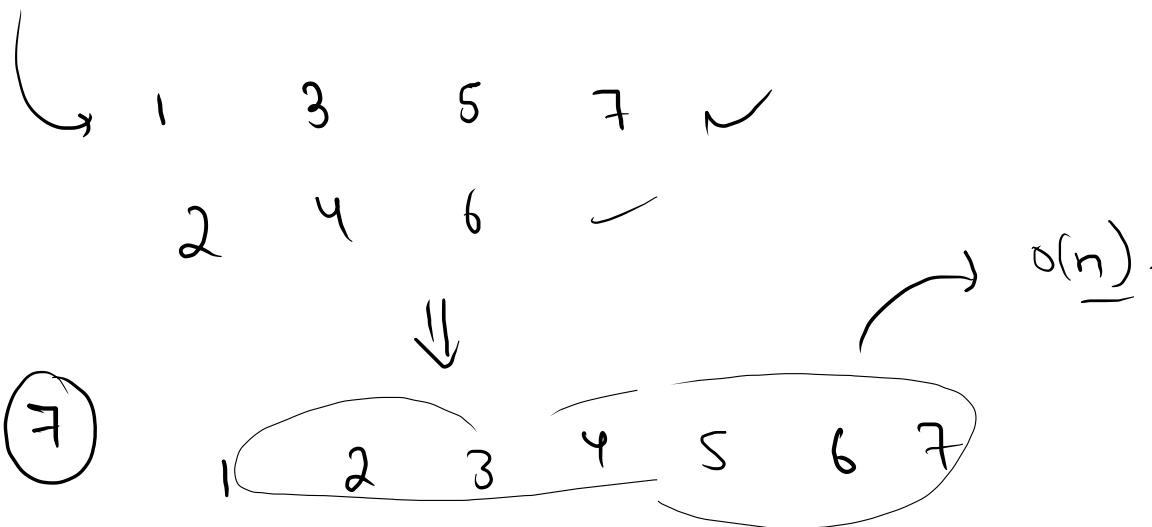
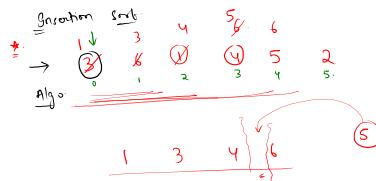
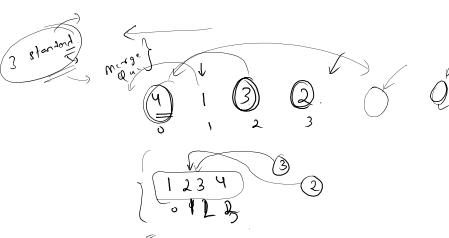
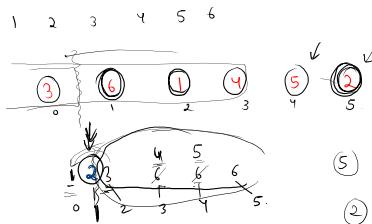


Merge 2 sorted array.





① ② ③ ④ ⑤ ⑥ ⑦



fin. every it
longest end.



5 1 4
1 5 ⑨

e.g.

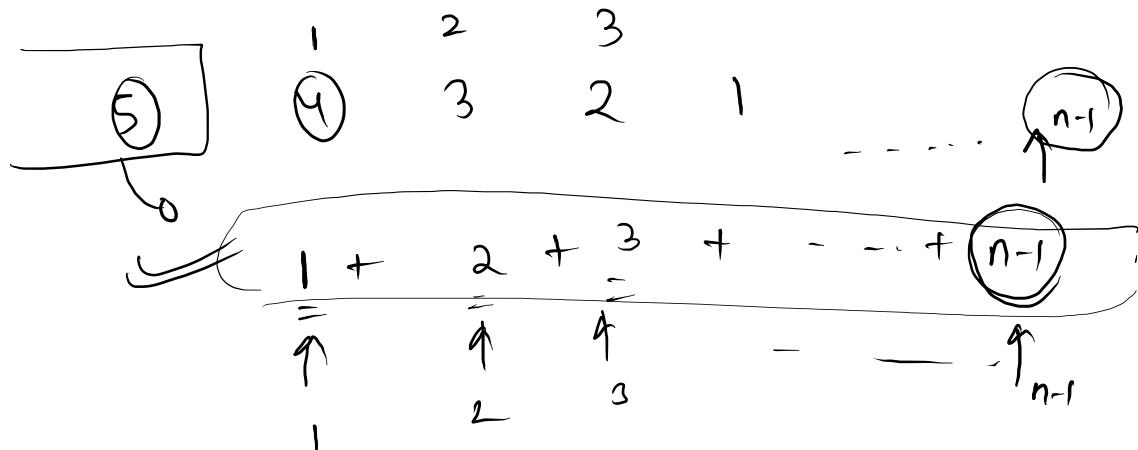
$$\begin{array}{c} 5 \\ \hline 1 & 4 \\ \hline 3 & 2 \\ \hline 1 \end{array}$$

