

# MA 5124 Financial Time Series Analysis & Forecasting

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# Course Syllabus

**Module Code:** MA 5124

**Title:** Financial Time Series Analysis & Forecasting

**Credits:** 4

## Pre-requiites

None

## Learning Objectives

- The purpose of this course is to provide students with introductory tools for the time series analysis of financial time series.
- Analyze of data series based on stochastic and non stochastic models

## Learning Outcomes

- On successful completion of this course, students will be able to provide more than an introductory treatment of the topics.
- Students are encouraged to pursue further study in this area if they find that the topics covered in this course.

## Outline Syllabus

- Definition and examples of time series
- back-shift and differencing-operators, - strong and weak stationarity, definition of ACF, PACF.

- Definitions and properties of the  $MA(q)$ ,  $MA(\infty)$ ,  $AR(p)$ ,  $AR(\infty)$  and  $ARMA(p, q)$ , in particular their acf's
- causal stationarity of AR
- invertibility of MA models and causal stationarity and invertibility of ARMA; - concept of spectral density function and its applications
- definition and properties of integrated  $ARIMA(p, d, q)$  processes
- definition and properties of random walks with or without drift.
- Model selection following the AIC and BIC
- brief introduction to linear prediction and calculation of forecasting intervals for normal ARMA models
- point and interval forecasts for normal random walks with or without drift.
- Definition and properties of the VAR (vector autoregressive) model, arrange a univariate time series as a multivariate Markov model.
- Nonlinear properties of financial time series
- definition and properties of the well known ARCH, GARCH etc.
- Cointegration in Single Equations, Modeling and Forecasting Financial Time Series.

## Method of Assessment

- Assignment 30%
- End-semester examination 70%

## Lecturer

Dr. Priyanga D. Talagala

## Schedule

Lectures:

- Sunday [9.00am -12.00 noon]

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## Chapter 1

# Intordution to Time Series Forecasting



## Chapter 2

# Time Series Graphics



## Chapter 3

# Time Series Decomposition



## Chapter 4

# Exponential Smoothing





## Chapter 5

# ARIMA models



## Chapter 6

# Multiple Regression and Forecasting



## Chapter 7

# Dynamic Regression Models



## Chapter 8

# Multivariate Time Series Models

- Unit root tests
- multivariate time series)
- (VAR )





## Chapter 9

# Cointegration



## Chapter 10

# Volatility Models

- (ARCH, GARCH)



## Chapter 11

# Time series with R

### 11.1 Lesson 1: Introduction to R

```
4+1
```

```
## [1] 5
```

```
mean(c(1,2,3,4))
```

```
## [1] 2.5
```

```
# These are equivalent
```

```
y=4
```

```
y<-4 #this was the original one used and that's why you will see it in many places
```

```
#load fpp2
```

```
library(fpp2)
```

```
## Registered S3 method overwritten by 'quantmod':
```

```
##   method      from
```

```
##   as.zoo.data.frame zoo
```

```
## -- Attaching packages ----- fpp2 2.4 --
```

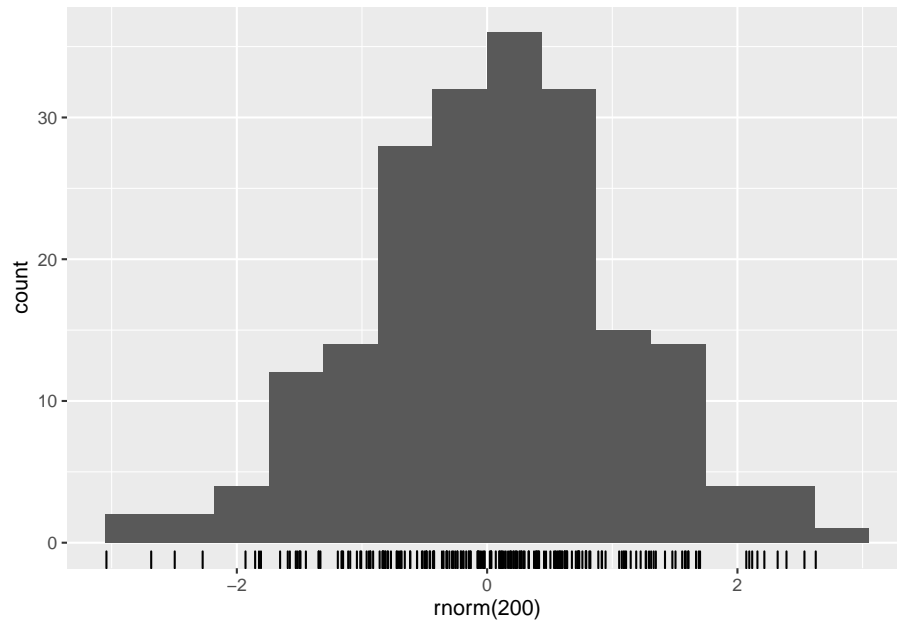
```
## v ggplot2 3.3.2    v fma      2.4
```

```
## v forecast 8.12    v expsmooth 2.3
```

##

`?fpp2`

```
gghistogram(rnorm(200)) #rnorm generates random numbers from a standard normal
```



```
# Equivalent to typing in the help menu
```

`?mean`

```
# Example in the help menu for the mean
```

```
x <- c(0:10, 50)
```

```
length(x)
```

## `[1] 12`

```
xm <- mean(x)
```

```
austa # what happens here?
```

## Time Series:

## Start = 1980

## End = 2015

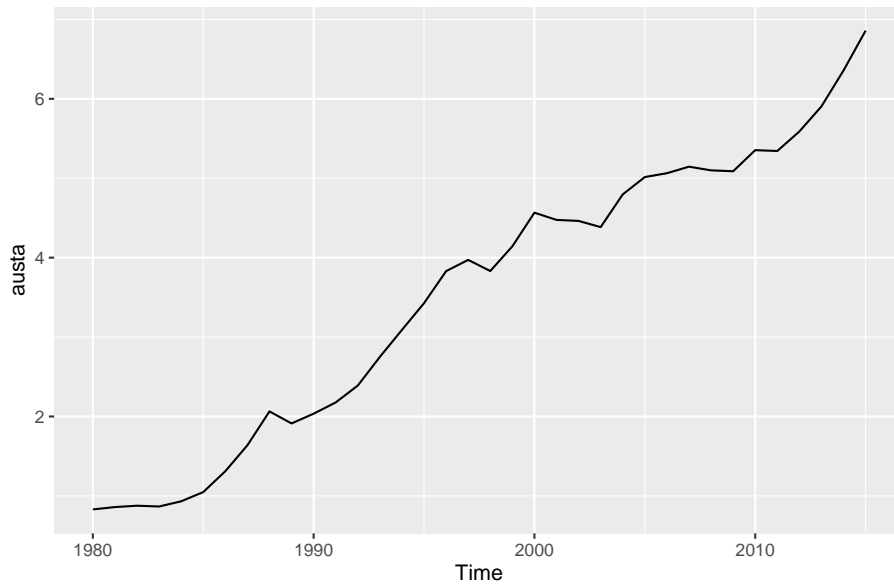
```
## Frequency = 1
## [1] 0.8298943 0.8595109 0.8766892 0.8667072 0.9320520 1.0482636 1.3111932
## [8] 1.6375623 2.0641074 1.9126828 2.0354457 2.1772113 2.3896834 2.7505921
## [15] 3.0906664 3.4266403 3.8306491 3.9719086 3.8316004 4.1431010 4.5665510
## [22] 4.4754100 4.4627960 4.3848290 4.7968610 5.0150490 5.0634350 5.1454890
## [29] 5.0994360 5.0881660 5.3537020 5.3433270 5.5891620 5.9048840 6.3571830
## [36] 6.8589530
```

```
# Ignore the error message and keep going
```

```
# Lets look at some data sets from fpp
austa #International vistors to Australia
```

```
## Time Series:
## Start = 1980
## End = 2015
## Frequency = 1
## [1] 0.8298943 0.8595109 0.8766892 0.8667072 0.9320520 1.0482636 1.3111932
## [8] 1.6375623 2.0641074 1.9126828 2.0354457 2.1772113 2.3896834 2.7505921
## [15] 3.0906664 3.4266403 3.8306491 3.9719086 3.8316004 4.1431010 4.5665510
## [22] 4.4754100 4.4627960 4.3848290 4.7968610 5.0150490 5.0634350 5.1454890
## [29] 5.0994360 5.0881660 5.3537020 5.3433270 5.5891620 5.9048840 6.3571830
## [36] 6.8589530
```

```
autoplot(austa)
```



```
# Summary command: prints an appropriate summary of what you asked from
summary(austa)
```

```
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
## 0.8299  2.0048  3.9018  3.5414  5.0696  6.8590
```

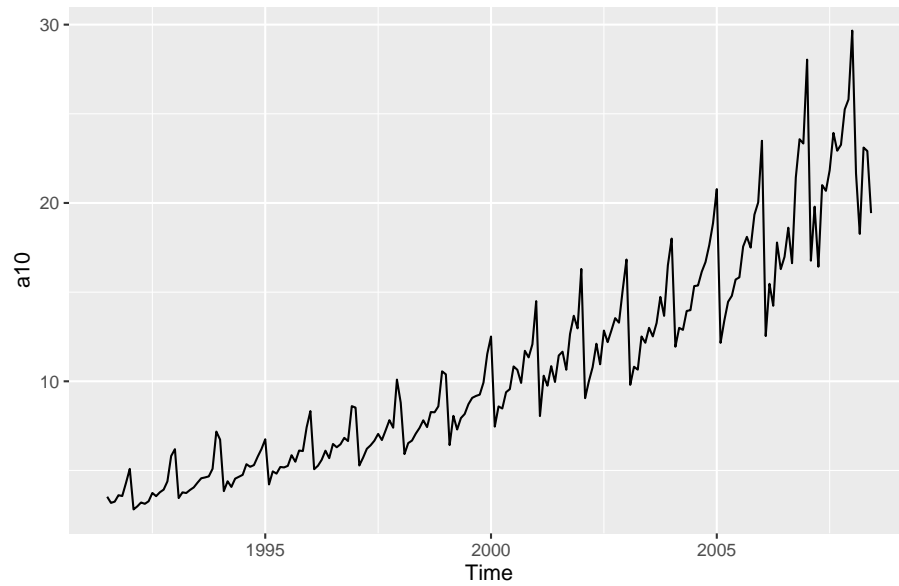
```
# Some monthly data
a10 # Monthly anti-diabetic drug sales in Australia from 1992 to 2008
```

```
##           Jan      Feb      Mar      Apr      May      Jun      Jul
## 1991                                     3.526591
## 1992  5.088335  2.814520  2.985811  3.204780  3.127578  3.270523  3.737851
## 1993  6.192068  3.450857  3.772307  3.734303  3.905399  4.049687  4.315566
## 1994  6.731473  3.841278  4.394076  4.075341  4.540645  4.645615  4.752607
## 1995  6.749484  4.216067  4.949349  4.823045  5.194754  5.170787  5.256742
## 1996  8.329452  5.069796  5.262557  5.597126  6.110296  5.689161  6.486849
## 1997  8.524471  5.277918  5.714303  6.214529  6.411929  6.667716  7.050831
## 1998  8.798513  5.918261  6.534493  6.675736  7.064201  7.383381  7.813496
## 1999 10.391416  6.421535  8.062619  7.297739  7.936916  8.165323  8.717420
## 2000 12.511462  7.457199  8.591191  8.474000  9.386803  9.560399 10.834295
## 2001 14.497581  8.049275 10.312891  9.753358 10.850382  9.961719 11.443601
## 2002 16.300269  9.053485 10.002449 10.788750 12.106705 10.954101 12.844566
## 2003 16.828350  9.800215 10.816994 10.654223 12.512323 12.161210 12.998046
```



```
## 2004 18.003768 11.938030 12.997900 12.882645 13.943447 13.989472 15.339097
## 2005 20.778723 12.154552 13.402392 14.459239 14.795102 15.705248 15.829550
## 2006 23.486694 12.536987 15.467018 14.233539 17.783058 16.291602 16.980282
## 2007 28.038383 16.763869 19.792754 16.427305 21.000742 20.681002 21.834890
## 2008 29.665356 21.654285 18.264945 23.107677 22.912510 19.431740
##           Aug           Sep           Oct           Nov           Dec
## 1991  3.180891  3.252221  3.611003  3.565869  4.306371
## 1992  3.558776  3.777202  3.924490  4.386531  5.810549
## 1993  4.562185  4.608662  4.667851  5.093841  7.179962
## 1994  5.350605  5.204455  5.301651  5.773742  6.204593
## 1995  5.855277  5.490729  6.115293  6.088473  7.416598
## 1996  6.300569  6.467476  6.828629  6.649078  8.606937
## 1997  6.704919  7.250988  7.819733  7.398101 10.096233
## 1998  7.431892  8.275117  8.260441  8.596156 10.558939
## 1999  9.070964  9.177113  9.251887  9.933136 11.532974
## 2000 10.643751  9.908162 11.710041 11.340151 12.079132
## 2001 11.659239 10.647060 12.652134 13.674466 12.965735
## 2002 12.196500 12.854748 13.542004 13.287640 15.134918
## 2003 12.517276 13.268658 14.733622 13.669382 16.503966
## 2004 15.370764 16.142005 16.685754 17.636728 18.869325
## 2005 17.554701 18.100864 17.496668 19.347265 20.031291
## 2006 18.612189 16.623343 21.430241 23.575517 23.334206
## 2007 23.930204 22.930357 23.263340 25.250030 25.806090
## 2008
```

```
autoplot(a10)
```



```
summary(a10)
```

```
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
##      2.815   5.844   9.319  10.694  14.290  29.665
```

```
# You will practice reading in your own data in the tutorials this week
# and next week. This will set you up well for the assignment
```

```
# This creates a vector y of observations
y=c(1,2,3,4,5,6)
mean(y)
```

```
## [1] 3.5
```

```
# Write your own function

average<-function(x)
{
  return(sum(x)/length(x))
}

ybar<-average(y)
```

## 11.2 Lesson 2: Time series graphic

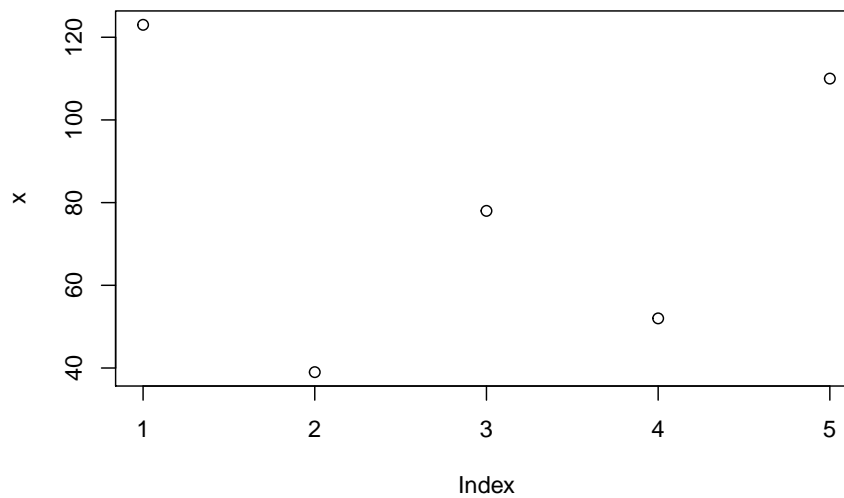
```
library(fpp2)

# ts objects

x <- c(123,39,78,52,110) # This is now just a column of numbers
x
```

```
## [1] 123  39  78  52 110
```

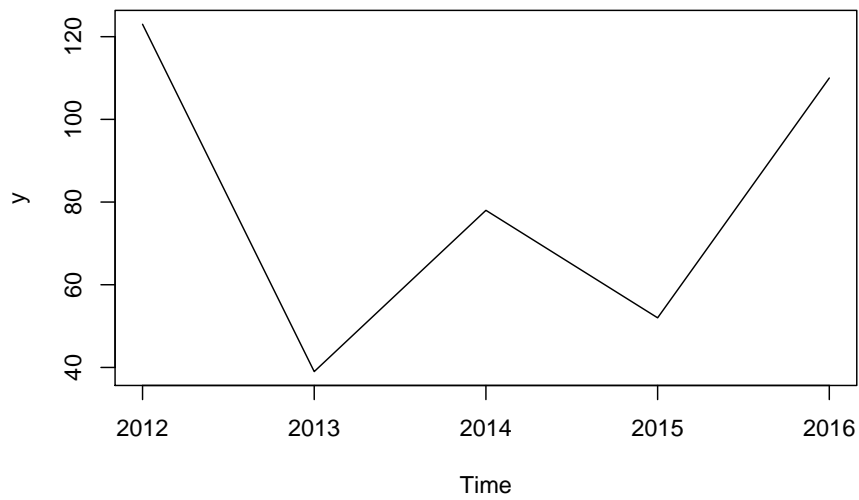
```
plot(x)
```



```
y <- ts(c(123,39,78,52,110), start=2012)
y
```

```
## Time Series:
## Start = 2012
## End = 2016
## Frequency = 1
## [1] 123  39  78  52 110
```

```
plot(y)
```

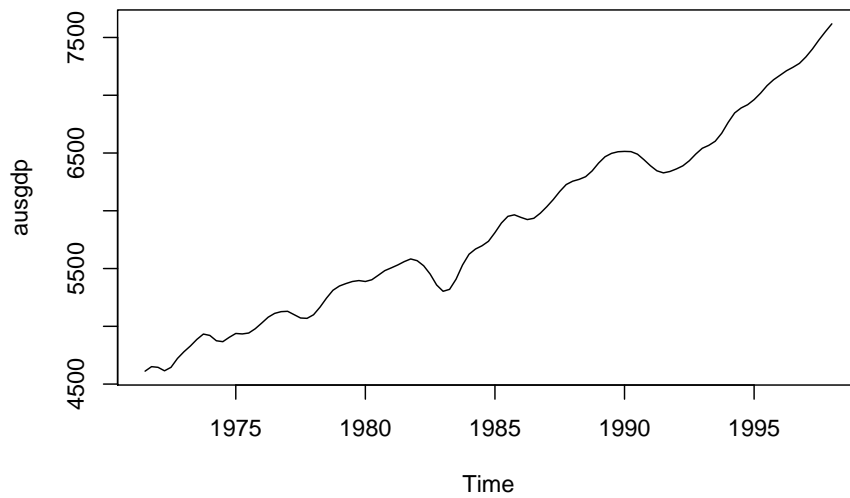


```
z <- ts(x, frequency=12, start=c(2003,1))
z
```

