# Prithvi Poddar 17191 Report 1

June 22, 2020

## 1 Assignment 4

## 2 Prithvi Poddar 17191

## 2.1 Report: Neural Network

In this report, I'll be running a neural network based completely on numpy and inspired from http://neuralnetworksanddeeplearning.com/index.html

The codes can be found in the same directory as this python notebook is.

P.S. Initially I'll be doing all the parameter tuning using train and test set splitting as this model converges quicker than Cross Validation. This will allow us to get better results in less number of epochs. Once we've decided our parameters, we'll finally use Cross validation to see if it gives better accuracy

#### 2.2 Part 1

2.2.1 Importing the neural network module and the data loader

```
[1]: import matplotlib.pyplot as plt
import numpy as np
import network
import data_loader
%matplotlib inline
plt.rcParams['figure.figsize']=(20,10)
```

2.2.2 Before starting, lets take a look at tunable parameters of this linear network model

```
weight_initializer = 'default' or 'large'

cost = 'CrossEntropy' or 'Quadratic'

activation = 'sigmoid' or 'tanh' or 'relu'
```

size = [n1, n2, ...] {where n1=no. of neurons in first layer, n2=no. of neurons in second layer, and so on}

#### 2.2.3 Parameters for training

training\_data, epochs, batch\_size, eta(learning rate), lmbda(regularization factor), test\_data

#### 2.2.4 Loading the training and testing data

We have total 3000 data entries. We'll be dividing it in 2500 for training and 500 for testing

```
[2]: training_data, testing_data = data_loader.load_full_data()
```

# 2.2.5 Now we call the neural network from the network.py file and start tuning our parameters

## 2.2.6 First, no hidden layer

Here we'll determine which cost function, activation function and weight initializer to use:

1. Choosing the weight initializer

'default' sets the weights randomly from gaussian distribution with mean 0 and standard deviation 1/sqrt(number of training data)

'large' sets the weights randomly from gaussian distribution with mean 0 and standard deviation 1

```
[3]: net = network.Linear_Network([784,10], weight_initializer='default')
```

```
[4]: net.SGD(training_data, 30, 10, 0.5, lmbda = 5.0, test_data=testing_data)
```

#### Epoch 1

Training loss: 1.3272248517655656637

Training accuracy: 82.36% Test accuracy: 76.4%

#### Epoch 2

Training loss: 0.71936398376920923024 Training accuracy: 90.8800000000001%

Test accuracy: 84.0%

#### Epoch 3

Training loss: 0.7287727998241616091

Training accuracy: 90.08%

Test accuracy: 81.6%

#### Epoch 4

Training loss: 0.8360652745009499089

Training accuracy: 89.12% Test accuracy: 82.6%

Epoch 5

Training loss: 0.6425745589650592904

Training accuracy: 92.04% Test accuracy: 86.6%

Epoch 6

Training loss: 0.6241366896945118083

Training accuracy: 92.0% Test accuracy: 83.0%

Epoch 7

Training loss: 0.59985113185178247337

Training accuracy: 92.96% Test accuracy: 84.2%

Epoch 8

Training loss: 0.68241411488689877727

Training accuracy: 91.52% Test accuracy: 83.8%

Epoch 9

Training loss: 0.6178573554240523534

Training accuracy: 92.72% Test accuracy: 84.0%

Epoch 10

Training loss: 0.76310250868291614135

Training accuracy: 89.28% Test accuracy: 83.2%

Epoch 11

Training loss: 0.625601111409811858
Training accuracy: 91.6000000000001%

Test accuracy: 84.0%

Epoch 12

Training loss: 0.7855628262008626621

Training accuracy: 87.88% Test accuracy: 82.8%

Epoch 13

Training loss: 0.5769184174395629903

Training accuracy: 93.56% Test accuracy: 85.0%

Training loss: 0.5563355127692802643 Training accuracy: 93.679999999999% Test accuracy: 85.399999999999%

Epoch 15

Training loss: 0.5379903095588351084

Training accuracy: 93.2% Test accuracy: 87.0%

Epoch 16

Training loss: 0.72949905138729781543

Training accuracy: 90.64% Test accuracy: 83.2%

Epoch 17

Training loss: 0.6482803319992067948

Training accuracy: 91.64% Test accuracy: 83.2%

Epoch 18

Training loss: 0.6061266507828651662 Training accuracy: 92.679999999999%

Test accuracy: 85.8%

Epoch 19

Training loss: 0.59069717762839155654

Training accuracy: 92.4% Test accuracy: 85.2%

Epoch 20

Training loss: 0.61283203722174617886

Training accuracy: 92.2%

Test accuracy: 84.399999999999%

Epoch 21

Training loss: 0.57973076543837441326

Training accuracy: 93.56%

Test accuracy: 85.6%

Epoch 22

Training loss: 0.84151611942292329506

Training accuracy: 88.36% Test accuracy: 81.8%

Epoch 23

Training loss: 0.70880471330908518813

Training accuracy: 89.96%

Test accuracy: 83.6%

Epoch 24

Training loss: 0.5461793207742172807

Training accuracy: 92.92%

Test accuracy: 85.3999999999999%

Epoch 25

Training loss: 0.5364074030537711383

Training accuracy: 92.84%

Test accuracy: 86.2%

Epoch 26

Training loss: 0.5921190950516245869 Training accuracy: 92.479999999999%

Test accuracy: 85.0%

Epoch 27

Training loss: 0.7042730509569844694

Training accuracy: 91.0%

Test accuracy: 82.399999999999%

Epoch 28

Training loss: 0.68189131938133071563

Training accuracy: 91.28%

Test accuracy: 84.399999999999%

Epoch 29

Training loss: 0.5808135480988476286

Training accuracy: 93.36%

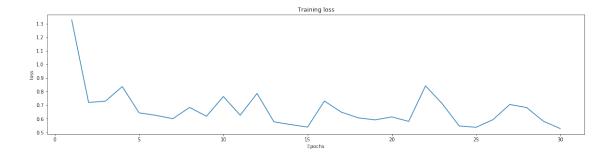
Test accuracy: 84.2%

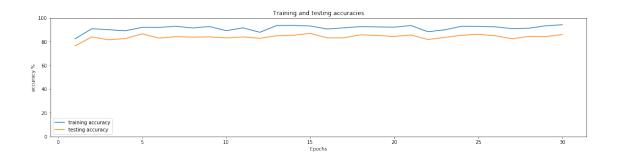
Epoch 30

Training loss: 0.5267710394529381758

Training accuracy: 94.24%

Test accuracy: 86.0%





We get top training accuracy of 93% and test accuracy of 84%

Checking the large weight initializer

```
[5]: net = network.Linear_Network([784,10], weight_initializer='large')
```

[6]: net.SGD(training\_data, 30, 10, 0.5, lmbda = 5.0, test\_data=testing\_data)

Epoch 1

Training loss: 1.4578713093857943548

Training accuracy: 83.56% Test accuracy: 76.0%

Epoch 2

Training loss: 0.89294562377752571017

Training accuracy: 88.44%

Test accuracy: 81.2%

Epoch 3

Training loss: 0.6914466719289004403

Training accuracy: 90.72%

Test accuracy: 83.3999999999999%

Epoch 4

Training loss: 0.70416204213083758145 Training accuracy: 91.479999999999%

Test accuracy: 82.0%

Epoch 5

Training loss: 0.6498968144804360314
Training accuracy: 91.3200000000001%

Test accuracy: 83.0%

Epoch 6

Training loss: 0.7011865655904408734

Training accuracy: 91.56%

Test accuracy: 83.399999999999%

Epoch 7

Training loss: 0.70585561103012643816

Training accuracy: 90.32%

Test accuracy: 82.6%

Epoch 8

Training loss: 0.7205639502113299712

Training accuracy: 89.52%

Test accuracy: 81.2%

Epoch 9

Training loss: 0.601893005602259888

Training accuracy: 92.92%

Test accuracy: 84.6%

Epoch 10

Training loss: 0.64886662271131890844

Training accuracy: 91.4% Test accuracy: 83.8%

Epoch 11

Training loss: 0.58694003587963932534

Training accuracy: 92.24%

Test accuracy: 84.8%

Epoch 12

Training loss: 0.61938680469315643656

Training accuracy: 92.12%

Test accuracy: 84.0%

Epoch 13

Training loss: 0.5812377080604218361 Training accuracy: 92.479999999999%

Test accuracy: 84.2%

Epoch 14

Training loss: 0.5568395041875347067

Training accuracy: 93.16%

Test accuracy: 87.0%

Epoch 15

Training loss: 0.59555967628173598065

Training accuracy: 93.04%

Test accuracy: 84.8%

Training loss: 0.6654119533684015922

Training accuracy: 91.52%

Test accuracy: 82.0%

Epoch 17

Training loss: 0.5900631852942883275

Training accuracy: 92.88%

Test accuracy: 85.2%

Epoch 18

Training loss: 0.555863960001395426

Training accuracy: 93.84%

Test accuracy: 84.8%

Epoch 19

Training loss: 0.57954733397477828925

Training accuracy: 92.84%

Test accuracy: 85.8%

Epoch 20

Training loss: 0.59664816990770241906

Training accuracy: 92.92%

Test accuracy: 83.8%

Epoch 21

Training loss: 0.61190289303504129405

Training accuracy: 92.12%

Test accuracy: 83.6%

Epoch 22

Training loss: 0.7103513545524271277

Training accuracy: 90.32%

Test accuracy: 84.2%

Epoch 23

Training loss: 0.61178790046544688855

Training accuracy: 92.36%

Test accuracy: 83.3999999999999%

Epoch 24

Training loss: 0.60308399103683367525

Training accuracy: 92.08%

Test accuracy: 84.8%

Epoch 25

Training loss: 0.5386263573189866411

Training accuracy: 93.36%

Test accuracy: 84.0%

Epoch 26

Training loss: 0.601493377321824918

Training accuracy: 92.44%

Test accuracy: 83.6%

Epoch 27

Training loss: 0.5593667069569982776

Training accuracy: 92.96%

Test accuracy: 83.8%

Epoch 28

Training loss: 0.58097065791399862047

Training accuracy: 93.04%

Test accuracy: 86.6%

Epoch 29

Training loss: 0.63557041976418269966

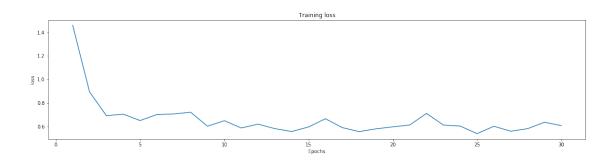
Training accuracy: 91.2% Test accuracy: 84.6%

Epoch 30

Training loss: 0.6067781788950730768

Training accuracy: 93.04%

Test accuracy: 83.2%





'large' weight initializer performs similar to the 'default' initializer with max test accuracy of 84% and training accuracy of 93%

## Hence we stick to 'default' weight initializer

2. Choosing cost function

First we try out the 'Quadratic' cost

```
[7]: net = network.Linear_Network([784,10], weight_initializer='default', ⊔

cost='Quadratic')
```

```
[8]: net.SGD(training_data, 30, 10, 0.5, lmbda = 5.0, test_data=testing_data)
```

Epoch 1

Training loss: 0.14430774391452515734

Training accuracy: 87.12% Test accuracy: 81.6%

Epoch 2

Training loss: 0.124346020914344430095

Training accuracy: 89.44%

Test accuracy: 83.2%

Epoch 3

Training loss: 0.115573315212080905765

Training accuracy: 89.96%

Test accuracy: 84.399999999999%

Epoch 4

Training loss: 0.10971693140937655258

Training accuracy: 90.44%

Test accuracy: 84.399999999999%

Epoch 5

Training loss: 0.10820816462001523951

Training accuracy: 90.4% Test accuracy: 85.2%

Epoch 6

Training loss: 0.10918127544937454743

Training accuracy: 90.36%

Test accuracy: 84.2%

Epoch 7

Training loss: 0.10515369190497852874

Training accuracy: 91.24%

Test accuracy: 85.399999999999%

Epoch 8

Training loss: 0.10510713413921377183

Training accuracy: 91.12%

Test accuracy: 84.8%

Epoch 9

Training loss: 0.10571742606670785589

Training accuracy: 90.8%

Test accuracy: 85.399999999999%

Epoch 10

Training loss: 0.103638973411906549415

Training accuracy: 91.28%

Test accuracy: 86.0%

Epoch 11

Training loss: 0.100888317744808204255

Training accuracy: 92.08%

Test accuracy: 84.399999999999%

Epoch 12

Training loss: 0.101918052915637961766

Training accuracy: 91.0% Test accuracy: 84.8%

Epoch 13

Training loss: 0.10527601839393982388

Training accuracy: 90.84%

Test accuracy: 84.8%

Epoch 14

Training loss: 0.10327954535826308309

Training accuracy: 91.72%

Test accuracy: 85.399999999999%

Epoch 15

Training loss: 0.10295923682437099695 Training accuracy: 91.60000000000001%

Test accuracy: 84.2%

Epoch 16

Training loss: 0.099238975557068284096 Training accuracy: 91.6000000000001%

Test accuracy: 85.6%

Training loss: 0.100934193076398050036

Training accuracy: 91.64%

Test accuracy: 84.2%

Epoch 18

Training loss: 0.10092141939111313164

Training accuracy: 91.64%

Test accuracy: 84.2%

Epoch 19

Training loss: 0.101285341750599067025

Training accuracy: 91.72%

Test accuracy: 86.0%

Epoch 20

Training loss: 0.10120532614748231064

Training accuracy: 91.28%

Test accuracy: 85.0%

Epoch 21

Training loss: 0.100735801236247800164

Training accuracy: 91.56%

Test accuracy: 85.399999999999%

Epoch 22

Training loss: 0.099846189579484215685 Training accuracy: 91.0800000000001%

Test accuracy: 85.6%

Epoch 23

Training loss: 0.10024747364784468513

Training accuracy: 91.4%

Test accuracy: 85.399999999999%

Epoch 24

Training loss: 0.10022707787123517257

Training accuracy: 91.92%

Test accuracy: 85.0%

Epoch 25

Training loss: 0.098565199902015944624

Training accuracy: 91.88%

Test accuracy: 85.399999999999%

Epoch 26

Training loss: 0.100775069707188423974
Training accuracy: 91.6000000000001%

Test accuracy: 84.6%

Epoch 27

Training loss: 0.09849728591976504718

Training accuracy: 91.8% Test accuracy: 85.6%

Epoch 28

Training loss: 0.102366198436458460494

Training accuracy: 91.4% Test accuracy: 85.2%

Epoch 29

Training loss: 0.10038632306984616855

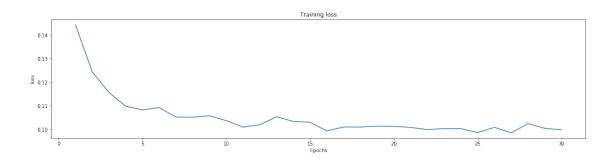
Training accuracy: 91.28%

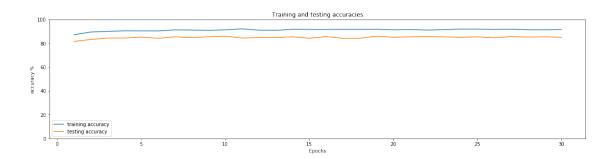
Test accuracy: 85.399999999999%

Epoch 30

Training loss: 0.099725184937177996566
Training accuracy: 91.6000000000001%

Test accuracy: 85.0%





'Quadratic' cost gives training accuracy of 91% and test accuracy of 85%

Trying 'CrossEntropy'

[10]: net.SGD(training\_data, 30, 10, 0.5, lmbda = 5.0, test\_data=testing\_data)

#### Epoch 1

Training loss: 1.1400620321095680596

Training accuracy: 84.84%
Test accuracy: 78.8%

#### Epoch 2

Training loss: 1.1351648544076420024

Training accuracy: 81.72% Test accuracy: 72.2%

#### Epoch 3

Training loss: 0.65034009401556294516

Training accuracy: 91.64% Test accuracy: 85.0%

#### Epoch 4

Training loss: 0.7527512377906450604

Training accuracy: 90.32% Test accuracy: 82.8%

#### Epoch 5

Training loss: 0.6661909609644937047

Training accuracy: 91.24% Test accuracy: 84.2%

#### Epoch 6

Training loss: 0.63578586763901611236 Training accuracy: 92.60000000000001%

Test accuracy: 84.6%

#### Epoch 7

Training loss: 0.64226355571199650633

Training accuracy: 91.64%

Test accuracy: 81.399999999999%

## Epoch 8

Training loss: 0.5922074087873146851

Training accuracy: 92.56%

Test accuracy: 84.399999999999%

## Epoch 9

Training loss: 0.63043149207374716317

Training accuracy: 92.759999999999%

Test accuracy: 85.2%

Epoch 10

Training loss: 0.8473234829533657159

Training accuracy: 89.4% Test accuracy: 81.6%

Epoch 11

Training loss: 0.60644628140989874333

Training accuracy: 91.92% Test accuracy: 83.0%

Epoch 12

Training loss: 1.0088905407902601304 Training accuracy: 82.679999999999%

Test accuracy: 76.0%

Epoch 13

Training loss: 0.54999673055911138666 Training accuracy: 93.52000000000001%

Test accuracy: 85.2%

Epoch 14

Training loss: 0.5722264926432652073

Training accuracy: 93.04%

Test accuracy: 86.8%

Epoch 15

Training loss: 0.65501607543581852203

Training accuracy: 91.72%

Test accuracy: 82.399999999999%

Epoch 16

Training loss: 0.5986362680342832776

Training accuracy: 91.8%

Test accuracy: 84.399999999999%

Epoch 17

Training loss: 0.5761357506820018151

Training accuracy: 92.64%

Test accuracy: 84.8%

Epoch 18

Training loss: 0.56294678282739809406

Training accuracy: 92.64%

Test accuracy: 84.8%

Training loss: 0.7116680829999793707

Training accuracy: 90.44%

Test accuracy: 82.399999999999%

Epoch 20

Training loss: 0.61512079966337630707

Training accuracy: 92.36%

Test accuracy: 86.2%

Epoch 21

Training loss: 0.8908456305872533953

Training accuracy: 87.64%

Test accuracy: 81.0%

Epoch 22

Training loss: 0.5851243713355452483

Training accuracy: 92.04%
Test accuracy: 85.0%

Epoch 23

Training loss: 0.55932565572145434823

Training accuracy: 93.84%

Test accuracy: 86.4%

Epoch 24

Training loss: 0.73933033889102701497

Training accuracy: 90.96%

Test accuracy: 84.0%

Epoch 25

Training loss: 0.5862781926799022349

Training accuracy: 93.24%

Test accuracy: 84.0%

Epoch 26

Training loss: 0.63679211979251014507

Training accuracy: 92.04%

Test accuracy: 83.8%

Epoch 27

Training loss: 0.5848565171300773471

Training accuracy: 93.24%

Test accuracy: 85.399999999999%

Epoch 28

Training loss: 0.5411677063095106016

Training accuracy: 93.72%

Test accuracy: 86.0%

Epoch 29

Training loss: 0.7150090699505372132

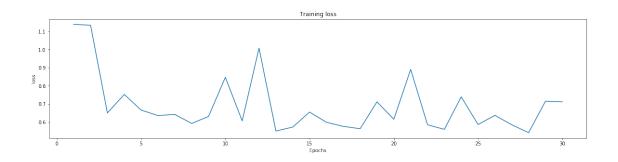
Training accuracy: 89.52%

Test accuracy: 84.399999999999%

Epoch 30

Training loss: 0.7116959135353462823 Training accuracy: 90.039999999999%

Test accuracy: 82.0%





We see that 'CrossEntropy' gives a slightly better performance of 93% traing and 85% testing accuracy.

But we notice from the loss graph that the drop in loss for Quadratic is much smoother than for CrossEntropy.

For now we'll stick to CrossEntropy and hope that the loss graph for the CrossEntropy function will smoothen out as we do further parameter tunning. If not then we'll visti this again and do another comparison between these two after the parameters have been set.