$$\frac{1 + 2 + 3 + 4 + \dots + n-1}{1 + 2 + 3 + 4 + \dots + n-1 + \cancel{n}}$$

$$\frac{n(n+1)}{2}$$

$$\frac{(n-1)(n)}{2}$$

$$\approx O(\underline{n^2}).$$



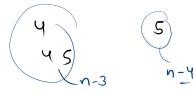
Total

$$\underline{1 + 2 + 3 + 4 + \dots + (n-1)}$$

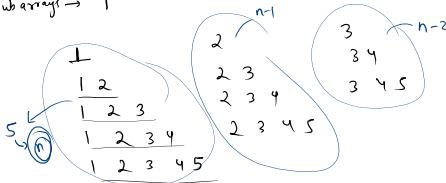
$$\begin{aligned}
 1 + \dots + n &\Rightarrow \frac{n(n+1)}{2} \Rightarrow \frac{(n-1)(n)}{2} \\
 &= \frac{n^2 - n}{2} \\
 &= O(n^2).
 \end{aligned}$$

Print All subarray?

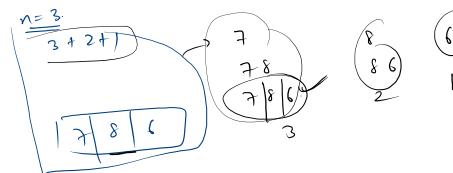
1	2	3	4	5
---	---	---	---	---



subarrays \rightarrow 7



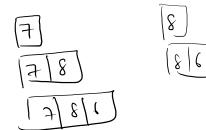
$$n = 5 \\ 5 + 4 + 3 + 2 + 1$$



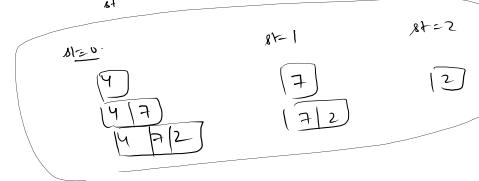
$$n = 4 \rightarrow 4 + 3 + 2 + 1 \\ \frac{n(n+1)}{2}$$

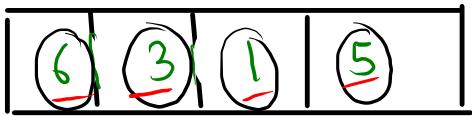
$$T_{\text{total}} \Rightarrow \frac{n(n+1)}{2}$$

$$\boxed{7} \quad \boxed{8} \quad \boxed{6} \longrightarrow n \rightarrow \frac{n(n+1)}{2}$$



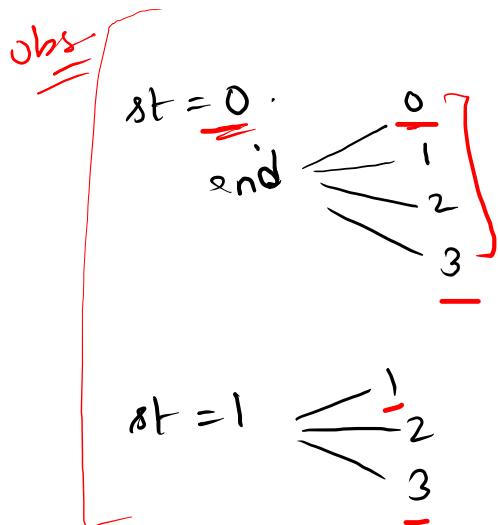
$$\text{e.g. } \boxed{4} \quad \boxed{7} \quad \boxed{2}$$