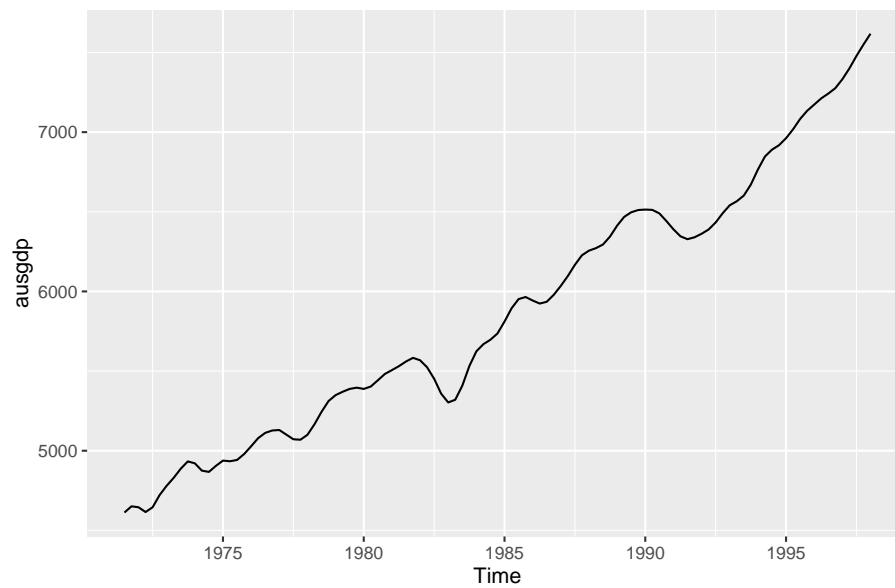
```
##      Jan Feb Mar Apr May
## 2003 123  39  78  52 110
```

```
# For higher frequency data use the frequency argument
# setwd("C:/George/Teaching/ETF3231/2018/RinLectures")
x <- scan(here::here("data", "gdp.dat"))

ausgdp <- ts(x, frequency=4,
             start=1971.5) # Data starts in Q3
plot(ausgdp) # part of base graphics
```

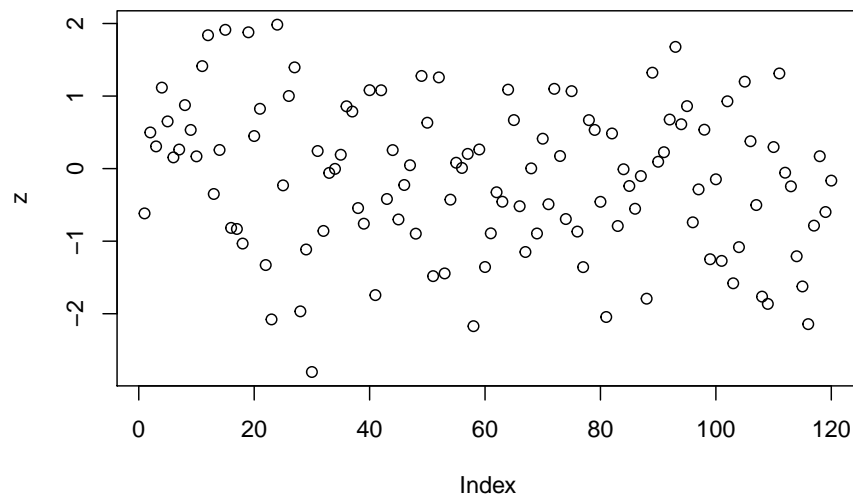


```
autoplot(ausgdp) # part of forecast and interaction with ggplot2
```



```
# better plots only for ts objects
```

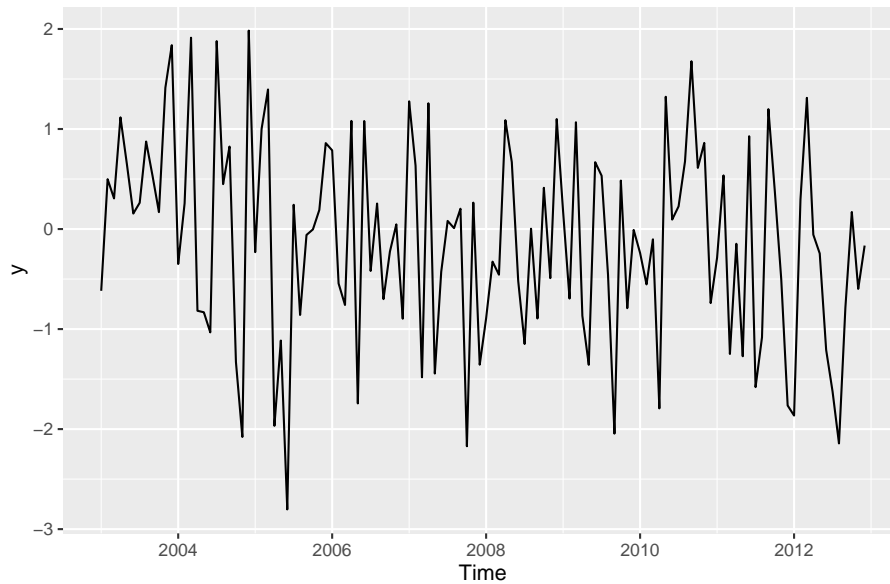
```
z=rnorm(120)  
#autoplot(z)  
plot(z)
```



```
y <- ts(z, start=2003, frequency=12)  
attributes(y)
```

```
## $tsp  
## [1] 2003.000 2012.917 12.000  
##  
## $class  
## [1] "ts"
```

```
autoplot(y)
```



```
# Some ready ts
elecsales
```

```
## Time Series:
## Start = 1989
## End = 2008
## Frequency = 1
## [1] 2354.34 2379.71 2318.52 2468.99 2386.09 2569.47 2575.72 2762.72 2844.50
## [10] 3000.70 3108.10 3357.50 3075.70 3180.60 3221.60 3176.20 3430.60 3527.48
## [19] 3637.89 3655.00
```

```
?elecsales
# Everyone to plot
# Also ask them to use the help command - you will need to do
# this a lot

# ? is shorthand for help()

# Ask everyone to type melsyd to see what they get

melsyd # let's have a look
```

```
## Time Series:
## Start = c(1987, 26)
```

```
## End = c(1992, 48)
## Frequency = 52
##      First.Class Business.Class Economy.Class
## 1987.481      1.912             NA      20.167
## 1987.500      1.848             NA      20.161
## 1987.519      1.856             NA      19.993
## 1987.538      2.142             NA      20.986
## 1987.558      2.118             NA      20.497
## 1987.577      2.048             NA      20.770
## 1987.596      2.111             NA      21.111
## 1987.615      2.199             NA      20.675
## 1987.635      2.231             NA      22.092
## 1987.654      2.081             NA      20.772
## 1987.673      2.213             NA      21.642
## 1987.692      2.131             NA      21.911
## 1987.712      NA              NA      NA
## 1987.731      2.131             NA      23.777
## 1987.750      2.034             NA      22.658
## 1987.769      2.190             NA      23.515
## 1987.788      2.262             NA      21.384
## 1987.808      2.579             NA      24.344
## 1987.827      2.367             NA      21.137
## 1987.846      2.432             NA      23.069
## 1987.865      2.640             NA      23.664
## 1987.885      2.614             NA      23.219
## 1987.904      2.569             NA      23.192
## 1987.923      2.523             NA      23.475
## 1987.942      2.260             NA      22.377
## 1987.962      1.117             NA      16.606
## 1987.981      0.590             NA      13.987
## 1988.000      0.966             NA      16.251
## 1988.019      1.235             NA      18.439
## 1988.038      2.001             NA      20.262
## 1988.058      1.696             NA      19.535
## 1988.077      2.089             NA      22.467
## 1988.096      2.716             NA      24.559
## 1988.115      2.483             NA      24.591
## 1988.135      2.461             NA      24.511
## 1988.154      2.533             NA      24.524
## 1988.173      2.273             NA      23.119
## 1988.192      2.273             NA      23.106
## 1988.212      2.370             NA      23.292
## 1988.231      1.782             NA      21.566
## 1988.250      1.385             NA      18.565
## 1988.269      2.322             NA      24.361
## 1988.288      2.340             NA      22.983
```



## 1988.308	2.203	NA	21.062
## 1988.327	2.300	NA	21.766
## 1988.346	2.125	NA	22.285
## 1988.365	2.345	NA	22.867
## 1988.385	2.224	NA	23.276
## 1988.404	1.952	NA	20.924
## 1988.423	2.212	NA	21.716
## 1988.442	2.028	NA	20.908
## 1988.462	1.906	NA	21.410
## 1988.481	1.834	NA	21.361
## 1988.500	1.797	NA	22.412
## 1988.519	1.869	NA	21.290
## 1988.538	1.886	NA	22.247
## 1988.558	2.131	NA	22.445
## 1988.577	2.021	NA	21.260
## 1988.596	2.199	NA	22.771
## 1988.615	2.140	NA	23.723
## 1988.635	2.190	NA	23.757
## 1988.654	1.917	NA	23.482
## 1988.673	2.096	NA	23.653
## 1988.692	2.254	NA	26.054
## 1988.712	2.251	NA	25.695
## 1988.731	2.072	NA	26.720
## 1988.750	0.993	NA	15.033
## 1988.769	1.675	NA	22.340
## 1988.788	1.463	NA	19.297
## 1988.808	2.256	NA	23.761
## 1988.827	2.216	NA	22.150
## 1988.846	2.218	NA	22.236
## 1988.865	2.568	NA	23.157
## 1988.885	2.483	NA	24.387
## 1988.904	2.545	NA	23.844
## 1988.923	2.599	NA	23.681
## 1988.942	2.483	NA	24.456
## 1988.962	1.793	NA	19.899
## 1988.981	0.516	NA	13.662
## 1989.000	0.873	NA	15.698
## 1989.019	1.195	NA	18.189
## 1989.038	1.525	NA	19.448
## 1989.058	1.906	NA	20.891
## 1989.077	2.246	NA	22.284
## 1989.096	2.247	NA	23.247
## 1989.115	2.316	NA	24.440
## 1989.135	2.276	NA	22.519
## 1989.154	2.403	NA	22.818
## 1989.173	2.432	NA	23.472

## 1989.192	2.490	NA	24.117
## 1989.212	2.013	NA	24.435
## 1989.231	1.508	NA	20.589
## 1989.250	2.251	NA	23.427
## 1989.269	2.079	NA	20.923
## 1989.288	2.210	NA	22.959
## 1989.308	1.960	NA	19.152
## 1989.327	2.251	NA	22.011
## 1989.346	2.013	NA	20.228
## 1989.365	2.252	NA	21.332
## 1989.385	2.067	NA	20.500
## 1989.404	1.831	NA	19.090
## 1989.423	2.069	NA	21.692
## 1989.442	1.953	NA	20.157
## 1989.462	2.199	NA	22.231
## 1989.481	1.771	NA	20.914
## 1989.500	1.696	NA	21.454
## 1989.519	1.788	NA	21.345
## 1989.538	1.636	1.524	19.260
## 1989.558	1.741	2.212	18.781
## 1989.577	1.597	1.777	17.445
## 1989.596	1.943	2.552	19.628
## 1989.615	1.660	1.889	17.692
## 1989.635	0.616	0.851	7.046
## 1989.654	0.000	0.000	0.000
## 1989.673	0.000	0.000	0.000
## 1989.692	0.000	0.000	0.000
## 1989.712	0.000	0.000	0.000
## 1989.731	0.000	0.000	0.000
## 1989.750	0.000	0.000	0.000
## 1989.769	0.000	0.000	0.000
## 1989.788	0.053	0.618	11.569
## 1989.808	0.040	0.565	11.973
## 1989.827	0.354	0.414	11.123
## 1989.846	0.505	0.543	11.479
## 1989.865	0.711	0.712	16.969
## 1989.885	0.723	0.652	15.997
## 1989.904	0.796	0.709	16.555
## 1989.923	0.856	0.793	17.959
## 1989.942	0.845	0.838	18.868
## 1989.962	0.807	0.763	15.400
## 1989.981	0.276	0.266	10.544
## 1990.000	0.339	0.362	12.755
## 1990.019	0.581	0.665	19.020
## 1990.038	0.894	0.957	20.077
## 1990.058	0.936	1.145	22.124

## 1990.077	1.111	1.312	19.920
## 1990.096	1.446	1.689	17.215
## 1990.115	1.517	1.762	17.662
## 1990.135	1.513	2.160	19.828
## 1990.154	1.508	1.877	18.754
## 1990.173	1.636	2.048	20.390
## 1990.192	1.380	1.824	18.383
## 1990.212	1.453	1.986	19.377
## 1990.231	1.459	2.032	20.133
## 1990.250	1.538	1.956	19.210
## 1990.269	1.327	1.503	20.736
## 1990.288	1.027	1.256	18.821
## 1990.308	1.365	1.752	20.952
## 1990.327	1.475	1.878	20.565
## 1990.346	1.365	1.945	20.311
## 1990.365	1.351	1.735	17.859
## 1990.385	1.231	1.825	19.385
## 1990.404	1.447	1.715	17.962
## 1990.423	1.408	1.594	19.569
## 1990.442	1.089	1.377	17.894
## 1990.462	1.357	1.686	18.114
## 1990.481	1.287	1.560	19.170
## 1990.500	1.087	1.692	18.713
## 1990.519	1.017	1.597	20.520
## 1990.538	1.090	1.729	20.345
## 1990.558	1.343	1.733	20.015
## 1990.577	1.164	1.813	18.027
## 1990.596	1.169	1.725	19.697
## 1990.615	1.465	1.909	19.897
## 1990.635	1.242	1.765	19.213
## 1990.654	1.220	1.781	19.773
## 1990.673	1.231	1.717	20.128
## 1990.692	1.266	1.884	21.181
## 1990.712	1.337	1.881	21.933
## 1990.731	1.079	1.433	20.049
## 1990.750	1.223	1.534	23.358
## 1990.769	1.351	1.926	21.120
## 1990.788	1.269	1.870	21.970
## 1990.808	1.382	1.942	21.411
## 1990.827	1.435	2.222	22.569
## 1990.846	1.371	1.909	20.849
## 1990.865	1.341	2.089	20.658
## 1990.885	1.399	2.026	21.192
## 1990.904	1.440	2.009	21.502
## 1990.923	1.236	2.034	22.152
## 1990.942	1.441	2.085	21.904

## 1990.962	0.988	1.330	20.634
## 1990.981	0.300	0.318	15.535
## 1991.000	0.401	0.522	16.690
## 1991.019	0.529	0.824	19.150
## 1991.038	0.786	1.113	21.128
## 1991.058	1.086	1.285	21.136
## 1991.077	0.725	1.107	19.693
## 1991.096	1.127	1.591	21.576
## 1991.115	1.146	1.726	21.449
## 1991.135	1.086	1.758	22.298
## 1991.154	1.134	1.883	21.056
## 1991.173	1.020	2.089	19.014
## 1991.192	1.022	2.198	19.511
## 1991.212	1.224	2.449	20.162
## 1991.231	0.895	1.739	21.158
## 1991.250	0.658	1.480	19.059
## 1991.269	0.977	2.152	21.972
## 1991.288	0.916	2.258	22.877
## 1991.308	0.830	1.776	22.190
## 1991.327	0.990	2.355	22.533
## 1991.346	0.770	2.140	20.682
## 1991.365	0.801	1.988	21.788
## 1991.385	0.839	2.083	21.299
## 1991.404	0.835	2.115	20.663
## 1991.423	0.802	1.884	21.948
## 1991.442	0.763	1.797	21.009
## 1991.462	0.770	1.944	20.443
## 1991.481	0.838	2.001	21.418
## 1991.500	0.742	1.668	23.273
## 1991.519	0.793	1.527	25.763
## 1991.538	0.900	1.477	26.045
## 1991.558	0.960	1.949	23.831
## 1991.577	0.800	1.914	22.742
## 1991.596	0.807	1.632	22.962
## 1991.615	0.841	1.796	25.253
## 1991.635	0.880	1.696	25.239
## 1991.654	0.818	1.718	27.387
## 1991.673	0.817	1.442	26.824
## 1991.692	0.819	1.713	27.294
## 1991.712	0.998	1.796	28.935
## 1991.731	1.220	1.860	31.642
## 1991.750	0.966	1.554	32.468
## 1991.769	0.895	1.623	27.673
## 1991.788	0.978	1.641	28.890
## 1991.808	0.913	1.818	26.465
## 1991.827	0.947	1.969	28.296

## 1991.846	1.002	1.886	29.274
## 1991.865	1.081	2.030	30.686
## 1991.885	0.977	1.883	29.786
## 1991.904	1.027	1.871	31.155
## 1991.923	0.895	1.910	28.459
## 1991.942	0.900	1.921	27.195
## 1991.962	0.762	1.672	26.274
## 1991.981	0.329	0.386	25.204
## 1992.000	0.351	0.446	24.434
## 1992.019	0.419	0.819	27.323
## 1992.038	0.618	1.238	27.303
## 1992.058	0.845	1.761	30.334
## 1992.077	0.727	1.650	26.833
## 1992.096	1.200	2.031	25.811
## 1992.115	1.801	2.064	27.238
## 1992.135	1.727	2.418	28.788
## 1992.154	1.992	2.171	27.263
## 1992.173	1.865	2.362	27.217
## 1992.192	1.801	2.328	26.410
## 1992.212	1.661	2.336	26.118
## 1992.231	2.366	10.301	18.642
## 1992.250	2.003	9.964	16.518
## 1992.269	2.092	10.433	17.276
## 1992.288	1.703	8.281	21.662
## 1992.308	1.337	6.128	20.473
## 1992.327	1.985	9.709	18.336
## 1992.346	1.808	8.828	17.018
## 1992.365	1.839	8.078	18.111
## 1992.385	1.714	7.527	18.410
## 1992.404	1.730	7.486	20.541
## 1992.423	1.725	6.711	21.408
## 1992.442	1.456	5.930	21.545
## 1992.462	1.447	5.462	21.732
## 1992.481	1.357	3.710	26.173
## 1992.500	1.280	2.894	27.432
## 1992.519	1.363	3.008	28.362
## 1992.538	1.228	2.829	29.827
## 1992.558	1.411	3.252	29.870
## 1992.577	1.130	3.021	26.534
## 1992.596	1.153	2.667	26.434
## 1992.615	1.257	2.740	26.137
## 1992.635	1.259	2.807	27.365
## 1992.654	1.153	2.961	27.910
## 1992.673	1.202	2.570	26.311
## 1992.692	1.185	2.671	27.538
## 1992.712	1.247	2.809	29.445

```
## 1992.731      1.434      2.712      28.326
## 1992.750      1.450      2.606      30.203
## 1992.769      1.227      2.500      27.838
## 1992.788      1.245      2.898      27.760
## 1992.808      1.417      3.152      27.322
## 1992.827      1.458      3.053      28.837
## 1992.846      1.398      2.745      26.548
## 1992.865      1.423      3.156      27.279
## 1992.885      1.358      3.069      27.306
## 1992.904      1.488      3.379      28.299
```

