



INTERMEDIATE PORTFOLIO ANALYSIS IN R

# **Welcome to Intermediate Portfolio Analysis in R**

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# What you will learn:

- Build on fundamental concepts from "Introduction to Portfolio Analysis in R"
- Explore advanced concepts in the portfolio optimization process
- Use the R package `PortfolioAnalytics` to solve portfolio optimization problems that mirror real world problems

# Modern Portfolio Theory

Modern Portfolio Theory (MPT) was introduced by Harry Markowitz in 1952.

MPT states that an investor's objective is to maximize **portfolio expected return** for a given amount of **risk**.

Common Objectives:

- Maximize a measure of gain per unit measure of risk
- Minimize a measure of risk

# Mean - Standard Deviation Example: Setup

```
> library(PortfolioAnalytics)
> data(edhec)
> data <- edhec[,1:8]

# Create the portfolio specification
> port_spec <- portfolio.spec(colnames(data))

> port_spec <- add.constraint(portfolio = port_spec,
                             type = "full_investment")
> port_spec <- add.constraint(portfolio = port_spec,
                             type = "long_only")

> port_spec <- add.objective(portfolio = port_spec,
                             type = "return",
                             name = "mean")
> port_spec <- add.objective(portfolio = port_spec,
                             type = "risk",
                             name = "StdDev")
```

# Mean - Standard Deviation Example: Output

```
> print(port_spec)
*****
PortfolioAnalytics Portfolio Specification
*****
Call:
portfolio.spec(assets = colnames(data))

Number of assets: 8

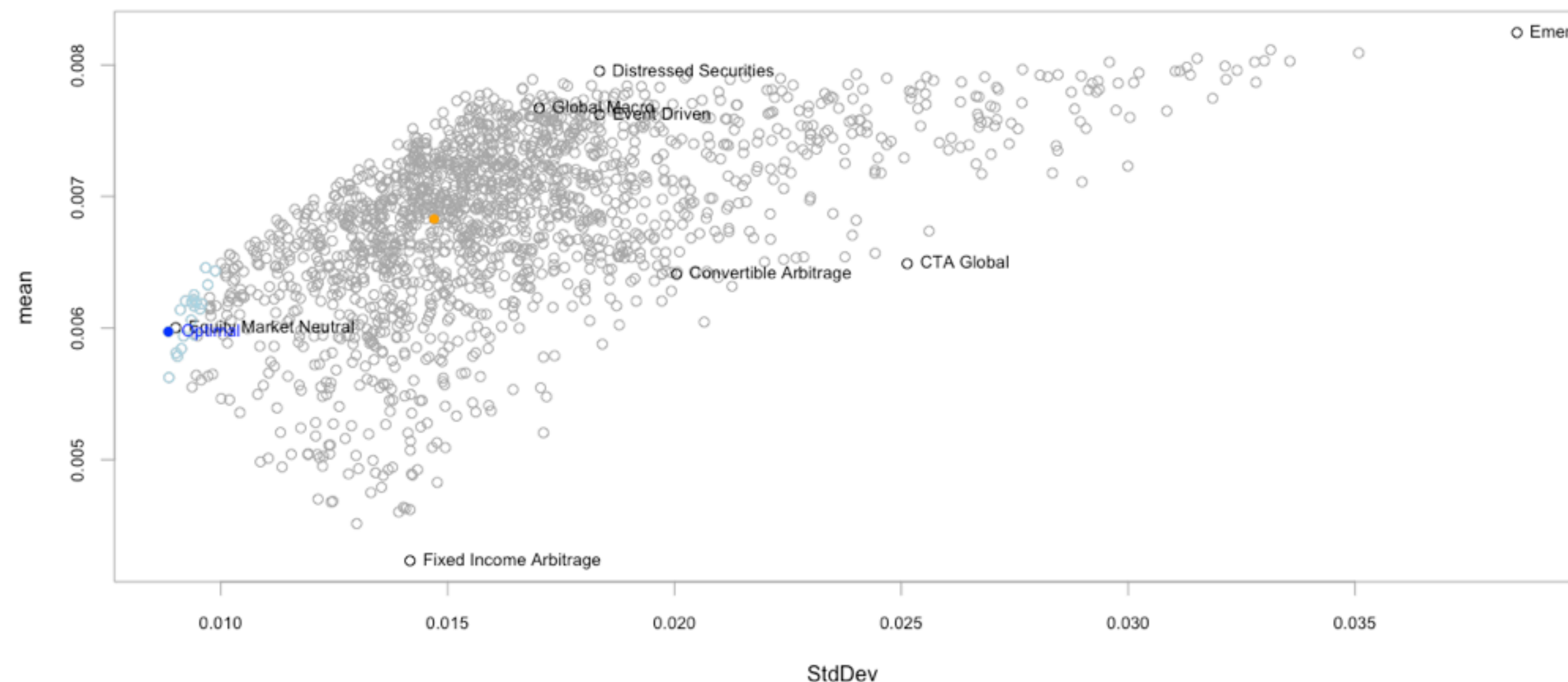
Asset Names
[1] "Convertible Arbitrage" "CTA Global" "Distressed Securities"
[4] "Emerging Markets" "Equity Market Neutral" "Event Driven"
[7] "Fixed Income Arbitrage" "Global Macro"

Constraints
Enabled constraint types
- full_investment
- long_only

Objectives:
Enabled objective names
- mean
- StdDev
```