#### 3. Choosing activation function

First we try 'sigmoid'

```
[11]: net = network.Linear_Network([784,10], weight_initializer='default',__
       ⇔cost='Quadratic',
                                   activation = 'sigmoid')
[12]: net.SGD(training_data, 30, 10, 0.5, lmbda = 5.0, test_data=testing_data)
     Epoch 1
     Training loss: 0.14122971164088507967
     Training accuracy: 87.56%
     Test accuracy: 81.6%
     Epoch 2
     Training loss: 0.12183825604439538239
     Training accuracy: 89.8800000000001%
     Test accuracy: 82.6%
     Epoch 3
     Training loss: 0.11069726174276199918
     Training accuracy: 90.64%
     Test accuracy: 84.6%
     Epoch 4
     Training loss: 0.111057099726467961
     Training accuracy: 90.72%
     Test accuracy: 84.0%
     Epoch 5
     Training loss: 0.10838269080122015666
     Training accuracy: 90.32%
     Test accuracy: 83.2%
     Epoch 6
     Training loss: 0.11343002714292998762
     Training accuracy: 89.84%
     Test accuracy: 83.6%
     Epoch 7
     Training loss: 0.105037625832915775505
     Training accuracy: 91.24%
     Test accuracy: 84.8%
     Epoch 8
     Training loss: 0.103404341202121716296
     Training accuracy: 91.96%
```

18

Test accuracy: 84.8%

Epoch 9

Training loss: 0.10419560153325619538

Training accuracy: 91.16% Test accuracy: 83.8%

Epoch 10

Training loss: 0.10144401874467356361

Training accuracy: 91.8% Test accuracy: 84.6%

Epoch 11

Training loss: 0.102604120742263210374

Training accuracy: 91.16% Test accuracy: 85.2%

Epoch 12

Training loss: 0.102964981346572091526

Training accuracy: 90.84% Test accuracy: 85.8%

Epoch 13

Training loss: 0.1066126987253369264

Training accuracy: 90.96% Test accuracy: 85.0%

Epoch 14

Training loss: 0.10742839994708550137

Training accuracy: 91.2%

Test accuracy: 83.399999999999%

Epoch 15

Training loss: 0.101078667480840834095

Training accuracy: 91.36% Test accuracy: 85.0%

Epoch 16

Training loss: 0.10167868850154676023

Training accuracy: 91.72% Test accuracy: 85.0%

Epoch 17

Training loss: 0.10119786940045463477

Training accuracy: 91.84%

Test accuracy: 85.0%

Epoch 18

Training loss: 0.10217698647409774651

Training accuracy: 91.16%

Test accuracy: 85.399999999999%

Training loss: 0.10139874662149048952

Training accuracy: 91.0% Test accuracy: 84.2%

Epoch 20

Training loss: 0.0987169394456307345

Training accuracy: 91.8% Test accuracy: 84.8%

Epoch 21

Training loss: 0.103417567356149265744

Training accuracy: 91.36% Test accuracy: 85.0%

Epoch 22

Training loss: 0.1077361743222739469

Training accuracy: 91.4% Test accuracy: 83.8%

Epoch 23

Training loss: 0.098269939442113426556

Training accuracy: 91.96%

Test accuracy: 85.399999999999%

Epoch 24

Training loss: 0.10101376421813314317

Training accuracy: 91.4% Test accuracy: 84.0%

Epoch 25

Training loss: 0.10143763757343051315

Training accuracy: 91.92% Test accuracy: 85.0%

Epoch 26

Training loss: 0.09920781098870465662

Training accuracy: 92.0% Test accuracy: 85.0%

Epoch 27

Training loss: 0.101642044614305744825 Training accuracy: 91.479999999999%

Test accuracy: 85.0%

Epoch 28

Training loss: 0.102940995343994103054

Training accuracy: 91.6000000000001%

Test accuracy: 85.2%

Epoch 29

Training loss: 0.10024126340416166763

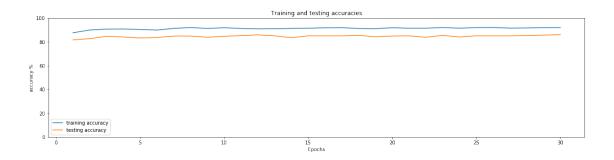
Training accuracy: 91.88% Test accuracy: 85.6%

Epoch 30

Training loss: 0.1006897247175448399

Training accuracy: 91.92% Test accuracy: 86.0%





Next we try 'tanh'

```
[14]: net.SGD(training_data, 30, 10, 0.5, lmbda = 5.0, test_data=testing_data)
```

Epoch 1

Training loss: 3.2303686435523601016

Training accuracy: 23.76%

Test accuracy: 25.8%

Epoch 2

Training loss: 2.8391497719870323316 Training accuracy: 51.51999999999996% Test accuracy: 47.1999999999996%

Epoch 3

Training loss: 3.0352400608258571068

Training accuracy: 52.72%

Test accuracy: 54.6%

Epoch 4

Training loss: 2.935100450170637811

Training accuracy: 18.2% Test accuracy: 18.6%

Epoch 5

Training loss: 3.1471953116887459011

Training accuracy: 37.6% Test accuracy: 35.0%

Epoch 6

Training loss: 3.0969188531546436255

Training accuracy: 16.16%

Test accuracy: 16.2%

Epoch 7

Training loss: 2.8658553208136144576

Training accuracy: 45.4% Test accuracy: 44.4%

Epoch 8

Training loss: 2.9958681236315074536

Training accuracy: 56.56%

Test accuracy: 53.2%

Epoch 9

Training loss: 2.8750594990381577432

Training accuracy: 40.64%

Test accuracy: 39.4%

Epoch 10

Training loss: 2.821630697405130503
Training accuracy: 54.12000000000000%

Test accuracy: 49.2%

Epoch 11

Training loss: 2.6034395529350308773
Training accuracy: 61.040000000000000%

Test accuracy: 56.0000000000001%

Epoch 12

Training loss: 2.6777453698931522534 Training accuracy: 58.3200000000001%

Test accuracy: 54.6%

Epoch 13

Training loss: 2.6481718717010123277

Training accuracy: 57.24% Test accuracy: 55.2%

Epoch 14

Training loss: 2.7441753971279190145

Training accuracy: 22.6% Test accuracy: 22.2%

Epoch 15

Training loss: 2.7118954620663923759

Training accuracy: 39.36% Test accuracy: 34.0%

Epoch 16

Training loss: 2.8885067015254884827 Training accuracy: 24.2799999999998% Test accuracy: 23.5999999999998%

Epoch 17

Training loss: 3.2009306612989373016

Training accuracy: 40.48% Test accuracy: 41.0%

Epoch 18

Training loss: 2.8446437104100511053
Training accuracy: 50.2399999999999%

Test accuracy: 46.0%

Epoch 19

Training loss: 3.065784714651874284

Training accuracy: 53.44%

Test accuracy: 49.8%

Epoch 20

Training loss: 2.762009200160105247

Training accuracy: 51.2% Test accuracy: 46.2%

Training loss: 2.9784520175320587086

Training accuracy: 51.04% Test accuracy: 48.0%

Epoch 22

Training loss: 2.6870582312597372815

Training accuracy: 52.32% Test accuracy: 43.4%

Epoch 23

Training loss: 3.1708376953627454556

Training accuracy: 44.84% Test accuracy: 39.4%

Epoch 24

Training loss: 2.836906156888301584

Training accuracy: 41.32% Test accuracy: 37.4%

Epoch 25

Training loss: 3.015421873947301406 Training accuracy: 41.19999999999996%

Test accuracy: 38.4%

Epoch 26

Training loss: 3.1471990475947490733 Training accuracy: 31.3199999999997% Test accuracy: 28.7999999999997%

Epoch 27

Training loss: 3.3073441086690658689

Training accuracy: 51.6% Test accuracy: 45.2%

Epoch 28

Training loss: 2.521124851750993633

Training accuracy: 68.24% Test accuracy: 66.2%

Epoch 29

Training loss: 2.7465482805800106004

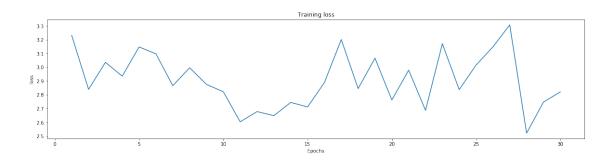
Training accuracy: 47.0% Test accuracy: 45.0%

Epoch 30

Training loss: 2.8205753850486988596

Training accuracy: 57.04%

Test accuracy: 53.800000000000004%





Next is 'relu'

[16]: net.SGD(training\_data, 30, 10, 0.5, lmbda = 5.0, test\_data=testing\_data)

## Epoch 1

Training loss: 0.4998753750037329

Training accuracy: 10.16%

Test accuracy: 11.600000000000001%

Epoch 2

Training loss: 0.5

Training accuracy: 10.12%

Test accuracy: 11.600000000000001%

Epoch 3

Training loss: 0.5

Training accuracy: 10.12%

Test accuracy: 11.600000000000001%

Training loss: 0.49998475007594734
Training accuracy: 10.2800000000001%
Test accuracy: 11.60000000000001%

Epoch 5

Training loss: 0.4999076350386032

Training accuracy: 10.16%

Test accuracy: 11.60000000000001%

Epoch 6

Training loss: 0.4995488523378649

Training accuracy: 10.24%

Test accuracy: 11.600000000000001%

Epoch 7

Training loss: 0.5000017563420155

Training accuracy: 10.12%

Test accuracy: 11.600000000000001%

Epoch 8

Training loss: 0.49999794468983255

Training accuracy: 10.12%

Test accuracy: 11.7999999999999%

Epoch 9

Training loss: 0.500003075029748

Training accuracy: 10.12%

Test accuracy: 11.600000000000001%

Epoch 10

Training loss: 0.4995272756174767

Training accuracy: 10.36%

Test accuracy: 11.600000000000001%

Epoch 11

Training loss: 0.4994626165659598

Training accuracy: 10.4%

Test accuracy: 11.600000000000001%

Epoch 12

Training loss: 0.5000008708440793

Training accuracy: 10.12%

Test accuracy: 11.600000000000001%

Epoch 13

Training loss: 0.5000001957784715

Training accuracy: 10.12%

Test accuracy: 11.600000000000001%

Epoch 14

Training loss: 0.5000006908692093

Training accuracy: 10.12%

Test accuracy: 11.600000000000001%

Epoch 15

Training loss: 0.5000002145128356

Training accuracy: 10.12%

Test accuracy: 11.600000000000001%

Epoch 16

Training loss: 0.5000022365878521

Training accuracy: 10.08%

Test accuracy: 11.600000000000001%

Epoch 17

Training loss: 0.4996294796616622

Training accuracy: 10.36%

Test accuracy: 11.7999999999999%

Epoch 18

Training loss: 0.49972734299694477

Training accuracy: 10.2%

Test accuracy: 11.600000000000001%

Epoch 19

Training loss: 0.49960776562871306

Training accuracy: 10.16%

Test accuracy: 11.600000000000001%

Epoch 20

Training loss: 0.4996009639194086

Training accuracy: 10.2%

Test accuracy: 11.600000000000001%

Epoch 21

Training loss: 0.4987192194041874

Training accuracy: 10.6399999999999% Test accuracy: 11.799999999999%

Epoch 22

Training loss: 0.5000006661991736

Training accuracy: 10.12%

Test accuracy: 11.600000000000001%

Training loss: 0.5000005869100168

Training accuracy: 10.12%

Test accuracy: 11.600000000000001%

Epoch 24

Training loss: 0.49740447488982736

Training accuracy: 10.92%

Test accuracy: 12.4%

Epoch 25

Training loss: 0.5000008572344935

Training accuracy: 10.12%

Test accuracy: 11.600000000000001%

Epoch 26

Training loss: 0.5000002644267925

Training accuracy: 10.12%

Test accuracy: 11.600000000000001%

Epoch 27

Training loss: 0.4999995713251814

Training accuracy: 10.16%

Test accuracy: 11.600000000000001%

Epoch 28

Training loss: 0.5000008954464134

Training accuracy: 10.04000000000001% Test accuracy: 11.60000000000001%

Epoch 29

Training loss: 0.500000089223235

Training accuracy: 10.12%

Test accuracy: 11.600000000000001%

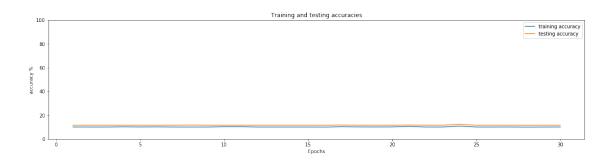
Epoch 30

Training loss: 0.49980072677276055

Training accuracy: 10.16%

Test accuracy: 11.600000000000001%





Hence we can clearly see that 'sigmoid' is the best option we have

Since our initial parameters are set, we can move on to the number of layers and the stochastic gradient parameter tuning. I haqve already set the above parameters as default for our network so that we don't have to call them agian and again

#### 2.2.7 Now we decide the number of neurons and the number of hidden layers

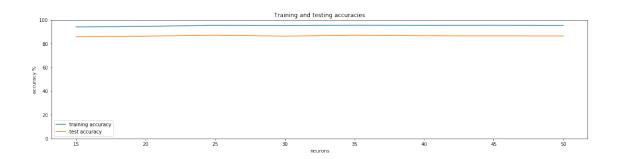
1. 1 hidden layer. Testing for 15 to 50 neurons:

```
[22]: n = [15,20,25,30,35,40,45,50]
    train_accuracies=[]
    test_accuracies=[]
    for neurons in n:
        net = network.Linear_Network([784, neurons, 10])
        tr_a, te_a = net.SGD(training_data, 30, 10, 0.5, lmbda = 5.0, □
        →test_data=testing_data,
            show_eval=False, show_graph=False, return_accuracies=True)
        train_accuracies.append(tr_a)
        test_accuracies.append(te_a)
        print(str(neurons)+" neurons:")
        print("Training acc.: "+str(tr_a)+"% Testing acc.: "+str(te_a)+"%")
        print()
```

```
plt.subplot(2, 1, 1)
plt.plot(n, train_accuracies, label='training accuracy')
plt.plot(n, test_accuracies, label='test accuracy')
plt.legend()
plt.title("Training and testing accuracies")
plt.xlabel("neurons")
plt.ylabel("accuracy %")
plt.ylim(0, 100)
plt.show()
15 neurons:
Training acc.: 94.096% Testing acc.: 85.8399999999999%
20 neurons:
Training acc.: 94.576% Testing acc.: 86.32%
25 neurons:
Training acc.: 95.4720000000001% Testing acc.: 87.16%
30 neurons:
Training acc.: 95.2640000000001% Testing acc.: 86.32%
35 neurons:
Training acc.: 95.583999999999% Testing acc.: 87.16%
40 neurons:
Training acc.: 95.4480000000001% Testing acc.: 86.68%
45 neurons:
Training acc.: 95.5519999999999% Testing acc.: 86.56%
```



Training acc.: 95.2719999999999% Testing acc.: 86.4799999999999%

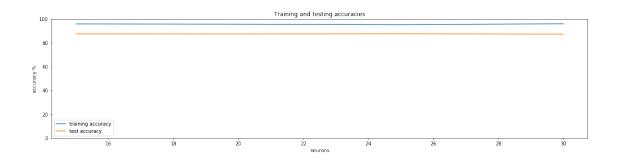


The result is pretty uniform. So lets stick to 35 neurons in the first layer.

Now we test the second hidden layer

30 neurons:

```
[23]: n = [15,20,25,30]
      train_accuracies=[]
      test_accuracies=[]
      for neurons in n:
          net = network.Linear_Network([784, 35, neurons, 10])
          tr_a, te_a = net.SGD(training_data, 30, 10, 0.5, lmbda = 5.0,
       →test_data=testing_data,
                 show_eval=False, show_graph=False, return_accuracies=True)
          train_accuracies.append(tr_a)
          test_accuracies.append(te_a)
          print(str(neurons)+" neurons:")
          print("Training acc.: "+str(tr a)+"% Testing acc.: "+str(te a)+"%")
          print()
      plt.subplot(2, 1, 1)
      plt.plot(n, train_accuracies, label='training accuracy')
      plt.plot(n, test_accuracies, label='test accuracy')
      plt.legend()
      plt.title("Training and testing accuracies")
      plt.xlabel("neurons")
      plt.ylabel("accuracy %")
      plt.ylim(0, 100)
     plt.show()
     15 neurons:
     Training acc.: 95.84% Testing acc.: 87.4400000000001%
     20 neurons:
     Training acc.: 95.6% Testing acc.: 87.3600000000001%
     25 neurons:
     Training acc.: 95.208% Testing acc.: 87.5200000000001%
```



Training acc.: 95.9600000000001% Testing acc.: 87.2400000000001%

Here we stick to 25 neurons in 2nd layer

## Testing for 3rd hidden layer

```
[26]: n = [15,20]
      train_accuracies=[]
      test_accuracies=[]
      for neurons in n:
          net = network.Linear_Network([784, 35, 25, neurons, 10])
          tr_a, te_a = net.SGD(training_data, 30, 10, 0.5, lmbda = 5.0,

→test_data=testing_data,

                 show_eval=False, show_graph=False, return_accuracies=True)
          train_accuracies.append(tr_a)
          test_accuracies.append(te_a)
          print(str(neurons)+" neurons:")
          print("Training acc.: "+str(tr_a)+"% Testing acc.: "+str(te_a)+"%")
          print()
      plt.subplot(2, 1, 1)
      plt.plot(n, train_accuracies, label='training accuracy')
      plt.plot(n, test_accuracies, label='test accuracy')
      plt.legend()
      plt.title("Training and testing accuracies")
      plt.xlabel("neurons")
      plt.ylabel("accuracy %")
      plt.ylim(0, 100)
      plt.show()
```

#### 15 neurons:

Training acc.: 92.744% Testing acc.: 85.28%

## 20 neurons:

Training acc.: 92.92% Testing acc.: 85.8%



With a decrease in accuracies, we finally stick to 2 hidden layers.

First hidden layer has 35 neurons and seconf hidden layer has 25 neurons

Checking the learning rate now. We increase the number of epochs and reduce the learning rate to see where the accuracies saturate Initially we try 50 epochs with eta=0.1

```
[27]: net = network.Linear_Network([784, 35, 25, 10])
net.SGD(training_data, 50, 10, 0.1, lmbda = 5.0, test_data=testing_data)
```

