

# Options Part 4

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# Calculating PNL (1 of 8)

- ▶ Suppose you trade an option  $\mathcal{O}$  at a price  $P$  on trade-date  $T_1$ .
- ▶ Suppose you hold the option until expiration, which is trade-date  $T_n$ .
- ▶ The letter  $i$  will serve as an index over the trade-dates, so  $i = 1, \dots, n$ .

## Calculating PNL (2 of 8)

- ▶ Let  $B_i$  and  $A_i$  be the end-of-day bid/ask prices of the option for trade-date  $T_i$ .
- ▶ Note that  $B_n = A_n = \text{option-payoff}$ .
- ▶  $D_i$  - daily PNL for the trade as of end-of-day  $T_i$ .
- ▶  $C_i$  - trade-to-date (cumulative) PNL for the trade as of end-of-day  $T_i$ .
- ▶ **Intuition:** The cumulative PNL on a trade is how much money you make if you unwind the trade at current market values.

## Calculating PNL (3 of 8)

*Cummulative as Sum of Daily:* **BUY**

$$D_i = \begin{cases} B_1 - P & i = 1 \\ B_i - B_{i-1} & i > 1 \end{cases}$$

$$C_i = \sum_{k=1}^i D_k$$

**Exercise:** Show that  $C_j = B_j - P$ .

## Calculating PNL (4 of 8)

*Cummulative as Sum of Daily:* **SELL**

$$D_i = \begin{cases} P - A_1 & i = 1 \\ A_{i-1} - A_i & i > 1 \end{cases}$$

$$C_i = \sum_{k=1}^i D_k$$

**Exercise:** Show that  $C_i = P - A_i$ .

## Calculating PNL (5 of 8)

*Daily as Change in Cumulative:* **BUY**

$$C_i = B_i - P$$

$$D_i = \begin{cases} C_1 & i = 1 \\ C_i - C_{i-1} & i > 1 \end{cases}$$

**Exercise:** Show that both formulations of  $D_i$  are equivalent.

## Calculating PNL (6 of 8)

*Daily as Change in Cumulative:* **SELL**

$$C_i = P - A_i$$

$$D_i = \begin{cases} C_1 & i = 1 \\ C_i - C_{i-1} & i > 1 \end{cases}$$

**Exercise:** Show that both formulations of  $D_i$  are equivalent.

## Calculating PNL (7 of 8)

- ▶ Suppose on 9/16/2013 we buy the 169 SPY expiring 9/21, paying EOD Ask.
- ▶ Here is the price data for that option until expiration:

```
## # A tibble: 5 x 3
##   trade_date    bid    ask
##   <date>      <dbl> <dbl>
## 1 2013-09-16  0.82   0.84
## 2 2013-09-17  0.580  0.59
## 3 2013-09-18  0.09   0.1
## 4 2013-09-19  0.05   0.06
## 5 2013-09-20  0       0
```



# Calculating PNL (8 of 8)

**Exercise:** Verify the following PNL calculations.

```
## # A tibble: 5 x 5
##   trade_date   bid   ask    D_i    C_i
##   <date>     <dbl> <dbl>   <dbl> <dbl>
## 1 2013-09-16 0.82   0.84 -0.02  -0.02
## 2 2013-09-17 0.580   0.59 -0.24  -0.26
## 3 2013-09-18 0.09    0.1  -0.49  -0.75
## 4 2013-09-19 0.05    0.06 -0.0400 -0.79
## 5 2013-09-20 0        0    -0.05  -0.84
```

# Black-Scholes-Merton Formula (1 of 1)

$$m = \text{BSM}(p/c, K, T, S_t, \sigma, \delta, r)$$

## Contract Features

- ▶  $p/c$  - put or call
- ▶  $K$  - strike price
- ▶  $T$  - expiration date (time to expiration)

## Market Values

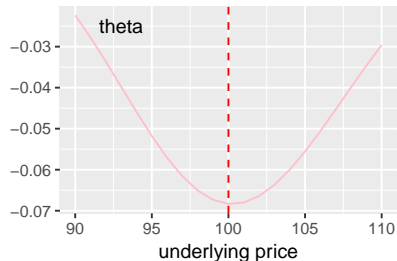
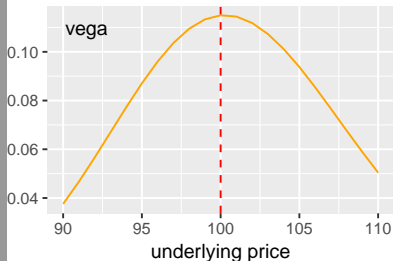
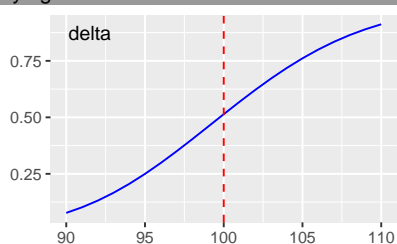
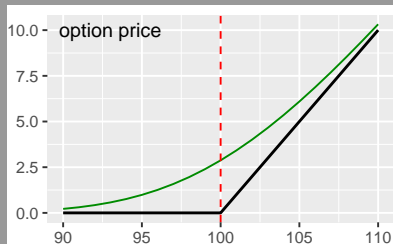
- ▶  $S_t$  - current underlying price
- ▶  $\sigma$  - estimate of the standard deviation log-return of the price of underlying between now and expiration
- ▶  $\delta$  - estimate of dividends paid over the life of the option
- ▶  $r$  - risk-free interest rate

