How good is the Bayes Posterior in Deep Neural Networks really?

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Bayesian Learning Series (#11)

Robotic Vision Lab (RVL) Weekly Seminars 03/03/2021

Outline

- 1 Introduction
 - Bayesian Deep Learning
 - Why should Bayes (T=1) be better?

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Introduction

(in the past five years)

Inference procedures have been developed that allow for **Bayesian inference in Deep Neural Networks**

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- Efficiently approximate

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- Algorithmic progress
- Improved uncertainty quantification

(in the past five years)

Inference procedures have been developed that allow for **Bayesian inference in Deep Neural Networks**

- Increasingly accurate
- Efficiently approximate
 - +
- Algorithmic progress
- Improved uncertainty quantification and sample efficiency

Introduction

(as of early 2020)

Despite all that, ...

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 No publicized deployments of Bayesian neural networks in industrial practice

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Lnt roduction

Introduction

Cast doubts on,

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 current understanding of Bayes posteriors in popular deep neural networks

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 Bayesian posterior predictives yield systematically worse predictions compared to simpler methods (e.g., point estimates obtained from SGD)

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- Bayesian posterior predictives yield systematically worse predictions compared to simpler methods (e.g., point estimates obtained from SGD)
- predictive performance improved through use of a cold posterior that overcounts evidence.

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- Put forward several hypotheses that could explain cold posteriors

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- Put forward several hypotheses that could explain cold posteriors
- **Evaluate** hypotheses through experiments
- **Question** the goal of accurate posterior approximations in Bayesian Deep Learning

Introduction

Question the goal of accurate posterior approximations

■ If the true Bayes posterior is poor, ...

Introduction

Question the goal of accurate posterior approximations

If the true Bayes posterior is poor, what is the use of more accurate approximations?

Question the goal of accurate posterior approximations

- If the true Bayes posterior is poor, what is the use of more accurate approximations?
- Time to focus on understanding of origin of improved performance of cold posteriors

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- lacktriangleright training dataset $\mathcal{D} = \{x_i, y_i\}_{i=1,\dots,n}$
- lacktriangle probabilistic model $p(y|x, m{\theta})$
- to minimize regularized cross-entropy objective

$$L(\boldsymbol{\theta}) := -\frac{1}{n} \sum_{i=1}^{n} \log p(y_i|x_i, \boldsymbol{\theta}) + \Omega(\boldsymbol{\theta})$$
 (1)

Bayesian Deep Learning

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Bayesian Deep Learning

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- do **not** optimize for a *single* likely model
- instead want to discover **all** likely models
- **approximate** the **posterior distribution** over model parameters, $p(\theta|\mathcal{D}) \propto exp(-U(\theta)/T)$, where $U(\theta)$ is the **posterior energy function**,

$$U(\boldsymbol{\theta}) := -\sum_{i=1}^{n} \log p(y_i|x_i, \boldsymbol{\theta}) - \log p(\boldsymbol{\theta})$$
 (2)

■ Given $p(\theta|\mathcal{D})$, we *predict* on a new instance x, by averaging over all likely models,

$$p(y|x,\mathcal{D}) = \int p(y|x,\boldsymbol{\theta})p(\boldsymbol{\theta}|\mathcal{D})d\boldsymbol{\theta},$$
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where (3) is also known as **posterior predictive** or **Bayes ensemble**.

Bayesian Deep Learning

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Bayesian Deep Learning

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Bayesian Deep Learning

- solving (3) exactly is not possible
- instead approximate it using sample approximation $p(y|x,\mathcal{D}) \approx \frac{1}{S} \sum_{s=1}^{S} p(y|x, \boldsymbol{\theta}^{(s)})$, where $\boldsymbol{\theta}^{(s)}$ is approximately sampled from $p(\boldsymbol{\theta}|\mathcal{D})$

Bayesian Deep Learning

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Cold Posteriors: among all temperized posteriors the best posterior predictive performance on holdout data is achieved at temperature $\mathsf{T} < 1$.

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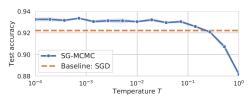


Figure 1. The "cold posterior" effect: for a ResNet-20 on CIFAR-10 we can improve the generalization performance significantly by cooling the posterior with a temperature $T\ll 1$, deviating from the Bayes posterior $p(\boldsymbol{\theta}|\mathcal{D})\propto \exp(-U(\boldsymbol{\theta})/T)$ at T=1.

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Why expect that predictions made by the *ensemble model* (3) could improve over predictions made at a single well-chosen parameter?

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Introduction
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Why should Bayes (T=1) be better?

Three reasons:

■ **Theory**: known that (3) can dominate common point-wise estimators based on likelihood, even in case of misspecification

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- **Theory**: known that (3) can dominate common point-wise estimators based on likelihood, even in case of misspecification
- Classical empirical evidence: for classical statistical models, averaged predictions (3) have been observed to be more robust in practice
- Model averaging:recent deep learning models based on deterministic model averages have shown good predictive performance

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- Note that a large body of work in Bayesian Deep Learning is motivated by the assertion that predicting using (3) is desirable
- Authors confront the assertion through simple experiments
- Show that our understanding of the Bayes posterior in deep models is limited

Contributions

■ **Demonstrate** two models and tasks (ResNet-20 on CIFAR-10 and CNN-LSTM on IMDB) that the Bayes posterior predictive has **poor performance** compared to SGD-trained models

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- Put forth and systematically examine hypotheses that could explain the observed behaviour

Contributions

- **Demonstrate** two models and tasks (ResNet-20 on CIFAR-10 and CNN-LSTM on IMDB) that the Bayes posterior predictive has **poor performance** compared to SGD-trained models
- Put forth and systematically examine hypotheses that could explain the observed behaviour
- Introduce two new diagnostic tools for assessing the approximation quality of stochastic gradient Markov chain Monte Carlo methods (SG-MCMC) and demonstrate that the posterior is accurately simulated by existing SG-MCMC methods