#### Epoch 1

Training loss: 3.2032931311622133827
Training accuracy: 13.600000000000001%

Test accuracy: 13.8%

## Epoch 2

Training loss: 2.979357053247336601

Training accuracy: 41.88% Test accuracy: 43.8%

#### Epoch 3

Training loss: 2.3166261117557005891

Training accuracy: 64.96%

Test accuracy: 59.1999999999996%

### Epoch 4

Training loss: 1.9229003357879172885

Training accuracy: 71.16% Test accuracy: 65.4%

#### Epoch 5

Training loss: 1.6672206102524891513

Training accuracy: 72.64%

Test accuracy: 67.8000000000001%

#### Epoch 6

Training loss: 1.4578467746512805906

Training accuracy: 80.64% Test accuracy: 78.4%

#### Epoch 7

Training loss: 1.3022954671634116282 Training accuracy: 79.039999999999%

Test accuracy: 75.8%

#### Epoch 8

Training loss: 1.1923338158331425587

Training accuracy: 84.2%

Test accuracy: 81.399999999999%

Epoch 9

Training loss: 1.104272894144313197
Training accuracy: 83.9600000000001%

Test accuracy: 79.2%

Epoch 10

Training loss: 1.0260431540807957934

Training accuracy: 88.2% Test accuracy: 84.8%

Epoch 11

Training loss: 0.9518740348069485484

Training accuracy: 89.4% Test accuracy: 85.6%

Epoch 12

Training loss: 0.9026574478291545418

Training accuracy: 89.36%

Test accuracy: 84.8%

Epoch 13

Training loss: 0.8368121554262523727

Training accuracy: 90.36%

Test accuracy: 85.8%

Epoch 14

Training loss: 0.8015666519443689536

Training accuracy: 90.56%

Test accuracy: 86.2%

Epoch 15

Training loss: 0.74793894548781152023

Training accuracy: 91.64%

Test accuracy: 86.8%

Epoch 16

Training loss: 0.7202715751531060989 Training accuracy: 92.3200000000001%

Test accuracy: 87.0%

Epoch 17

Training loss: 0.6819053678877821798
Training accuracy: 92.6000000000001%

Test accuracy: 87.8%

Epoch 18

Training loss: 0.6675191944689199315

Training accuracy: 93.04%

Test accuracy: 86.6%

Epoch 19

Training loss: 0.6438959099241531791

Training accuracy: 93.04%

Test accuracy: 85.2%

Epoch 20

Training loss: 0.6301744153544253214

Training accuracy: 93.36%

Test accuracy: 85.399999999999%

Epoch 21

Training loss: 0.6082534277698551203

Training accuracy: 93.4% Test accuracy: 87.6%

Epoch 22

Training loss: 0.5855477356087875859

Training accuracy: 93.64%

Test accuracy: 87.6%

Epoch 23

Training loss: 0.58102895297055570987

Training accuracy: 94.08% Test accuracy: 86.4%

Epoch 24

Training loss: 0.56245226340447469743

Training accuracy: 94.0% Test accuracy: 87.6%

Epoch 25

Training loss: 0.5477023301539234164

Training accuracy: 94.6% Test accuracy: 88.0%

Epoch 26

Training loss: 0.54806605583476812615

Training accuracy: 94.28%

Test accuracy: 87.6%

Epoch 27

Training loss: 0.53581361380082646775

Training accuracy: 94.6% Test accuracy: 86.8%

Training loss: 0.52250660036221330485

Training accuracy: 94.84% Test accuracy: 87.6%

Epoch 29

Training loss: 0.5322095325667175552

Training accuracy: 95.04% Test accuracy: 87.4%

Epoch 30

Training loss: 0.5401955676587451312

Training accuracy: 94.12% Test accuracy: 87.8%

Epoch 31

Training loss: 0.50370827997148981316

Training accuracy: 95.04% Test accuracy: 87.8%

Epoch 32

Training loss: 0.5024204703821459328

Training accuracy: 95.44%
Test accuracy: 87.6%

Epoch 33

Training loss: 0.48950475770784996677 Training accuracy: 95.2400000000001%

Test accuracy: 87.6%

Epoch 34

Training loss: 0.49309646067488661992

Training accuracy: 95.6% Test accuracy: 88.0%

Epoch 35

Training loss: 0.4854083650874701685

Training accuracy: 95.44%

Test accuracy: 88.4%

Epoch 36

Training loss: 0.48967493190505669443 Training accuracy: 95.399999999999%

Test accuracy: 87.6%

Epoch 37

Training loss: 0.47158326383664636035

Training accuracy: 95.9600000000001%

Test accuracy: 88.2%

Epoch 38

Training loss: 0.47664284314299774835

Training accuracy: 95.84%

Test accuracy: 87.0%

Epoch 39

Training loss: 0.470897145197710012

Training accuracy: 95.8% Test accuracy: 87.8%

Epoch 40

Training loss: 0.48417765487660274814

Training accuracy: 95.08%

Test accuracy: 87.8%

Epoch 41

Training loss: 0.46822515180435101073

Training accuracy: 96.08%

Test accuracy: 88.0%

Epoch 42

Training loss: 0.4570609948228599176

Training accuracy: 96.32%

Test accuracy: 87.0%

Epoch 43

Training loss: 0.44977651379688632152 Training accuracy: 96.399999999999%

Test accuracy: 88.4%

Epoch 44

Training loss: 0.45223173702288123118

Training accuracy: 95.76%

Test accuracy: 87.8%

Epoch 45

Training loss: 0.45139669997598413754 Training accuracy: 95.9600000000001%

Test accuracy: 88.8%

Epoch 46

Training loss: 0.45710616916202450057

Training accuracy: 96.36%

Test accuracy: 87.8%

Training loss: 0.44614847732084361088

Training accuracy: 96.0% Test accuracy: 87.8%

### Epoch 48

Training loss: 0.44101348263886575344 Training accuracy: 96.399999999999%

Test accuracy: 87.4%

### Epoch 49

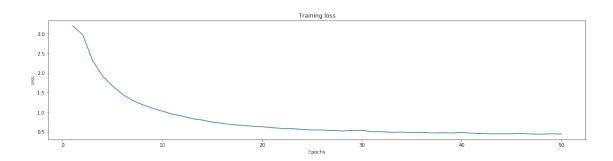
Training loss: 0.44976422677027937648

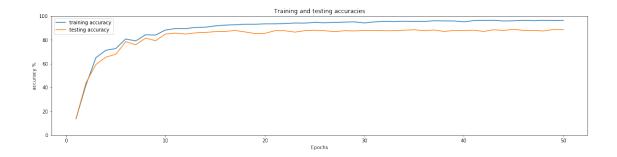
Training accuracy: 96.2% Test accuracy: 88.6%

### Epoch 50

Training loss: 0.44304126623144652935

Training accuracy: 96.32% Test accuracy: 88.6%





# Trying eta=0.01 for 100 epochs

[28]: net = network.Linear\_Network([784, 35, 25, 10])
net.SGD(training\_data, 100, 10, 0.01, lmbda = 5.0, test\_data=testing\_data)

Test accuracy: 12.4%

### Epoch 2

Training loss: 3.239028594460498077
Training accuracy: 11.9599999999999%

Test accuracy: 12.4%

### Epoch 3

Training loss: 3.235895415070075321
Training accuracy: 11.9599999999999%

Test accuracy: 12.4%

### Epoch 4

Training loss: 3.232279988576710235 Training accuracy: 11.9599999999999%

Test accuracy: 12.4%

### Epoch 5

Training loss: 3.2280075513184290456 Training accuracy: 11.9599999999999%

Test accuracy: 12.4%

### Epoch 6

Training loss: 3.2248574488085505977
Training accuracy: 11.2000000000001%
Test accuracy: 8.79999999999999

### Epoch 7

Training loss: 3.219469202006140357

Training accuracy: 19.28%

Test accuracy: 16.4000000000000002%

#### Epoch 8

Training loss: 3.2135988254186800164

Training accuracy: 20.44%

Test accuracy: 18.0%

### Epoch 9

Training loss: 3.20811834918552255

Training accuracy: 19.88%

Test accuracy: 21.4%

## Epoch 10

Training loss: 3.2010051766086239586

Training accuracy: 12.0%

Test accuracy: 12.6%

Epoch 11

Training loss: 3.1922122905115274695

Training accuracy: 16.08%

Test accuracy: 14.7999999999999%

Epoch 12

Training loss: 3.1828051604763835975

Training accuracy: 22.0% Test accuracy: 22.8%

Epoch 13

Training loss: 3.171549337209243616

Training accuracy: 20.48% Test accuracy: 22.2%

Epoch 14

Training loss: 3.1579692570564938745
Training accuracy: 18.2799999999998%

Test accuracy: 19.6%

Epoch 15

Training loss: 3.142504897605991459

Training accuracy: 40.12% Test accuracy: 37.6%

Epoch 16

Training loss: 3.122797757948355835

Training accuracy: 37.72%

Test accuracy: 35.19999999999996%

Epoch 17

Training loss: 3.1004062036062451215

Training accuracy: 38.76%

Test accuracy: 36.19999999999996%

Epoch 18

Training loss: 3.074397703183800599

Training accuracy: 41.92%

Test accuracy: 41.19999999999996%

Epoch 19

Training loss: 3.044349118716373748

Training accuracy: 40.2% Test accuracy: 37.2%

Epoch 20

Training loss: 3.0091303008163201964

Training accuracy: 46.6% Test accuracy: 45.4%

Epoch 21

Training loss: 2.9684991816499108842

Training accuracy: 46.44% Test accuracy: 46.0%

Epoch 22

Training loss: 2.92469611200130771

Training accuracy: 48.32% Test accuracy: 48.0%

Epoch 23

Training loss: 2.8759409221530301218
Training accuracy: 51.16000000000004%
Test accuracy: 48.1999999999996%

Epoch 24

Training loss: 2.8240886380030860686

Training accuracy: 49.68% Test accuracy: 47.4%

Epoch 25

Training loss: 2.7697902628774254458

Training accuracy: 49.84% Test accuracy: 48.8%

Epoch 26

Training loss: 2.7162277572661148433

Training accuracy: 49.36% Test accuracy: 49.6%

Epoch 27

Training loss: 2.6597446797016051545

Training accuracy: 53.04% Test accuracy: 51.4%

Epoch 28

Training loss: 2.6061288412169825428

Training accuracy: 55.84%

Test accuracy: 53.800000000000004%

Epoch 29

Training loss: 2.5530383081132731824

Training accuracy: 55.32%

Test accuracy: 52.800000000000004%

Training loss: 2.5018998306884877557

Training accuracy: 53.72%

Test accuracy: 52.800000000000004%

Epoch 31

Training loss: 2.4508792215258656015 Training accuracy: 55.679999999999%

Test accuracy: 53.2%

Epoch 32

Training loss: 2.4012865598298434712
Training accuracy: 55.55999999999995%
Test accuracy: 54.400000000000006%

Epoch 33

Training loss: 2.3541694968697522428

Training accuracy: 56.44%

Test accuracy: 54.800000000000004%

Epoch 34

Training loss: 2.3078569588949350783
Training accuracy: 56.12000000000000%

Test accuracy: 54.6%

Epoch 35

Training loss: 2.2637557417282180897 Training accuracy: 56.59999999999994% Test accuracy: 54.800000000000004%

Epoch 36

Training loss: 2.221228771235827473
Training accuracy: 58.1999999999996%
Test accuracy: 57.59999999999994%

Epoch 37

Training loss: 2.1798856352725289572
Training accuracy: 58.3200000000001%
Test accuracy: 56.999999999999%

Epoch 38

Training loss: 2.1404746908608168305

Training accuracy: 59.96% Test accuracy: 57.8%

Epoch 39

Training loss: 2.1037621162467799647

Training accuracy: 59.24%

Test accuracy: 57.999999999999%

Epoch 40

Training loss: 2.0685769382234162049 Training accuracy: 62.0399999999999% Test accuracy: 59.5999999999994%

Epoch 41

Training loss: 2.0359159212131779585

Training accuracy: 61.12% Test accuracy: 58.8%

Epoch 42

Training loss: 2.0048847311586729329

Training accuracy: 61.28% Test accuracy: 58.8%

Epoch 43

Training loss: 1.974848235023085078
Training accuracy: 63.160000000000004%

Test accuracy: 60.4%

Epoch 44

Training loss: 1.9473420165813056105 Training accuracy: 63.639999999999%

Test accuracy: 61.6%

Epoch 45

Training loss: 1.9208079851927383835 Training accuracy: 63.6399999999999% Test accuracy: 61.1999999999996%

Epoch 46

Training loss: 1.8957143576823315464

Training accuracy: 64.28%

Test accuracy: 60.8%

Epoch 47

Training loss: 1.8717288913158866705

Training accuracy: 64.52%

Test accuracy: 61.1999999999996%

Epoch 48

Training loss: 1.848219909449681893

Training accuracy: 65.92%

Test accuracy: 62.4%

Training loss: 1.8260729254400167509 Training accuracy: 66.679999999999%

Test accuracy: 62.6%

Epoch 50

Training loss: 1.8047938109639787926

Training accuracy: 67.2% Test accuracy: 63.2%

Epoch 51

Training loss: 1.7834129408990705926

Training accuracy: 67.72%

Test accuracy: 63.2%

Epoch 52

Training loss: 1.7629601038715065655

Training accuracy: 67.88% Test accuracy: 63.4%

Epoch 53

Training loss: 1.7434503943780405013

Training accuracy: 69.08%

Test accuracy: 65.4%

Epoch 54

Training loss: 1.7237760193977251957

Training accuracy: 69.56%

Test accuracy: 65.8%

Epoch 55

Training loss: 1.7055133364057228889 Training accuracy: 70.52000000000001%

Test accuracy: 67.4%

Epoch 56

Training loss: 1.6856116623531849346

Training accuracy: 71.12%

Test accuracy: 67.60000000000001%

Epoch 57

Training loss: 1.6670932176954086682

Training accuracy: 71.36%

Test accuracy: 67.6000000000001%

Epoch 58

Training loss: 1.6490286058734865947

Training accuracy: 71.28%

Test accuracy: 68.4%

Epoch 59

Training loss: 1.6305001383306866711

Training accuracy: 72.36%

Test accuracy: 68.2%

Epoch 60

Training loss: 1.6130062561568574205 Training accuracy: 73.2400000000001%

Test accuracy: 68.4%

Epoch 61

Training loss: 1.5946559071688159602

Training accuracy: 73.68%

Test accuracy: 69.199999999999%

Epoch 62

Training loss: 1.5770382621481562106

Training accuracy: 73.8% Test accuracy: 68.8%

Epoch 63

Training loss: 1.5588948405875222796

Training accuracy: 75.36%

Test accuracy: 70.1999999999999%

Epoch 64

Training loss: 1.5417844324714328183 Training accuracy: 75.1600000000001% Test accuracy: 70.399999999999%

Epoch 65

Training loss: 1.5241947466488462496

Training accuracy: 75.8% Test accuracy: 71.6%

Epoch 66

Training loss: 1.5066104174884922006

Training accuracy: 77.08%

Test accuracy: 72.6%

Epoch 67

Training loss: 1.4899628374798290287

Training accuracy: 77.64%

Test accuracy: 73.6%

Epoch 68

Training loss: 1.4724902043963055593

Training accuracy: 77.28% Test accuracy: 72.8%

Epoch 69

Training loss: 1.4548622997156738217

Training accuracy: 78.0% Test accuracy: 74.4%

Epoch 70

Training loss: 1.4377368092651069656

Training accuracy: 78.72% Test accuracy: 75.2%

Epoch 71

Training loss: 1.4208452418719656946

Training accuracy: 79.16% Test accuracy: 75.4%

Epoch 72

Training loss: 1.4038049094047345091

Training accuracy: 79.36% Test accuracy: 75.8%

Epoch 73

Training loss: 1.3872365292509588534

Training accuracy: 80.16% Test accuracy: 76.6%

Epoch 74

Training loss: 1.3704860215398357733

Training accuracy: 80.72% Test accuracy: 77.2%

Epoch 75

Training loss: 1.3542485419195613612

Training accuracy: 80.96%

Test accuracy: 77.6000000000001%

Epoch 76

Training loss: 1.3389831627064600793

Training accuracy: 81.8% Test accuracy: 78.0%

Epoch 77

Training loss: 1.3219832630852059864

Training accuracy: 82.12% Test accuracy: 79.0%

Training loss: 1.3063851778332541608

Training accuracy: 82.84%

Test accuracy: 79.6000000000001%

Epoch 79

Training loss: 1.291205768735197076

Training accuracy: 83.2%

Test accuracy: 79.6000000000001%

Epoch 80

Training loss: 1.2756564658444705095

Training accuracy: 83.76%

Test accuracy: 80.8000000000001%

Epoch 81

Training loss: 1.260856611725711458
Training accuracy: 83.5200000000001%
Test accuracy: 80.8000000000001%

Epoch 82

Training loss: 1.2454534042063571398

Training accuracy: 84.2% Test accuracy: 81.6%

Epoch 83

Training loss: 1.2308656061274645392 Training accuracy: 84.399999999999% Test accuracy: 81.399999999999%

Epoch 84

Training loss: 1.2165548989951122977

Training accuracy: 84.76%

Test accuracy: 82.1999999999999%

Epoch 85

Training loss: 1.2028314733363346907 Training accuracy: 84.9600000000001% Test accuracy: 82.399999999999%

Epoch 86

Training loss: 1.1886340126235066866

Training accuracy: 85.64%

Test accuracy: 82.1999999999999%

Epoch 87

Training loss: 1.1748772795262187512

Training accuracy: 86.04%

Test accuracy: 83.6%

Epoch 88

Training loss: 1.1616291866280881721
Training accuracy: 85.96000000000001%

Test accuracy: 82.8%

Epoch 89

Training loss: 1.1485587851601321016

Training accuracy: 86.08% Test accuracy: 83.0%

Epoch 90

Training loss: 1.1357762153106187144

Training accuracy: 86.56%

Test accuracy: 84.0%

Epoch 91

Training loss: 1.1236120774360980917

Training accuracy: 86.32% Test accuracy: 83.8%

Epoch 92

Training loss: 1.1112726251411067034

Training accuracy: 86.88%

Test accuracy: 83.8%

Epoch 93

Training loss: 1.0990041061046098446

Training accuracy: 86.92% Test accuracy: 84.2%

Epoch 94

Training loss: 1.0874187265099264566

Training accuracy: 87.08%

Test accuracy: 84.0%

Epoch 95

Training loss: 1.0760050708785375866

Training accuracy: 87.44%

Test accuracy: 84.0%

Epoch 96

Training loss: 1.0646318248633173022

Training accuracy: 87.76%

Test accuracy: 84.399999999999%

Training loss: 1.0539327871630847478

Training accuracy: 88.2% Test accuracy: 84.6%

### Epoch 98

Training loss: 1.0437634386080763659

Training accuracy: 88.4%

Test accuracy: 84.3999999999999%

### Epoch 99

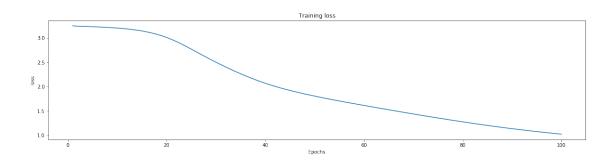
Training loss: 1.0328500565623754981 Training accuracy: 88.039999999999%

Test accuracy: 84.6%

### Epoch 100

Training loss: 1.0225673635624652969

Training accuracy: 88.48% Test accuracy: 85.2%





Since we didnt reach saturation, let's try with 200 epochs

[29]: net = network.Linear\_Network([784, 35, 25, 10])
net.SGD(training\_data, 200, 10, 0.01, lmbda = 5.0, test\_data=testing\_data)

Training loss: 3.2448648598402080197
Training accuracy: 11.95999999999999%

Test accuracy: 12.4%

### Epoch 2

Training loss: 3.2373135604231627444
Training accuracy: 11.9599999999999%

Test accuracy: 12.4%

### Epoch 3

Training loss: 3.2316508006551143098

Training accuracy: 18.4% Test accuracy: 15.2%

### Epoch 4

Training loss: 3.2263156506888010654
Training accuracy: 18.240000000000000%

Test accuracy: 15.4%

#### Epoch 5

Training loss: 3.2183598531551415537
Training accuracy: 16.400000000000000%

Test accuracy: 17.0%

### Epoch 6

Training loss: 3.210233225292959681
Training accuracy: 13.2399999999998%

Test accuracy: 13.8%

### Epoch 7

Training loss: 3.2010835726235456465
Training accuracy: 19.040000000000003%

Test accuracy: 20.4%

#### Epoch 8

Training loss: 3.1905204702988827826

Training accuracy: 29.92%

Test accuracy: 29.79999999999997%

### Epoch 9

Training loss: 3.17673840059719404
Training accuracy: 28.36000000000003%
Test accuracy: 28.000000000000004%

### Epoch 10

Training loss: 3.1617877300963245946
Training accuracy: 29.080000000000000%

Test accuracy: 28.19999999999996%

Epoch 11

Training loss: 3.1439759453097912707

Training accuracy: 28.88%

Test accuracy: 28.000000000000004%

Epoch 12

Training loss: 3.1229978301627211515

Training accuracy: 32.28%

Test accuracy: 30.4%

Epoch 13

Training loss: 3.0981339858470488106 Training accuracy: 31.0800000000000002%

Test accuracy: 31.2%

Epoch 14

Training loss: 3.0698266047872981837

Training accuracy: 27.48%

Test accuracy: 28.19999999999996%

Epoch 15

Training loss: 3.036665429925219199
Training accuracy: 29.720000000000000%

Test accuracy: 31.6%

Epoch 16

Training loss: 2.9997690267258597739
Training accuracy: 36.12000000000000%

Test accuracy: 34.2%

Epoch 17

Training loss: 2.9596269673826975566

Training accuracy: 35.36%

Test accuracy: 34.59999999999994%

Epoch 18

Training loss: 2.9154516722581708269

Training accuracy: 39.2%

Test accuracy: 36.6%

Epoch 19

Training loss: 2.8684099699877610638

Training accuracy: 44.04%

Test accuracy: 40.8%

Epoch 20

Training loss: 2.8189767979938176908

Training accuracy: 42.32% Test accuracy: 37.8%

Epoch 21

Training loss: 2.7675733086435321336

Training accuracy: 44.72%

Test accuracy: 40.400000000000006%

Epoch 22

Training loss: 2.7131023592527464367

Training accuracy: 44.64%

Test accuracy: 39.6%

Epoch 23

Training loss: 2.6567429832600327336

Training accuracy: 48.72%

Test accuracy: 43.8%

Epoch 24

Training loss: 2.5985438096183832908

Training accuracy: 48.76%

Test accuracy: 42.0%

Epoch 25

Training loss: 2.5375138751746777331

Training accuracy: 54.04%

Test accuracy: 47.4%

Epoch 26

Training loss: 2.4755215038864055888
Training accuracy: 52.95999999999994%

Test accuracy: 47.4%

Epoch 27

Training loss: 2.412296344343621339 Training accuracy: 56.5999999999994%

Test accuracy: 51.4%

Epoch 28

Training loss: 2.349044874459079787

Training accuracy: 58.68%

Test accuracy: 53.400000000000006%

Epoch 29

Training loss: 2.287425276675670176
Training accuracy: 60.44000000000005%
Test accuracy: 57.1999999999996%

