



# CHAROTAR UNIVERSITY OF SCIENCE AND TECHNOLOGY

## CHAROTAR UNIVERSITY OF SCIENCE & TECHNOLOGY

### Fifth Semester of B. Tech. (CE/CSE) Examination

December 2020

#### Design and Analysis of Algorithms [CE342]

Marks: 70

Duration: 225 mins.

#### MCQ

Answer all the questions.

Attempt All MCQ

- 1) Consider two strings  $A = "qpqrr"$  and  $B = "pqprrrp"$ . Let  $x$  be the length of the longest common subsequence (not necessarily contiguous) between  $A$  and  $B$  and let  $y$  be the number of such longest common subsequences between  $A$  and  $B$ . Then  $x + 10y = \underline{\hspace{1cm}}$ . (2)
- 1) 33    2) 34    3) 23    4) 43
- 2) Four matrices  $M_1, M_2, M_3$  and  $M_4$  of dimensions  $p \times q, q \times r, r \times s$  and  $s \times t$  respectively can be multiplied in several ways with different number of total scalar multiplications. For example, when multiplied as  $((M_1 \times M_2) \times (M_3 \times M_4))$ , the total number of multiplications is  $pqr + rst + prt$ . When multiplied as  $((M_1 \times M_2) \times M_3) \times M_4$ , the total number of scalar multiplications is  $pqr + prs + pst$ . If  $p = 10, q = 100, r = 20, s = 5$  and  $t = 80$ , then the optimal number of scalar multiplications needed is (2)
- 1) 25000    2) 248000    3) 19000    4) 44000
- 3) Given a pattern of length- 5 window, find the spurious hit in the given text string.  
Pattern: 3 1 4 1 5  
Modulus: 13  
Text: 2 3 5 9 0 2 3 1 4 1 5 2 6 7 3 9 9 2 1 3 9 (1)
- 1) 1    2) 2    3) 3    4) 4
- 4) What is the best case and worst-case complexity of ordered linear search? (1)
- 1)  $O(n \log n), O(\log n)$     2)  $O(\log n), O(n \log n)$     3)  $O(n), O$     4)  $O, O(n)$
- 5) Arrange the following function in ascending order of their growth?  
 $F_1(n)=2^n, F_2(n)=n^{3/2}, F_3(n)=n \log_2 n, F_4(n)=n^{\log_2 n}$  (1)
- 1)  $F_3, F_2, F_4, F_1$     2)  $F_3, F_2, F_1, F_4$     3)  $F_2, F_3, F_1, F_4$     4)  $F_2, F_3, F_4, F_1$
- 6) Kruskal's algorithm uses \_\_\_\_\_ and Prim's algorithm uses \_\_\_\_\_ in determining the MST. (1)
- 1) edge, vertex    2) vertex, edge    3) edges, edges    4) vertex, vertex
- 7) Which of the following sorting algorithms in its typical implementation gives the best performance when applied on an array that is sorted or almost sorted (maximum 1 or two elements are misplaced)? (1)

1) Quick Sort    2) Insertion Sort    3) Merge Sort    4) Heap Sort

- 8) You are given a knapsack that can carry a maximum weight of 60. There are 4 items with weights {20, 30, 40, 70} and values {70, 80, 90, 200}. What is the maximum value of the items you can carry using the knapsack? (2)

1) 160    2) 200    3) 170    4) 90

- 9) In dynamic programming, the technique of storing the previously calculated values is called \_\_\_\_\_. (1)

1) Saving value property    2) Storing value property    3) Memoization    4) Mapping

- 10) The difference between Divide and Conquer and Dynamic Programming is:

Whether the 1) subproblems overlap or not	The division of problems 2) and combination of subproblems	The way we 3) solve the base case	The depth 4) of recurrence	(1)
---	--	---	----------------------------------	-----

- 11) Division Pattern of Problems in Divide and Conquer approach Select one:

1) Iterative    2) Recursive Correct    3) Parallel    4) Random (1)

- 12) Backtracking algorithm is implemented by constructing a tree of choices called as?

Backtracking tree (1)

1) State-space tree    2) State-chart tree    3) Node tree    4)

- 13) You are given infinite coins of denominations 1, 3, 4. What is the total number of ways in which a sum of 7 can be achieved using these coins if the order of the coins is not important? (2)

1) 4    2) 3    3) 5    4) 6

- 14) NP-Complete  $\cap$  P = \_\_\_\_\_ which of the following is true?