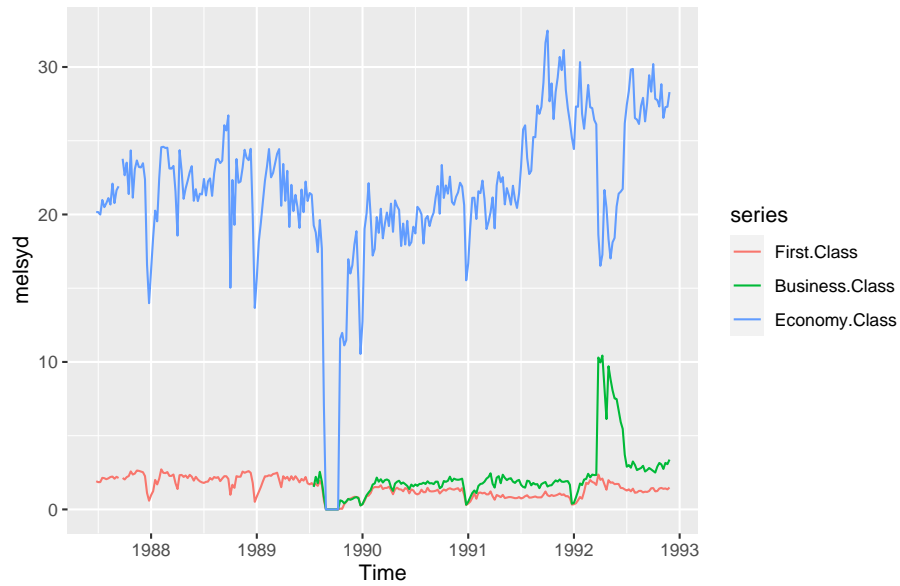
```
head(melsyd)
```

```
## Time Series:
## Start = c(1987, 26)
## End = c(1987, 31)
## Frequency = 52
##           First.Class Business.Class Economy.Class
## 1987.481      1.912             NA      20.167
## 1987.500      1.848             NA      20.161
## 1987.519      1.856             NA      19.993
## 1987.538      2.142             NA      20.986
## 1987.558      2.118             NA      20.497
## 1987.577      2.048             NA      20.770
```

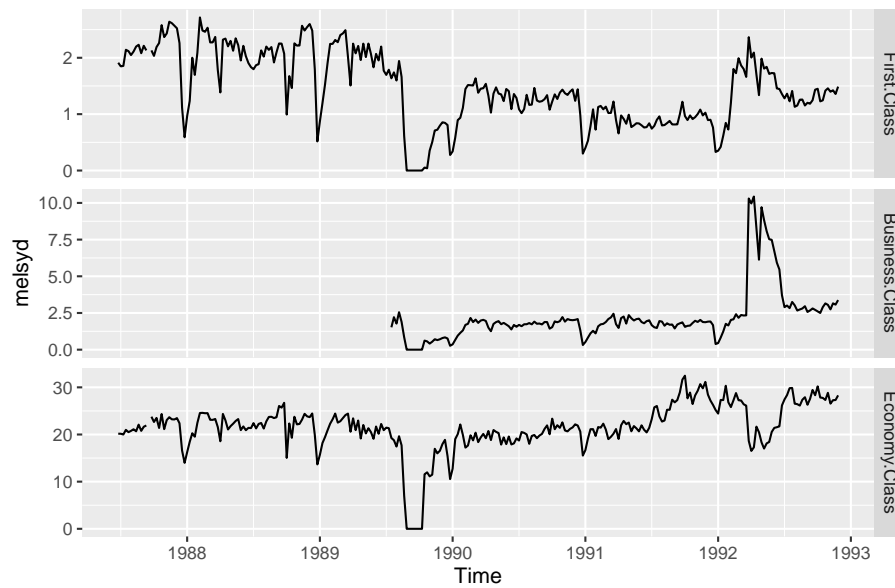
```
tail(melsyd)
```

```
## Time Series:
## Start = c(1992, 43)
## End = c(1992, 48)
## Frequency = 52
##           First.Class Business.Class Economy.Class
## 1992.808      1.417             3.152      27.322
## 1992.827      1.458             3.053      28.837
## 1992.846      1.398             2.745      26.548
## 1992.865      1.423             3.156      27.279
## 1992.885      1.358             3.069      27.306
## 1992.904      1.488             3.379      28.299
```

```
autoplot(melsyd)
```



```
autoplot(melsyd, facets = TRUE)
```



```
# Back to slides

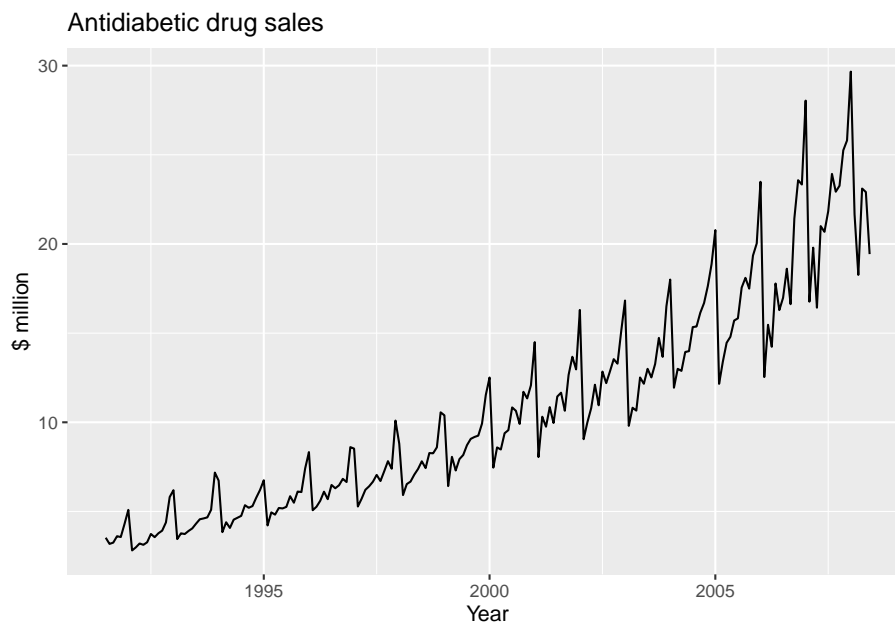
# Time plot
autoplot(melsyd[, "Economy.Class"])
```



```
# Adding main title and
# also add labels to the x and y axes

autoplot(a10) + ylab("$ million") + xlab("Year") +
  ggtitle("Antidiabetic drug sales")
```



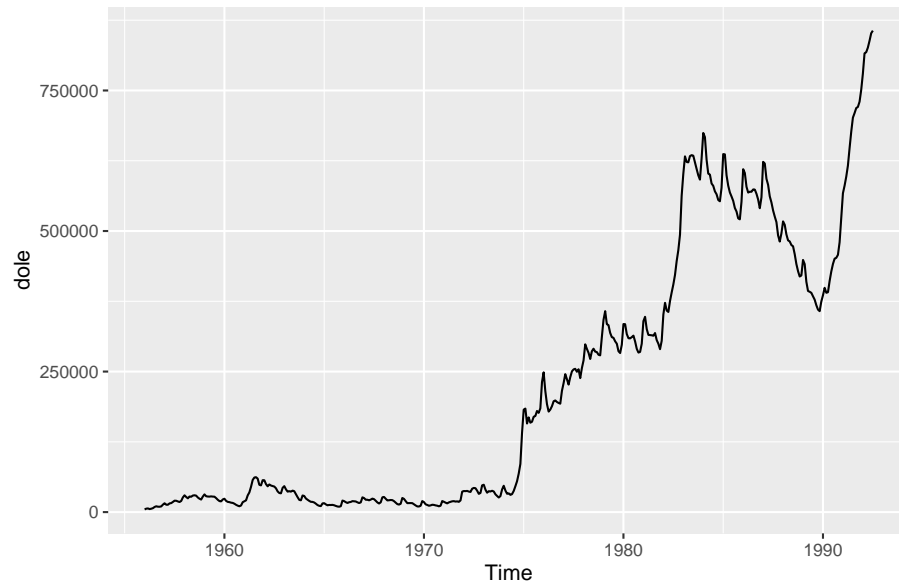


```
?autoplot
```

```
## Help on topic 'autoplot' was found in the following packages:
##
##   Package          Library
##   forecast         /Library/Frameworks/R.framework/Versions/4.0/Resources/library
##   ggplot2           /Library/Frameworks/R.framework/Versions/4.0/Resources/library
##
##
## Using the first match ...
```

```
# Your turn
```

```
?dole
autoplot(dole)
```



```
?lynx
```

```
## Help on topic 'lynx' was found in the following packages:
```

```
##
```

```
##   Package           Library
```

```
##   fma                /Library/Frameworks/R.framework/Versions/4.0/Resources/libr
```

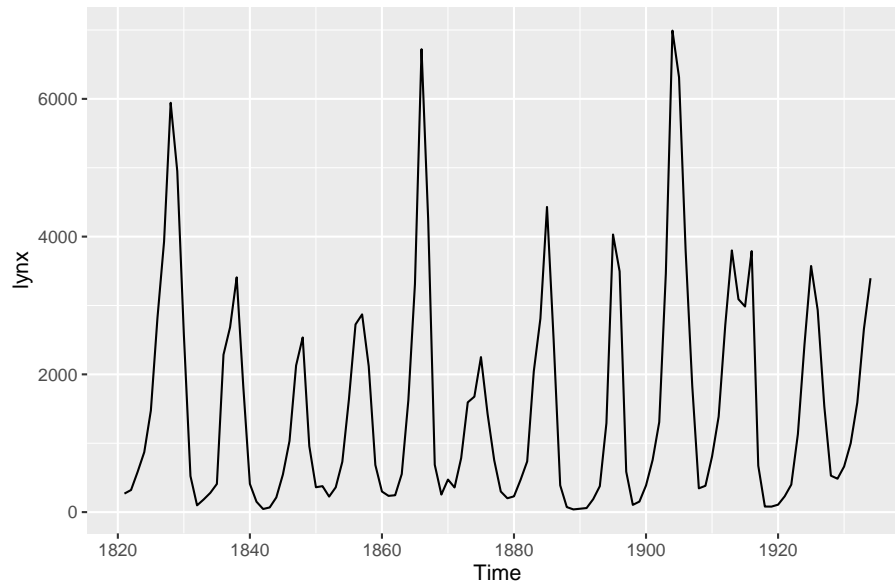
```
##   datasets          /Library/Frameworks/R.framework/Versions/4.0/Resources/libr
```

```
##
```

```
##
```

```
## Using the first match ...
```

```
autoplot(lynx)
```



```
?goog
```

```
autoplot(goog)+  
  xlab("Year") + ylab("Price ($)") +  
  ggtitle("Google closing stock price")
```



```
# Back to slides
```

```
# The elecdaily data
```

```
?elecdaily
```

```
head(elecdaily,15)
```

```
## Time Series:
```

```
## Start = c(1, 4)
```

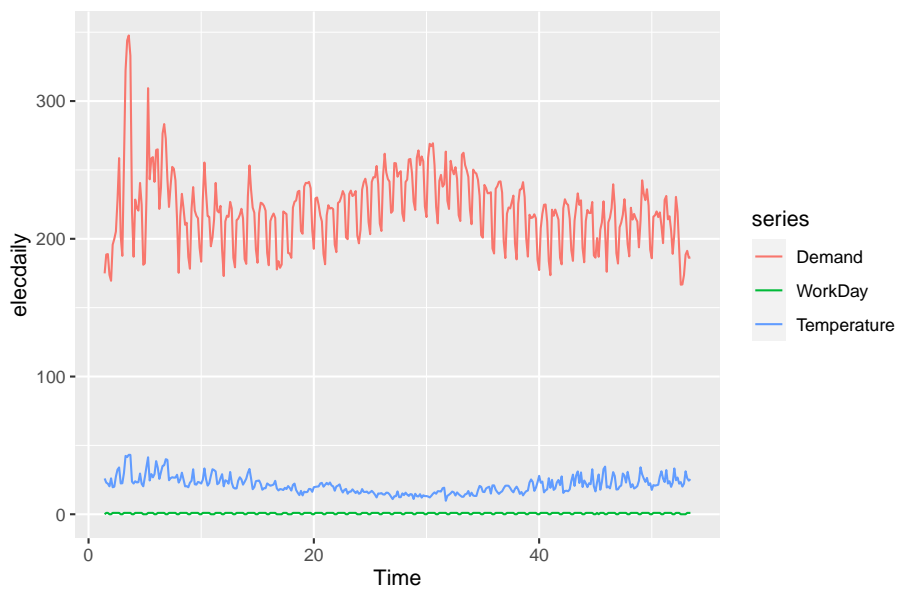
```
## End = c(3, 4)
```

```
## Frequency = 7
```

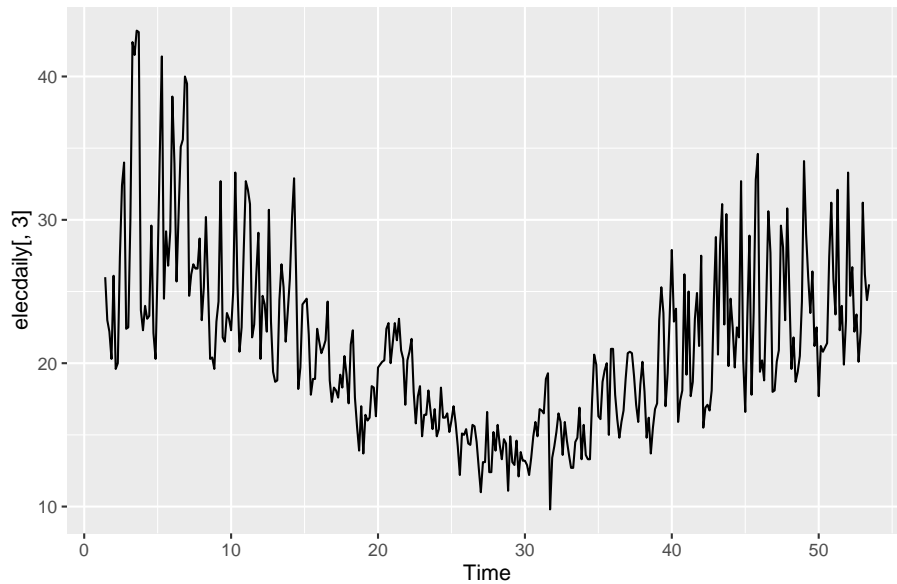
```
##           Demand WorkDay Temperature
## 1.428571 174.8963         0         26.0
## 1.571429 188.5909         1         23.0
## 1.714286 188.9169         1         22.2
## 1.857143 173.8142         0         20.3
## 2.000000 169.5152         0         26.1
## 2.142857 195.7288         1         19.6
## 2.285714 199.9029         1         20.0
## 2.428571 205.3375         1         27.4
## 2.571429 228.0782         1         32.4
## 2.714286 258.5984         1         34.0
## 2.857143 201.7970         0         22.4
## 3.000000 187.6298         0         22.5
## 3.142857 254.6636         1         30.0
```

```
## 3.285714 322.2323      1      42.4  
## 3.428571 343.9934      1      41.5
```

```
autoplot(elecdaily)
```



```
autoplot(elecdaily[,3])
```



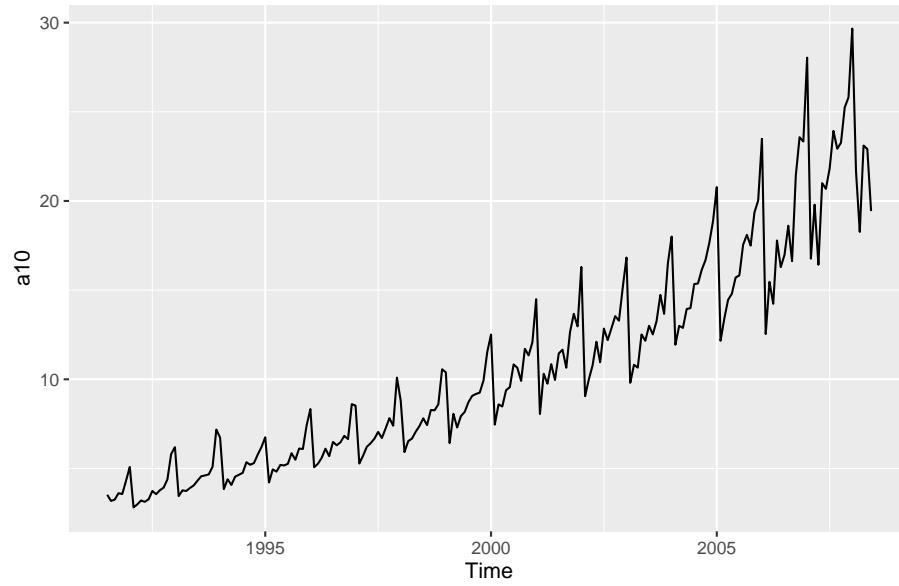
```
time(elecdaily)
```

```
## Time Series:
## Start = c(1, 4)
## End = c(53, 4)
## Frequency = 7
## [1] 1.428571 1.571429 1.714286 1.857143 2.000000 2.142857 2.285714
## [8] 2.428571 2.571429 2.714286 2.857143 3.000000 3.142857 3.285714
## [15] 3.428571 3.571429 3.714286 3.857143 4.000000 4.142857 4.285714
## [22] 4.428571 4.571429 4.714286 4.857143 5.000000 5.142857 5.285714
## [29] 5.428571 5.571429 5.714286 5.857143 6.000000 6.142857 6.285714
## [36] 6.428571 6.571429 6.714286 6.857143 7.000000 7.142857 7.285714
## [43] 7.428571 7.571429 7.714286 7.857143 8.000000 8.142857 8.285714
## [50] 8.428571 8.571429 8.714286 8.857143 9.000000 9.142857 9.285714
## [57] 9.428571 9.571429 9.714286 9.857143 10.000000 10.142857 10.285714
## [64] 10.428571 10.571429 10.714286 10.857143 11.000000 11.142857 11.285714
## [71] 11.428571 11.571429 11.714286 11.857143 12.000000 12.142857 12.285714
## [78] 12.428571 12.571429 12.714286 12.857143 13.000000 13.142857 13.285714
## [85] 13.428571 13.571429 13.714286 13.857143 14.000000 14.142857 14.285714
## [92] 14.428571 14.571429 14.714286 14.857143 15.000000 15.142857 15.285714
## [99] 15.428571 15.571429 15.714286 15.857143 16.000000 16.142857 16.285714
## [106] 16.428571 16.571429 16.714286 16.857143 17.000000 17.142857 17.285714
## [113] 17.428571 17.571429 17.714286 17.857143 18.000000 18.142857 18.285714
## [120] 18.428571 18.571429 18.714286 18.857143 19.000000 19.142857 19.285714
```