Training loss: 2.227593976773718862 Training accuracy: 61.5199999999999%

Test accuracy: 56.8%

Epoch 31

Training loss: 2.171830491115984002 Training accuracy: 63.160000000000004%

Test accuracy: 59.8%

Epoch 32

Training loss: 2.118947942669142957
Training accuracy: 63.480000000000004%

Test accuracy: 59.0%

Epoch 33

Training loss: 2.070304883854367748

Training accuracy: 66.0% Test accuracy: 62.6%

Epoch 34

Training loss: 2.0234420703287843942

Training accuracy: 64.48% Test accuracy: 61.0%

Epoch 35

Training loss: 1.9815780164013248907

Training accuracy: 64.52%

Test accuracy: 61.6%

Epoch 36

Training loss: 1.9421671172035465943

Training accuracy: 65.68% Test accuracy: 62.0%

Epoch 37

Training loss: 1.9048386327800478276

Training accuracy: 67.04%

Test accuracy: 63.4%

Epoch 38

Training loss: 1.870198086286800898

Training accuracy: 67.84% Test accuracy: 63.0%

Epoch 39

Training loss: 1.8371729189072062828

Training accuracy: 68.479999999999%

Test accuracy: 64.2%

Epoch 40

Training loss: 1.8059812594806316281

Training accuracy: 69.56%

Test accuracy: 65.60000000000001%

Epoch 41

Training loss: 1.7766110573477318171

Training accuracy: 69.56%

Test accuracy: 65.0%

Epoch 42

Training loss: 1.7493029259867606846 Training accuracy: 71.2400000000001%

Test accuracy: 66.0%

Epoch 43

Training loss: 1.7221326063389069891 Training accuracy: 72.2400000000001%

Test accuracy: 67.4%

Epoch 44

Training loss: 1.6963154362727693296

Training accuracy: 71.64%

Test accuracy: 66.2%

Epoch 45

Training loss: 1.6719976240586162215

Training accuracy: 72.0%

Test accuracy: 65.60000000000001%

Epoch 46

Training loss: 1.6478905005764351338

Training accuracy: 73.52%

Test accuracy: 67.0%

Epoch 47

Training loss: 1.625622332341793169

Training accuracy: 72.92%

Test accuracy: 67.0%

Epoch 48

Training loss: 1.6026926432925977457

Training accuracy: 74.72%

Test accuracy: 68.2%

Training loss: 1.5810781387832224743

Training accuracy: 74.92%

Test accuracy: 68.2%

Epoch 50

Training loss: 1.5602948782306045695

Training accuracy: 75.76%

Test accuracy: 68.8%

Epoch 51

Training loss: 1.5401601152220052131

Training accuracy: 75.84%

Test accuracy: 69.8%

Epoch 52

Training loss: 1.5201670845523957551

Training accuracy: 76.2% Test accuracy: 68.8%

Epoch 53

Training loss: 1.5009311419924430381

Training accuracy: 77.24%

Test accuracy: 70.1999999999999%

Epoch 54

Training loss: 1.4819905806030879341
Training accuracy: 77.60000000000001%

Test accuracy: 69.8%

Epoch 55

Training loss: 1.4638336856048307897

Training accuracy: 77.56%

Test accuracy: 71.8%

Epoch 56

Training loss: 1.4451548647403959276

Training accuracy: 78.68%

Test accuracy: 72.0%

Epoch 57

Training loss: 1.4273283430360277579

Training accuracy: 78.56%

Test accuracy: 71.8%

Epoch 58

Training loss: 1.4097489279625173905

Training accuracy: 78.64%

Test accuracy: 72.0%

Epoch 59

Training loss: 1.3927237857007958264

Training accuracy: 78.68%

Test accuracy: 71.399999999999%

Epoch 60

Training loss: 1.3755970593340858997

Training accuracy: 79.28%

Test accuracy: 72.0%

Epoch 61

Training loss: 1.3593934381885453783 Training accuracy: 79.60000000000001%

Test accuracy: 73.2%

Epoch 62

Training loss: 1.3433029808291595912

Training accuracy: 79.72%

Test accuracy: 74.4%

Epoch 63

Training loss: 1.3270371784703640441

Training accuracy: 81.0% Test accuracy: 76.0%

Epoch 64

Training loss: 1.3113332840049581442

Training accuracy: 81.36%

Test accuracy: 75.8%

Epoch 65

Training loss: 1.2970018796200158722 Training accuracy: 81.399999999999%

Test accuracy: 76.8%

Epoch 66

Training loss: 1.2812429799740605171

Training accuracy: 82.12%

Test accuracy: 77.2%

Epoch 67

Training loss: 1.2666396076368702449
Training accuracy: 82.679999999999%

Test accuracy: 78.2%

Epoch 68

Training loss: 1.2533590894455205921

Training accuracy: 83.36% Test accuracy: 79.2%

Epoch 69

Training loss: 1.2378935003378603682

Training accuracy: 82.56% Test accuracy: 79.4%

Epoch 70

Training loss: 1.2248447174763241473

Training accuracy: 83.72% Test accuracy: 79.4%

Epoch 71

Training loss: 1.2117561228666764345

Training accuracy: 84.28%

Test accuracy: 78.6000000000001%

Epoch 72

Training loss: 1.1975948763352138132

Training accuracy: 83.6%

Test accuracy: 80.8000000000001%

Epoch 73

Training loss: 1.1846408183400811487

Training accuracy: 84.56% Test accuracy: 80.2%

Epoch 74

Training loss: 1.1720948207842566809

Training accuracy: 84.28%

Test accuracy: 80.8000000000001%

Epoch 75

Training loss: 1.1602747021176393314

Training accuracy: 84.44%

Test accuracy: 80.6000000000001%

Epoch 76

Training loss: 1.1476667480533851068

Training accuracy: 85.16%

Test accuracy: 81.399999999999%

Epoch 77

Training loss: 1.1365720097217338381
Training accuracy: 85.24000000000001%

Test accuracy: 81.8%

Training loss: 1.1247255847502848179

Training accuracy: 85.84% Test accuracy: 81.6%

Epoch 79

Training loss: 1.1149158336767258999

Training accuracy: 85.68%

Test accuracy: 81.3999999999999%

Epoch 80

Training loss: 1.1039917171596402458

Training accuracy: 85.08% Test accuracy: 81.0%

Epoch 81

Training loss: 1.0920787058580155763

Training accuracy: 85.84% Test accuracy: 81.8%

Epoch 82

Training loss: 1.081715399744579795

Training accuracy: 86.56%

Test accuracy: 82.1999999999999%

Epoch 83

Training loss: 1.0724316371901005924

Training accuracy: 86.64%

Test accuracy: 82.0%

Epoch 84

Training loss: 1.0618783918153546165

Training accuracy: 86.4%

Test accuracy: 82.1999999999999%

Epoch 85

Training loss: 1.0523028605508784877

Training accuracy: 86.56%

Test accuracy: 82.199999999999%

Epoch 86

Training loss: 1.0428309317496282559

Training accuracy: 86.72%

Test accuracy: 82.399999999999%

Epoch 87

Training loss: 1.0335930147888180488

Training accuracy: 87.28%

Test accuracy: 82.8%

Epoch 88

Training loss: 1.0251894726401689612

Training accuracy: 87.72%

Test accuracy: 83.6%

Epoch 89

Training loss: 1.0157816026483921518

Training accuracy: 87.64%

Test accuracy: 83.0%

Epoch 90

Training loss: 1.0076949990941851434
Training accuracy: 87.96000000000001%

Test accuracy: 83.399999999999%

Epoch 91

Training loss: 0.9990189168665997991

Training accuracy: 87.92%

Test accuracy: 83.3999999999999%

Epoch 92

Training loss: 0.9906598544992383033 Training accuracy: 88.0399999999999%

Test accuracy: 83.0%

Epoch 93

Training loss: 0.9829733850150172254 Training accuracy: 88.0399999999999%

Test accuracy: 83.2%

Epoch 94

Training loss: 0.9753109816219269748

Training accuracy: 88.68%

Test accuracy: 84.0%

Epoch 95

Training loss: 0.9673540793529894392

Training accuracy: 88.8% Test accuracy: 84.0%

Epoch 96

Training loss: 0.9597514970576607972 Training accuracy: 89.039999999999%

Test accuracy: 83.8%

Training loss: 0.95234425147898404333 Training accuracy: 89.039999999999%

Test accuracy: 84.2%

Epoch 98

Training loss: 0.9451673288892534151

Training accuracy: 88.96%

Test accuracy: 84.399999999999%

Epoch 99

Training loss: 0.93805962067274864513 Training accuracy: 88.8800000000001%

Test accuracy: 84.2%

Epoch 100

Training loss: 0.9315577093472887503

Training accuracy: 89.28% Test accuracy: 83.8%

Epoch 101

Training loss: 0.9241622647584131939

Training accuracy: 89.12%

Test accuracy: 84.0%

Epoch 102

Training loss: 0.9180485451998891938

Training accuracy: 89.36%

Test accuracy: 83.8%

Epoch 103

Training loss: 0.9109929078513542769

Training accuracy: 89.44%

Test accuracy: 83.8%

Epoch 104

Training loss: 0.9048270072692862695 Training accuracy: 89.7599999999999%

Test accuracy: 84.0%

Epoch 105

Training loss: 0.899356816572868636

Training accuracy: 89.56%

Test accuracy: 84.6%

Epoch 106

Training loss: 0.89225139936257858846 Training accuracy: 89.60000000000001% Test accuracy: 84.399999999999%

Epoch 107

Training loss: 0.886676226204396169

Training accuracy: 89.84%

Test accuracy: 84.0%

Epoch 108

Training loss: 0.88030074843402830335

Training accuracy: 89.8%

Test accuracy: 84.399999999999%

Epoch 109

Training loss: 0.8746853764703772553

Training accuracy: 89.84%

Test accuracy: 84.6%

Epoch 110

Training loss: 0.86912751639407075734

Training accuracy: 89.92%

Test accuracy: 84.6%

Epoch 111

Training loss: 0.8632107469139967564

Training accuracy: 89.96%

Test accuracy: 84.6%

Epoch 112

Training loss: 0.8576764708850190823

Training accuracy: 90.08%

Test accuracy: 85.0%

Epoch 113

Training loss: 0.85230878540240242243

Training accuracy: 90.32%

Test accuracy: 85.2%

Epoch 114

Training loss: 0.84686883539164960715

Training accuracy: 90.52%

Test accuracy: 85.2%

Epoch 115

Training loss: 0.8416985475681299664 Training accuracy: 90.60000000000001%

Test accuracy: 85.0%

Epoch 116

Training loss: 0.83747999645107525774

Training accuracy: 90.64%

Test accuracy: 85.0%

Epoch 117

Training loss: 0.8314217745867625897

Training accuracy: 90.4%

Test accuracy: 85.399999999999%

Epoch 118

Training loss: 0.82679126937779197115

Training accuracy: 90.72%

Test accuracy: 85.399999999999%

Epoch 119

Training loss: 0.82153390364633254014

Training accuracy: 90.8%

Test accuracy: 85.399999999999%

Epoch 120

Training loss: 0.81688116694402794596 Training accuracy: 90.8800000000001% Test accuracy: 85.399999999999%

Epoch 121

Training loss: 0.81219536999729301344 Training accuracy: 90.6000000000001% Test accuracy: 85.399999999999%

Epoch 122

Training loss: 0.8071922856760298857

Training accuracy: 91.0%

Test accuracy: 85.399999999999%

Epoch 123

Training loss: 0.80294261598008158837

Training accuracy: 91.2% Test accuracy: 85.8%

Epoch 124

Training loss: 0.7987991118468399861

Training accuracy: 91.12%

Test accuracy: 86.0%

Epoch 125

Training loss: 0.79391852202519442157

Training accuracy: 91.24%

Test accuracy: 86.2%

Training loss: 0.7896756589047557638 Training accuracy: 91.3200000000001%

Test accuracy: 86.0%

Epoch 127

Training loss: 0.78607630643014459924

Training accuracy: 91.28% Test accuracy: 85.8%

Epoch 128

Training loss: 0.7811274433262855312

Training accuracy: 91.4% Test accuracy: 86.4%

Epoch 129

Training loss: 0.7767869721471583545 Training accuracy: 91.60000000000001%

Test accuracy: 85.8%

Epoch 130

Training loss: 0.77240243738995738434 Training accuracy: 91.479999999999%

Test accuracy: 86.4%

Epoch 131

Training loss: 0.7691039853575153948

Training accuracy: 92.04%

Test accuracy: 86.2%

Epoch 132

Training loss: 0.7649061175713949493

Training accuracy: 91.96% Test accuracy: 86.0%

Epoch 133

Training loss: 0.7608901847267768064

Training accuracy: 91.64%

Test accuracy: 86.6%

Epoch 134

Training loss: 0.75866994663786567374

Training accuracy: 92.04% Test accuracy: 86.6%

Epoch 135

Training loss: 0.752960017202732477

Training accuracy: 91.88%

Test accuracy: 86.4%

Epoch 136

Training loss: 0.75055359193349202644

Training accuracy: 91.88%

Test accuracy: 86.8%

Epoch 137

Training loss: 0.7455113116188975216

Training accuracy: 92.2% Test accuracy: 86.4%

Epoch 138

Training loss: 0.7436768530742874325

Training accuracy: 92.08%

Test accuracy: 86.8%

Epoch 139

Training loss: 0.7383576093752210722

Training accuracy: 91.96%

Test accuracy: 86.0%

Epoch 140

Training loss: 0.7348899017214693404

Training accuracy: 92.12%

Test accuracy: 86.8%

Epoch 141

Training loss: 0.73145469834716003417

Training accuracy: 92.2% Test accuracy: 86.8%

Epoch 142

Training loss: 0.728139260403335867

Training accuracy: 92.36%

Test accuracy: 86.4%

Epoch 143

Training loss: 0.7246311330291147691

Training accuracy: 92.24%

Test accuracy: 86.4%

Epoch 144

Training loss: 0.72155424234031550725 Training accuracy: 92.479999999999%

Test accuracy: 87.0%

Training loss: 0.7183018109222813925

Training accuracy: 92.24%

Test accuracy: 86.8%

Epoch 146

Training loss: 0.7156373309897406

Training accuracy: 92.44%

Test accuracy: 87.2%

Epoch 147

Training loss: 0.71161071769414887205

Training accuracy: 92.24%

Test accuracy: 86.6%

Epoch 148

Training loss: 0.70867872488624437607 Training accuracy: 92.479999999999%

Test accuracy: 86.8%

Epoch 149

Training loss: 0.70617170926885193717

Training accuracy: 92.64%

Test accuracy: 87.0%

Epoch 150

Training loss: 0.70274955892325414786 Training accuracy: 92.479999999999%

Test accuracy: 86.8%

Epoch 151

Training loss: 0.6997328141277668819

Training accuracy: 92.52%

Test accuracy: 86.6%

Epoch 152

Training loss: 0.69629242198541990857

Training accuracy: 92.52%

Test accuracy: 87.0%

Epoch 153

Training loss: 0.6941443313843758697 Training accuracy: 92.6000000000001%

Test accuracy: 87.4%

Epoch 154

Training loss: 0.6908471337415322669

Training accuracy: 92.64%

Test accuracy: 86.8%

Epoch 155

Training loss: 0.68853430768362481034

Training accuracy: 92.64%

Test accuracy: 87.0%

Epoch 156

Training loss: 0.68514003060513119995

Training accuracy: 92.88%

Test accuracy: 87.0%

Epoch 157

Training loss: 0.6825781068075870057

Training accuracy: 92.84%

Test accuracy: 87.2%

Epoch 158

Training loss: 0.6802750108143772526

Training accuracy: 92.72%

Test accuracy: 86.8%

Epoch 159

Training loss: 0.6770158656481711667

Training accuracy: 92.96%

Test accuracy: 87.0%

Epoch 160

Training loss: 0.6746036332645691025

Training accuracy: 92.72%

Test accuracy: 87.4%

Epoch 161

Training loss: 0.6720427757983118415

Training accuracy: 92.88%

Test accuracy: 87.6%

Epoch 162

Training loss: 0.66940962661114800097

Training accuracy: 92.92%

Test accuracy: 87.4%

Epoch 163

Training loss: 0.6669632219010615594

Training accuracy: 93.08%

Test accuracy: 87.4%

Epoch 164

Training loss: 0.6648791954771500335

Training accuracy: 92.96%

Test accuracy: 87.4%

Epoch 165

Training loss: 0.66190244500986940865

Training accuracy: 93.08%

Test accuracy: 87.4%

Epoch 166

Training loss: 0.65944103395232555405

Training accuracy: 93.04%

Test accuracy: 87.4%

Epoch 167

Training loss: 0.65691821273306173854

Training accuracy: 93.2% Test accuracy: 87.8%

Epoch 168

Training loss: 0.65498798182789156897

Training accuracy: 93.16%

Test accuracy: 87.6%

Epoch 169

Training loss: 0.65238680611439229254

Training accuracy: 93.28%

Test accuracy: 87.4%

Epoch 170

Training loss: 0.6501144064130033243
Training accuracy: 93.3200000000001%

Test accuracy: 87.8%

Epoch 171

Training loss: 0.6483810013036173176 Training accuracy: 93.3200000000001%

Test accuracy: 87.4%

Epoch 172

Training loss: 0.64608502843123692656

Training accuracy: 93.24%

Test accuracy: 87.4%

Epoch 173

Training loss: 0.64436892396917374757

Training accuracy: 93.28%

Test accuracy: 87.6%

Training loss: 0.64165690900774034197

Training accuracy: 93.24% Test accuracy: 87.6%

Epoch 175

Training loss: 0.63952935322323386337

Training accuracy: 93.36% Test accuracy: 87.6%

Epoch 176

Training loss: 0.63837159085818753605 Training accuracy: 93.479999999999%

Test accuracy: 87.6%

Epoch 177

Training loss: 0.63519229436790445974

Training accuracy: 93.28% Test accuracy: 87.4%

Epoch 178

Training loss: 0.63332676032971372713 Training accuracy: 93.52000000000001%

Test accuracy: 87.4%

Epoch 179

Training loss: 0.63094469646691017146

Training accuracy: 93.44%

Test accuracy: 87.6%

Epoch 180

Training loss: 0.6292672903165051361

Training accuracy: 93.56% Test accuracy: 87.6%

Epoch 181

Training loss: 0.62713882196761277555

Training accuracy: 93.4% Test accuracy: 87.4%

Epoch 182

Training loss: 0.6253841666763890473

Training accuracy: 93.44%
Test accuracy: 87.4%

Epoch 183

Training loss: 0.624090923552555987

Training accuracy: 93.64%

Test accuracy: 87.4%

Epoch 184

Training loss: 0.6214213639034449173 Training accuracy: 93.5200000000001%

Test accuracy: 87.8%

Epoch 185

Training loss: 0.61996924809412455446

Training accuracy: 93.56% Test accuracy: 87.4%

Epoch 186

Training loss: 0.618022682014588171

Training accuracy: 93.8% Test accuracy: 88.0%

Epoch 187

Training loss: 0.616361126888142262 Training accuracy: 93.5200000000001%

Test accuracy: 87.6%

Epoch 188

Training loss: 0.6143469426363560454

Training accuracy: 93.76%

Test accuracy: 87.8%

Epoch 189

Training loss: 0.6131238347822947631

Training accuracy: 93.72%

Test accuracy: 87.6%

Epoch 190

Training loss: 0.61127910880563941993

Training accuracy: 93.84%

Test accuracy: 88.0%

Epoch 191

Training loss: 0.60890157521974988634

Training accuracy: 93.92%

Test accuracy: 87.4%

Epoch 192

Training loss: 0.60758724443976687315

Training accuracy: 93.8% Test accuracy: 87.6%

Training loss: 0.6056600340362162441

Training accuracy: 93.84%

Test accuracy: 88.0%

Epoch 194

Training loss: 0.60412219758631545516

Training accuracy: 93.96%

Test accuracy: 87.8%

Epoch 195

Training loss: 0.602337904903135703

Training accuracy: 93.88%

Test accuracy: 88.0%

Epoch 196

Training loss: 0.60057651468884508877

Training accuracy: 93.84%

Test accuracy: 87.6%

Epoch 197

Training loss: 0.5990361561873028138

Training accuracy: 93.92%

Test accuracy: 87.6%

Epoch 198

Training loss: 0.597834502980628766

Training accuracy: 93.92%

Test accuracy: 87.6%

Epoch 199

Training loss: 0.5966503912371351327

Training accuracy: 94.16%

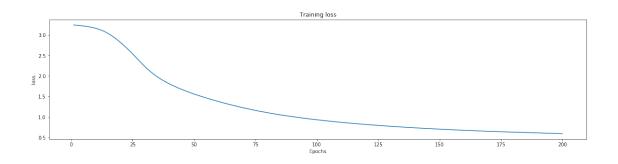
Test accuracy: 87.6%

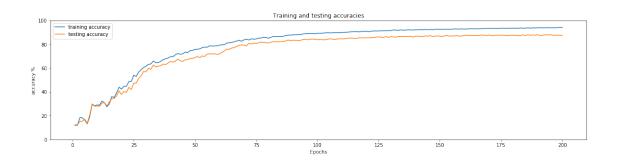
Epoch 200

Training loss: 0.5945048589134503131

Training accuracy: 94.04%

Test accuracy: 87.4%





Since we tend to get similar results for both eta=0.1 and eta=0.01, we continue with eta=0.1