1) NP-Hard    2)  $\emptyset$     3) P    4) NP-Complete (2)

- 15) The Highest Lower Bound on the number of Comparisons in the worst case for comparison-based sorting order of (1)

1) n    2)  $n^2$     3)  $n \log n$     4)  $n \log_2 n$

### Section-1

**Answer 5 out of 6 questions.**

**Do as Directed [Any five/**

- 16) How to choose an algorithm for solving a single problem, when you have multiple algorithms for solving the same problem? Which from the below functions take less time to solve the given problem? Justify your answer: (5)
- a).  $G(n)=2G(n-1) + 1$
- b).  $G(n)=G(n-1) + n$

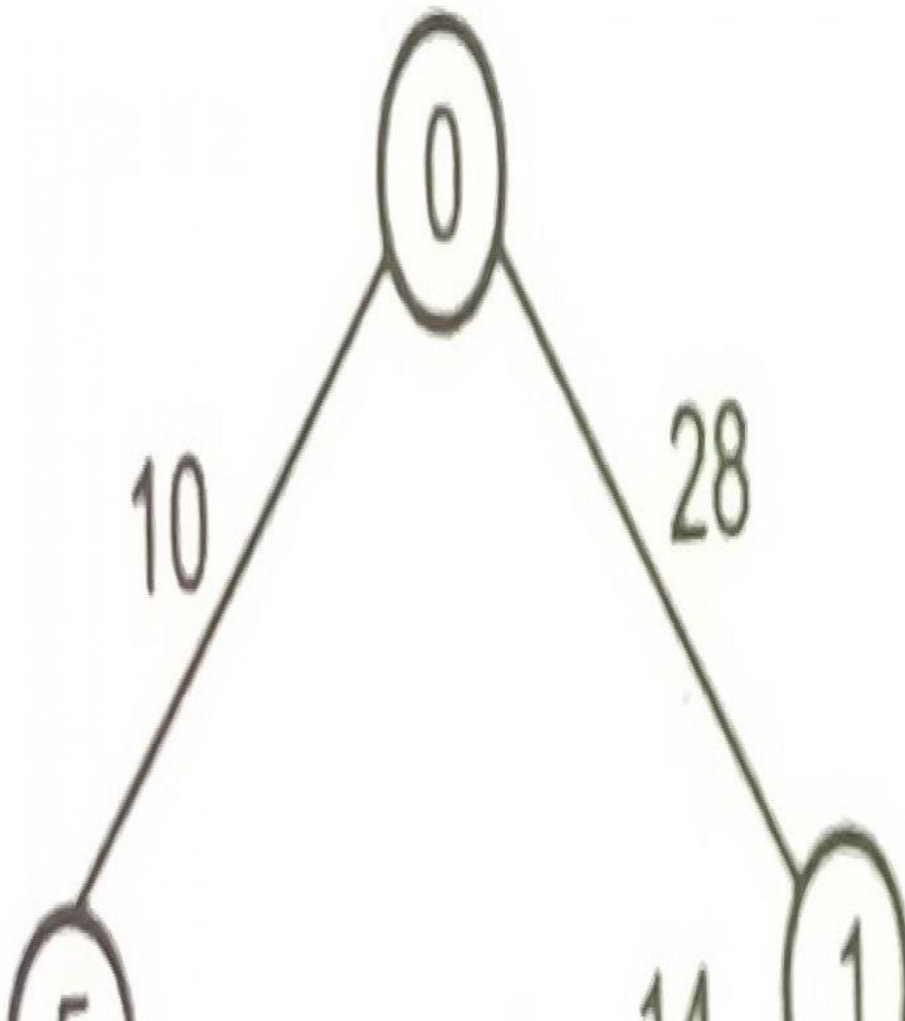
- 17) Apply Rabin-karp string matching algorithm to find out pattern 31415 in the text 2359023141526739921 to find valid match and spurious hits. Take value of  $q=13$ . Compare the result with, if we take value of  $q=11$ . (5)
- 18) Amar takes 2, 6 and 7 hours of time to perform cooking, gardening and cleaning respectively. Akbar takes 4, 8 and 3 hours of time to perform cooking, gardening and cleaning respectively. Anthony takes 9, 5 and 1 hours of time to perform cooking, gardening and cleaning respectively. Find out optimal job assignment for Amar, Akbar and Anthony. (5)
- 19) You are given two machine with capability to solve given problems  $(10^{(-4)} \cdot (2^n))$  Seconds and  $(10^{(-6)} \cdot (2^n))$  Seconds respectively. Show the calculation that proves which machine is better for input instance size  $n=10, 15, 20, 30$  and  $45$ . Instead of machine A if we choose to use machine C with capability  $(10^{(-2)} \cdot (n^3))$  Seconds, what kind of significant improvement we may get. Show the complete detail analysis. (5)
- 20) Derive complexity for divide and conquer based matrix multiplication. Is there any approach by which we can reduce matrix multiplication complexity? If yes, then how? (5)
- 21) What do you mean by algorithm designing approach? Do Comparison of Backtrack, Branch bound and Dynamic programming. (5)