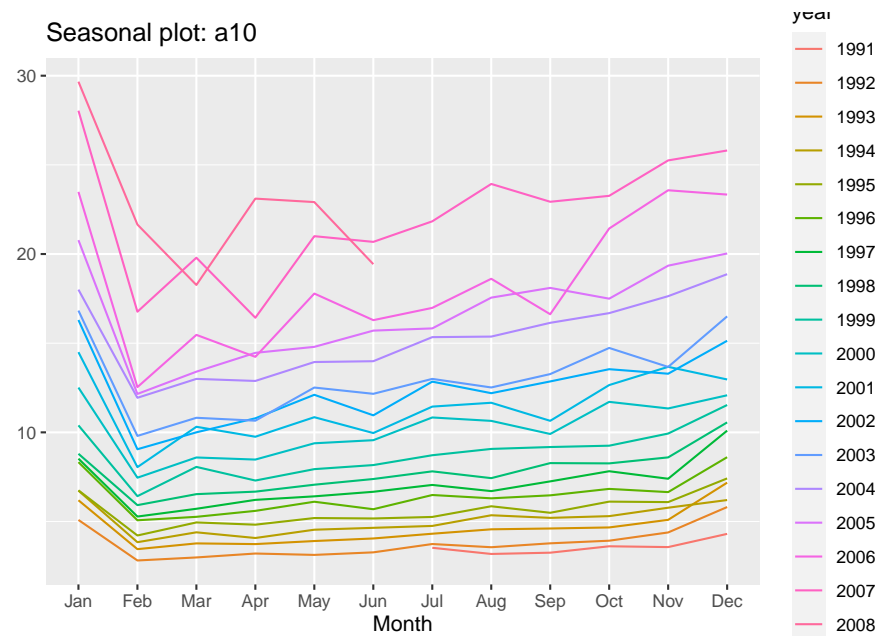
```
## [127] 19.428571 19.571429 19.714286 19.857143 20.000000 20.142857 20.285714
## [134] 20.428571 20.571429 20.714286 20.857143 21.000000 21.142857 21.285714
## [141] 21.428571 21.571429 21.714286 21.857143 22.000000 22.142857 22.285714
## [148] 22.428571 22.571429 22.714286 22.857143 23.000000 23.142857 23.285714
## [155] 23.428571 23.571429 23.714286 23.857143 24.000000 24.142857 24.285714
## [162] 24.428571 24.571429 24.714286 24.857143 25.000000 25.142857 25.285714
## [169] 25.428571 25.571429 25.714286 25.857143 26.000000 26.142857 26.285714
## [176] 26.428571 26.571429 26.714286 26.857143 27.000000 27.142857 27.285714
## [183] 27.428571 27.571429 27.714286 27.857143 28.000000 28.142857 28.285714
## [190] 28.428571 28.571429 28.714286 28.857143 29.000000 29.142857 29.285714
## [197] 29.428571 29.571429 29.714286 29.857143 30.000000 30.142857 30.285714
## [204] 30.428571 30.571429 30.714286 30.857143 31.000000 31.142857 31.285714
## [211] 31.428571 31.571429 31.714286 31.857143 32.000000 32.142857 32.285714
## [218] 32.428571 32.571429 32.714286 32.857143 33.000000 33.142857 33.285714
## [225] 33.428571 33.571429 33.714286 33.857143 34.000000 34.142857 34.285714
## [232] 34.428571 34.571429 34.714286 34.857143 35.000000 35.142857 35.285714
## [239] 35.428571 35.571429 35.714286 35.857143 36.000000 36.142857 36.285714
## [246] 36.428571 36.571429 36.714286 36.857143 37.000000 37.142857 37.285714
## [253] 37.428571 37.571429 37.714286 37.857143 38.000000 38.142857 38.285714
## [260] 38.428571 38.571429 38.714286 38.857143 39.000000 39.142857 39.285714
## [267] 39.428571 39.571429 39.714286 39.857143 40.000000 40.142857 40.285714
## [274] 40.428571 40.571429 40.714286 40.857143 41.000000 41.142857 41.285714
## [281] 41.428571 41.571429 41.714286 41.857143 42.000000 42.142857 42.285714
## [288] 42.428571 42.571429 42.714286 42.857143 43.000000 43.142857 43.285714
## [295] 43.428571 43.571429 43.714286 43.857143 44.000000 44.142857 44.285714
## [302] 44.428571 44.571429 44.714286 44.857143 45.000000 45.142857 45.285714
## [309] 45.428571 45.571429 45.714286 45.857143 46.000000 46.142857 46.285714
## [316] 46.428571 46.571429 46.714286 46.857143 47.000000 47.142857 47.285714
## [323] 47.428571 47.571429 47.714286 47.857143 48.000000 48.142857 48.285714
## [330] 48.428571 48.571429 48.714286 48.857143 49.000000 49.142857 49.285714
## [337] 49.428571 49.571429 49.714286 49.857143 50.000000 50.142857 50.285714
## [344] 50.428571 50.571429 50.714286 50.857143 51.000000 51.142857 51.285714
## [351] 51.428571 51.571429 51.714286 51.857143 52.000000 52.142857 52.285714
## [358] 52.428571 52.571429 52.714286 52.857143 53.000000 53.142857 53.285714
## [365] 53.428571
```

```
# Seasonal plots
```

```
autoplot(a10)
```

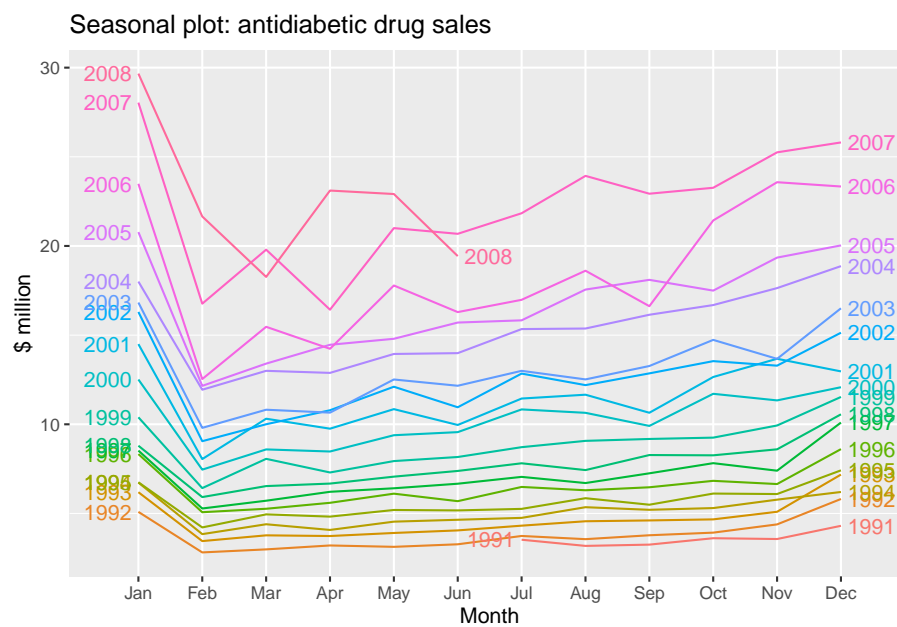


```
ggseasonplot(a10)
```

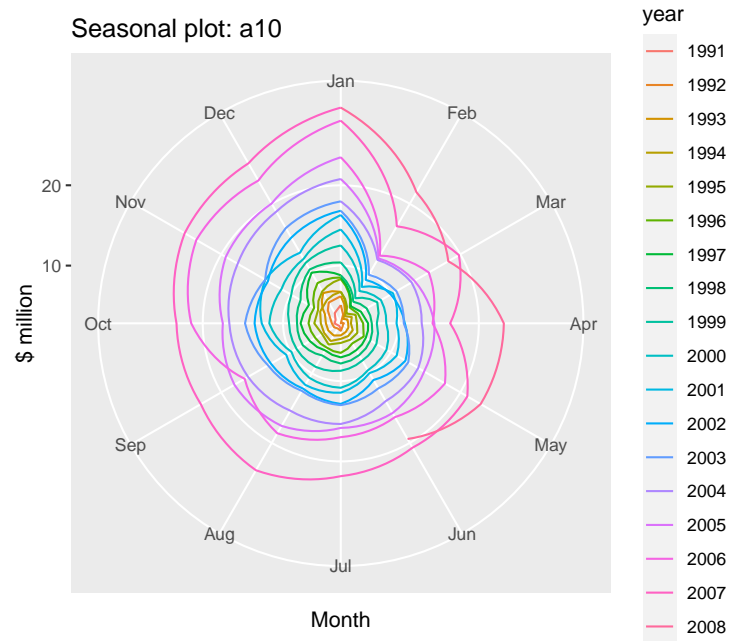




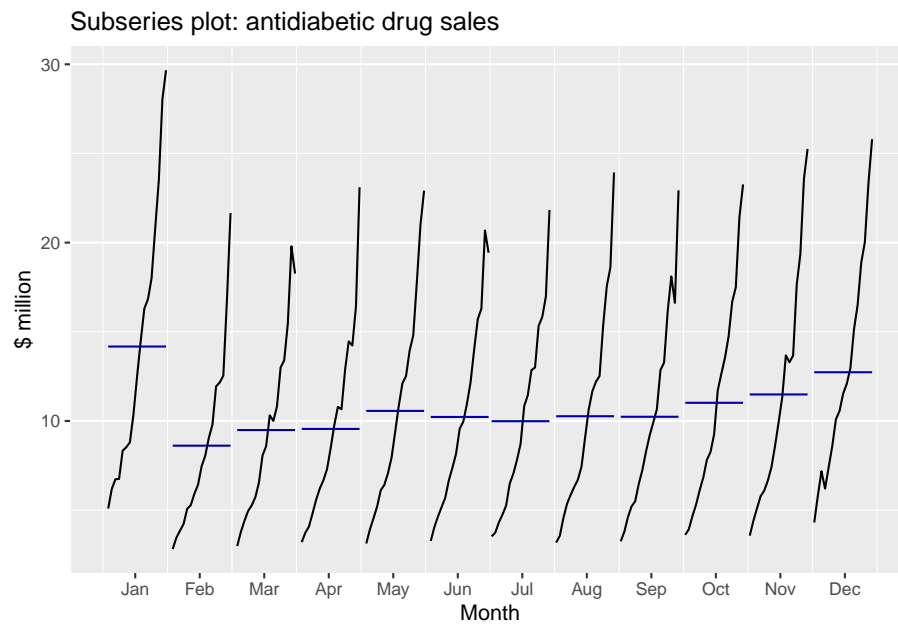
```
ggseasonplot(a10, year.labels=TRUE, year.labels.left=TRUE) +
  ylab("$ million") +
  ggtitle("Seasonal plot: antidiabetic drug sales")
```



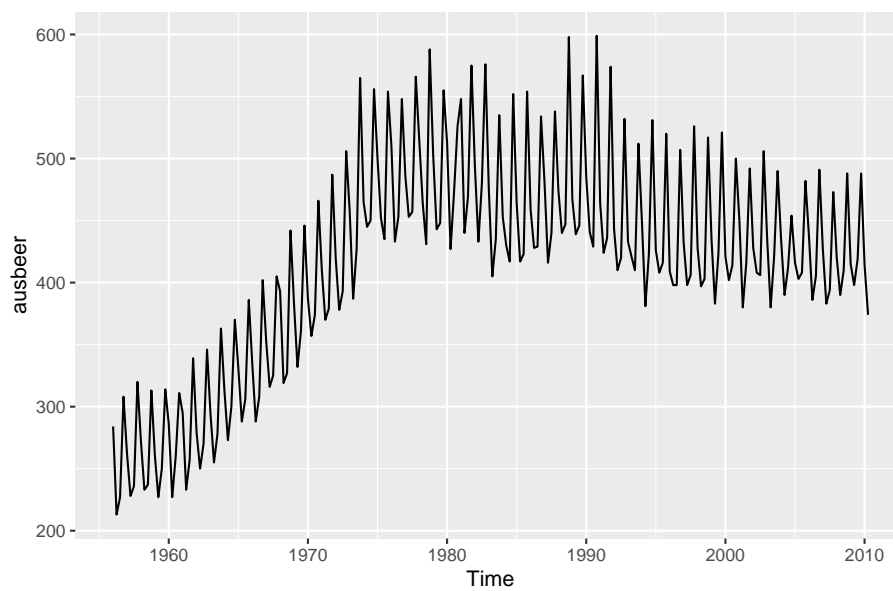
```
ggseasonplot(a10, polar=TRUE) + ylab("$ million")
```



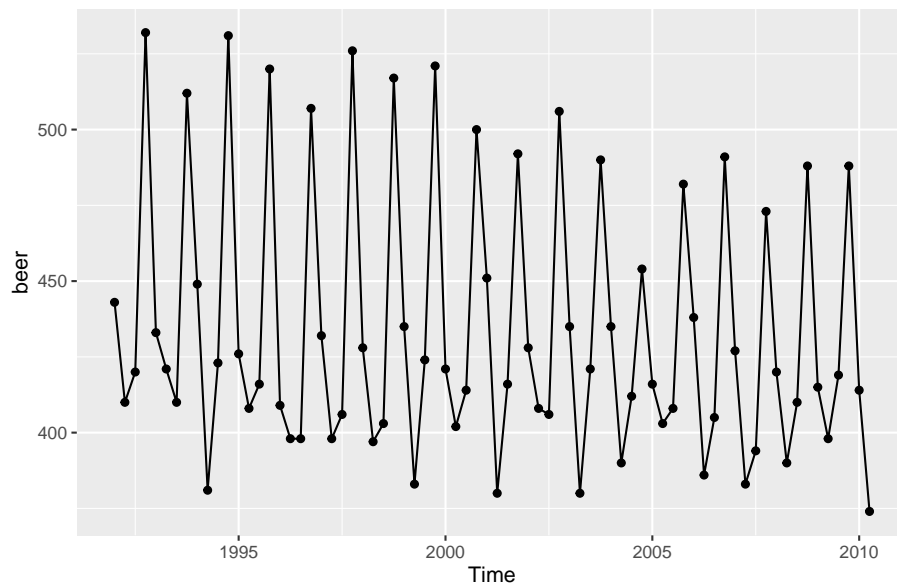
```
# Seasonal subseries plots
ggsubseriesplot(a10) + ylab("$ million") +
  ggtitle("Subseries plot: antidiabetic drug sales")
```



```
# Australian quarterly beer production 1956:Q1 to 2008:Q3.  
autoplot(ausbeer)
```

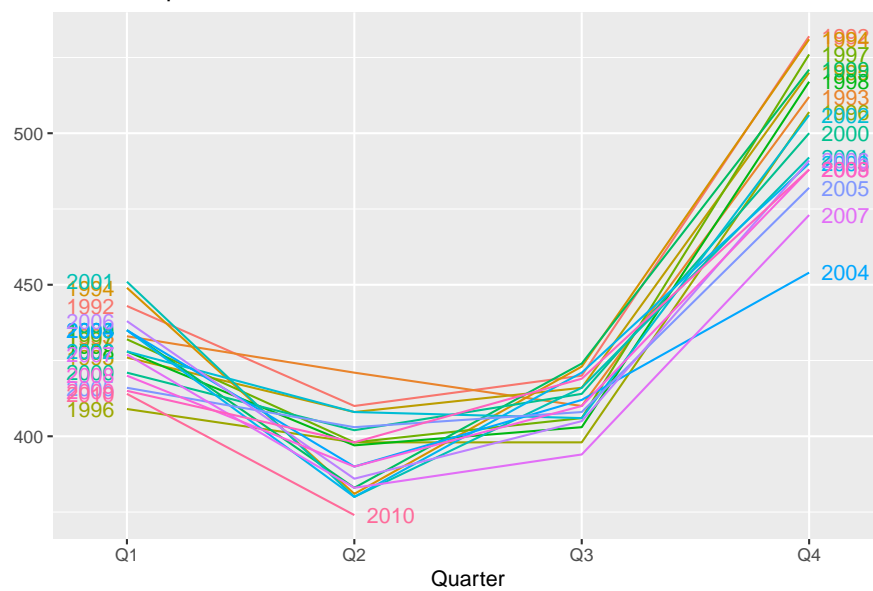


```
# Take a window of it starting in 1992  
beer=window(ausbeer,start=1992)  
  
autoplot(beer)+geom_point()
```

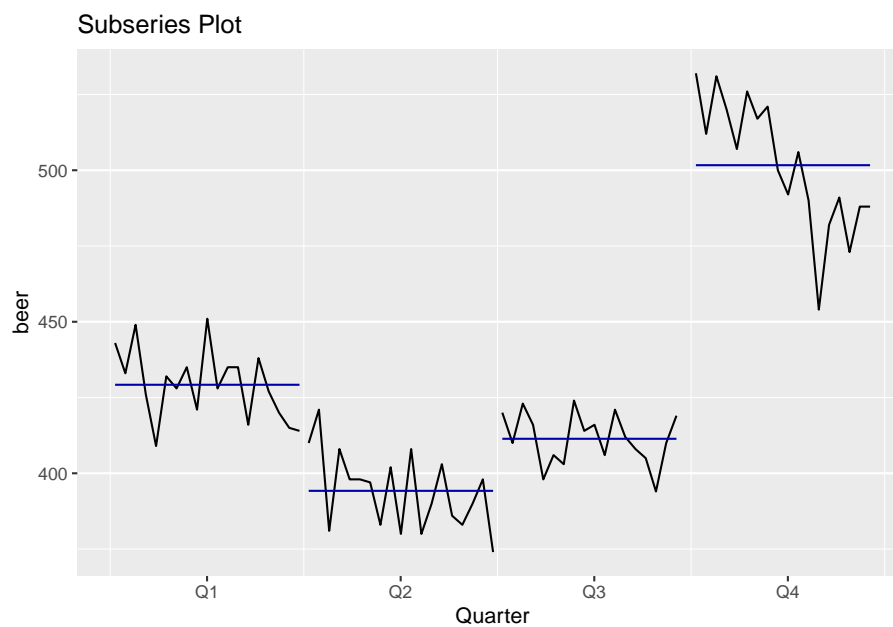


```
ggseasonplot(beer, year.labels=TRUE,
             year.labels.left=TRUE)
```

Seasonal plot: beer



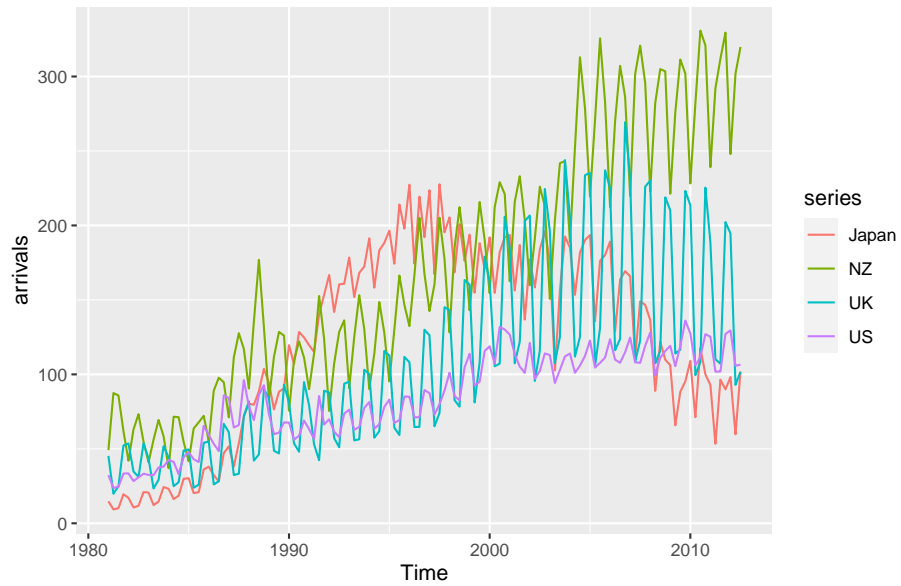
```
ggsubseriesplot(beer)+ggtitle("Subseries Plot")
```