# Mean - Standard Deviation Example: Optimize

```
# Run optimization and chart results in risk-reward space  
> opt <- optimize.portfolio(data, portfolio = port_spec,  
                             optimize_method = "random",  
                             trace = TRUE)  
  
> chart.RiskReward(opt, risk.col = "StdDev", return.col = "mean",  
                    chart.assets = TRUE)
```





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**Let's practice!**



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# Challenges of Portfolio Optimization



# Challenges:

- Many solvers are not specific to portfolio optimization
- Understanding the capabilities and limits of solvers to select the appropriate solver for the problem or formulate the problem to fit the solver
- Difficult to switch between solvers
- Closed-Form solver (eg. quadratic programming)
- Global solver (eg. differential evolution optimization)

# Quadratic Utility

Maximize:  $w^T * \mu - \lambda * w^T * \Sigma * w$

Subject To:

- $w_i \geq 0$
- $\sum_{i=1}^n w_i = 1$

Where:

- $w$  is the weight vector
- $\mu$  is the expected return vector
- $\lambda$  is the risk aversion parameter
- $\Sigma$  is the variance - covariance matrix

# Quadratic Programming Solver

Use the R package `quadprog` to solve the quadratic utility optimization problem.

`solve.QP()` solves quadratic programming problems of the form:

- $$\min(-d^T b + \frac{1}{2} b^T D b)$$

Subject to the constraint:

- $$A^T b \geq b_0$$

# Quadratic Utility Optimization

```
# Load quadprog
> library(quadprog)
> data(edhec)
> dat <- edhec[,1:4]

# Create the constraint matrix
> Amat <- cbind(1, diag(ncol(dat)), -diag(ncol(dat)))

# Create the constraint vector
> bvec <- c(1, rep(0, ncol(dat)), -rep(1, ncol(dat)))

# Create the objective matrix
> Dmat <- 10 * cov(dat)

# Create the objective vector
> dvec <- colMeans(dat)

# Specify the number of equality constraints
> meq <- 1

# Solve the optimization problem
> opt <- solve.QP(Dmat, dvec, Amat, bvec, meq)
```



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# **Introduction to PortfolioAnalytics**