$\overline{1} = \begin{matrix} 0 \\ 1 \\ 2 \\ 3 \end{matrix}$

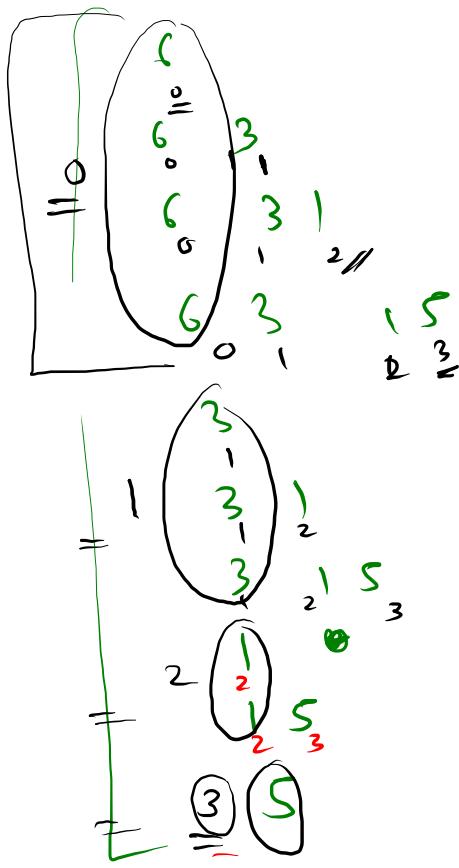
$st \rightarrow [0, n-1]$



$st=2 \begin{matrix} 2 \\ 3 \end{matrix}$

$M=3 \begin{matrix} 3 \end{matrix}$

Kunal. \rightarrow dry run.



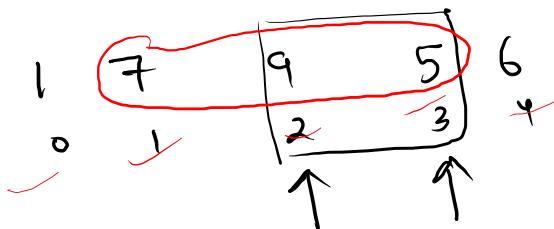
Yesterday.

1. Insertion sort
2. All Subarray.

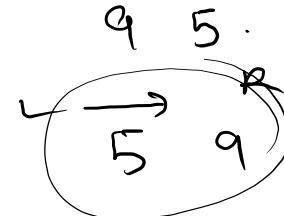


L → R

Sub array.

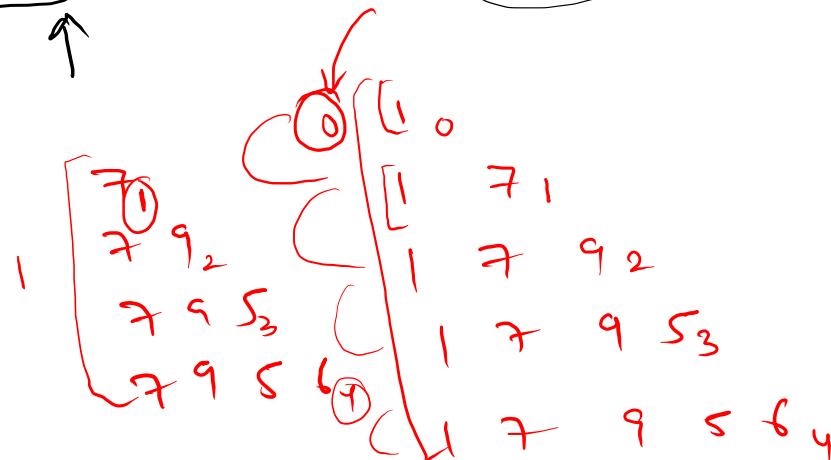


[1 , 3] .



```

for(int st = 0 ; st < n ; st++){
    for(int ed = st; ed < n; ed++){
        for(int k = st; k <= ed; k++){
            System.out.print(arr[k] + " ");
        }
        System.out.println();
    }
}
  
```

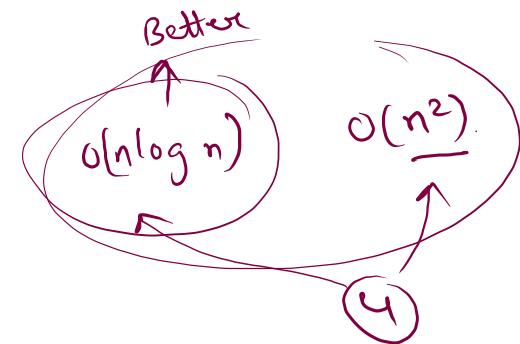
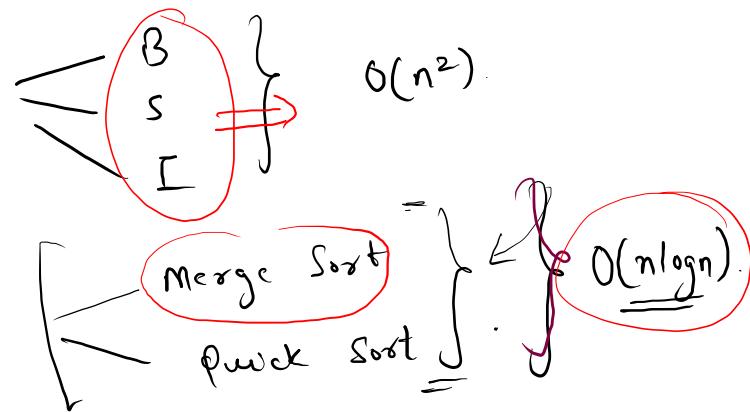


