

## ASSIGNMENT-11.10.4.9

**Question :** Find the value of  $p$  so that the three lines  $3x + y - 2 = 0$ ,  $px + 2y - 3 = 0$  and  $2x - y - 3 = 0$  may intersect at one point.

**Solution :**

$$\begin{pmatrix} 3 & 1 & -2 \\ p & 2 & -3 \\ 2 & -1 & -3 \end{pmatrix} \quad (1)$$

$$\xrightarrow[\substack{R'_2=3R_2-pR_1 \\ R'_3=3R_3-2R_1}]{\phantom{R'_2=3R_2-pR_1}} \begin{pmatrix} 3 & 1 & -2 \\ 0 & 6-p & -9+2p \\ 0 & -5 & -5 \end{pmatrix} \quad (2)$$

$$\xrightarrow{R'_3=R_3(6-p)+5R_2} \begin{pmatrix} 3 & 1 & -2 \\ 0 & 6-p & -9+2p \\ 0 & 0 & -75+15p \end{pmatrix} \quad (3)$$

$$\implies -75 + 15p = 0 \quad (4)$$

$$p = 5 \quad (5)$$

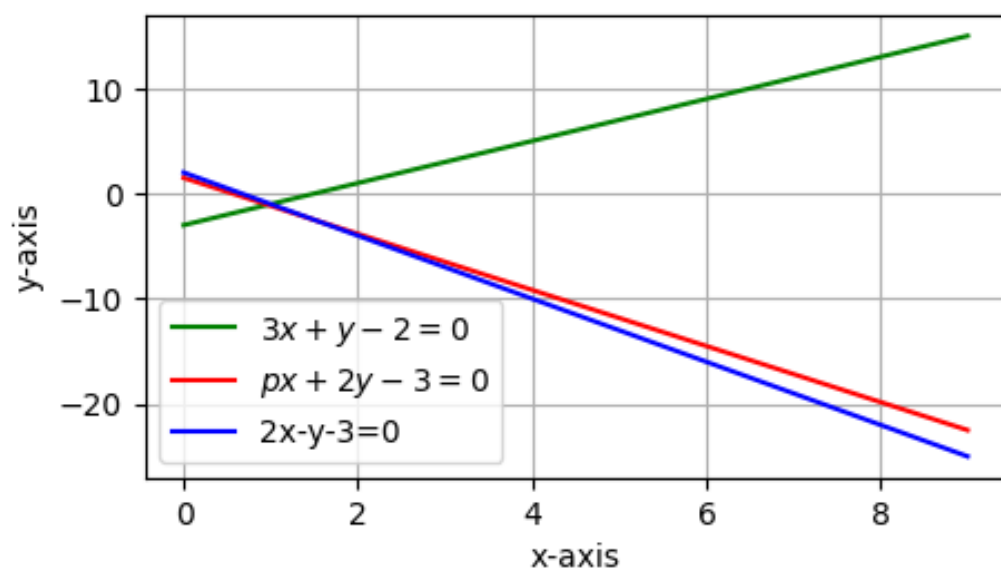


Figure 1: