

# # 1 (class Assignment)

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## P\_MEETING :

Calculated Formula :  $^{2N}C_N/2^{2N}$

Sol:

Consider Left move as “-1” and right move as “+1” . Now For both the drinkers to meet they must have same number of “+1” and hence same number of “-1” as number of moves are N.

so Total moves are  $2N$  .

let 1<sup>st</sup> drinker has  $x$  number of “+1” so it will have  $N-x$  number of “-1”.

Possible ways =  $^NC_x$

Total Ways =  $2^N$ , So

$P(x) = ^NC_x/2^N$

Now since they both drinkers movement is independent of each other,

$P(\text{having } x \text{ number of “+1”}) = P(x)*P(x)$ .

and we know that  $x = 0, 1, 2 \dots N$ .

So  $P(\text{of meeting of drinkers}) = P(0)^2 + P(1)^2 \dots + P(N)^2$ .

Which Comes out to be  $^{2N}C_N/2^{2N}$ .

## MEAN\_DISPLACEMENT :

Calculated Formula : 0

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Sol:

Let  $\langle S \rangle$  be the mean displacement over many experiments performed, which is equal to sum of all moves, so :

$$\langle S \rangle = \langle A_1 + A_2 + \dots + A_N \rangle$$

which further can be written as :

$$\langle S \rangle = \langle A_1 \rangle + \langle A_2 \rangle + \dots + \langle A_N \rangle ;$$

$\langle A_i \rangle$  is the mean of  $i^{\text{th}}$  move, because if we repeated the experiment many many times, and  $A_1$  has an equal probability of being “-1” or “+1”, hence we expect the average of  $A_1$  to be 0 i.e. stays at the same place.

Hence

$$\langle S \rangle = 0 + 0 + \dots + 0 = 0$$

**P\_ORIGIN :**

Calculated Formula :  $\begin{matrix} {}^N C_{N/2} / 2^N & ; \text{ if } N \text{ is even} \\ 0 & ; \text{ if } N \text{ is odd} \end{matrix}$

Sol :

Consider forward walk as “+1” and backward walk as “-1”.

Now for the drunker to come back to Origin. Total Forward moves should equal to Total Backward moves i.e.

number of “+1” = number of “-1”      -(i)

Case I : N is odd

Here  $N/2 \neq 0$  , here eq (I) can not be satisfied so

Favorable cases = 0, hence

$P(\text{origin}) = 0$ .

Case II : N is even

Favorable cases =  ${}^N C_{N/2}$  ( distributing  $N/2$  “+1” over N blanks )

Total cases =  $2^N$

Hence,

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$$P(\text{origin}) = \begin{matrix} {}^N C_{N/2} / 2^N & ; \text{ if } N \text{ is even} \\ 0 & ; \text{ if } N \text{ is odd} \end{matrix}$$

## MEAN\_SQ\_DISPLACEMENT:

Calculated Formula :  $N$

Sol:

Just like the mean Displacement we have -

Consider Left move as “-1” and right move as “+1” and the path on the number line with drunker starting at origin. Using this it will be a lot easier to solve.

$\langle S^2 \rangle$  is the mean squared displacement over a large number of experiments.  $a_1, a_2 \dots a_N$  are the moves taken by drunker.

$\langle a_i \rangle$  represents mean of  $i^{\text{th}}$  move over all the experiments.

So,

$$\langle S^2 \rangle = \langle (a_1 + a_2 + \dots + a_N)^2 \rangle = \langle (a_1 + a_2 + \dots + a_N) (a_1 + a_2 + \dots + a_N) \rangle = (\langle a_1 a_1 \rangle + \langle a_2 a_2 \rangle + \dots \langle a_N a_N \rangle) + 2 (\langle a_1 a_2 \rangle + \langle a_1 a_3 \rangle + \dots)$$

$$\langle S^2 \rangle = (\langle a_1^2 \rangle + \langle a_2^2 \rangle + \dots + \langle a_N^2 \rangle) + 2 (\langle a_1 a_2 \rangle + \langle a_2 a_3 \rangle + \dots) = (1 + 1 + 1 + \dots + 1) + 2 (0 + 0 + \dots) = N$$

Since  $\langle a_1 a_2 \rangle$  these terms will be zero but  $\langle a_i^2 \rangle$  will be 1.

$\langle a_1 a_2 \rangle$  is “+1” or “-1” with same probability i.e.  $1/2$ .

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$a_1$	$a_2$	$a_1 a_2$
1	1	1
1	-1	-1
-1	1	-1
-1	-1	1