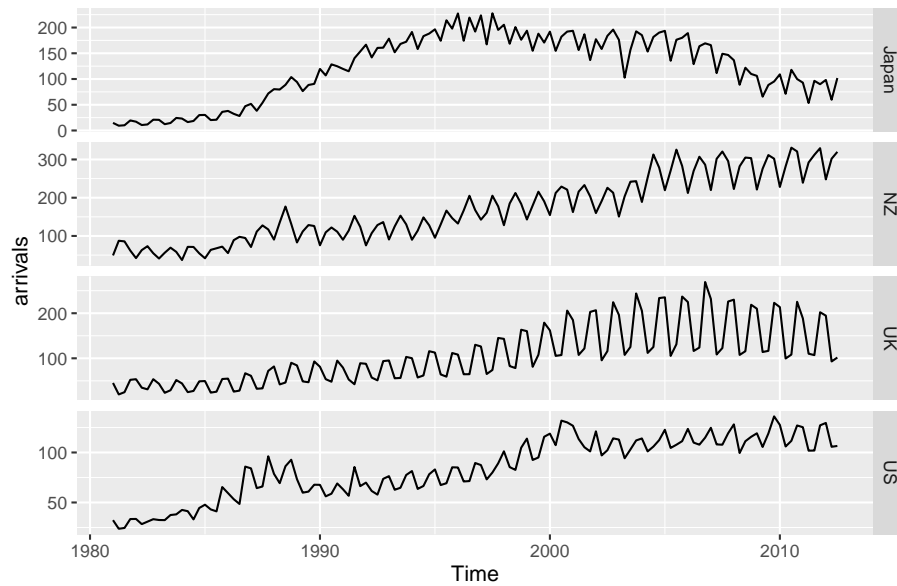
```
# Students to run arrivals code below
# Your turn 1
?arrivals
head(arrivals)
```

```
##           Japan      NZ      UK      US
## 1981 Q1 14.763 49.140 45.266 32.316
## 1981 Q2  9.321 87.467 19.886 23.721
## 1981 Q3 10.166 85.841 24.839 24.533
## 1981 Q4 19.509 61.882 52.264 33.438
## 1982 Q1 17.117 42.045 53.636 33.527
## 1982 Q2 10.617 63.081 34.802 28.366
```

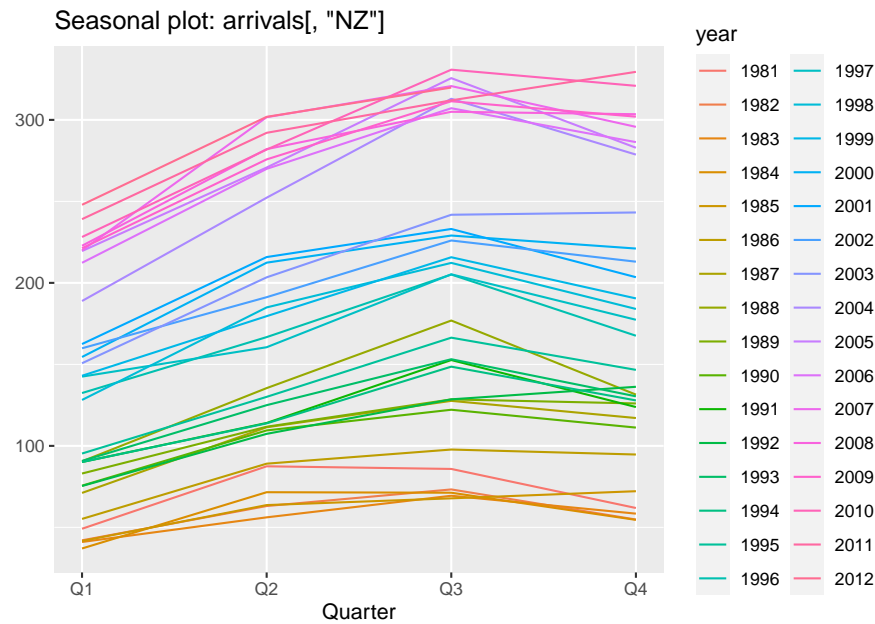
```
autoplot(arrivals)
```



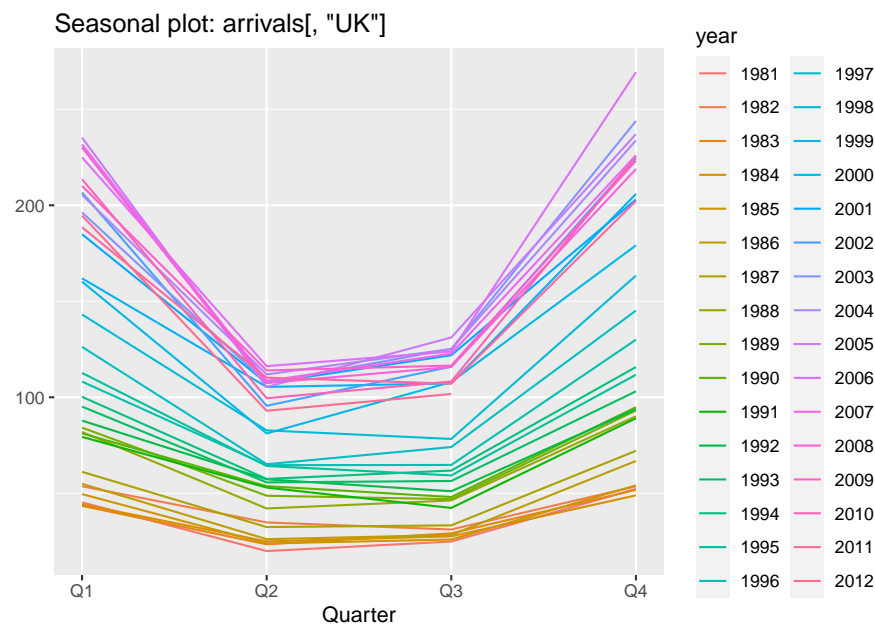
```
autoplot(arrivals, facets = TRUE)
```



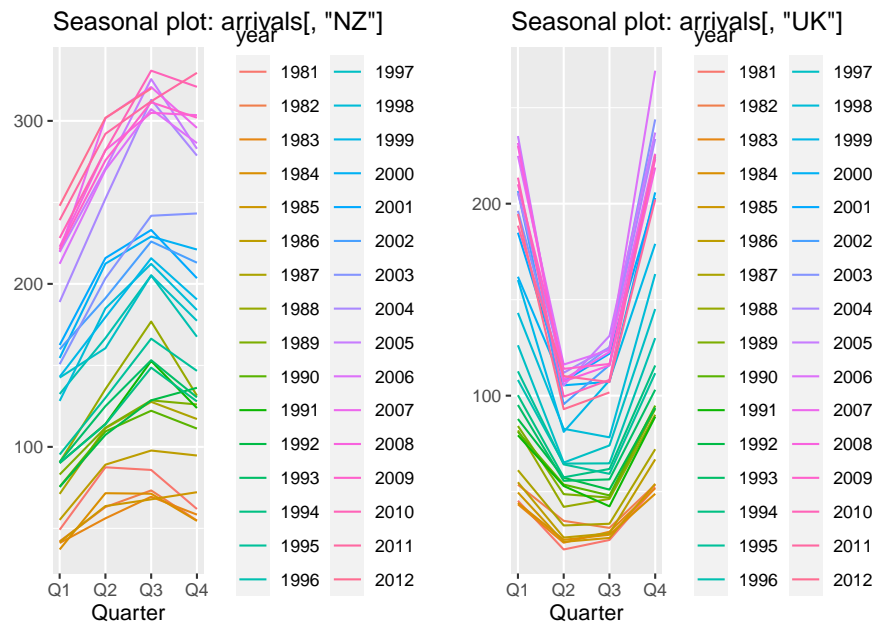
```
ggseasonplot(arrivals[, "NZ"])
```



```
ggseasonplot(arrivals[, "UK"])
```



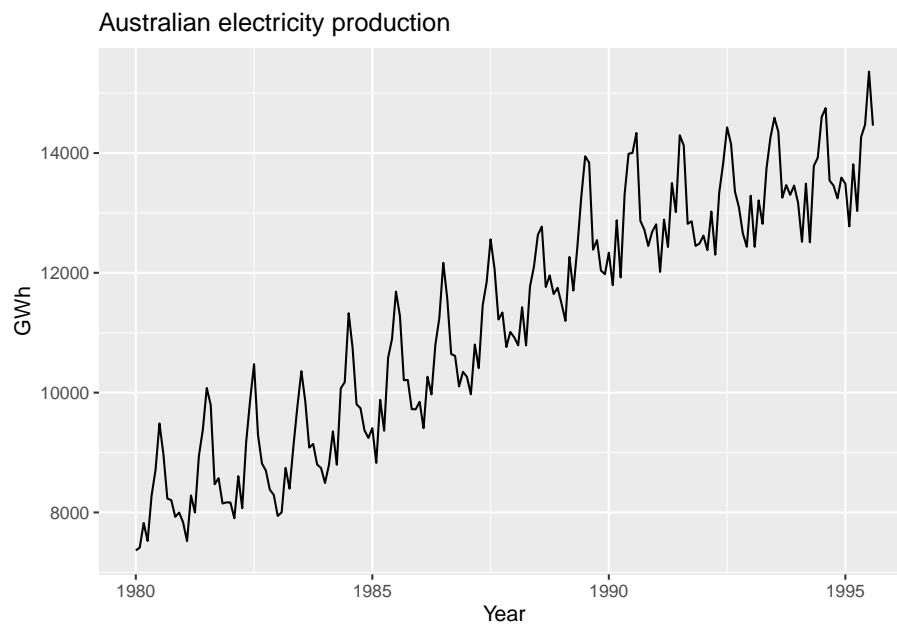
```
# Plot these together to have a closer look
p1 <- ggseasonplot(arrivals[, "NZ"])
p2 <- ggseasonplot(arrivals[, "UK"])
gridExtra::grid.arrange(p1, p2, nrow=1)
```



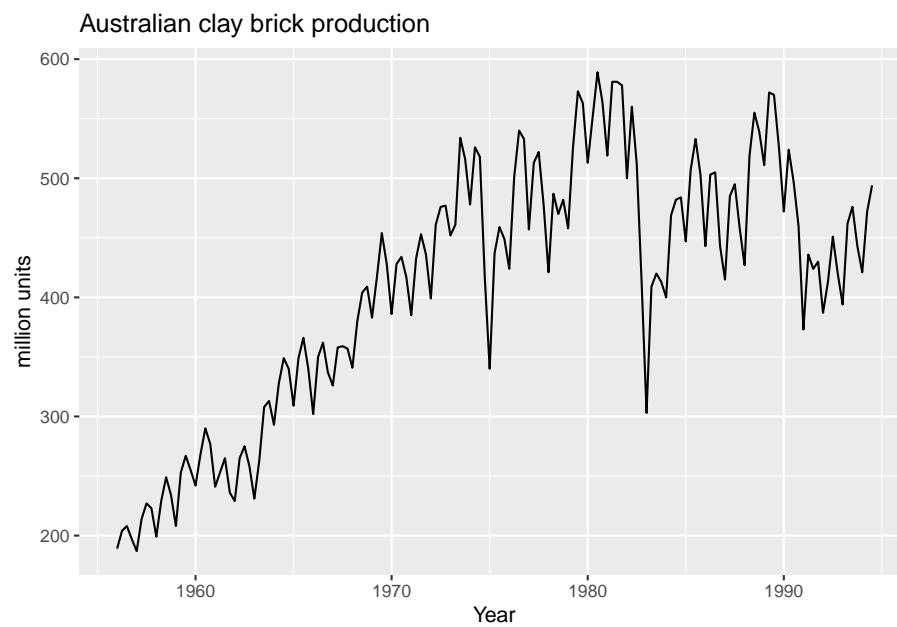
```
#Back to lecture slides
```

```
# Time series patterns
autoplot(window(elec, start=1980)) +
  ggtitle("Australian electricity production") +
  xlab("Year") + ylab("GWh")
```

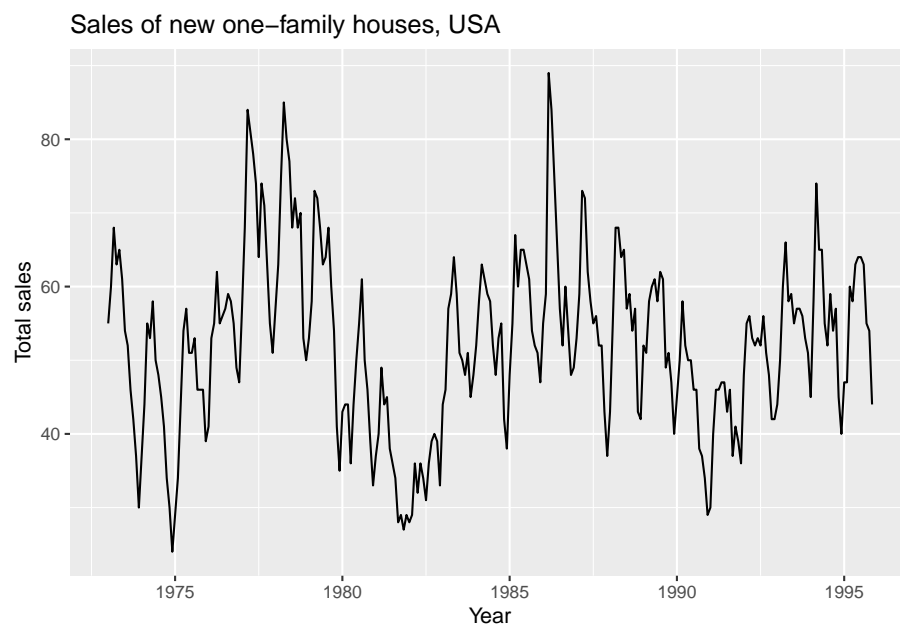




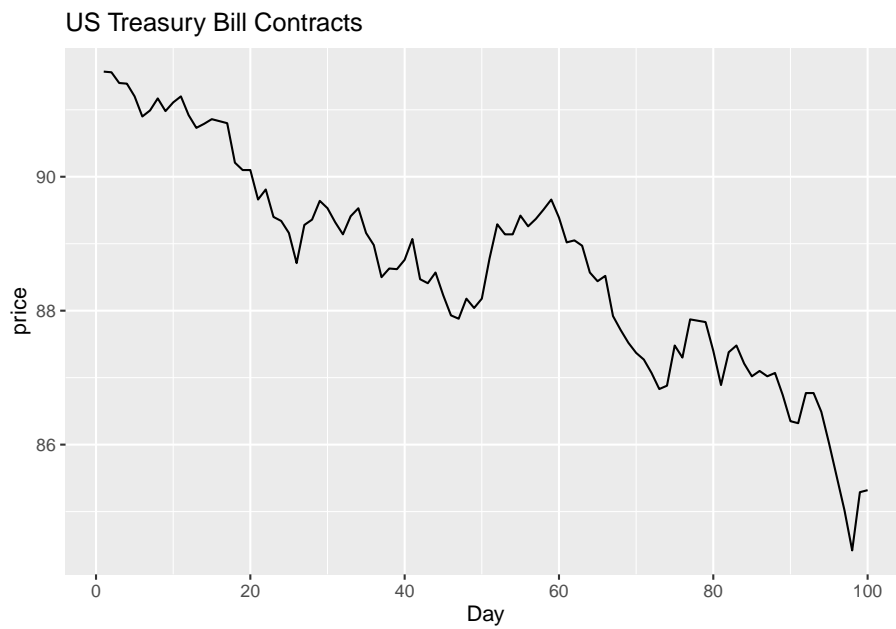
```
autoplot(bricksq) +  
  ggtitle("Australian clay brick production") +  
  xlab("Year") + ylab("million units")
```



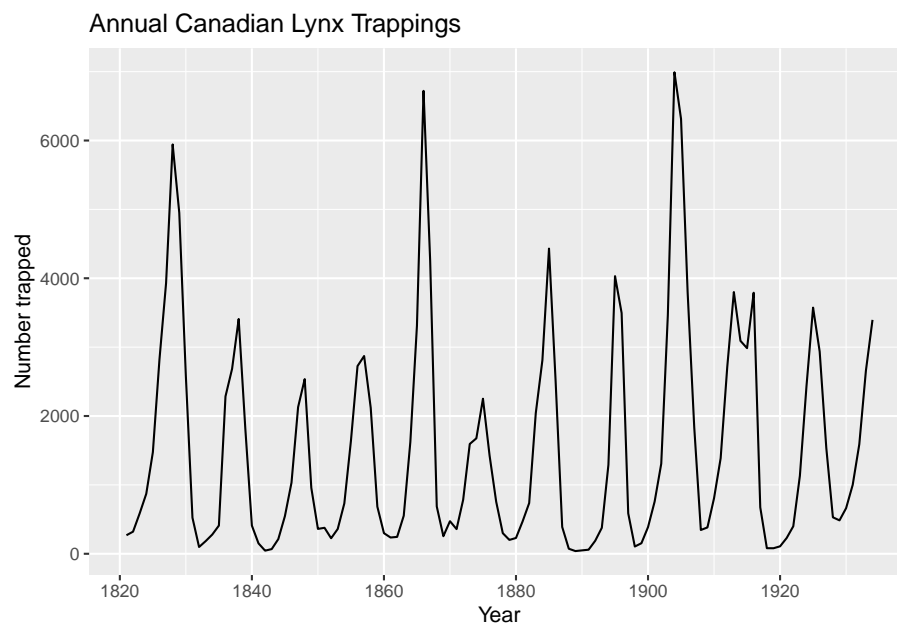
```
autoplot(hsales) +  
  ggtitle("Sales of new one-family houses, USA") +  
  xlab("Year") + ylab("Total sales")
```



```
autoplot(ustreas) +  
  ggtitle("US Treasury Bill Contracts") +  
  xlab("Day") + ylab("price")
```



```
autoplot(lynx) +  
  ggtitle("Annual Canadian Lynx Trappings") +  
  xlab("Year") + ylab("Number trapped")
```