# Finally we check if regularization is helpful or not First with no regularization

[30]: net = network.Linear\_Network([784, 35, 25, 10])
net.SGD(training\_data, 50, 10, 0.1, lmbda = 0.0, test\_data=testing\_data)

### Epoch 1

Training loss: 3.1566247878512270909

Training accuracy: 19.16%

Test accuracy: 19.2%

### Epoch 2

Training loss: 2.638599112819415536

Training accuracy: 53.2% Test accuracy: 48.8%

# Epoch 3

Training loss: 1.9805994656752686879

Training accuracy: 63.56%

Test accuracy: 59.4%

## Epoch 4

Training loss: 1.608633046737969135

Training accuracy: 76.84%

Test accuracy: 74.2%

Epoch 5

Training loss: 1.3345860039540976656

Training accuracy: 81.04%

Test accuracy: 77.8%

Epoch 6

Training loss: 1.1284489039738173178
Training accuracy: 83.5200000000001%
Test accuracy: 79.6000000000001%

Epoch 7

Training loss: 1.0026843595724710446
Training accuracy: 86.96000000000001%

Test accuracy: 83.0%

Epoch 8

Training loss: 0.86874549684692934

Training accuracy: 89.16%

Test accuracy: 84.6%

Epoch 9

Training loss: 0.7653506640010482795

Training accuracy: 90.48%

Test accuracy: 85.6%

Epoch 10

Training loss: 0.6954871826036289916

Training accuracy: 91.0% Test accuracy: 86.4%

Epoch 11

Training loss: 0.635146010930845314

Training accuracy: 91.8% Test accuracy: 87.0%

Epoch 12

Training loss: 0.57202693843374002706

Training accuracy: 93.36%

Test accuracy: 86.8%

Epoch 13

Training loss: 0.52869511146036359293

Training accuracy: 94.0% Test accuracy: 86.8%

Epoch 14

Training loss: 0.49522335450114631322 Training accuracy: 94.52000000000001%

Test accuracy: 87.2%

Epoch 15

Training loss: 0.4555449436507736489

Training accuracy: 94.64% Test accuracy: 88.0%

Epoch 16

Training loss: 0.42898493685530982074 Training accuracy: 95.2400000000001%

Test accuracy: 87.6%

Epoch 17

Training loss: 0.399284533070007757

Training accuracy: 95.56% Test accuracy: 87.4%

Epoch 18

Training loss: 0.38202419382888428833

Training accuracy: 95.76% Test accuracy: 87.0%

Epoch 19

Training loss: 0.35723311841749348362 Training accuracy: 96.2400000000001%

Test accuracy: 87.0%

Epoch 20

Training loss: 0.34810640722746674254

Training accuracy: 96.16% Test accuracy: 87.6%

Epoch 21

Training loss: 0.3231433343829978936

Training accuracy: 96.28% Test accuracy: 87.8%

Epoch 22

Training loss: 0.2905622877744582346

Training accuracy: 97.0% Test accuracy: 88.2%

Epoch 23

Training loss: 0.27556723798554143794

Training accuracy: 97.28% Test accuracy: 88.0%

Training loss: 0.26657158046482363966 Training accuracy: 97.399999999999%

Test accuracy: 87.6%

Epoch 25

Training loss: 0.24837797672056164642

Training accuracy: 97.84%

Test accuracy: 87.4%

Epoch 26

Training loss: 0.23185170300059365869 Training accuracy: 97.9600000000001%

Test accuracy: 88.0%

Epoch 27

Training loss: 0.2204594919446421013

Training accuracy: 98.04%

Test accuracy: 87.0%

Epoch 28

Training loss: 0.20808602338657359802

Training accuracy: 98.16% Test accuracy: 87.8%

Epoch 29

Training loss: 0.19481388368811271211

Training accuracy: 98.32%

Test accuracy: 87.6%

Epoch 30

Training loss: 0.18746235075330992874

Training accuracy: 98.52%

Test accuracy: 87.8%

Epoch 31

Training loss: 0.17624785879693008033

Training accuracy: 98.68%

Test accuracy: 88.2%

Epoch 32

Training loss: 0.16684809755391320649 Training accuracy: 98.839999999999%

Test accuracy: 87.8%

Epoch 33

Training loss: 0.15794250167174995801

Training accuracy: 98.839999999999%

Test accuracy: 88.2%

Epoch 34

Training loss: 0.14858422332373452581

Training accuracy: 99.0% Test accuracy: 87.2%

Epoch 35

Training loss: 0.14277124008601227345 Training accuracy: 99.119999999999%

Test accuracy: 88.0%

Epoch 36

Training loss: 0.13485401159964168761 Training accuracy: 99.119999999999%

Test accuracy: 88.0%

Epoch 37

Training loss: 0.12945302037582401789

Training accuracy: 99.2% Test accuracy: 87.4%

Epoch 38

Training loss: 0.12693830053463929211

Training accuracy: 99.36%

Test accuracy: 87.4%

Epoch 39

Training loss: 0.12491073151483849345

Training accuracy: 99.32%

Test accuracy: 88.0%

Epoch 40

Training loss: 0.11309156008954263679

Training accuracy: 99.4% Test accuracy: 87.8%

Epoch 41

Training loss: 0.10671730965437816927

Training accuracy: 99.48%

Test accuracy: 88.6%

Epoch 42

Training loss: 0.10223956193534999181

Training accuracy: 99.52%

Test accuracy: 88.4%

Training loss: 0.098737920743430498724

Training accuracy: 99.52%

Test accuracy: 88.2%

Epoch 44

Training loss: 0.096304470109465864944

Training accuracy: 99.6% Test accuracy: 88.0%

Epoch 45

Training loss: 0.09017947684613037218

Training accuracy: 99.64%

Test accuracy: 88.0%

Epoch 46

Training loss: 0.087573065413591265116

Training accuracy: 99.68% Test accuracy: 88.6%

Epoch 47

Training loss: 0.084378827461023778266

Training accuracy: 99.68%

Test accuracy: 88.4%

Epoch 48

Training loss: 0.07969449837067826522

Training accuracy: 99.68%

Test accuracy: 88.4%

Epoch 49

Training loss: 0.078168595932950542455

Training accuracy: 99.68%

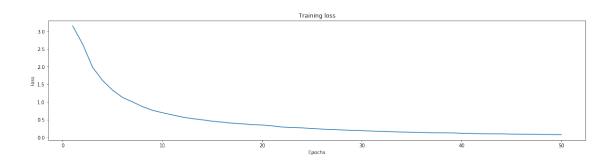
Test accuracy: 88.0%

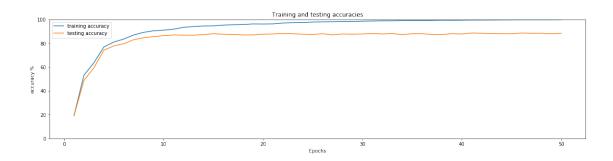
Epoch 50

Training loss: 0.07624919357889873241

Training accuracy: 99.72%

Test accuracy: 88.4%





Clearly there has been over fitting as the training accuracy is 99%. It doesn't show up on the test accuracy as the testing set is too small. Hence we try different regularization factors to see which fits best

```
[34]: regs = [1.0, 2.0, 3.0, 4.0, 5.0, 6.0, 7.0, 8.0, 9.0]
      train accuracies=[]
      test_accuracies=[]
      for reg in regs:
          net = network.Linear_Network([784, 35, 25, 10])
          tr_a, te_a = net.SGD(training_data, 50, 10, 0.1, lmbda = reg,_
       →test_data=testing_data,
                 show_eval=False, show_graph=False, return_accuracies=True)
          train_accuracies.append(tr_a)
          test_accuracies.append(te_a)
          print("regularization factor:"+str(reg))
          print("Training acc.: "+str(tr_a)+"% Testing acc.: "+str(te_a)+"%")
          print()
      plt.subplot(2, 1, 1)
      plt.plot(regs, train_accuracies, label='training accuracy')
      plt.plot(regs, test_accuracies, label='test accuracy')
      plt.legend()
      plt.title("Training and testing accuracies")
      plt.xlabel("neurons")
      plt.ylabel("accuracy %")
```

```
plt.ylim(0, 100)
plt.show()
```

regularization factor:1.0

Training acc.: 99.512% Testing acc.: 88.6799999999999%

regularization factor:2.0

Training acc.: 99.0239999999999% Testing acc.: 88.6799999999999%

regularization factor: 3.0

Training acc.: 98.016% Testing acc.: 87.6799999999999%

regularization factor: 4.0

Training acc.: 97.088% Testing acc.: 87.2400000000001%

regularization factor:5.0

Training acc.: 96.48% Testing acc.: 87.8000000000001%

regularization factor:6.0

Training acc.: 95.6480000000001% Testing acc.: 87.36%

regularization factor:7.0

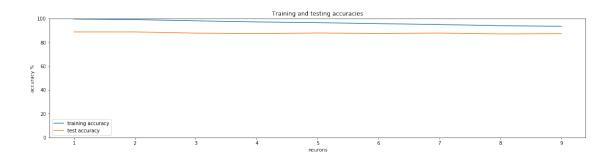
Training acc.: 94.912% Testing acc.: 87.72%

regularization factor:8.0

Training acc.: 93.928% Testing acc.: 87.0%

regularization factor:9.0

Training acc.: 93.4% Testing acc.: 87.2%



We see the training accuracy constantly dropping while the testing accuracy remained constant. This is indicative of over fitting. But we can't be too sure as the training and testing data is too small. We'd need at least a bigger testing data to be entirely sure.

So for now, we stick to regularization of 7.0

We'll revist the regularization tuning when we look at Cross Validation Now that we finally have all our parameters, let's take a list them down. Then we'll visualize the results on the testing data

- 1. size = [784, 35, 25, 10]
- 2. weight\_initializer = 'default'
- 3. cost = 'CrossEntropy'
- 4. activation = 'sigmoid'
- 5. epochs = 50
- 6. batch size = 10
- 7. eta = 0.1
- 8. lmbda = 7.0

Final run of the mdoel

```
[3]: net = network.Linear_Network([784,35,25,10])
net.SGD(training_data, 50, 10, 0.1, lmbda = 7.0, test_data = testing_data)
```

### Epoch 1

Training loss: 3.2326841205725281342
Training accuracy: 10.28000000000001%
Test accuracy: 11.79999999999999

#### Epoch 2

Training loss: 2.9537459618658661222

Training accuracy: 39.04%

Test accuracy: 36.1999999999996%

# Epoch 3

Training loss: 2.4236604054472806506 Training accuracy: 50.96000000000001%

Test accuracy: 49.0%

### Epoch 4

Training loss: 2.0560941779011762964
Training accuracy: 61.76000000000000%

Test accuracy: 58.4%

# Epoch 5

Training loss: 1.7851758473356474966

Training accuracy: 73.64% Test accuracy: 68.2%

Epoch 6

Training loss: 1.5828159690652832289

Training accuracy: 75.48%

Test accuracy: 71.2%

# Epoch 7

Training loss: 1.4069334791200266226 Training accuracy: 79.759999999999%

Test accuracy: 75.2%

Epoch 8

Training loss: 1.2701079597692875129

Training accuracy: 84.28%

Test accuracy: 81.2%

Epoch 9

Training loss: 1.1523511466166390834

Training accuracy: 86.88% Test accuracy: 83.6%

Epoch 10

Training loss: 1.0689898801611050113

Training accuracy: 88.36% Test accuracy: 84.2%

Epoch 11

Training loss: 0.9958489060768214889

Training accuracy: 89.24% Test accuracy: 85.6%

Epoch 12

Training loss: 0.94237863925684892477

Training accuracy: 89.24% Test accuracy: 85.2%

Epoch 13

Training loss: 0.89018769680228264287

Training accuracy: 90.8% Test accuracy: 85.8%

Epoch 14

Training loss: 0.8528112852957638264 Training accuracy: 91.08000000000001%

Test accuracy: 86.0%

Epoch 15

Training loss: 0.8458220951912395739

Training accuracy: 91.56%

Test accuracy: 85.2%

Epoch 16

Training loss: 0.79749523820170468784

Training accuracy: 90.92% Test accuracy: 86.2%

Training loss: 0.78889735394966301713

Training accuracy: 90.64% Test accuracy: 86.6%

Epoch 18

Training loss: 0.7622515288662194772

Training accuracy: 91.92%

Test accuracy: 87.4%

Epoch 19

Training loss: 0.7348530839081167861

Training accuracy: 91.92%

Test accuracy: 87.2%

Epoch 20

Training loss: 0.7299510551153513726

Training accuracy: 92.16%

Test accuracy: 87.6%

Epoch 21

Training loss: 0.71238620434335595336

Training accuracy: 92.96% Test accuracy: 87.8%

Epoch 22

Training loss: 0.6891577904927793396

Training accuracy: 93.28%

Test accuracy: 87.4%

Epoch 23

Training loss: 0.69107512165084638786

Training accuracy: 93.12%

Test accuracy: 87.4%

Epoch 24

Training loss: 0.68156985734990621346

Training accuracy: 93.36%

Test accuracy: 87.0%

Epoch 25

Training loss: 0.6626684695361602232

Training accuracy: 93.16%

Test accuracy: 88.0%

Epoch 26

Training loss: 0.65078858219642967206

Training accuracy: 93.76%

Test accuracy: 88.2%

Epoch 27

Training loss: 0.6458221216025693004

Training accuracy: 94.08%

Test accuracy: 87.8%

Epoch 28

Training loss: 0.63586314620361638754

Training accuracy: 94.24%

Test accuracy: 87.6%

Epoch 29

Training loss: 0.63400881903736921677

Training accuracy: 93.84%

Test accuracy: 87.8%

Epoch 30

Training loss: 0.6251042179150910963 Training accuracy: 94.5200000000001%

Test accuracy: 88.2%

Epoch 31

Training loss: 0.61695678820882455173

Training accuracy: 94.64%

Test accuracy: 88.0%

Epoch 32

Training loss: 0.6177354067088967172

Training accuracy: 94.48%

Test accuracy: 87.8%

Epoch 33

Training loss: 0.61754338812817334466

Training accuracy: 94.44%

Test accuracy: 87.6%

Epoch 34

Training loss: 0.6165443884876816758

Training accuracy: 94.12%

Test accuracy: 87.6%

Epoch 35

Training loss: 0.6033791667883454335

Training accuracy: 94.44%

Test accuracy: 87.6%

Training loss: 0.6021970325391033135

Training accuracy: 94.56%

Test accuracy: 87.8%

Epoch 37

Training loss: 0.5987250311007248646

Training accuracy: 94.64%

Test accuracy: 88.2%

Epoch 38

Training loss: 0.6112678590840087999

Training accuracy: 93.84%

Test accuracy: 88.4%

Epoch 39

Training loss: 0.60098091201283159623

Training accuracy: 94.16%

Test accuracy: 88.0%

Epoch 40

Training loss: 0.5943690540855281772 Training accuracy: 94.399999999999%

Test accuracy: 88.2%

Epoch 41

Training loss: 0.59540718384031455964

Training accuracy: 95.12%

Test accuracy: 87.6%

Epoch 42

Training loss: 0.5805668478565324346 Training accuracy: 94.679999999999%

Test accuracy: 87.4%

Epoch 43

Training loss: 0.59134911657571848293 Training accuracy: 94.3200000000001%

Test accuracy: 87.6%

Epoch 44

Training loss: 0.58343780479105319026

Training accuracy: 94.76%

Test accuracy: 88.2%

Epoch 45

Training loss: 0.5813726071401272093

Training accuracy: 94.8%

Test accuracy: 88.6%

Epoch 46

Training loss: 0.5746104797288835689

Training accuracy: 95.12%

Test accuracy: 87.8%

Epoch 47

Training loss: 0.57736468906669823493 Training accuracy: 95.199999999999%

Test accuracy: 87.4%

Epoch 48

Training loss: 0.57321975893967532943 Training accuracy: 95.199999999999%

Test accuracy: 87.0%

Epoch 49

Training loss: 0.57746910449444494555

Training accuracy: 94.96%

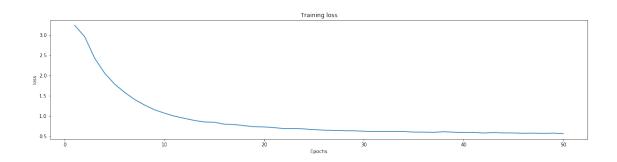
Test accuracy: 87.6%

Epoch 50

Training loss: 0.56415261698794610885

Training accuracy: 95.16%

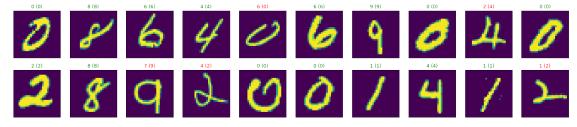
Test accuracy: 88.0%





Now we are ready to visualize some results: Let's run it on 20 test datas

```
[22]: from PIL import Image
      test_set = testing_data[:20]
      prediction=[]
      label=[]
      images=[]
      for (x,y) in test_set:
          prediction.append(np.argmax(net.feedforward(x)))
          label.append(y)
          image = x[0]
          image = x.reshape(28,28)*255
          images.append(image)
      fig = plt.figure(figsize=(25, 5))
      for idx in np.arange(20):
          ax = fig.add_subplot(2, 10, idx+1, xticks=[], yticks=[])
          plt.imshow(images[idx])
          ax.set_title("{} ({})".format(str(prediction[idx]), str(label[idx].item())),
                       color=("green" if prediction[idx]==label[idx] else "red"))
```



# 2.2.8 Now, finally lets use Cross validation to see if we get any improvement

We'll be using k-fold cross validation with k=10

```
[24]: training_data_CV = data_loader.load_full_data_cross_validate()
```

First, without any regularization

```
[28]: net2 = network.Linear_Network_CrossValidation([784,35,25,10])
```

```
[29]: net2.SGD(training_data_CV, 200, 10, 0.5, lmbda=0.0)
```

Training loss: 3.233537854495628635
Training accuracy: 14.41666666666668%
Test accuracy: 11.6666666666668%

# Epoch 2

Training loss: 3.2136444536432516718
Training accuracy: 17.833333333333336%
Test accuracy: 14.333333333333332%

### Epoch 3

Training loss: 3.1936151538179284432
Training accuracy: 22.583333333333336%
Test accuracy: 17.16666666666664%

## Epoch 4

Training loss: 3.1697761742039304717 Training accuracy: 27.5833333333333332% Test accuracy: 26.66666666666664%

### Epoch 5

Training loss: 3.1344249098431653114
Training accuracy: 35.54166666666667%
Test accuracy: 30.16666666666664%

# Epoch 6

Training loss: 3.0894104136105461755 Training accuracy: 40.458333333333333 Test accuracy: 38.66666666666664%

### Epoch 7

Training loss: 3.0208982340898541958 Training accuracy: 44.249999999999%

Test accuracy: 45.0%

#### Epoch 8

### Epoch 9

Training loss: 2.811105203930599877

Training accuracy: 46.125%

Test accuracy: 45.16666666666667%

## Epoch 10

Training loss: 2.6667257286226191304

Training accuracy: 49.75%

Test accuracy: 48.0000000000001%

Epoch 11

Training loss: 2.5389568290337344732 Training accuracy: 52.833333333333336%

Test accuracy: 55.5%

Epoch 12

Training loss: 2.3855806663028148716

Training accuracy: 55.375%

Test accuracy: 51.5%

Epoch 13

Training loss: 2.271666654296425065 Training accuracy: 58.7083333333333%

Test accuracy: 61.0%

Epoch 14

Training loss: 2.163025813302426088 Training accuracy: 62.583333333333336%

Test accuracy: 61.6666666666667%

Epoch 15

Training loss: 2.0537074913546677784
Training accuracy: 65.20833333333334%
Test accuracy: 61.833333333333336%