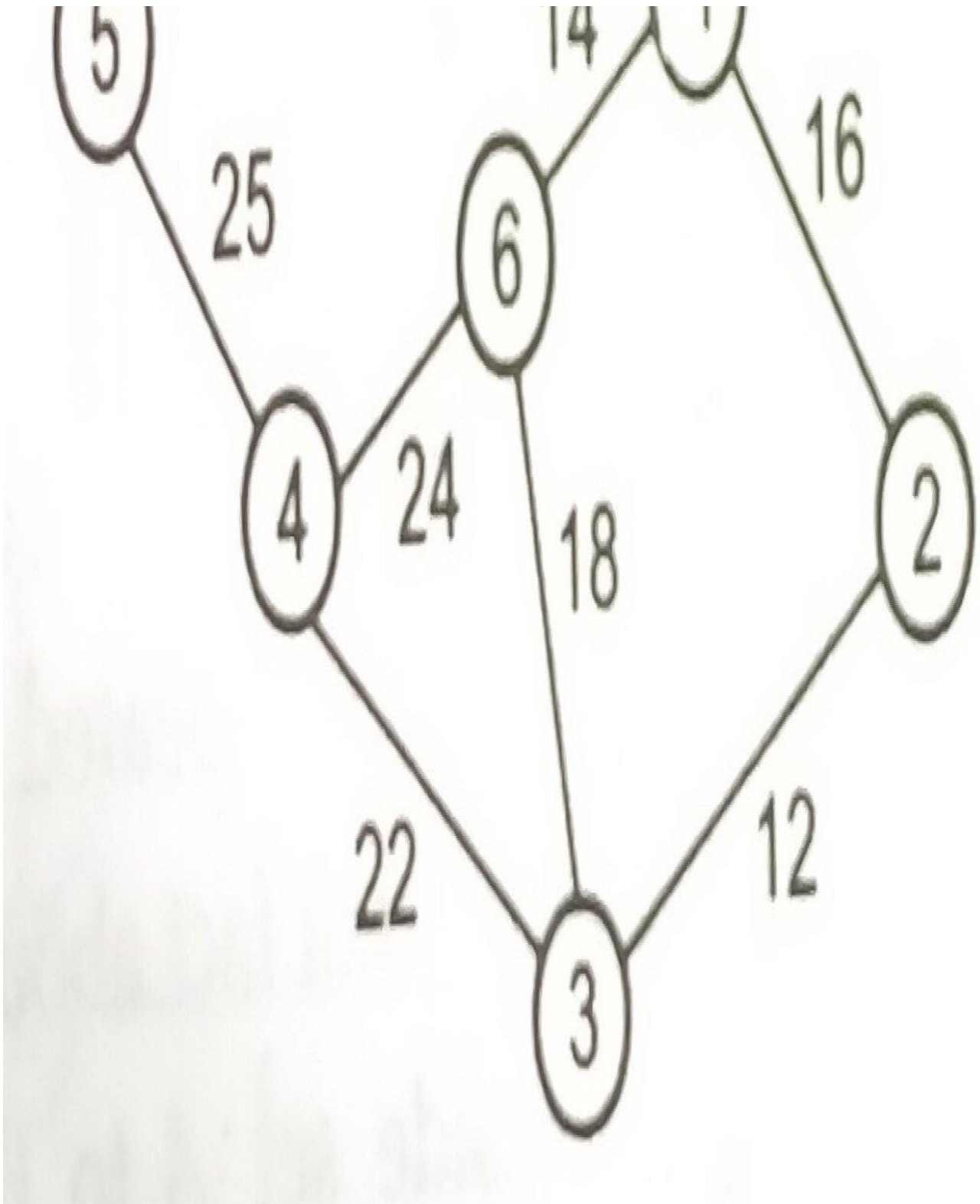
## Section-2

Answer 5 out of 6 questions.

Do as Directed [Any five/

- 22) Generate minimum cost spanning tree for the following graph using Prim's Algorithm. (5)





- 23) State Master Theorem. Solve the following recurrence equations using Master Theorem:
- $T(n) = 2T(n/2) + n \log n$  (5)
  - $T(n) = 3T(n/3) + \sqrt{n}$
- 24) Apply activity selection process of greedy approach to get maximum activities to be conducted for given activities (i) with start time ( $S_i$ ) and finish time ( $F_i$ ). (5)

i	1	2	3	4	5	6	7	8	9	10	11
---	---	---	---	---	---	---	---	---	---	----	----

S <sub>i</sub>	1	3	0	5	3	5	6	8	8	2	12
F <sub>i</sub>	4	5	6	7	8	9	10	11	12	13	14

25) Write short note on following:

1. Polynomial Reduction
  2. NP-Complete
  3. NP-Hard
- (5)

26) Find the binomial coefficient  $C(8,6)$  using dynamic programming. (5)

27) Derive time recurrence relation of Quick Sort in worst case and solve the recurrence by iterative method. (5)

-----End-----