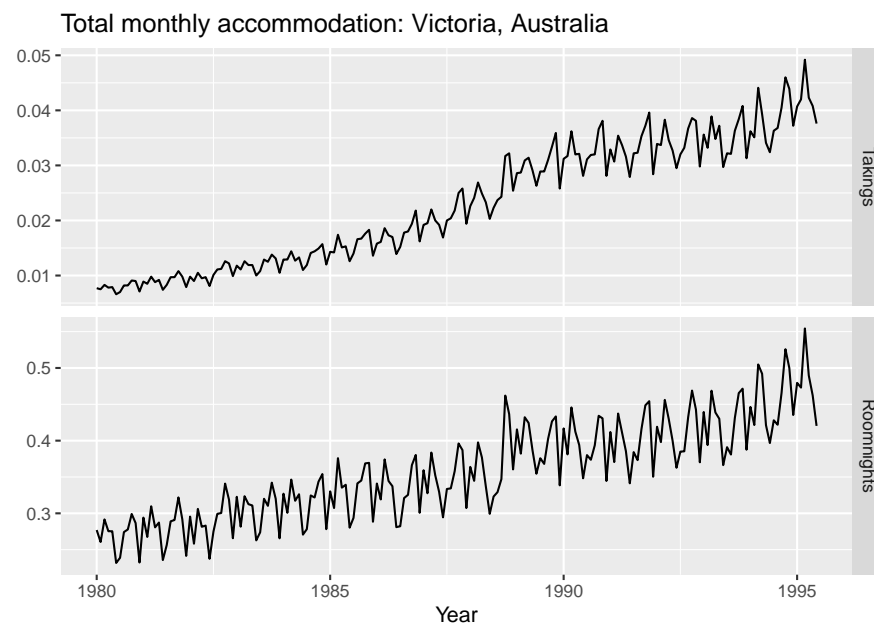


```
#Back to lecture slides
```

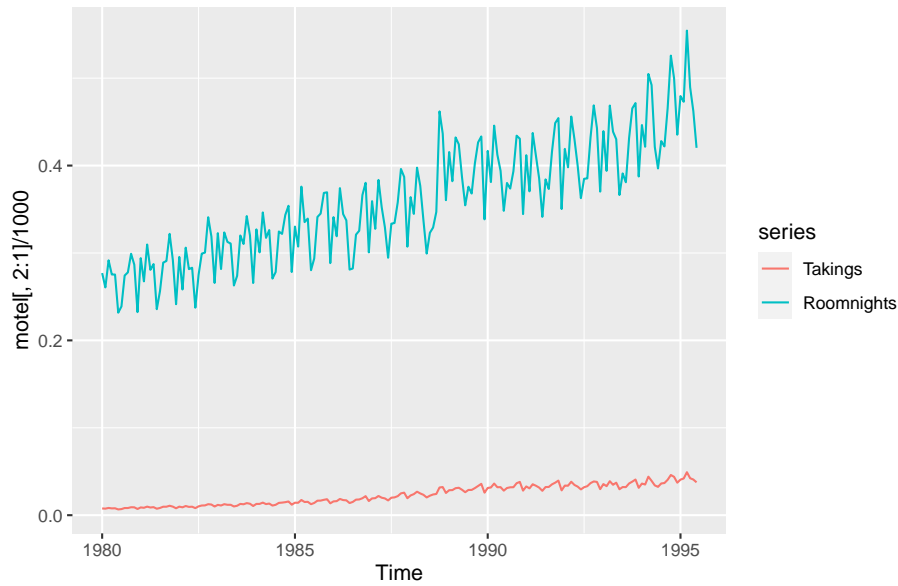
```
# Scatterplots  
head(motel)
```

```
##           Roomnights Takings  
## Jan 1980      277.0      7.7  
## Feb 1980      260.6      7.5  
## Mar 1980      291.6      8.3  
## Apr 1980      275.4      7.8  
## May 1980      275.3      7.9  
## Jun 1980      231.7      6.6
```

```
autoplot(motel[,2:1]/1000, facet=TRUE) +  
  xlab("Year") + ylab("") +  
  ggtitle("Total monthly accommodation: Victoria, Australia")
```

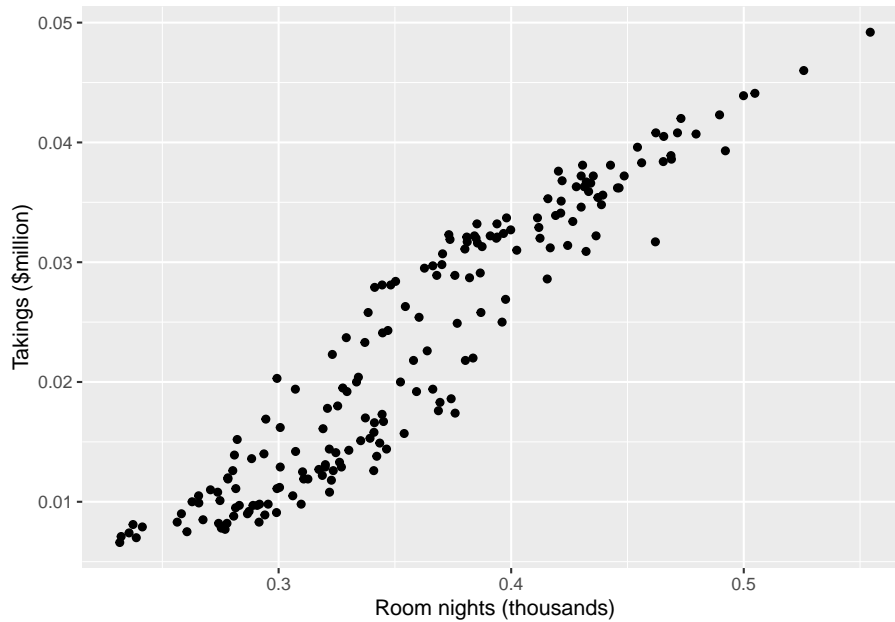


```
# See what happens without the facet=TRUE argument  
autoplot(motel[,2:1]/1000)
```



*# doesn't make much sense because of the differences in scale*

```
qplot(Roomnights/1000, Takings/1000, data=as.data.frame(motel)) +  
  ylab("Takings ($million)") + xlab("Room nights (thousands)")
```



```
head(motel)
```

```
##           Roomnights Takings
## Jan 1980      277.0      7.7
## Feb 1980      260.6      7.5
## Mar 1980      291.6      8.3
## Apr 1980      275.4      7.8
## May 1980      275.3      7.9
## Jun 1980      231.7      6.6
```

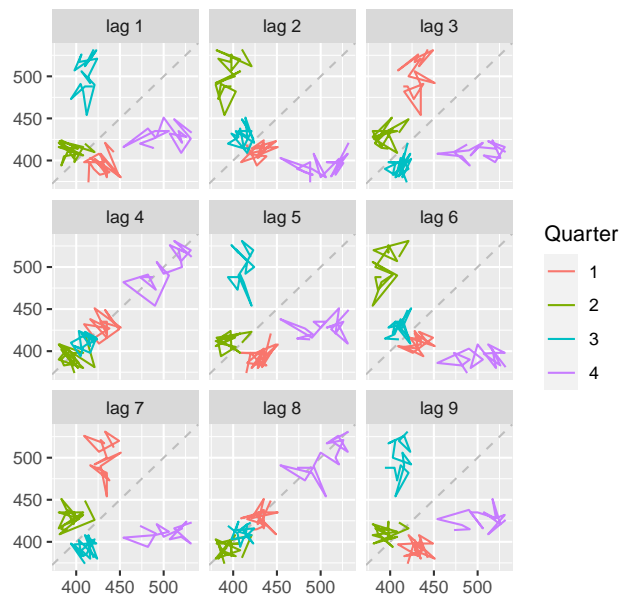
```
head(as.data.frame(motel))
```

```
##   Roomnights Takings
## 1      277.0      7.7
## 2      260.6      7.5
## 3      291.6      8.3
## 4      275.4      7.8
## 5      275.3      7.9
## 6      231.7      6.6
```

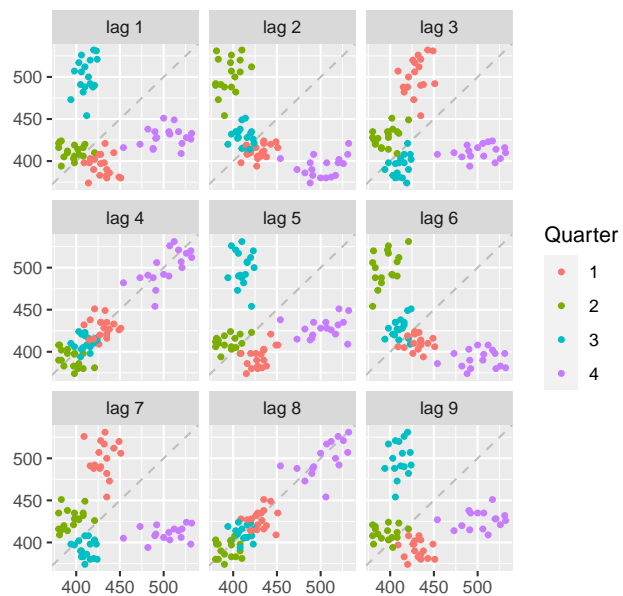
```
#Back to slides
```

```
# Lag plots and autocorrelation
```

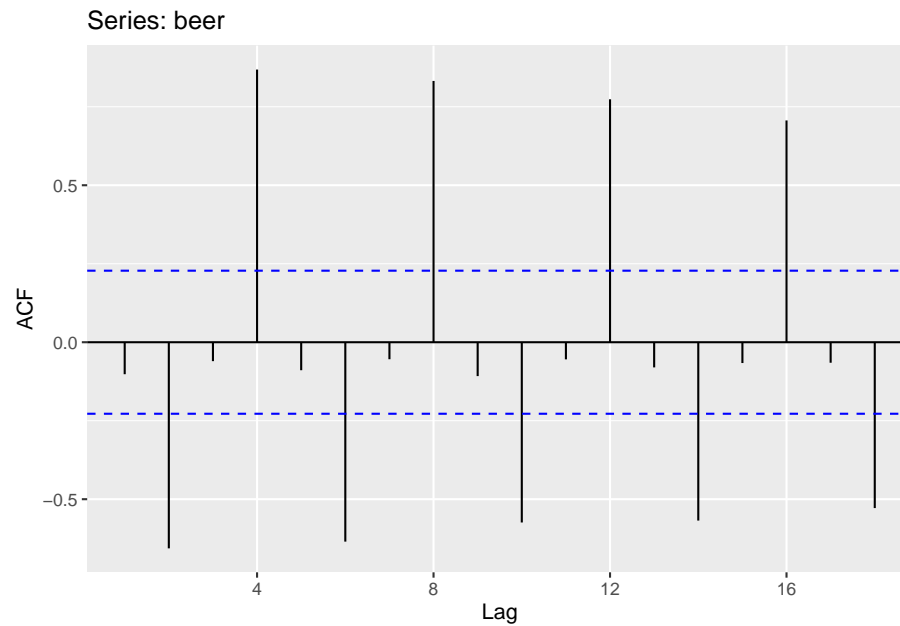
```
beer <- window(ausbeer, start=1992)
gglagplot(beer, lags=9)
```



```
# What does the 'do.lines=FALSE' do?
gglagplot(beer, lags=9, do.lines=FALSE)
```



```
# ACF
ggAcf(beer) #from forecast package
```



```
r<-ggAcf(beer)
attributes(r)
```

```
## $names
## [1] "data"      "layers"    "scales"    "mapping"    "theme"
## [6] "coordinates" "facet"     "plot_env"  "labels"
##
## $class
## [1] "gg"      "ggplot"
```

```
r$data
```

```
##      Var2 Var3      Freq lag
## 2      A    A -0.1019094  1
## 3      A    A -0.65661956  2
## 4      A    A -0.06027634  3
## 5      A    A  0.86852930  4
## 6      A    A -0.08915021  5
## 7      A    A -0.63513179  6
## 8      A    A -0.05416215  7
```



```
## 9      A      A  0.83224495  8
## 10     A      A -0.10787557  9
## 11     A      A -0.57419959 10
## 12     A      A -0.05460320 11
## 13     A      A  0.77379390 12
## 14     A      A -0.08019609 13
## 15     A      A -0.56805745 14
## 16     A      A -0.06626388 15
## 17     A      A  0.70642954 16
## 18     A      A -0.06535949 17
## 19     A      A -0.52825861 18
```

```
r$data$Freq
```

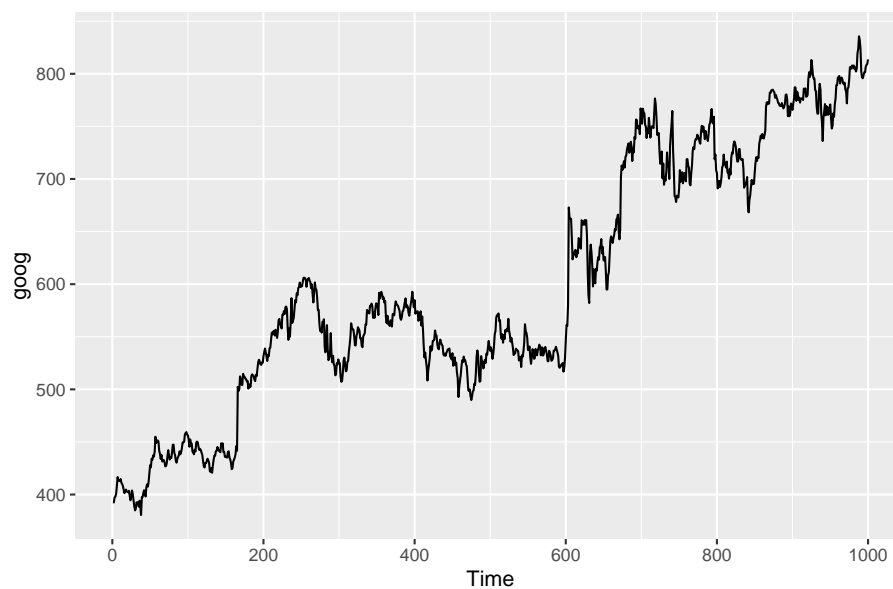
```
## [1] -0.10190904 -0.65661956 -0.06027634  0.86852930 -0.08915021 -0.63513179
## [7] -0.05416215  0.83224495 -0.10787557 -0.57419959 -0.05460320  0.77379390
## [13] -0.08019609 -0.56805745 -0.06626388  0.70642954 -0.06535949 -0.52825861
```

```
r$data$Freq[4]
```

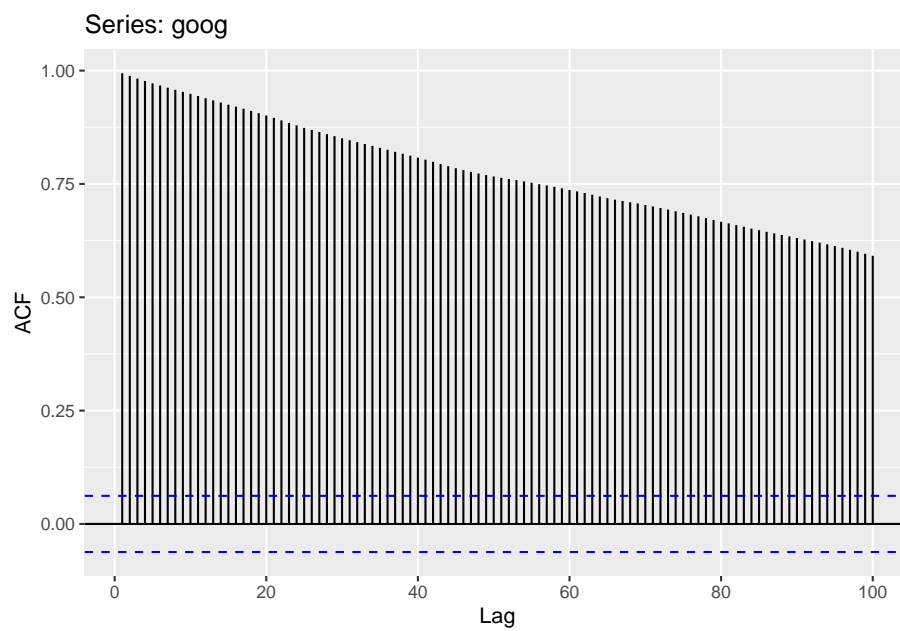
```
## [1] 0.8685293
```

```
# Back to slides
```

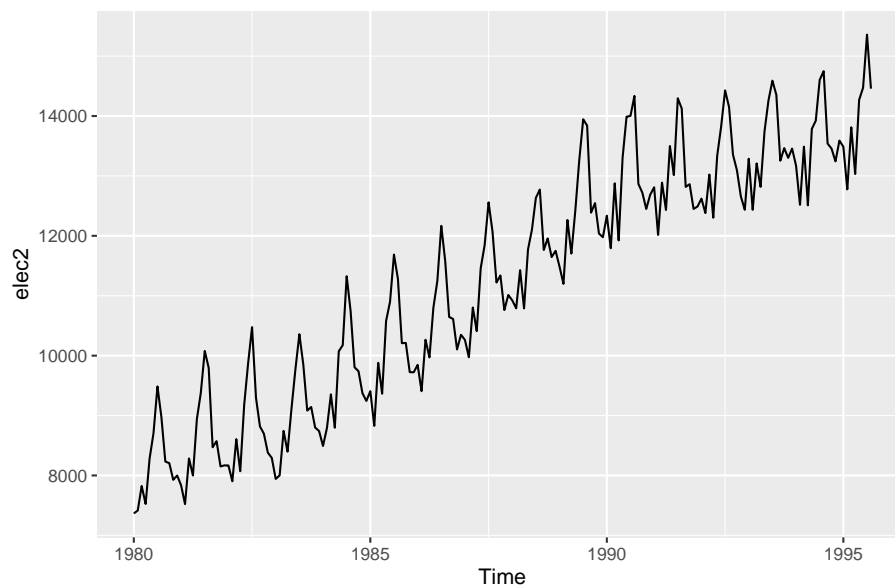
```
autoplot(goog)
```



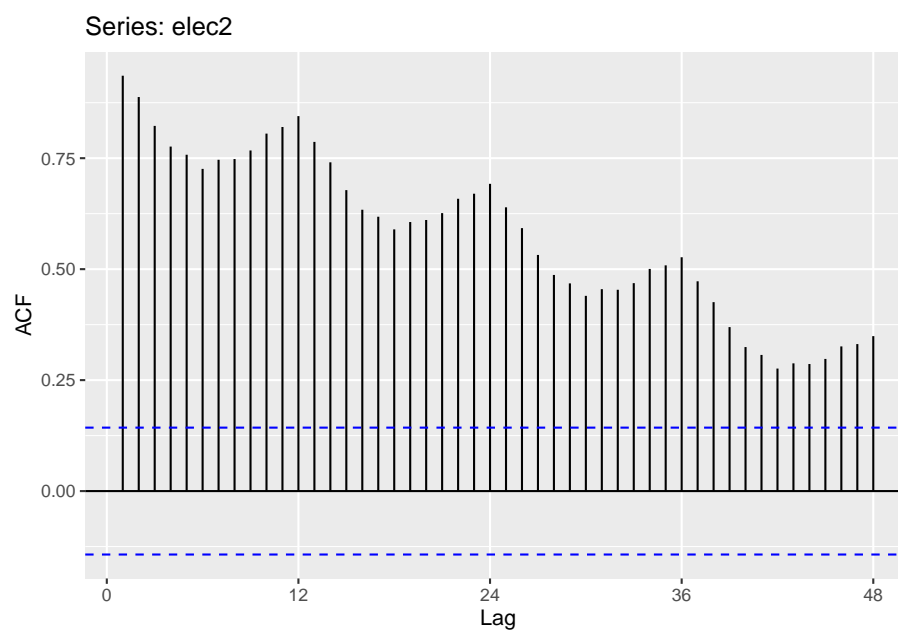
```
ggAcf(goog, lag.max=100)
```



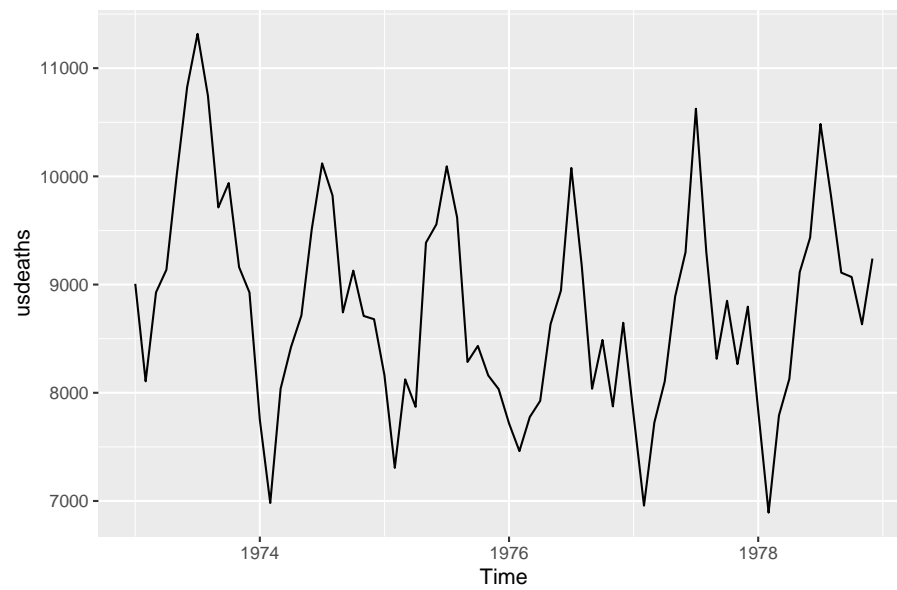
```
elec2 <- window(elec, start=1980)  
autoplot(elec2)
```



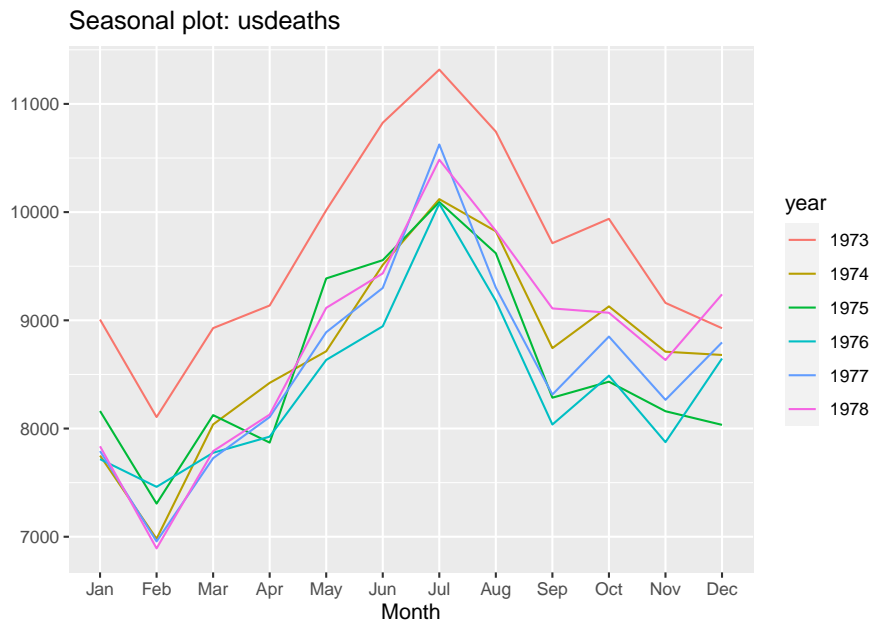
```
ggAcf(elec2, lag.max=48)
```



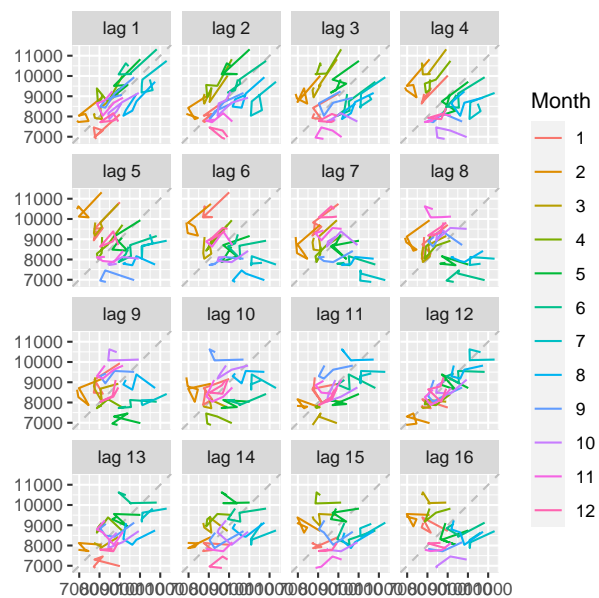
```
# Students to run  
?usdeaths  
autoplot(usdeaths)
```



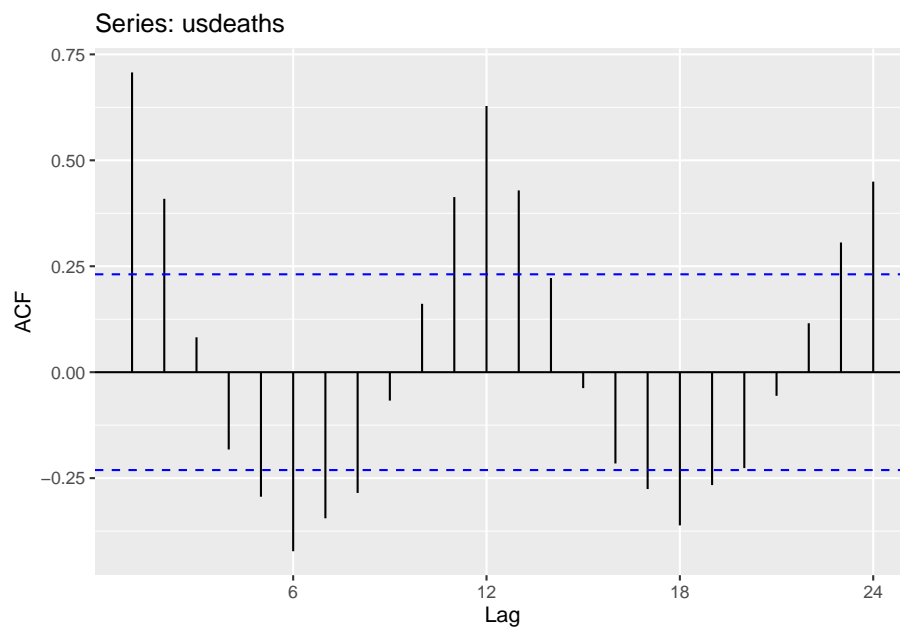
```
ggseasonplot(usdeaths)
```



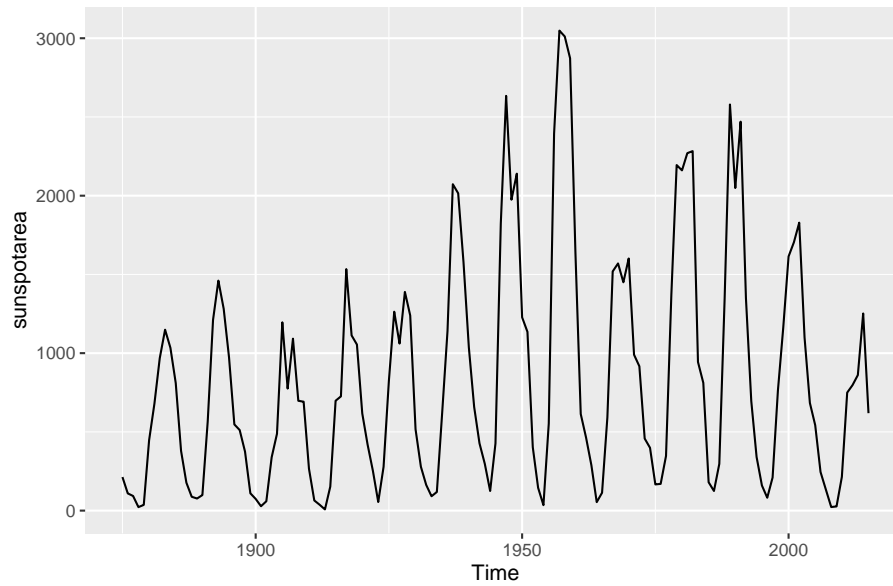
```
gglagplot(usdeaths)
```



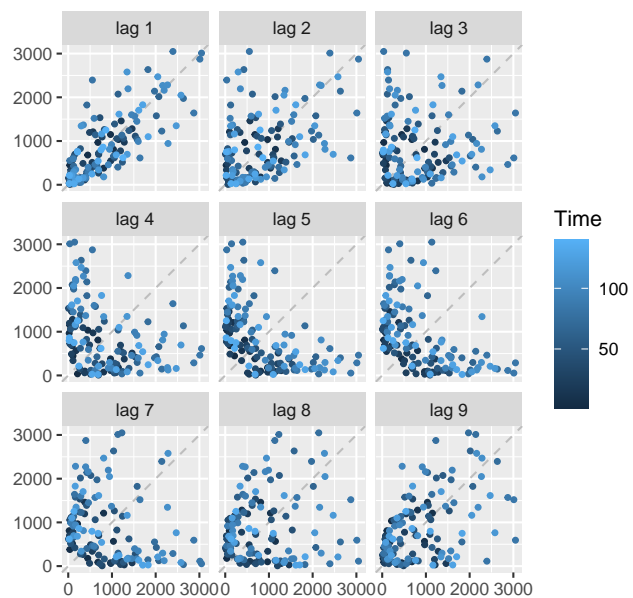
```
ggAcf(usdeaths)
```



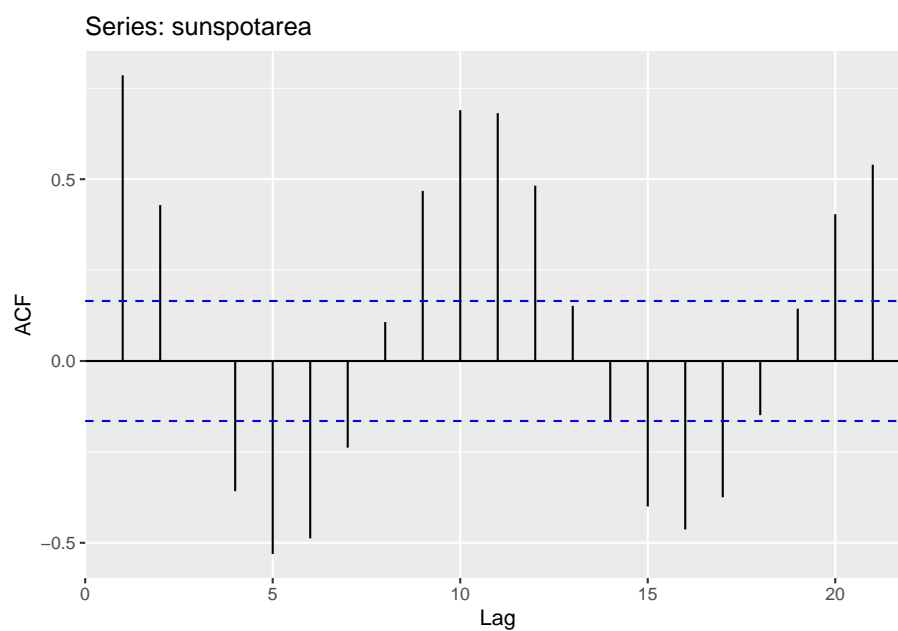
```
?sunspotarea  
autoplot(sunspotarea)
```



```
gglagplot(sunspotarea, do.lines=FALSE)
```



```
ggAcf(sunspotarea)
```



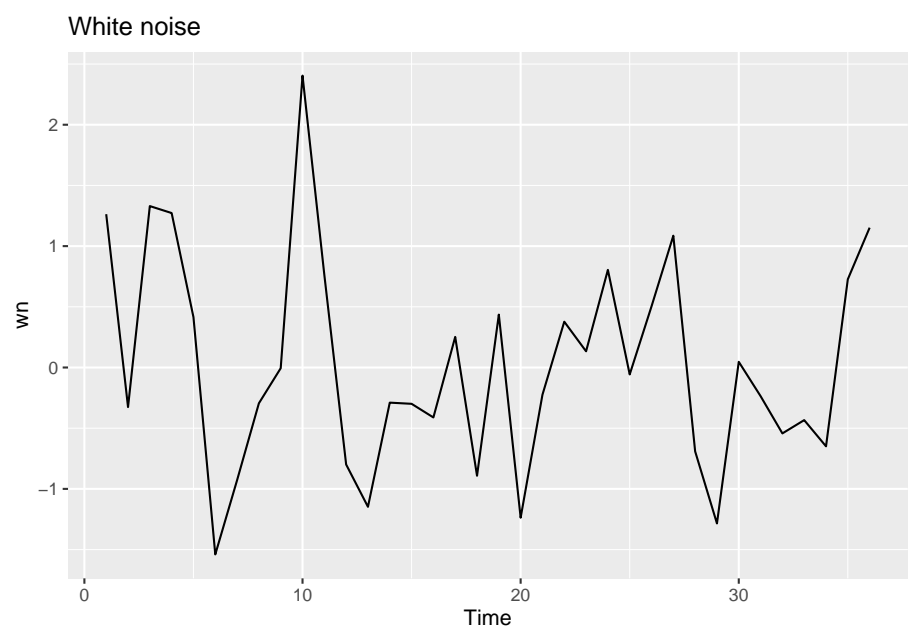
```
# back to slides.

# White noise

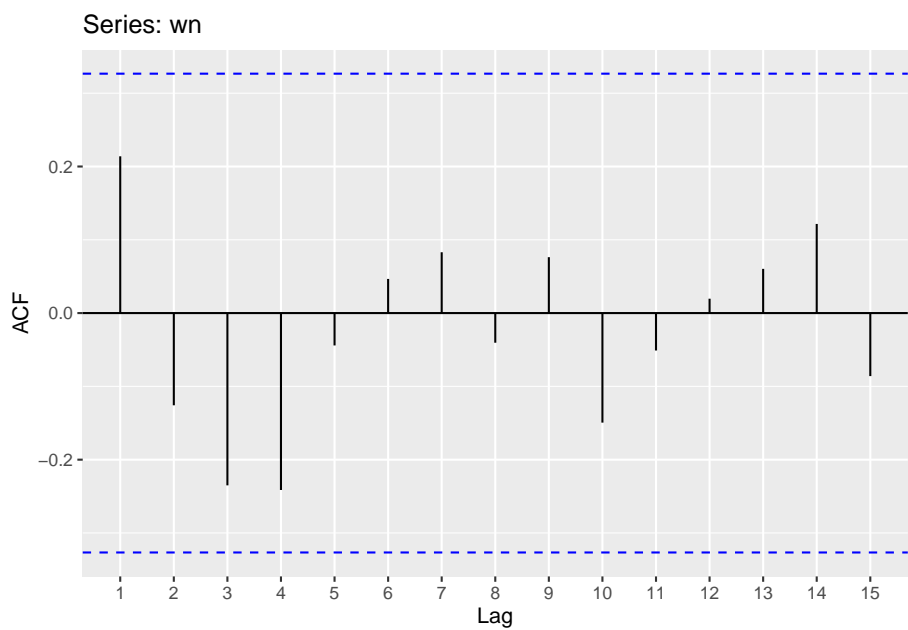
# Set the seed for the random number generator in R
# This guarantees the same random numbers every time

set.seed(0)
wn <- ts(rnorm(36)) #rnorm(n, mean = 0, sd = 1)
autoplot(wn)+ggtitle("White noise")
```

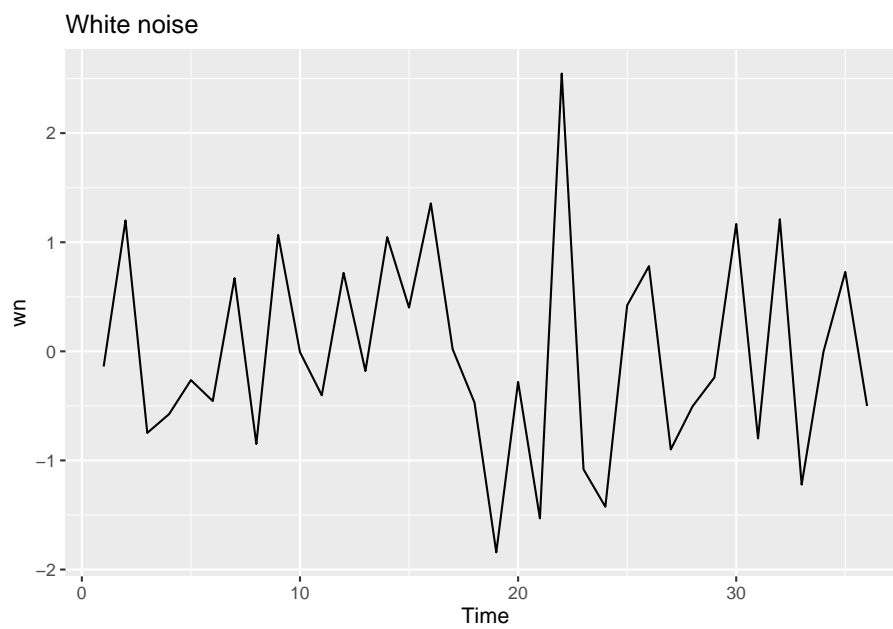




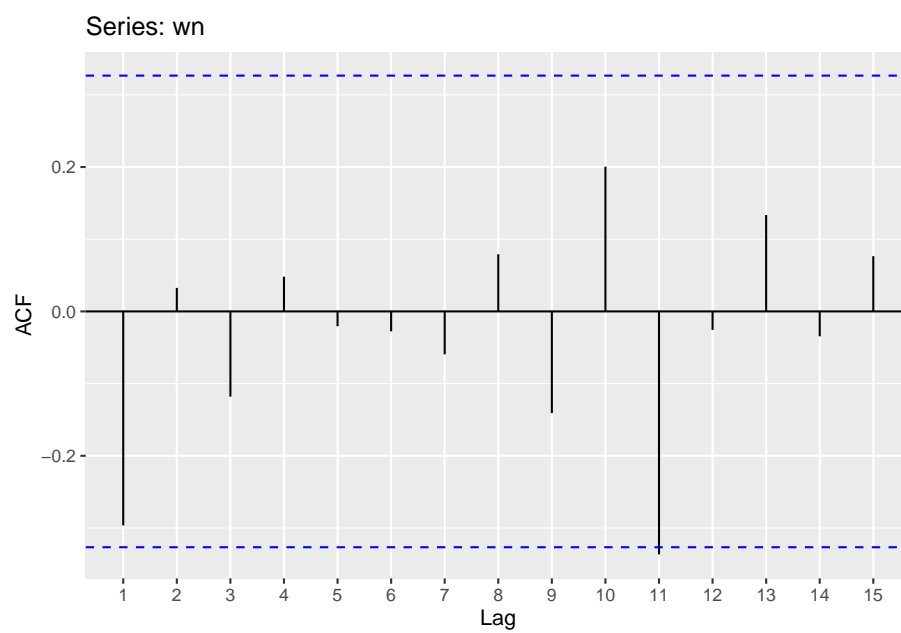
```
ggAcf(wn)
```



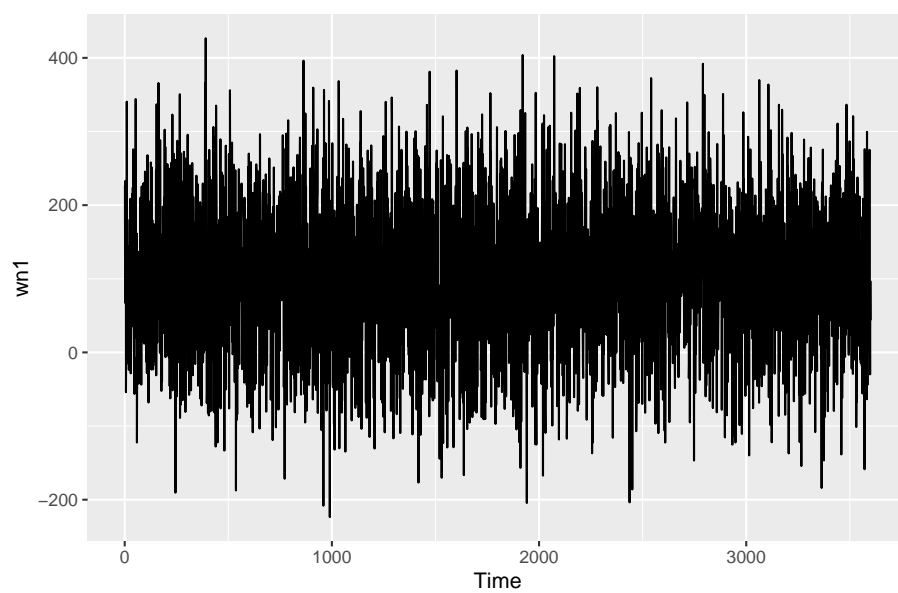
```
set.seed(34)
wn <- ts(rnorm(36)) #rnorm(n, mean = 0, sd = 1)
autoplot(wn)+ggtitle("White noise")
```



