Unit 3

Production & Cost Analyses PRODUCTION ANALYSIS

PRODUCTION FUNCTION

The production function represents the relationship between the inputs (factors of production) and the resulting output. It shows how different combinations of inputs result in different levels of output.

Mathematical Representation

$$Q = f(L, K)$$

Where:

- Q = Output
- L = Labour
- K = Capital

Assumes technology is constant and resources are used efficiently.

TIME PERIOD IN PRODUCTION

Short Run

- Some inputs (like capital) are fixed.
- Only labour or raw material can be changed.
- Relevant for Law of Variable Proportion.

Long Run

- All inputs are variable.
- Firms can change the scale of production.
- Relevant for Returns to Scale.



FIXED AND VARIABLE INPUTS

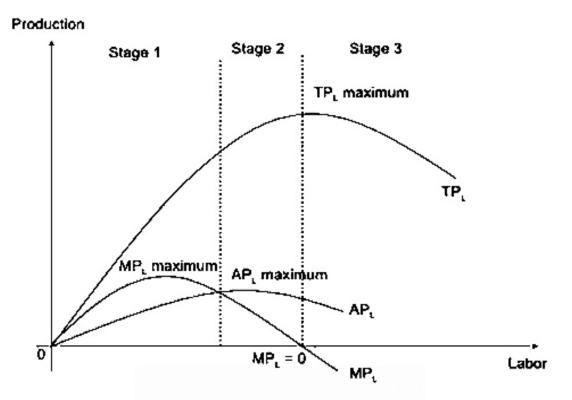
Factor Type	Description	Examples
Fixed Inputs	Do not change with output in short run	Plant, Building, Machinery
Variable Inputs	Change with output level	Labour, Raw Materials, Fuel

TOTAL, MARGINAL, AND AVERAGE PRODUCT

Term	Definition	Formula
Total Product (TP)	Total output from given inputs	Sum of all output
Marginal Product (MP)	Additional output from one more unit of input	Δ TP / Δ Input
Average Product (AP)	Output per unit of input	TP / Input

SHAPES OF TP, MP, AND AP CURVES

- **TP Curve**: Rises, flattens, and then falls.
- MP Curve: Increases, peaks, falls, and becomes negative.
- AP Curve: Rises, peaks when MP = AP, and then declines.



LAW OF VARIABLE PROPORTIONS

As more units of a variable input are added to fixed inputs, total output increases initially at an increasing rate, then at a decreasing rate, and finally starts declining.

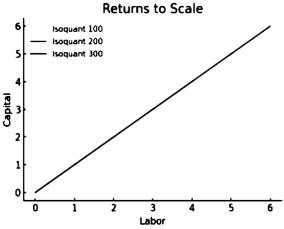
Three Stages

- 1. Stage I Increasing Returns: MP increases.
- 2. Stage II Diminishing Returns: MP decreases, but positive. (Most efficient stage)
- 3. Stage III Negative Returns: MP becomes negative, TP falls.

RETURNS TO SCALE (LONG RUN CONCEPT)

Refers to changes in output when all inputs are changed by the same proportion.

Туре	Description	
Increasing Returns	Output increases more than inputs	
Constant Returns	Output increases in the same proportion	
Decreasing Returns	Output increases less than inputs	



Returns to scale are shown through isoquants where distance between isoquants changes based on the type of return.

COST ANALYSIS

COST

Economies of scale are cost advantages that businesses experience when they increase production. This happens because fixed costs are spread out over more units, and because businesses can negotiate lower prices for materials when they buy in bulk.

TYPES OF COSTS

Туре	Description	Formula
Fixed Cost (FC)	Constant in short run	Rent, salaries
Variable Cost (VC)	Changes with output	Wages, raw materials
Total Cost (TC)	Sum of FC and VC	TC = FC + VC
Average Cost (AC)	Cost per unit	AC = TC / Q
Average Fixed Cost (AFC)	FC per unit	AFC = FC / Q
Average Variable Cost (AVC)	VC per unit	AVC = VC / Q
Marginal Cost (MC)	Cost of one more unit	$MC = \Delta TC / \Delta Q$

ECONOMIES OF SCALE

A cost reduction that occurs when a business increases production. it happens when Fixed costs are spread out over more units.

Internal Economies (within firm):

Technical, Managerial, Financial, Marketing, Risk-bearing

External Economies (industry-level):

Infrastructure, skilled labour, R&D clusters

HOW ECONOMIES OF SCALE WORK