Epoch 16

Training loss: 1.9638222763344113231
Training accuracy: 67.666666666666666%

Test accuracy: 67.0%

Epoch 17

Training loss: 1.8835723106574945352

Training accuracy: 68.75%

Test accuracy: 70.5%

Epoch 18

Training loss: 1.8045931964493152448
Training accuracy: 71.79166666666667%

Test accuracy: 72.0%

Epoch 19

Training loss: 1.7324466340130144214 Training accuracy: 73.1249999999999% Test accuracy: 73.333333333333333

Epoch 20

Training loss: 1.6648586208553211743
Training accuracy: 75.54166666666666%

Test accuracy: 76.5%

## Epoch 21

Training loss: 1.5946132950316805122 Training accuracy: 76.8750000000001% Test accuracy: 75.999999999999%

## Epoch 22

Training loss: 1.535241905843814365 Training accuracy: 77.5416666666667% Test accuracy: 76.1666666666667%

### Epoch 23

Training loss: 1.4709052516064160574
Training accuracy: 79.70833333333334%
Test accuracy: 75.5000000000001%

#### Epoch 24

Training loss: 1.4430616623719659966
Training accuracy: 79.58333333333334%

Test accuracy: 82.5%

### Epoch 25

Training loss: 1.3864291292202437616 Training accuracy: 81.33333333333334% Test accuracy: 82.4999999999999

## Epoch 26

Training loss: 1.3301467053309693075 Training accuracy: 82.91666666666667%

Test accuracy: 81.0%

## Epoch 27

Training loss: 1.2926144981573606048
Training accuracy: 83.20833333333334%

Test accuracy: 83.5%

# Epoch 28

Training loss: 1.2445197852773281304 Training accuracy: 84.3749999999999% Test accuracy: 82.83333333333334%

# Epoch 29

Training loss: 1.1908512600625459742
Training accuracy: 85.33333333333333%

Test accuracy: 82.5%

Epoch 31

Epoch 32

Epoch 33

Training loss: 1.0557087938613798154

Training accuracy: 87.0%

Test accuracy: 86.6666666666666%

Epoch 34

Training loss: 1.026124732991103635

Training accuracy: 87.25% Test accuracy: 87.5%

Epoch 35

Training loss: 0.99993741448852918466 Training accuracy: 87.58333333333334% Test accuracy: 87.33333333333334%

Epoch 36

Training loss: 0.9602884423170300631 Training accuracy: 88.33333333333333%

Test accuracy: 85.5%

Epoch 37

Training loss: 0.94301490964553000794 Training accuracy: 88.3333333333334% Test accuracy: 88.8333333333334%

Epoch 38

Training loss: 0.9045795184717783384 Training accuracy: 88.9999999999999% Test accuracy: 86.833333333333333

Epoch 39

Training loss: 0.8872087088640832861

Training accuracy: 88.3333333333333333333

Test accuracy: 88.5%

Epoch 40

Training loss: 0.86917929699570480116 Training accuracy: 89.1666666666667% Test accuracy: 88.3333333333334%

Epoch 41

Training loss: 0.82985020283456606676 Training accuracy: 89.95833333333333%

Test accuracy: 85.0%

Epoch 42

Training loss: 0.81448734432867398516

Training accuracy: 89.875%

Test accuracy: 87.66666666666666%

Epoch 43

Training loss: 0.803156388806158129 Training accuracy: 90.41666666666666%

Test accuracy: 87.5%

Epoch 44

Epoch 45

Epoch 46

Epoch 47

Training loss: 0.7446162045200841144

Training accuracy: 90.875%

Test accuracy: 89.33333333333334%

Epoch 48

Training loss: 0.7441090282189275952 Training accuracy: 90.25000000000001%

Test accuracy: 92.0%

Epoch 50

Training loss: 0.70909111842985812345

Training accuracy: 90.875%

Test accuracy: 90.83333333333334%

Epoch 51

Training loss: 0.68323298413620381093 Training accuracy: 91.20833333333334% Test accuracy: 90.33333333333334%

Epoch 52

Training loss: 0.66851598356334323447 Training accuracy: 91.45833333333334% Test accuracy: 90.83333333333334%

Epoch 53

Training loss: 0.64968153618653084574 Training accuracy: 91.70833333333333%

Test accuracy: 89.0%

Epoch 54

Training loss: 0.6398616372196474671 Training accuracy: 91.62500000000001% Test accuracy: 90.1666666666667%

Epoch 55

Training loss: 0.6412475480804507115

Training accuracy: 91.75%

Test accuracy: 90.3333333333333333%

Epoch 56

Epoch 57

Training loss: 0.614212794631739877
Training accuracy: 92.2500000000001%

Test accuracy: 91.0%

Epoch 58

Training loss: 0.6136251767230409955

Training accuracy: 92.0%

Test accuracy: 92.5%

Epoch 59

Training loss: 0.59304443407742042275 Training accuracy: 92.20833333333334% Test accuracy: 91.499999999999%

Epoch 60

Training loss: 0.57930135996502677673 Training accuracy: 92.4166666666667% Test accuracy: 90.83333333333333%

Epoch 61

Training loss: 0.57294108257769131814
Training accuracy: 92.458333333333334%

Test accuracy: 92.0%

Epoch 62

Training loss: 0.5642136022420478326 Training accuracy: 92.58333333333334%

Test accuracy: 91.0%

Epoch 63

Epoch 64

Training loss: 0.5393062154227270558

Training accuracy: 93.0%

Test accuracy: 90.83333333333334%

Epoch 65

Training loss: 0.5346263021869130283

Training accuracy: 93.125%

Test accuracy: 91.5%

Epoch 66

Training loss: 0.53614029488283986713 Training accuracy: 93.20833333333334% Test accuracy: 91.83333333333333%

Epoch 67

Training loss: 0.5238537524958866116 Training accuracy: 93.3749999999999% Test accuracy: 92.1666666666666%

Epoch 68

Training loss: 0.5141374183858615948 Training accuracy: 93.54166666666667% Test accuracy: 90.6666666666666%

### Epoch 69

Training loss: 0.5034502230425772184
Training accuracy: 93.541666666666666%

Test accuracy: 91.5%

### Epoch 70

Training loss: 0.49332982763752986497 Training accuracy: 93.95833333333334% Test accuracy: 91.66666666666667%

### Epoch 71

Training loss: 0.4981555185247075186 Training accuracy: 93.62500000000001% Test accuracy: 92.1666666666666%

#### Epoch 72

Training loss: 0.4859485794092234187 Training accuracy: 93.7916666666667% Test accuracy: 93.1666666666666%

### Epoch 73

Training loss: 0.49292245857212593703 Training accuracy: 93.58333333333334% Test accuracy: 95.333333333333333

# Epoch 74

Training loss: 0.48058538978474888274

Training accuracy: 94.0% Test accuracy: 94.0%

## Epoch 75

Training loss: 0.46670350525377085426 Training accuracy: 94.45833333333334% Test accuracy: 92.83333333333333%

# Epoch 76

Training loss: 0.46580880439297319
Training accuracy: 94.04166666666667%

Test accuracy: 94.5%

# Epoch 77

Training loss: 0.45025278126030846286 Training accuracy: 94.4166666666666% Test accuracy: 93.83333333333333%

Training loss: 0.44568515329730115244

Training accuracy: 94.625%

Test accuracy: 93.1666666666666%

### Epoch 79

Training loss: 0.45728493769409120825 Training accuracy: 94.04166666666666%

Test accuracy: 95.0%

### Epoch 80

Training loss: 0.43893024364561242532 Training accuracy: 94.41666666666666% Test accuracy: 94.16666666666666%

# Epoch 81

#### Epoch 82

# Epoch 83

Training loss: 0.42013993720283877297 Training accuracy: 94.66666666666666%

Test accuracy: 94.5%

## Epoch 84

Training loss: 0.4110694180304460797 Training accuracy: 94.9583333333333333 Test accuracy: 94.5000000000001%

# Epoch 85

Training loss: 0.396175139717582081 Training accuracy: 95.29166666666666% Test accuracy: 93.333333333333333

### Epoch 86

Training loss: 0.40289144932859024913

Training accuracy: 95.0% Test accuracy: 94.0%

# Epoch 87

Training loss: 0.3942100646964119145

Epoch 88

Training loss: 0.40213892306792189125 Training accuracy: 95.0000000000001% Test accuracy: 95.0000000000001%

Epoch 89

Training loss: 0.3930557160175613247 Training accuracy: 95.5416666666667% Test accuracy: 94.1666666666666%

Epoch 90

Training loss: 0.39824597951079950358 Training accuracy: 95.2916666666667% Test accuracy: 95.499999999999%

Epoch 91

Test accuracy: 95.5%

Epoch 92

Training loss: 0.37552515954703147158 Training accuracy: 95.6666666666667% Test accuracy: 94.16666666666666%

Epoch 93

Training loss: 0.3674534473840604852

Training accuracy: 95.625%

Test accuracy: 95.1666666666666%

Epoch 94

Training loss: 0.3760295920381473143
Training accuracy: 95.29166666666667%

Test accuracy: 96.0%

Epoch 95

Training loss: 0.36306118467090412694 Training accuracy: 95.7916666666667% Test accuracy: 94.6666666666667%

Epoch 96

Training loss: 0.3668929916001822132 Training accuracy: 95.83333333333334%

Test accuracy: 95.5%

Training loss: 0.35835375228697677834 Training accuracy: 95.70833333333334% Test accuracy: 96.33333333333333%

Epoch 98

Training loss: 0.34991033829118221109 Training accuracy: 95.958333333333334%

Test accuracy: 95.5%

Epoch 99

Training loss: 0.34653206556367312252 Training accuracy: 96.1666666666666% Test accuracy: 95.499999999999%

Epoch 100

Training loss: 0.34749667747319227767 Training accuracy: 96.124999999999% Test accuracy: 96.166666666666%

Epoch 101

Training loss: 0.33248805795580390975 Training accuracy: 96.50000000000001%

Test accuracy: 94.5%

Epoch 102

Training loss: 0.33296794195569076542 Training accuracy: 96.4166666666666% Test accuracy: 95.5000000000001%

Epoch 103

Training loss: 0.3230726531059142974

Training accuracy: 96.5%

Test accuracy: 95.1666666666666%

Epoch 104

Training loss: 0.3186702769406441511 Training accuracy: 96.708333333333334%

Test accuracy: 95.0%

Epoch 105

Training loss: 0.31552180475221269874 Training accuracy: 96.3750000000001% Test accuracy: 96.3333333333333333

Epoch 106

Training loss: 0.30715800825228927538 Training accuracy: 96.70833333333334% Test accuracy: 95.1666666666666%

Epoch 107

Training loss: 0.31372719525712916458 Training accuracy: 96.5416666666667% Test accuracy: 96.33333333333334%

Epoch 108

Training loss: 0.31147468389433702747 Training accuracy: 96.58333333333334% Test accuracy: 97.0000000000001%

Epoch 109

Training loss: 0.30401946100437874022 Training accuracy: 96.7500000000001% Test accuracy: 95.333333333333333

Epoch 110

Training loss: 0.29473213582329932522 Training accuracy: 97.04166666666666%

Test accuracy: 95.0%

Epoch 111

Training loss: 0.30458225851461759233 Training accuracy: 96.70833333333334% Test accuracy: 96.66666666666667%

Epoch 112

Training loss: 0.3024291566177774124 Training accuracy: 96.83333333333334% Test accuracy: 96.1666666666667%

Epoch 113

Epoch 114

Epoch 115

Training loss: 0.27537320018474425207 Training accuracy: 97.5416666666666% Test accuracy: 94.999999999999%

Epoch 116

Training loss: 0.28973314538900529308 Training accuracy: 97.0416666666666% Test accuracy: 96.33333333333334%

Epoch 117

Training loss: 0.27828360515138396428 Training accuracy: 97.2916666666667% Test accuracy: 96.333333333333333

Epoch 118

Training loss: 0.2748774380718776696 Training accuracy: 97.1249999999999% Test accuracy: 96.6666666666666%

Epoch 119

Training loss: 0.27885319655724924705 Training accuracy: 97.37500000000001%

Test accuracy: 98.0%

Epoch 120

Training loss: 0.2607242075577945485

Training accuracy: 97.625%

Test accuracy: 96.333333333333333333

Epoch 121

Training loss: 0.27190881512309718004 Training accuracy: 97.4166666666666% Test accuracy: 97.83333333333334%

Epoch 122

Training loss: 0.27499029498764918783 Training accuracy: 97.416666666666666%

Test accuracy: 97.5%

Epoch 123

Training loss: 0.26492011557657773056 Training accuracy: 97.5416666666667% Test accuracy: 96.33333333333334%

Epoch 124

Training loss: 0.26281708558338961248 Training accuracy: 97.79166666666666%

Test accuracy: 97.0%

Epoch 125

Training loss: 0.2594877697893804848

Training accuracy: 97.5%

Test accuracy: 97.333333333333333333

Training loss: 0.24801046766115878418 Training accuracy: 97.5833333333333333 Test accuracy: 97.9999999999999%

Epoch 127

Training loss: 0.2544819256691145019 Training accuracy: 97.66666666666666% Test accuracy: 97.33333333333334%

Epoch 128

Training loss: 0.2510110560142390494 Training accuracy: 97.83333333333334% Test accuracy: 97.5000000000001%

Epoch 129

Training loss: 0.24983823585143704555 Training accuracy: 97.749999999999% Test accuracy: 97.83333333333334%

Epoch 130

Training loss: 0.23796188689254582613

Training accuracy: 97.75%

Test accuracy: 97.1666666666666%

Epoch 131

Training loss: 0.24288715871391874937 Training accuracy: 97.79166666666666%

Test accuracy: 98.5%

Epoch 132

Training loss: 0.23844946243967035447 Training accuracy: 98.20833333333334% Test accuracy: 97.16666666666666%

Epoch 133

Training loss: 0.23248424737769048774
Training accuracy: 98.1666666666667%
Test accuracy: 97.0000000000001%

Epoch 134

Training loss: 0.23234957393184391429 Training accuracy: 98.1666666666666% Test accuracy: 97.3333333333333333

Epoch 135

Training loss: 0.23069132606995833797

Epoch 136

Training loss: 0.22076983262285283384

Training accuracy: 98.25%

Test accuracy: 98.0%

Epoch 137

Training loss: 0.22856290434131055765

Training accuracy: 98.25%

Test accuracy: 97.999999999999%

Epoch 138

Training loss: 0.23152964668479385666

Training accuracy: 98.375%

Test accuracy: 98.33333333333334%

Epoch 139

Training loss: 0.21639159129902917635

Training accuracy: 98.5%

Test accuracy: 96.999999999999%

Epoch 140

Training loss: 0.21353158560195480684

Training accuracy: 98.375%

Test accuracy: 97.83333333333334%

Epoch 141

Training loss: 0.2068775154896613747 Training accuracy: 98.66666666666666%

Test accuracy: 97.0%

Epoch 142

Training loss: 0.21651357599337643696

Training accuracy: 98.25%

Test accuracy: 98.6666666666666%

Epoch 143

Training loss: 0.21344324591054655433 Training accuracy: 98.29166666666666% Test accuracy: 98.333333333333333

Epoch 144

Training loss: 0.2050188983531804092

Training accuracy: 98.375%

Test accuracy: 98.33333333333334%

Training loss: 0.19500051027553397246 Training accuracy: 98.83333333333334% Test accuracy: 97.66666666666667%

Epoch 146

Training loss: 0.21241827381397513069

Training accuracy: 98.375%

Test accuracy: 98.6666666666667%

Epoch 147

Training loss: 0.19445402009707637442
Training accuracy: 98.583333333333334%
Test accuracy: 97.99999999999999

Epoch 148

Epoch 149

Training loss: 0.1964831167542076017 Training accuracy: 98.4583333333333333 Test accuracy: 98.66666666666666%

Epoch 150

Training loss: 0.20080591498319494352 Training accuracy: 98.4166666666667% Test accuracy: 99.33333333333334%

Epoch 151

Epoch 152

Training loss: 0.19249646562606721745 Training accuracy: 98.5416666666666% Test accuracy: 98.83333333333334%

Epoch 153

Training loss: 0.19488623774093451176 Training accuracy: 98.583333333333333%

Test accuracy: 99.0%

Epoch 154

Training loss: 0.18104430865038142136 Training accuracy: 98.6249999999999% Test accuracy: 98.33333333333334%

Epoch 155

Training loss: 0.1800293033728428389 Training accuracy: 98.66666666666666%

Test accuracy: 98.5%

Epoch 156

Training loss: 0.17708346129552741228 Training accuracy: 98.95833333333334% Test accuracy: 97.9999999999999

Epoch 157

Training loss: 0.16836035965957944655

Training accuracy: 98.875%

Test accuracy: 98.1666666666666%

Epoch 158

Training loss: 0.17230847323947600167 Training accuracy: 98.91666666666666% Test accuracy: 98.333333333333333

Epoch 159

Training loss: 0.17912693189021032777

Training accuracy: 98.75%

Test accuracy: 98.499999999999%

Epoch 160

Training loss: 0.17388458647384169331 Training accuracy: 98.833333333333333 Test accuracy: 99.16666666666667%

Epoch 161

Training loss: 0.1730708292116527965 Training accuracy: 98.7916666666667% Test accuracy: 98.83333333333333

Epoch 162

Training loss: 0.17582647651474587496 Training accuracy: 98.7916666666666% Test accuracy: 98.83333333333334%

Epoch 163

Training loss: 0.16697540169145183065 Training accuracy: 99.08333333333334% Test accuracy: 98.33333333333333

Epoch 164

Training loss: 0.17309629249206558117 Training accuracy: 98.79166666666667%

Test accuracy: 99.0%

Epoch 165

Epoch 166

Training loss: 0.16564558997883734772 Training accuracy: 98.8749999999999%

Test accuracy: 99.0%

Epoch 167

Training loss: 0.16820310344190631736

Training accuracy: 99.0%

Test accuracy: 99.1666666666667%

Epoch 168

Training loss: 0.1532430830000172007

Training accuracy: 99.0%

Test accuracy: 98.6666666666667%

Epoch 169

Training loss: 0.15882823152176912601 Training accuracy: 98.958333333333333 Test accuracy: 98.666666666666666%

Epoch 170

Training loss: 0.1548341771018890666

Training accuracy: 99.0%

Test accuracy: 98.33333333333334%

Epoch 171

Training loss: 0.15523995129799627125

Training accuracy: 99.0%

Test accuracy: 98.83333333333334%

Epoch 172

Training loss: 0.14957948841058119952 Training accuracy: 98.95833333333334% Test accuracy: 98.83333333333333%

Epoch 173

Training loss: 0.14611684124963931899

Training accuracy: 99.125%

Test accuracy: 98.33333333333334%

Training loss: 0.15140465326693490838 Training accuracy: 99.124999999999% Test accuracy: 98.666666666666%

#### Epoch 175

Training loss: 0.14590294970227477

Training accuracy: 99.125%

Test accuracy: 98.83333333333334%

### Epoch 176

Training loss: 0.15298028938280705454 Training accuracy: 98.83333333333334% Test accuracy: 99.666666666666666%

# Epoch 177

Training loss: 0.14639683234569530505 Training accuracy: 99.04166666666666%

Test accuracy: 99.5%

### Epoch 178

Training loss: 0.14749199265373726139 Training accuracy: 99.16666666666666%

Test accuracy: 99.0%

### Epoch 179

Training loss: 0.14646913557516882468 Training accuracy: 99.1666666666667% Test accuracy: 99.3333333333333333

## Epoch 180

Training loss: 0.14253620112813249294 Training accuracy: 99.2500000000001% Test accuracy: 99.1666666666666%

### Epoch 181

Training loss: 0.14190517383155897439 Training accuracy: 99.16666666666667%

Test accuracy: 99.5%

# Epoch 182

Training loss: 0.14018644935665947645 Training accuracy: 99.2083333333333%

Test accuracy: 99.5%

# Epoch 183

Training loss: 0.14080945784592921594

Training accuracy: 99.2916666666667% Test accuracy: 98.8333333333333333

Epoch 184

Training loss: 0.13775736094223302348 Training accuracy: 99.2500000000001% Test accuracy: 99.1666666666666%

Epoch 185

Training loss: 0.13406607285524639679

Training accuracy: 99.375%

Test accuracy: 98.83333333333333333

Epoch 186

Training loss: 0.13258924166296546687 Training accuracy: 99.2916666666666% Test accuracy: 99.1666666666666%