2 { 9
9 5
9 5 } 3 { 5
5 6 } 1 { 6 }

Arrays sort

Algo sorting

Java uses modified merge sort
 \downarrow
 $O(n \log n)$



CC2_01 Maximum Product of 3 Numbers

Take an integer array of size N as input and print the maximum product of three numbers.

Note: You should not use built-in sort function.

Sample Input 0

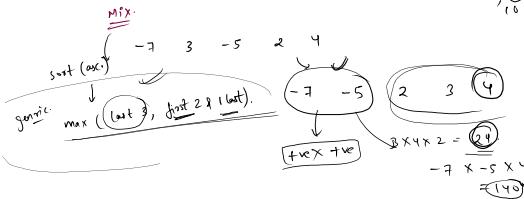
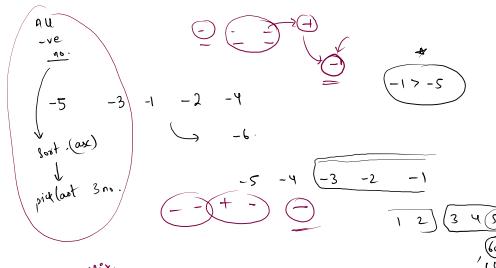
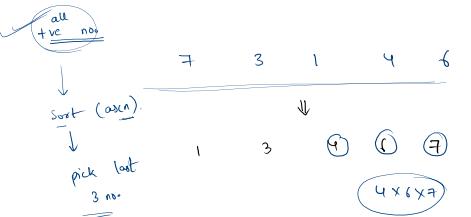
- Constraints
- $3 \leq N \leq 1000$
 - $-1000 \leq arr[i] \leq 1000$

Sample Output 0

$$\boxed{(-7 \times -5 \times 4) = 140}$$

eg. $\begin{array}{c} 5 \\ 1 \\ 4 \\ 3 \\ 2 \end{array}$
 $\text{ans} = 60$

eg. $\begin{array}{c} -1 \\ -4 \\ -5 \\ -3 \\ -2 \end{array}$
 $\text{ans} = -6$
 $\begin{array}{c} -5 \\ -4 \\ -3 \\ -2 \\ -1 \end{array} \rightarrow -5 \times -4 \times -3 = -6$



Ex:

$$\begin{array}{r} 5 \\ -7 \ 3 \ -5 \ 2 \ 4 \\ \hline \end{array}$$

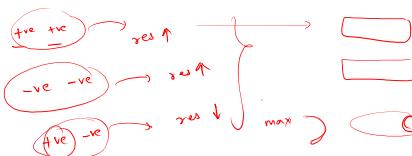
$$\begin{array}{r} -7 \ 3 \ -5 \\ -7 \ 3 \ 2 \\ \hline 3 \ -7 \ -5 \\ 3 \ -1 \ 2 \\ \hline 1 \ 3 \ -7 \ 4 \\ \hline \end{array}$$

Max of 3 max in array -7 3 4

$$1 \ 2 \ 3 \ -4 \ -5 \ 8$$

$$\begin{array}{r} -5 \ -4 \\ + 20 \times 8 = 160 \\ \hline \end{array}$$

$$\begin{array}{r} -5 \ 0 \\ + 8 \times -5 \times 1 = 0 \\ \hline \end{array} \quad \left. \begin{array}{l} 2 \times 2 \times 8 \\ = 48 \end{array} \right\}$$



$$\begin{array}{c} xy \ 2 \ abc \\ \max(xy.c, a.b.c) \end{array}$$

Ex:

$$7 \ -4 \ 3 \ 1 \ 2$$

$$\begin{array}{r} + \\ -40 \ -10 \\ \hline x_1 = 2 \cdot 3 \cdot 7 = 42 \\ x_2 = -4 \cdot 1 \cdot 7 = -28 \\ \hline \end{array} \quad \left. \begin{array}{l} \max(x_1, x_2) \\ 81 \end{array} \right\}$$

