 12.2875
                                             S
## 5
        1
## 6
              0
                   7538 9.2250
                                             S
        0
   [1] 34.5 47.0 62.0 27.0 22.0 14.0 30.0 26.0 18.0 21.0
                                                           NA 46.0 23.0 63.0 47.0
                                            NA 21.0 48.0 50.0 22.0 22.5 41.0
## [16] 24.0 35.0 21.0 27.0 45.0 55.0 9.0
## [31] 50.0 24.0 33.0
                       NA 30.0 18.5
                                       NA 21.0 25.0
                                                      NA
```

An array

- An array is an arrangement of raw numerical data in ascending or descending order of magnitude.
- Eg: Passenger age

```
## [1] 9.0 14.0 18.0 18.5 21.0 21.0 21.0 21.0 22.0 22.0 22.5 23.0 24.0 24.0 25.0 ## [16] 26.0 27.0 27.0 30.0 30.0 33.0 34.5 35.0 41.0 45.0 46.0 47.0 47.0 48.0 50.0 ## [31] 50.0 55.0 62.0 63.0
```

Frequency Table (Frequency Distributions)

- A frequency table (frequency distribution) is a listing of the values a variable takes in a data set, along with how often (frequently) each value occurs
- frequency can be recorded as a
 - frequency or count: the number of times a value occurs, or
 - percentage frequency: the percentage of times a value occurs
- Percentage frequency can be calculated as,

6.2. PRESENTATION OF DATCHAPTER 6. DESCRIPTIVE STATISTICS

Sets and Relations

Probability

Correlation and Regression