Epoch 187

Training loss: 0.13080697710423674828 Training accuracy: 99.25000000000001%

Test accuracy: 99.0%

Epoch 188

Training loss: 0.13426622844138323114 Training accuracy: 99.333333333333333 Test accuracy: 98.9999999999999%

Epoch 189

Training loss: 0.12549673862456182001 Training accuracy: 99.45833333333334% Test accuracy: 98.83333333333334%

Epoch 190

Training loss: 0.13033045967816450953 Training accuracy: 99.20833333333334%

Test accuracy: 99.5%

Epoch 191

Epoch 192

Training loss: 0.120301707585032027984 Training accuracy: 99.4166666666667% Test accuracy: 98.833333333333333

Training loss: 0.12077861821056685112

Training accuracy: 99.375%

Test accuracy: 99.1666666666666%

# Epoch 194

Training loss: 0.123122047850643746134 Training accuracy: 99.33333333333334% Test accuracy: 99.3333333333334%

### Epoch 195

Training loss: 0.1244189069402086804 Training accuracy: 99.5000000000001% Test accuracy: 99.0000000000001%

# Epoch 196

Training loss: 0.11702673569830103874 Training accuracy: 99.333333333333334%

Test accuracy: 99.5%

### Epoch 197

Training loss: 0.12590261000093152491 Training accuracy: 99.16666666666666%

Test accuracy: 100.0%

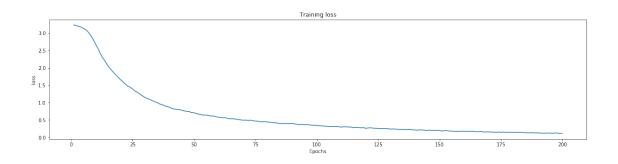
### Epoch 198

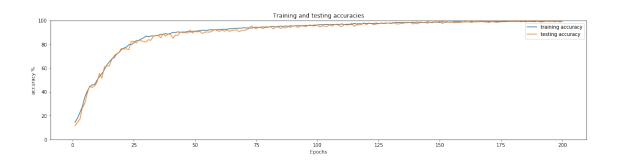
# Epoch 199

Training loss: 0.10853645496922166513 Training accuracy: 99.54166666666666% Test accuracy: 98.666666666666666%

### Epoch 200

Training loss: 0.11863103602889296698 Training accuracy: 99.3750000000001% Test accuracy: 99.333333333333333





Now trying with a regularizatin factor:

[26]: net2 = network.Linear\_Network\_CrossValidation([784,35,25,10])

[27]: net2.SGD(training\_data\_CV, 200, 10, 0.5, lmbda=5.0)

# Epoch 1

Training loss: 3.2479787792207839177
Training accuracy: 13.7083333333333334%

Test accuracy: 13.0%

# Epoch 2

Training loss: 3.2154712958092353582
Training accuracy: 16.083333333333336%
Test accuracy: 15.833333333333334%

# Epoch 3

Training loss: 3.2042990612529214736
Training accuracy: 18.75000000000004%
Test accuracy: 17.1666666666664%

# Epoch 4

Training loss: 3.182185956432032023
Training accuracy: 23.66666666666664%
Test accuracy: 19.000000000000004%

Training loss: 3.1563591483696204476

Training accuracy: 26.5%

Test accuracy: 23.49999999999996%

### Epoch 6

Training loss: 3.1190120285228041847
Training accuracy: 30.958333333333333%

Test accuracy: 30.0%

### Epoch 7

Training loss: 3.069249316275351229
Training accuracy: 34.04166666666664%
Test accuracy: 35.1666666666667%

# Epoch 8

Training loss: 2.9886785482640016581
Training accuracy: 36.291666666666664%

Test accuracy: 35.0%

### Epoch 9

Training loss: 2.8987725837657495876
Training accuracy: 37.208333333333336%
Test accuracy: 34.16666666666664%

### Epoch 10

Training loss: 2.7956088561542536055 Training accuracy: 37.4166666666667% Test accuracy: 31.4999999999993%

## Epoch 11

Training loss: 2.7089090824446049124
Training accuracy: 40.541666666666664%
Test accuracy: 39.3333333333333333

### Epoch 12

Training loss: 2.6062313580128571404 Training accuracy: 44.708333333333336% Test accuracy: 46.8333333333333%

# Epoch 13

Training loss: 2.5099035431732771692 Training accuracy: 47.7916666666667% Test accuracy: 49.333333333333336%

# Epoch 14

Training loss: 2.4219925465016178784

Training accuracy: 48.54166666666664% Test accuracy: 42.3333333333333336%

Epoch 15

Epoch 16

Training loss: 2.276330190651422131

Training accuracy: 56.0%

Test accuracy: 54.8333333333333336%

Epoch 17

Training loss: 2.2000531576148051117

Training accuracy: 57.25%

Test accuracy: 54.66666666666664%

Epoch 18

Training loss: 2.1370256995314808892 Training accuracy: 61.0416666666667% Test accuracy: 59.333333333333336%

Epoch 19

Training loss: 2.0848511237533405892 Training accuracy: 62.79166666666667%

Test accuracy: 65.5%

Epoch 20

Training loss: 2.0137205909015272482 Training accuracy: 67.0416666666667% Test accuracy: 66.166666666666%

Epoch 21

Training loss: 1.9533093302620241818 Training accuracy: 67.6249999999999% Test accuracy: 67.83333333333334%

Epoch 22

Epoch 23

Training loss: 1.8307328454711889418 Training accuracy: 70.8750000000001% Test accuracy: 67.6666666666666%

Epoch 25

Training loss: 1.7024188140817697199 Training accuracy: 74.20833333333333% Test accuracy: 73.1666666666666%

Epoch 26

Training loss: 1.6527680905120517129
Training accuracy: 75.583333333333334%
Test accuracy: 71.666666666666666%

Epoch 27

Training loss: 1.5972874361736717142
Training accuracy: 76.2916666666666%
Test accuracy: 72.83333333333334%

Epoch 28

Training loss: 1.5564497143070425788
Training accuracy: 76.958333333333334%

Test accuracy: 77.0%

Epoch 29

Training loss: 1.5136278775985920208

Training accuracy: 78.0%

Test accuracy: 78.333333333333334%

Epoch 30

Training loss: 1.4587659710007716225

Training accuracy: 80.125%

Test accuracy: 78.33333333333334%

Epoch 31

Training loss: 1.4288245516540630599 Training accuracy: 79.6249999999999% Test accuracy: 80.1666666666666%

Epoch 32

Training loss: 1.3919085680526149597

Training accuracy: 80.5%

Test accuracy: 79.33333333333333333

Epoch 33

Training loss: 1.3573732137636988203 Training accuracy: 81.37500000000001% Test accuracy: 80.6666666666666%

Epoch 34

Training loss: 1.3169464158206277386 Training accuracy: 82.33333333333334% Test accuracy: 80.1666666666667%

Epoch 35

Training loss: 1.3033419912520667014

Training accuracy: 82.875%

Test accuracy: 83.5%

Epoch 36

Training loss: 1.2511141410983288981 Training accuracy: 83.20833333333333 Test accuracy: 81.33333333333334%

Epoch 37

Training loss: 1.2312799379665704251

Training accuracy: 83.25%

Test accuracy: 83.0%

Epoch 38

Training loss: 1.1893164088582373971
Training accuracy: 84.20833333333334%
Test accuracy: 81.83333333333334%

Epoch 39

Training loss: 1.1833968778192231737

Training accuracy: 83.875%

Test accuracy: 85.0%

Epoch 40

Training loss: 1.1497179650784195005

Training accuracy: 84.375%

Test accuracy: 84.33333333333334%

Epoch 41

Epoch 42

Training loss: 1.0936943182485305148
Training accuracy: 85.16666666666666
Test accuracy: 84.83333333333334%

Epoch 43

Training loss: 1.068147430165589693

Training accuracy: 86.75%

Test accuracy: 84.3333333333333333%

Epoch 44

Training loss: 1.0534425528084259783
Training accuracy: 86.666666666666666
Test accuracy: 85.66666666666667%

Epoch 45

Training loss: 1.036295909911595317 Training accuracy: 86.95833333333334% Test accuracy: 84.666666666666%

Epoch 46

Training loss: 1.0191970198548043363 Training accuracy: 87.2916666666666% Test accuracy: 86.1666666666666%

Epoch 47

Training loss: 1.0244400105473987117
Training accuracy: 86.91666666666666
Test accuracy: 89.5000000000001%

Epoch 48

Training loss: 0.98375971192371858655 Training accuracy: 87.70833333333334% Test accuracy: 87.499999999999%

Epoch 49

Training loss: 0.97154038585373679593 Training accuracy: 87.5416666666666% Test accuracy: 89.33333333333334%

Epoch 50

Training loss: 0.9463017908414572534

Training accuracy: 88.625%

Test accuracy: 87.66666666666667%

Epoch 51

Training loss: 0.92899965423135429706 Training accuracy: 88.20833333333334%

Test accuracy: 89.0%

Epoch 52

Training loss: 0.91672584990988335954 Training accuracy: 89.2916666666666% Test accuracy: 88.1666666666666%

Training loss: 0.9005839156835550208 Training accuracy: 89.124999999999% Test accuracy: 88.3333333333333333

Epoch 54

Training loss: 0.88746445295095612287 Training accuracy: 89.1666666666667% Test accuracy: 89.66666666666666%

Epoch 55

Training loss: 0.87706860489942942773

Training accuracy: 89.625%

Test accuracy: 89.6666666666667%

Epoch 56

Training loss: 0.8639350547190934879 Training accuracy: 90.16666666666666% Test accuracy: 89.6666666666666%

Epoch 57

Training loss: 0.8433923231931204901 Training accuracy: 90.08333333333333%

Test accuracy: 88.5%

Epoch 58

Training loss: 0.82969915666658642685

Training accuracy: 90.25%

Test accuracy: 89.8333333333333333%

Epoch 59

Training loss: 0.81998067367123828866

Training accuracy: 90.25%

Test accuracy: 88.8333333333333333%

Epoch 60

Training loss: 0.80508808089076278405 Training accuracy: 90.70833333333334% Test accuracy: 88.33333333333334%

Epoch 61

Training loss: 0.805538576371802753

Training accuracy: 90.5%

Test accuracy: 89.6666666666666%

Epoch 62

Training loss: 0.7851636643906947198

Training accuracy: 90.625%

Test accuracy: 89.5%

Epoch 63

Epoch 64

Training loss: 0.78488597126647265166 Training accuracy: 90.70833333333333% Test accuracy: 91.66666666666666%

Epoch 65

Training loss: 0.76586877184553158544
Training accuracy: 91.04166666666666%

Test accuracy: 91.0%

Epoch 66

Training loss: 0.7627415076328802056 Training accuracy: 90.708333333333334%

Test accuracy: 91.5%

Epoch 67

Training loss: 0.7394111681129755427 Training accuracy: 91.12500000000001%

Test accuracy: 89.0%

Epoch 68

Training loss: 0.7414956570038536551 Training accuracy: 90.999999999999% Test accuracy: 92.0000000000001%

Epoch 69

Training loss: 0.73016313568748646167 Training accuracy: 91.33333333333334% Test accuracy: 91.66666666666666%

Epoch 70

Training loss: 0.710853685886049901 Training accuracy: 91.5000000000001% Test accuracy: 89.6666666666666%

Epoch 71

Training loss: 0.7012255025330277849

Training accuracy: 92.0% Test accuracy: 89.5%

Training loss: 0.69835240969558038207

Training accuracy: 91.875%

Test accuracy: 90.8333333333333333%

## Epoch 73

Training loss: 0.7096119642473644569 Training accuracy: 91.45833333333333%

Test accuracy: 92.0%

## Epoch 74

Training loss: 0.68662704130133062606 Training accuracy: 91.79166666666666% Test accuracy: 90.66666666666666%

## Epoch 75

Training loss: 0.6794407135588605874

Training accuracy: 92.125%

Test accuracy: 90.1666666666666%

#### Epoch 76

Training loss: 0.6791475667787470243

Training accuracy: 92.0%

Test accuracy: 90.5000000000001%

## Epoch 77

Training loss: 0.6777194222773522526 Training accuracy: 91.79166666666666%

Test accuracy: 92.5%

## Epoch 78

Training loss: 0.66271087886373034666 Training accuracy: 92.208333333333333 Test accuracy: 91.666666666666666%

#### Epoch 79

Training loss: 0.67312596809601807346 Training accuracy: 92.12500000000001% Test accuracy: 92.16666666666666%

## Epoch 80

Training loss: 0.66089598602693623737 Training accuracy: 92.1249999999999% Test accuracy: 92.6666666666667%

# Epoch 81

Training loss: 0.63810989381418171766 Training accuracy: 92.41666666666666% Test accuracy: 90.1666666666667%

Epoch 82

Training loss: 0.64148968075877913587 Training accuracy: 92.33333333333334% Test accuracy: 90.83333333333333%

Epoch 83

Training loss: 0.6265699034142066583

Training accuracy: 93.125%

Test accuracy: 89.0%

Epoch 84

Training loss: 0.6392864012220427994 Training accuracy: 92.6666666666666% Test accuracy: 92.83333333333334%

Epoch 85

Training loss: 0.6266006267387549588
Training accuracy: 92.58333333333333%

Test accuracy: 92.0%

Epoch 86

Training loss: 0.62211655318230423104 Training accuracy: 92.9583333333333333 Test accuracy: 91.16666666666666%

Epoch 87

Training loss: 0.60962395522159163467 Training accuracy: 92.708333333333334%

Test accuracy: 92.0%

Epoch 88

Training loss: 0.61555908748795964784
Training accuracy: 92.66666666666666
Test accuracy: 91.833333333333333

Epoch 89

Training loss: 0.6206448106112517699 Training accuracy: 92.70833333333334%

Test accuracy: 94.0%

Epoch 90

Training loss: 0.62019830209994132966

Training accuracy: 92.75%

Test accuracy: 93.83333333333333333%

Epoch 91

Training loss: 0.6065650652854656403 Training accuracy: 93.1249999999999%

Test accuracy: 93.0%

Epoch 92

Training loss: 0.58744448276939657263

Training accuracy: 93.625%

Test accuracy: 90.6666666666666%

Epoch 93

Training loss: 0.600956259946204607

Training accuracy: 93.5%

Test accuracy: 93.1666666666666%

Epoch 94

Training loss: 0.58942465346894128 Training accuracy: 93.2083333333334% Test accuracy: 91.8333333333334%

Epoch 95

Training loss: 0.5875020532472406944

Training accuracy: 93.5%

Test accuracy: 93.0000000000001%

Epoch 96

Training loss: 0.58659921324732605024 Training accuracy: 93.3750000000001% Test accuracy: 92.6666666666666%

Epoch 97

Training loss: 0.59270500196454628056 Training accuracy: 93.33333333333334% Test accuracy: 94.33333333333333%

Epoch 98

Training loss: 0.57404966506087506137

Training accuracy: 93.5%

Test accuracy: 93.1666666666666%

Epoch 99

Training loss: 0.5603962451653039363 Training accuracy: 93.95833333333333%

Test accuracy: 92.0%

Epoch 100

Training loss: 0.58139950112372748667 Training accuracy: 93.66666666666666 Test accuracy: 94.33333333333334%

Training loss: 0.5504932939981991767 Training accuracy: 94.33333333333334% Test accuracy: 90.6666666666667%

Epoch 102

Training loss: 0.56695328661168041204

Training accuracy: 93.875%

Test accuracy: 93.333333333333333333

Epoch 103

Training loss: 0.57478326237261645915

Training accuracy: 93.75% Test accuracy: 94.5%

Epoch 104

Epoch 105

Epoch 106

Training loss: 0.5520286629063114423 Training accuracy: 94.0416666666666% Test accuracy: 94.83333333333334%

Epoch 107

Training loss: 0.5460721922486810489
Training accuracy: 94.5000000000001%

Test accuracy: 93.0%

Epoch 108

Training loss: 0.55054706705771070394

Training accuracy: 94.25%

Test accuracy: 94.333333333333334%

Epoch 109

Training loss: 0.5269611817405436965 Training accuracy: 95.0416666666666% Test accuracy: 92.1666666666666%

Epoch 110

Training loss: 0.5317618483310746433

Training accuracy: 94.83333333333334% Test accuracy: 93.33333333333334%

Epoch 111

Epoch 112

Training loss: 0.53408761113067549655

Training accuracy: 94.625%

Test accuracy: 93.16666666666667%

Epoch 113

Training loss: 0.5348281387170761161 Training accuracy: 94.3333333333334% Test accuracy: 93.833333333333333

Epoch 114

Training loss: 0.5250364345596446813 Training accuracy: 94.4166666666667% Test accuracy: 94.166666666666%

Epoch 115

Training loss: 0.5234101195985151651 Training accuracy: 94.708333333333333 Test accuracy: 94.66666666666667%

Epoch 116

Training loss: 0.5217382568419288064 Training accuracy: 94.8749999999999% Test accuracy: 94.33333333333333

Epoch 117

Training loss: 0.51962051617765403315 Training accuracy: 94.708333333333333 Test accuracy: 93.66666666666667%

Epoch 118

Training loss: 0.52130206091476524255 Training accuracy: 94.958333333333334%

Test accuracy: 93.5%

Epoch 119

Training loss: 0.51533498021104942084 Training accuracy: 94.58333333333334%

Test accuracy: 95.5%

Training loss: 0.51609079989613041383

Training accuracy: 94.625%

Test accuracy: 94.83333333333333333%

## Epoch 121

Training loss: 0.50384150804798183155 Training accuracy: 94.8750000000001% Test accuracy: 94.166666666666%

## Epoch 122

Training loss: 0.50643285932262460805 Training accuracy: 95.20833333333334% Test accuracy: 93.6666666666666%

## Epoch 123

Training loss: 0.51582140268006260186 Training accuracy: 94.666666666666666%

Test accuracy: 95.5%

#### Epoch 124

Training loss: 0.5091117830962293215 Training accuracy: 95.20833333333334% Test accuracy: 94.1666666666667%

## Epoch 125

Training loss: 0.50716910626601717537 Training accuracy: 94.83333333333334% Test accuracy: 94.66666666666667%

## Epoch 126

Training loss: 0.5071110830179545531 Training accuracy: 95.0416666666667% Test accuracy: 94.166666666666%

#### Epoch 127

Training loss: 0.5039549932007919334 Training accuracy: 94.91666666666667% Test accuracy: 94.66666666666666%

## Epoch 128

Training loss: 0.50361859516030878464 Training accuracy: 94.9166666666667% Test accuracy: 95.8333333333333333

## Epoch 129

Training loss: 0.49259359032396152932 Training accuracy: 95.29166666666666% Test accuracy: 94.6666666666666%

Epoch 130

Training loss: 0.4907284238405285068 Training accuracy: 95.45833333333334% Test accuracy: 94.83333333333333%

Epoch 131

Training loss: 0.48310457404232942468 Training accuracy: 95.66666666666666%

Test accuracy: 93.0%

Epoch 132

Training loss: 0.48791446557895463304 Training accuracy: 95.41666666666666%

Test accuracy: 95.0%

Epoch 133

Training loss: 0.49101799830916978995

Training accuracy: 95.5%

Test accuracy: 94.1666666666666%

Epoch 134

Training loss: 0.49048526167185543665 Training accuracy: 95.45833333333334% Test accuracy: 94.33333333333333%

Epoch 135

Training loss: 0.47997909318411970857 Training accuracy: 95.5416666666667% Test accuracy: 95.1666666666666%

Epoch 136

Epoch 137

Training loss: 0.47108000085166319392 Training accuracy: 95.95833333333334% Test accuracy: 94.16666666666666%

Epoch 138

Training loss: 0.47646555171408798445 Training accuracy: 95.6666666666667% Test accuracy: 94.499999999999%

Epoch 139

Training loss: 0.4822893022515563341 Training accuracy: 95.45833333333333%

Test accuracy: 95.5%

Epoch 140

Training loss: 0.4762280371219583381 Training accuracy: 95.6666666666667% Test accuracy: 94.6666666666667%

Epoch 141

Training loss: 0.47495190126325154963 Training accuracy: 95.458333333333334%

Test accuracy: 96.0%

Epoch 142

Epoch 143

Training loss: 0.47046317324474728276

Training accuracy: 95.5%

Test accuracy: 94.833333333333333333

Epoch 144

Training loss: 0.46512828504929561052 Training accuracy: 95.6666666666667% Test accuracy: 94.9999999999999