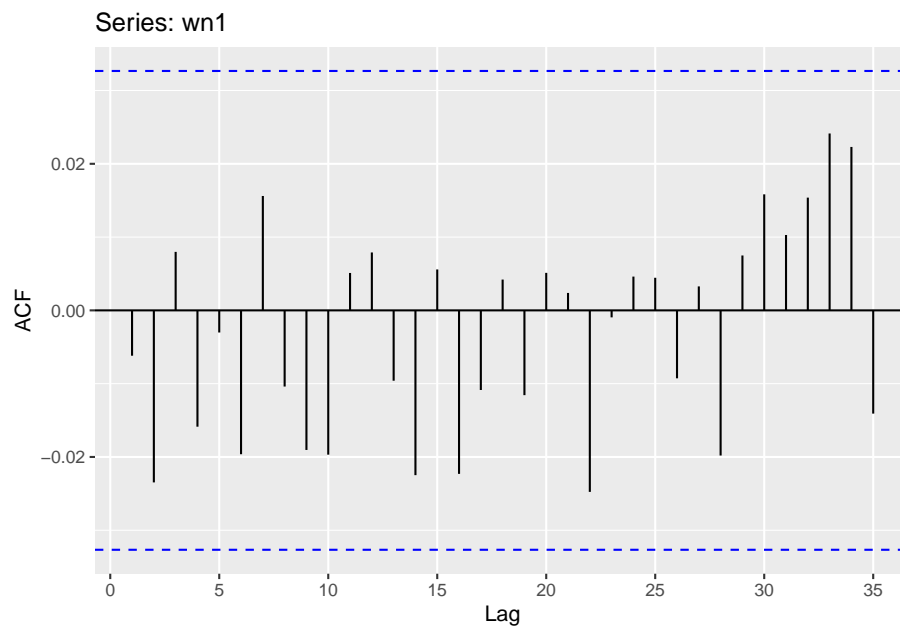
```
ggAcf(wn)
```



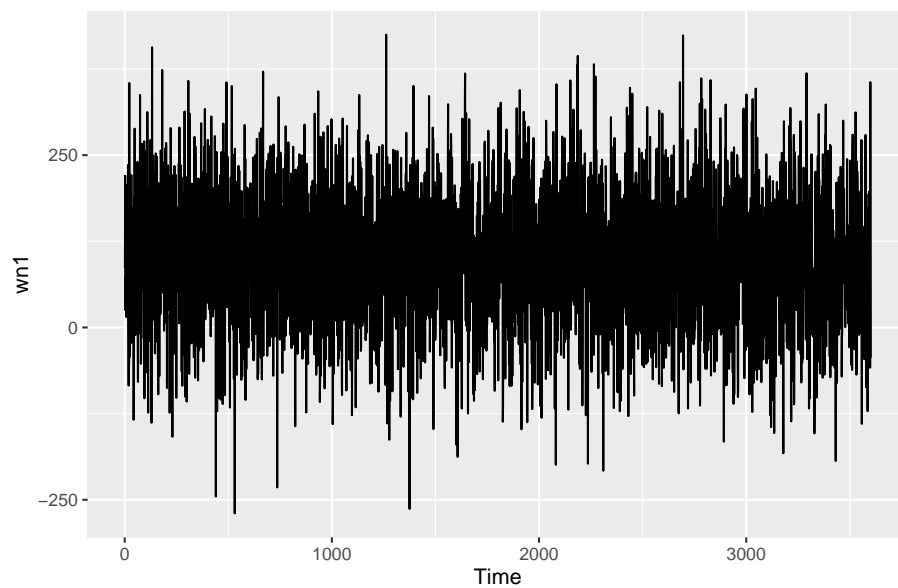
```
set.seed(0)
wn1=ts(rnorm(3600,mean=100,sd=100))
autoplot(wn1)
```



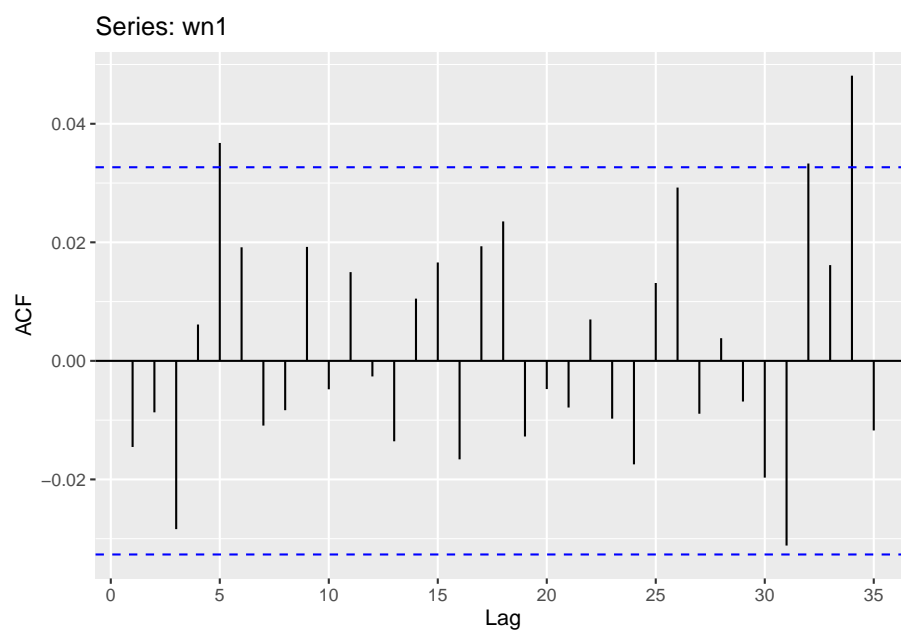
```
ggAcf(wn1) #lag.max
```



```
set.seed(34)  
wn1=ts(rnorm(3600,mean=100,sd=100))  
autoplot(wn1)
```



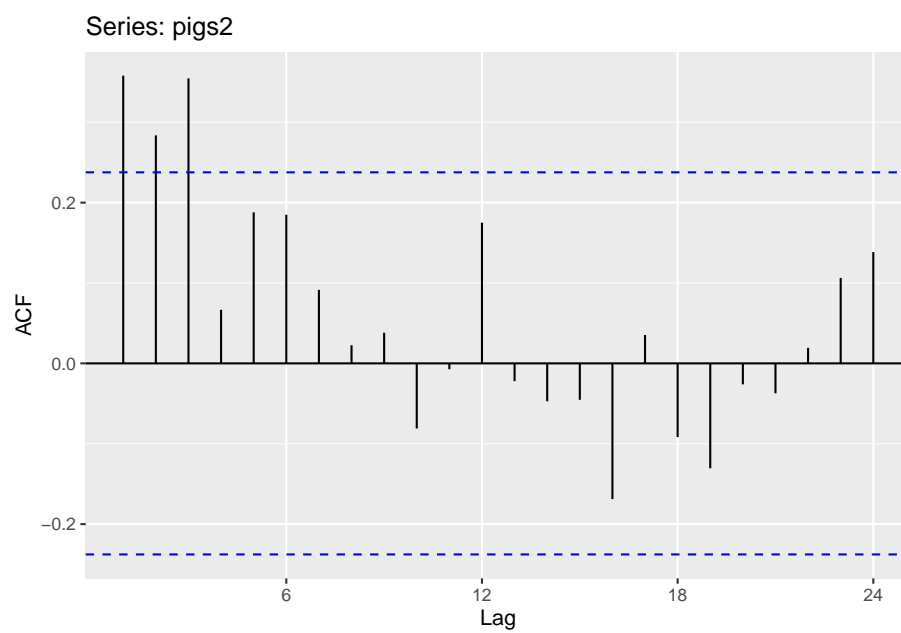
```
ggAcf(wn1)
```



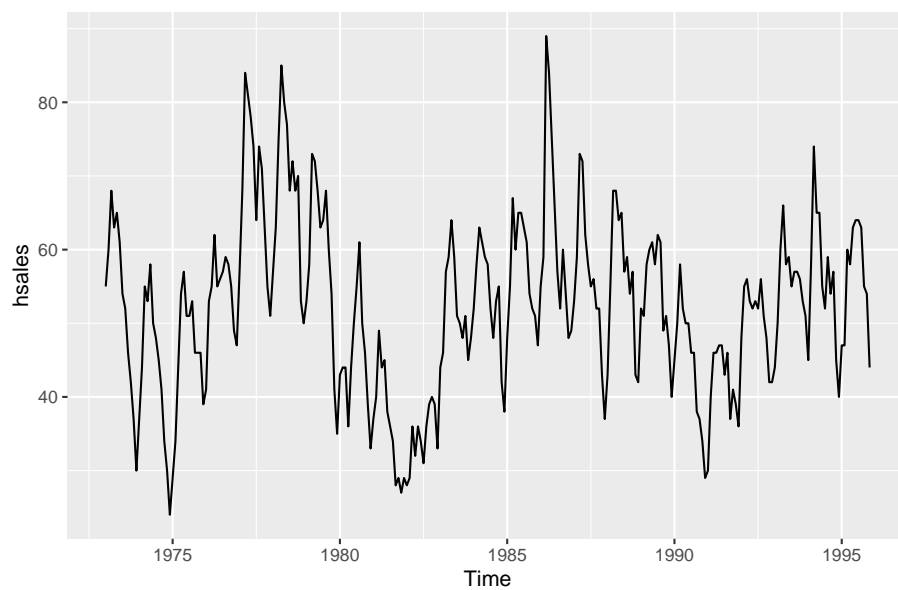
```
# Back to slides
# Pigs
pigs2 <- window(pigs, start=1990)
autoplot(pigs2) +
  xlab("Year") + ylab("thousands") +
  ggtitle("Number of pigs slaughtered in Victoria")
```



```
ggAcf(pigs2)
```

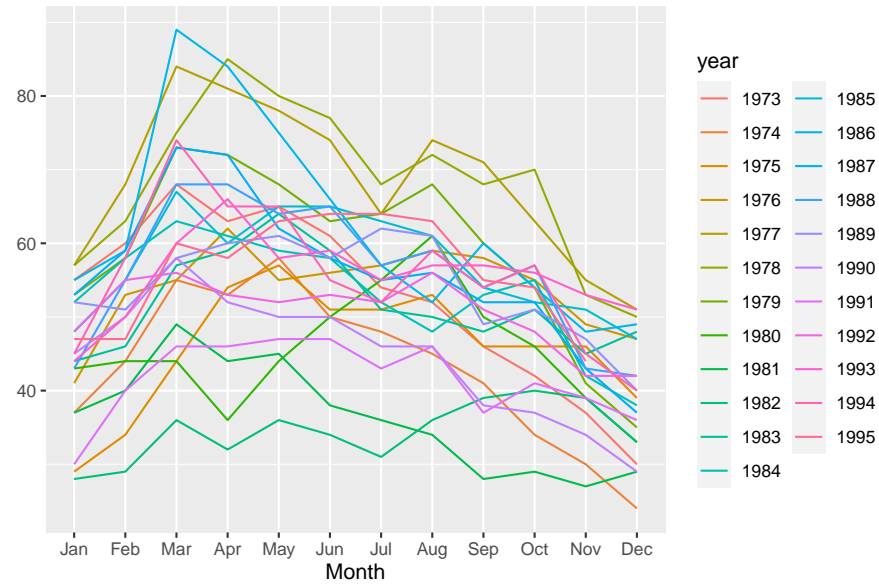


```
# Your turn 2  
autoplot(hsales)
```

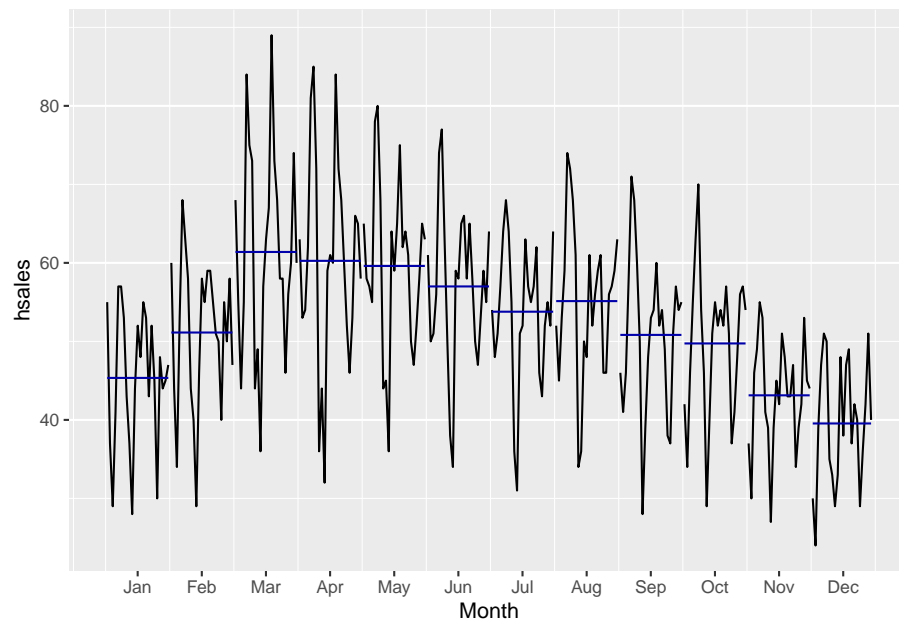


```
ggseasonplot(hsales)
```

Seasonal plot: hsales

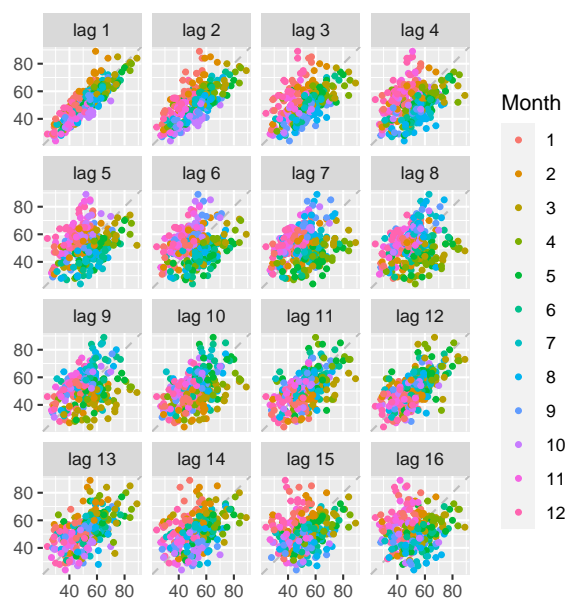


```
ggsubseriesplot(hsales)
```

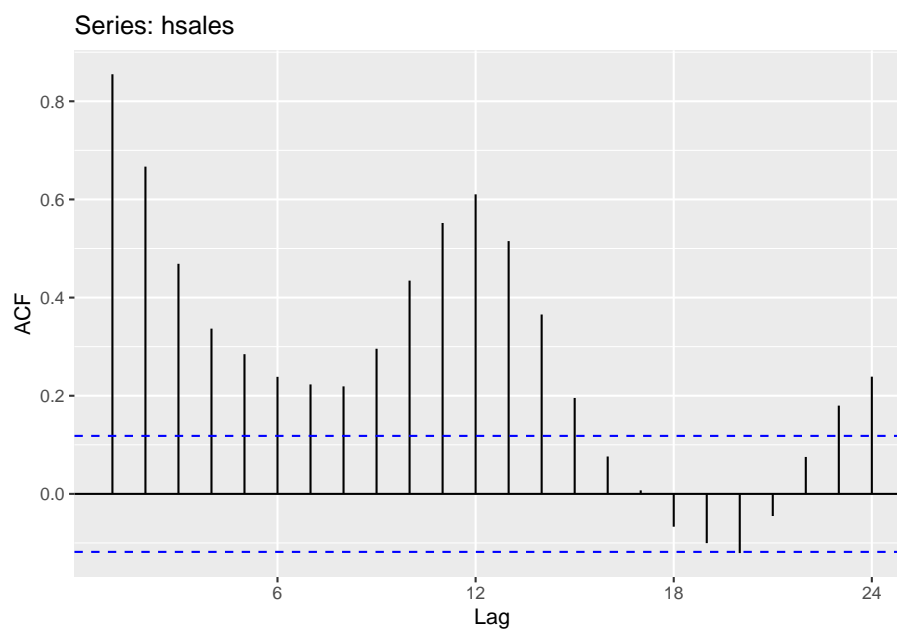




```
gglagplot(hsales,do.lines=FALSE)
```



```
ggAcf(hsales)
```



```
# + Seasonality evident in all plots  
# + Cyclicity seen in first two plots  
# + No trend  
# + ACF only shows seasonality. Cycle length too long to show up here.
```