# PortfolioAnalytics

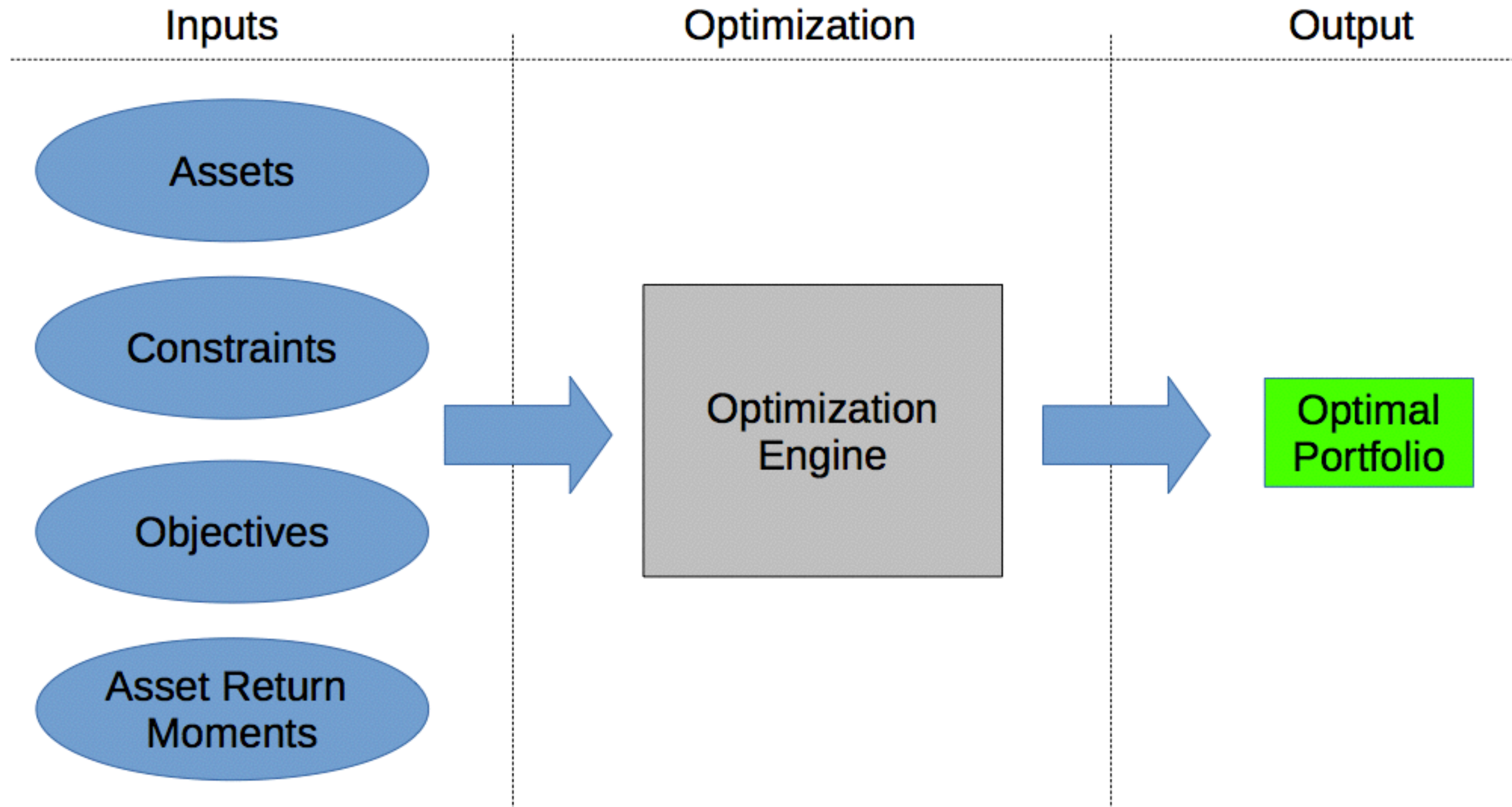
PortfolioAnalytics is designed to provide numerical solutions and visualizations for portfolio optimization problems with complex constraints and objectives.

Supports:

- Multiple and modular constraint and objective types
- An objective function can be any valid R function
- User defined moment functions (covariance matrix, return projections)
- Visualizations
- Solver agnostic
- Parallel computing



# PortfolioAnalytics Framework







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