

# Reg&Lab HW5.

2.

$$(a) y_{1j} = \beta_0 + \beta_1 x_{1j} + \beta_2 x_{2j} + \varepsilon_{1j}$$

$$= \beta_0 + \beta_1 + \varepsilon_{1j}$$

$$y_{2j} = \beta_0 + \beta_2 + \varepsilon_{2j}$$

$$y_{3j} = \beta_0 - \beta_1 - \beta_2 + \varepsilon_{3j}$$

$$E(y_{1j}) = \mu_1 = \beta_0 + \beta_1$$

$$E(y_{2j}) = \mu_2 = \beta_0 + \beta_2$$

$$E(y_{3j}) = \mu_3 = \beta_0 - \beta_1 - \beta_2$$

$$\Leftrightarrow \frac{\mu_1 + \mu_2 + \mu_3}{3} = \beta_0, \beta_1 = \mu_1 - \beta_0 = \mu_1 - \frac{\mu_1 + \mu_2 + \mu_3}{3}$$

$$\beta_2 = \mu_2 - \beta_0 = \mu_2 - \frac{\mu_1 + \mu_2 + \mu_3}{3}$$

$$(b) \mathbf{y} = \begin{pmatrix} y_1 \\ y_2 \\ y_3 \end{pmatrix} = \begin{pmatrix} y_{11} \\ \vdots \\ y_{1n} \\ y_{21} \\ \vdots \\ y_{2n} \\ y_{31} \\ \vdots \\ y_{3n} \end{pmatrix}$$

$$X = \begin{pmatrix} 1 & 1 & 0 \\ \vdots & \vdots & \vdots \\ 1 & 1 & 0 \\ 1 & 0 & 1 \\ \vdots & \vdots & \vdots \\ 1 & 0 & 1 \\ 1 & -1 & -1 \\ \vdots & \vdots & \vdots \\ 1 & -1 & -1 \end{pmatrix} \begin{matrix} \left. \begin{matrix} 1 & 1 & 0 \\ \vdots & \vdots & \vdots \\ 1 & 1 & 0 \end{matrix} \right\} n \times 3 \\ \left. \begin{matrix} 1 & 0 & 1 \\ \vdots & \vdots & \vdots \\ 1 & 0 & 1 \end{matrix} \right\} n \times 3 \\ \left. \begin{matrix} 1 & -1 & -1 \\ \vdots & \vdots & \vdots \\ 1 & -1 & -1 \end{matrix} \right\} n \times 3 \end{matrix}$$