$$x_2 = 400 \cdot 7 = 280$$

$$\begin{array}{r} -4 \ 1 \ -2 \ 3 \ 7 \\ \hline \end{array}$$

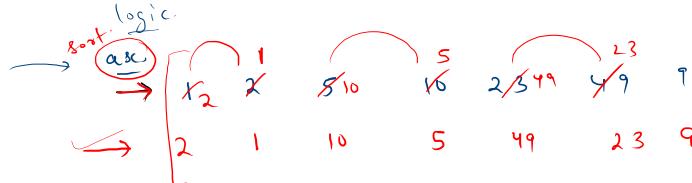
$$\begin{array}{r} -4 \ -2 \ 1 \ 3 \\ \hline x_1 = -4 \cdot -2 \cdot 7 = 56 \\ x_2 = 1 \cdot 2 \cdot 7 = 21 \\ \hline n = 5 \end{array}$$

Sort an array in wave form 1

Given an unsorted array of integers, sort the array into a wave like array. An array 'arr[0..n-1]' is sorted in wave form if $\text{arr}[0] \geq \text{arr}[1] \leq \text{arr}[2] \geq \text{arr}[3] \leq \text{arr}[4] \geq \dots$

Sample Input 0

7
10 90 49 2 1 5 23



Sample Output 0

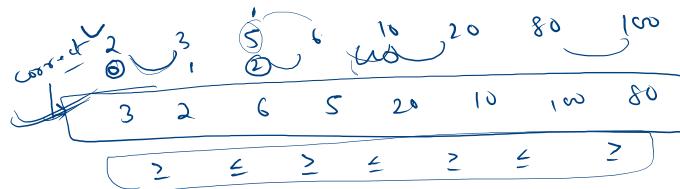
2 1 10 5 49 23 90

pseudo code.

1. sort (asc.)
2. swap alt. no.

Input: arr[] = {10, 5, 6, 3, 2, 20, 100, 80}

Output: arr[] = {10, 5, 6, 2, 20, 3, 100, 80}



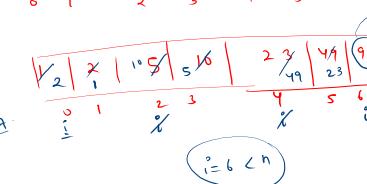
logic

index even \rightarrow ○

```
Arrays.sort(arr);  
for(int i = 0; i < n; i += 2){  
    int temp = arr[i];  
    arr[i] = arr[i+1];  
    arr[i+1] = temp;  
}  
for(int i = 0; i < n; i++){  
    System.out.print(arr[i] + " ");  
}
```



$i=0$



Max Subarray 2

Given an array $\text{arr}[0:N]$ of N integers. Find the contiguous sub-array (containing at least one number) which has the maximum sum and print its sum.

Sample Input 0

5
-1 2 3 -2 1

Sample Output 0

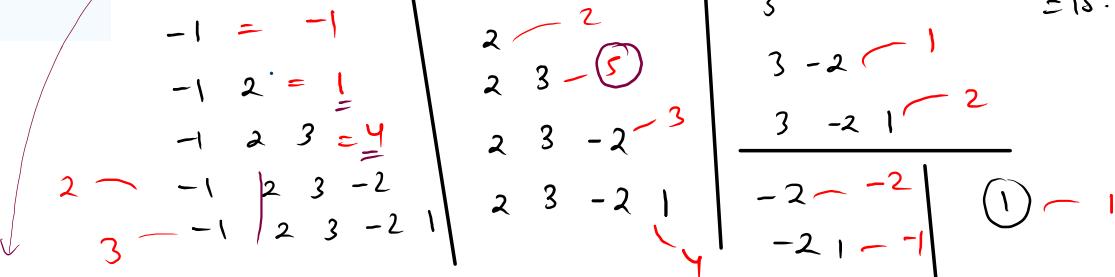
5

$$\max = -\infty \quad \cancel{-1} \quad \cancel{X} \quad \cancel{X} \quad \cancel{Y} \quad \cancel{5}$$

$$n=5$$

$$\frac{n(n+1)}{2}$$

$$= 15.$$



To print all sub-arrays.

Kadane's

-1 2 3 -2 1
 0 1 2 3 4

-1

-1

$$\text{curr_sum} = \emptyset \quad -1$$

$$\text{final ans} \rightarrow \max = 0$$