# Black-Scholes-Merton Formula (2 of)

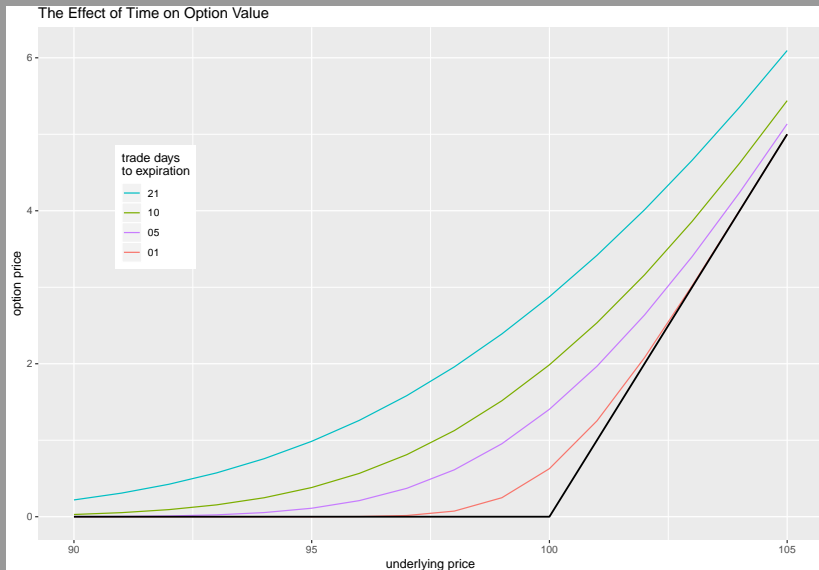
- ▶ For this class, we won't need to examine the BSM formula too closely, or write a BSM function from scratch.
- ▶ A more important skill will be to use pre-existing BSM functions (and implied volatility functions) in analysis code.
- ▶ I usually use the `fOptions` package.
- ▶ **Exercise:** Install the `fOptions` package and quickly read through pp 22-27 of its documentation PDF.

# Greeks Preview (1 of 4)

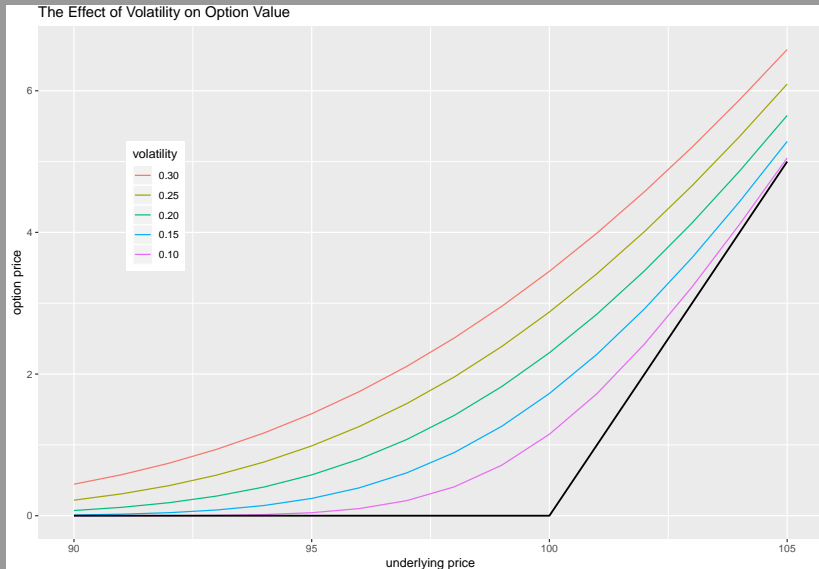
Greeks vs Underlying Price



# Greeks Preview (2 of 4)



# Greeks Preview (3 of 4)



# Greeks Preview (4 of 4)

## Some Facts

1. Optionality - as evidenced by vega, theta, gamma - is greatest when options are ATM.
2. Theta is Negative: an option loses value as it nears expiration.
3. Vega is Positive: the more volatile the underlying, the more valuable the option.
4. Regarding Delta:
  - ▶ Approximately 0.50 when option is ATM.
  - ▶ Approaches 0.00 as option gets farther out of the money.
  - ▶ Approaches 1.00 as option goes farther in the money.
  - ▶ *VERY roughly* the probability that the option expires ITM.
  - ▶ Used to refer to the moneyness of an option.