

1. Show that $(56, 72) = 56x + 72y$

$$\begin{array}{rcl}
 72 & 1 & 0 & 56 & 0 & 1 &] & X & 1 \\
 56 & 0 & 1 & 16 & 1 & -1 &] & X & 3 \\
 16 & 1 & -1 & 8 & -3 & 4 &] & X & 2 \\
 8 & -3 & 4 & 0 & & & & &
 \end{array}$$

$$8 = 72*(-3) + 56*4$$

$$d = 8$$

$$x = 4$$

$$y = -3$$

2. Show that $(1769, 2378) = 1769x + 2378y$

2378	1	0	1769	0	1]X1
1769	0	1	609	1	-1] X2
609	1	-1	551	-2	3]X1
551	-2	3	58	3	-4]X9
58	3	-4	29	-29	39
29	-29	39			

$$d = 29$$

$$x = 39$$

$$y = -29$$

3. Discuss which of the following equations can be solved?

(a) $6x + 51y = 22$ Not Solvable

(b) $33x + 14y = 115$ Solvable

(c) $14x + 35y = 93$ Not Solvable

4.Solve $56x + 72y = 40$

$$a = 56, b = 72, d = 8$$

$$8 = 72*(-3)+56*4$$

Multiply above equation by 5

$$40 = 72*(-15)+56*(20)$$

$$x_0 = 20, y_0 = -15$$

$$x = x_0 + 9t = 20 + 9t$$

$$y = y_0 - 7t = -15 - 7t$$

t is an integer.

5. $(4862542, 1754) = 4862542x + 1754y$

Find d, x, y