Epoch 145

Training loss: 0.4580644160030732293

Training accuracy: 96.125%

Test accuracy: 94.1666666666667%

Epoch 146

Training loss: 0.47095079387958331557 Training accuracy: 95.6666666666667% Test accuracy: 95.83333333333334%

Epoch 147

Training loss: 0.4687127681252226289

Training accuracy: 95.875%

Test accuracy: 96.0%

Epoch 148

Training loss: 0.45951635549687651399 Training accuracy: 96.1666666666667% Test accuracy: 95.16666666666666%

Training loss: 0.46718194888642835738

Training accuracy: 95.875%

Test accuracy: 95.5%

Epoch 150

Training loss: 0.464452477329352695

Training accuracy: 95.75%

Test accuracy: 95.83333333333334%

Epoch 151

Training loss: 0.4610188101660739184

Training accuracy: 96.0%

Test accuracy: 95.6666666666667%

Epoch 152

Training loss: 0.45564314486874410524

Training accuracy: 96.0%

Test accuracy: 95.1666666666666%

Epoch 153

Epoch 154

Training loss: 0.46589302702050002682 Training accuracy: 95.95833333333334% Test accuracy: 96.1666666666666%

Epoch 155

Epoch 156

Training loss: 0.44855392484374034855 Training accuracy: 95.83333333333334% Test accuracy: 95.33333333333334%

Epoch 157

Training loss: 0.46783527992994196118 Training accuracy: 95.83333333333334% Test accuracy: 96.666666666666666%

Epoch 158

Training loss: 0.44617249531030554245

Training accuracy: 96.083333333333334% Test accuracy: 95.5000000000001%

Epoch 159

Training loss: 0.44695191723628128672 Training accuracy: 96.1666666666667% Test accuracy: 95.33333333333334%

Epoch 160

Training loss: 0.45036137108818487636

Training accuracy: 96.125%

Test accuracy: 96.0%

Epoch 161

Training loss: 0.4580546348782063869 Training accuracy: 96.0416666666667% Test accuracy: 96.83333333333334%

Epoch 162

Training loss: 0.45555172418512725527 Training accuracy: 96.16666666666666% Test accuracy: 96.66666666666667%

Epoch 163

Training loss: 0.44272595571754029116
Training accuracy: 96.41666666666666
Test accuracy: 94.833333333333333

Epoch 164

Training loss: 0.4442842545900404404 Training accuracy: 96.20833333333334% Test accuracy: 95.666666666666666%

Epoch 165

Training loss: 0.43802554099214790318 Training accuracy: 96.3750000000001% Test accuracy: 95.1666666666667%

Epoch 166

Training loss: 0.44936497505826862903

Training accuracy: 96.5% Test accuracy: 95.5%

Epoch 167

Training loss: 0.44641058052415321457

Training accuracy: 96.25%

Test accuracy: 95.8333333333333333%

Training loss: 0.43520848574175497914 Training accuracy: 96.6249999999999% Test accuracy: 94.6666666666666%

Epoch 169

Training loss: 0.43161511494384770276

Training accuracy: 96.5%

Test accuracy: 95.333333333333334%

Epoch 170

Training loss: 0.43887963752914026493 Training accuracy: 96.66666666666667%

Test accuracy: 95.5%

Epoch 171

Training loss: 0.43442849268067308053

Training accuracy: 96.5%

Test accuracy: 95.6666666666666%

Epoch 172

Training loss: 0.43207938416741564582 Training accuracy: 96.45833333333333%

Test accuracy: 95.5%

Epoch 173

Training loss: 0.43798534118285132273

Training accuracy: 96.375%

Test accuracy: 95.499999999999%

Epoch 174

Training loss: 0.4395933946795436394

Training accuracy: 96.375%

Test accuracy: 96.499999999999%

Epoch 175

Training loss: 0.43344800167307012494 Training accuracy: 96.66666666666667%

Test accuracy: 96.0%

Epoch 176

Training loss: 0.41954139758632181642 Training accuracy: 96.4166666666667% Test accuracy: 95.6666666666666%

Epoch 177

Training loss: 0.42110946009268479306 Training accuracy: 97.0833333333333% Test accuracy: 93.83333333333334%

Epoch 178

Epoch 179

Training loss: 0.41451573947503286447 Training accuracy: 97.0833333333333%

Test accuracy: 94.0%

Epoch 180

Training loss: 0.42837178988459138066 Training accuracy: 96.66666666666666%

Test accuracy: 96.0%

Epoch 181

Training loss: 0.41777400980930845076

Training accuracy: 96.625%

Test accuracy: 95.5%

Epoch 182

Training loss: 0.4300578992498257296

Training accuracy: 96.375%

Test accuracy: 96.83333333333334%

Epoch 183

Epoch 184

Training loss: 0.41978967039299038634 Training accuracy: 97.08333333333334% Test accuracy: 95.66666666666667%

Epoch 185

Training loss: 0.4124393061934362509 Training accuracy: 97.20833333333334%

Test accuracy: 94.5%

Epoch 186

Training loss: 0.417288354227210665

Training accuracy: 97.0% Test accuracy: 95.0%

Epoch 187

Training loss: 0.4206368764987213967 Training accuracy: 96.916666666666666%

Test accuracy: 94.5%

Epoch 188

Epoch 189

Training loss: 0.4145557828829357251
Training accuracy: 96.50000000000001%

Test accuracy: 96.5%

Epoch 190

Training loss: 0.420670286377289013 Training accuracy: 96.37500000000001%

Test accuracy: 96.5%

Epoch 191

Training loss: 0.43247128160499316018 Training accuracy: 96.62500000000001% Test accuracy: 98.1666666666666%

Epoch 192

Training loss: 0.41842589671255519542 Training accuracy: 96.83333333333334% Test accuracy: 96.33333333333334%

Epoch 193

Training loss: 0.42039387861725794484 Training accuracy: 96.8749999999999% Test accuracy: 95.66666666666666%

Epoch 194

Training loss: 0.41658119987596791442 Training accuracy: 96.7916666666666% Test accuracy: 97.1666666666667%

Epoch 195

Training loss: 0.4084725959622829171
Training accuracy: 97.16666666666666%
Test accuracy: 96.00000000000001%

Epoch 196

Training loss: 0.41613037961262712774

Training accuracy: 97.0%

Test accuracy: 96.83333333333334%

Training loss: 0.41428437566116258127

Training accuracy: 96.875%

Test accuracy: 96.333333333333334%

## Epoch 198

Training loss: 0.4027377666574514209 Training accuracy: 96.916666666666667%

Test accuracy: 96.5%

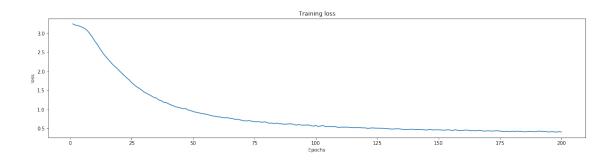
## Epoch 199

Training loss: 0.41719520111587007888

Training accuracy: 97.0% Test accuracy: 97.5%

# Epoch 200

Training loss: 0.40886217833198734307 Training accuracy: 97.16666666666666% Test accuracy: 96.166666666666%





We see that there has been a little drop in both training and testing accuracy. But we can't be sure it's overfitting as the train and test accuracies are the same.

# 2.2.9 So here I take the liberty to test my model using Cross Validation, on the entire MNIST data set.

```
[3]: import mnist_loader
[5]: training_data_MNIST, validation_data_MNIST, __ = mnist_loader.
      →load_data_wrapper()
[6]: net_mnist = network.Linear_Network_CrossValidation([784,35,25,10])
[7]: """No Regularization"""
     net_mnist.SGD(training_data_MNIST, 200, 10, 0.5, lmbda=0.0)
    Epoch 1
    Training loss: 3.2549137677927903634
    Training accuracy: 12.0%
    Test accuracy: 12.37000000000001%
    Epoch 2
    Training loss: 3.2303653631804196348
    Training accuracy: 13.15%
    Test accuracy: 13.62%
    Epoch 3
    Training loss: 3.21403511856918898
    Training accuracy: 15.615%
    Test accuracy: 15.78000000000001%
    Epoch 4
    Training loss: 3.1937961060341875327
    Training accuracy: 26.5625%
    Test accuracy: 27.37000000000005%
    Epoch 5
    Training loss: 3.1650126603191624968
    Training accuracy: 29.375%
    Test accuracy: 28.360000000000003%
    Epoch 6
    Training loss: 3.12670138108243522
    Training accuracy: 39.94%
    Test accuracy: 39.910000000000004%
    Epoch 7
    Training loss: 3.0709740305697261484
    Training accuracy: 46.9375%
    Test accuracy: 46.4299999999999%
```

Training loss: 2.9931596486721955392 Training accuracy: 50.139999999999% Test accuracy: 49.29000000000006%

Epoch 9

Training loss: 2.891747902007158164
Training accuracy: 52.81750000000001%

Test accuracy: 52.08%

Epoch 10

Training loss: 2.7685683583480938375

Training accuracy: 54.3925%

Test accuracy: 54.25%

Epoch 11

Training loss: 2.630258383457266856

Training accuracy: 56.735% Test accuracy: 56.48%

Epoch 12

Training loss: 2.4923512324388638832 Training accuracy: 58.602500000000006% Test accuracy: 59.12999999999995%

Epoch 13

Training loss: 2.3600355157016473136

Training accuracy: 60.625%

Test accuracy: 60.52999999999994%

Epoch 14

Training loss: 2.240377761388976314

Training accuracy: 62.4775%

Test accuracy: 61.8099999999999%

Epoch 15

Training loss: 2.1316149126602059413

Training accuracy: 64.3875%

Test accuracy: 64.59%

Epoch 16

Training loss: 2.0391558080466419735 Training accuracy: 65.9450000000001% Test accuracy: 65.789999999999%

Epoch 17

Training loss: 1.9522488193406969867

Training accuracy: 67.2625%

Test accuracy: 67.6%

Epoch 18

Training loss: 1.8733498855591442873

Training accuracy: 68.945%

Test accuracy: 68.6699999999999%

Epoch 19

Training loss: 1.805443993400869609

Training accuracy: 70.2725%

Test accuracy: 70.68%

Epoch 20

Training loss: 1.7426149503634943496

Training accuracy: 71.7375%

Test accuracy: 71.74%

Epoch 21

Training loss: 1.6820376008064805446

Training accuracy: 73.07% Test accuracy: 73.28%

Epoch 22

Training loss: 1.6244922816915998697

Training accuracy: 74.365%

Test accuracy: 74.1499999999999%

Epoch 23

Training loss: 1.571081227523225908
Training accuracy: 75.8175000000001%
Test accuracy: 74.9400000000001%

Epoch 24

Training loss: 1.5243752162732040671
Training accuracy: 76.64500000000001%

Test accuracy: 76.2%

Epoch 25

Training loss: 1.480156117464390088

Training accuracy: 77.7975%

Test accuracy: 77.53%

Epoch 26

Training loss: 1.4385026077754121182 Training accuracy: 78.39750000000001%

Test accuracy: 78.53%

Training loss: 1.3957791996356729744
Training accuracy: 79.42750000000001%

Test accuracy: 78.95%

Epoch 28

Training loss: 1.3602404962390186127

Training accuracy: 80.1% Test accuracy: 79.62%

Epoch 29

Training loss: 1.3283987004161619605

Training accuracy: 80.495% Test accuracy: 81.29%

Epoch 30

Training loss: 1.2930813677184594752 Training accuracy: 81.1874999999999%

Test accuracy: 80.9%

Epoch 31

Training loss: 1.261496540479844636

Training accuracy: 81.775%

Test accuracy: 81.5%

Epoch 32

Training loss: 1.2327775380045271845

Training accuracy: 82.3825%

Test accuracy: 82.0%

Epoch 33

Training loss: 1.2060662840206091873 Training accuracy: 82.799999999998% Test accuracy: 82.5399999999999%

Epoch 34

Training loss: 1.1844482896911789679

Training accuracy: 83.2775%

Test accuracy: 83.1%

Epoch 35

Training loss: 1.161595883817496025 Training accuracy: 83.4774999999999%

Test accuracy: 83.81%

Epoch 36

Training loss: 1.1392114834219438607 Training accuracy: 83.8224999999999% Test accuracy: 84.0499999999998%

Epoch 37

Training loss: 1.1166716869641731766

Training accuracy: 84.32% Test accuracy: 84.28%

Epoch 38

Training loss: 1.0979606377663168706 Training accuracy: 84.7075000000001% Test accuracy: 84.8200000000001%

Epoch 39

Training loss: 1.0785392624043462338 Training accuracy: 85.0249999999999% Test accuracy: 84.919999999999%

Epoch 40

Training loss: 1.0612535013347289558

Training accuracy: 85.255%

Test accuracy: 85.0500000000001%

Epoch 41

Training loss: 1.0426605148625425263 Training accuracy: 85.5499999999998%

Test accuracy: 85.51%

Epoch 42

Training loss: 1.0284946224904879825 Training accuracy: 85.77000000000001%

Test accuracy: 85.67%

Epoch 43

Training loss: 1.0157374918889092406

Training accuracy: 85.975%

Test accuracy: 86.199999999999%

Epoch 44

Training loss: 0.99515816367788840124

Training accuracy: 86.2475%

Test accuracy: 86.16%

Epoch 45

Training loss: 0.9801303680028433522

Training accuracy: 86.5325%

Test accuracy: 86.1799999999999%

Epoch 46

Training loss: 0.966785838606484092 Training accuracy: 86.6074999999999%

Test accuracy: 86.56%

Epoch 47

Training loss: 0.95068921172750765465

Training accuracy: 86.8925%

Test accuracy: 86.65%

Epoch 48

Training loss: 0.93652689937533321223

Training accuracy: 87.05% Test accuracy: 86.9%

Epoch 49

Training loss: 0.9254670877761319656

Training accuracy: 87.3125%

Test accuracy: 86.8000000000001%

Epoch 50

Training loss: 0.9140372425036052727

Training accuracy: 87.3675%

Test accuracy: 87.57%

Epoch 51

Training loss: 0.904290560709954509 Training accuracy: 87.5574999999999%

Test accuracy: 87.83%

Epoch 52

Training loss: 0.8867661538703144436 Training accuracy: 87.86000000000001%

Test accuracy: 87.26%

Epoch 53

Training loss: 0.875880878884457069

Training accuracy: 87.9525%

Test accuracy: 87.72%

Epoch 54

Training loss: 0.8615725011764432524 Training accuracy: 88.0874999999999%

Test accuracy: 88.01%

Epoch 55

Training loss: 0.85341504151270984396

Training accuracy: 88.25%

Test accuracy: 88.109999999999%

Training loss: 0.8417671681075545337

Training accuracy: 88.36% Test accuracy: 88.35%

Epoch 57

Training loss: 0.8289953714605576363 Training accuracy: 88.51750000000001%

Test accuracy: 88.32%

Epoch 58

Training loss: 0.81829261046099114

Training accuracy: 88.695%

Test accuracy: 88.36%

Epoch 59

Training loss: 0.80942514720686124503 Training accuracy: 88.7525000000001% Test accuracy: 88.9100000000001%

Epoch 60

Training loss: 0.7956351261920827223

Training accuracy: 88.9975%

Test accuracy: 88.45%

Epoch 61

Training loss: 0.78813499901126612214 Training accuracy: 89.0624999999999%

Test accuracy: 89.09%

Epoch 62

Training loss: 0.7788519710412564244
Training accuracy: 89.19500000000001%

Test accuracy: 89.09%

Epoch 63

Training loss: 0.7689662174097436863

Training accuracy: 89.34%

Test accuracy: 89.2100000000001%

Epoch 64

Training loss: 0.7575235873248800461

Training accuracy: 89.4525%

Test accuracy: 89.13%

Epoch 65

Training loss: 0.75145383160936609853

Training accuracy: 89.49% Test accuracy: 89.53%

Epoch 66

Training loss: 0.7419267448887730292

Training accuracy: 89.63%

Test accuracy: 89.52000000000001%

Epoch 67

Training loss: 0.7322442811956738567 Training accuracy: 89.76750000000001% Test accuracy: 89.57000000000002%

Epoch 68

Training loss: 0.72794642162758390637

Training accuracy: 89.745% Test accuracy: 90.18%

Epoch 69

Training loss: 0.7177915802939758386 Training accuracy: 89.95000000000002% Test accuracy: 89.979999999999%

Epoch 70

Training loss: 0.70870041609145359397

Training accuracy: 90.0925%

Test accuracy: 89.8800000000001%

Epoch 71

Training loss: 0.6999011838930103235 Training accuracy: 90.0975000000001% Test accuracy: 90.3800000000001%

Epoch 72

Training loss: 0.69583124688280737613

Training accuracy: 90.2325%

Test accuracy: 90.41%

Epoch 73

Training loss: 0.68438552760432424946

Training accuracy: 90.425%

Test accuracy: 89.83%

Epoch 74

Training loss: 0.67960758771305266126 Training accuracy: 90.3524999999999%

Test accuracy: 90.53%

Training loss: 0.66858719771266861184

Training accuracy: 90.59% Test accuracy: 90.03%

Epoch 76

Training loss: 0.66460862669553705126 Training accuracy: 90.63250000000001%

Test accuracy: 90.3%

Epoch 77

Training loss: 0.65845408640708696067 Training accuracy: 90.729999999999%

Test accuracy: 90.45%

Epoch 78

Training loss: 0.654727499811937681

Training accuracy: 90.675% Test accuracy: 90.84%

Epoch 79

Training loss: 0.64757340471736984797 Training accuracy: 90.7500000000001% Test accuracy: 90.9200000000002%

Epoch 80

Training loss: 0.63996706109492308386

Training accuracy: 90.9375%

Test accuracy: 90.56%

Epoch 81

Training loss: 0.6327073615411694417

Training accuracy: 91.0225%

Test accuracy: 90.63000000000001%

Epoch 82

Training loss: 0.62732354312631060137 Training accuracy: 91.0050000000001% Test accuracy: 90.8600000000001%

Epoch 83

Training loss: 0.6256448658602083171
Training accuracy: 91.00750000000001%

Test accuracy: 91.3%

Epoch 84

Training loss: 0.62019132893406158497

Training accuracy: 91.14%

Test accuracy: 91.3%

Epoch 85

Training loss: 0.61244786160191979116 Training accuracy: 91.2274999999999%

Test accuracy: 91.36%

Epoch 86

Training loss: 0.60711826459307285323

Training accuracy: 91.3025%

Test accuracy: 91.20000000000002%

Epoch 87

Training loss: 0.600184055851650193

Training accuracy: 91.43% Test accuracy: 91.08%

Epoch 88

Training loss: 0.5990108866896737519
Training accuracy: 91.2700000000001%
Test accuracy: 91.87000000000002%

Epoch 89

Training loss: 0.5900999045300778182

Training accuracy: 91.5375%

Test accuracy: 91.22%

Epoch 90

Training loss: 0.5852773988774215987
Training accuracy: 91.6125000000001%
Test accuracy: 91.2700000000001%

Epoch 91

Training loss: 0.58418047490896880857

Training accuracy: 91.58%

Test accuracy: 91.6900000000001%

Epoch 92

Training loss: 0.579592058875964512

Training accuracy: 91.66%

Test accuracy: 91.81000000000002%

Epoch 93

Training loss: 0.57360444315982017275

Training accuracy: 91.765%

Test accuracy: 91.62000000000002%

Epoch 94

Training loss: 0.56961162705048020506

Training accuracy: 91.78% Test accuracy: 91.87%

Epoch 95

Training loss: 0.56548790206478602877 Training accuracy: 91.8074999999999%

Test accuracy: 92.07%

Epoch 96

Training loss: 0.5634193632574755771

Training accuracy: 91.86%

Test accuracy: 92.20000000000002%

Epoch 97

Training loss: 0.55950622641808686315

Training accuracy: 91.9875%

Test accuracy: 91.98%

Epoch 98

Training loss: 0.55115533455225003954

Training accuracy: 92.145% Test accuracy: 91.75%

Epoch 99

Training loss: 0.5471877368783312996

Training accuracy: 92.155%

Test accuracy: 91.8800000000001%

Epoch 100

Training loss: 0.5448680766244118351 Training accuracy: 92.13250000000001%

Test accuracy: 92.16%

Epoch 101

Training loss: 0.54243870365330319565 Training accuracy: 92.0675000000001% Test accuracy: 92.45000000000002%

Epoch 102

Training loss: 0.5370593625097435376

Training accuracy: 92.2625%

Test accuracy: 92.039999999999%

Epoch 103

Training loss: 0.53105385026293428397

Training accuracy: 92.3125%

Test accuracy: 92.09%

Training loss: 0.5297263652094429525 Training accuracy: 92.31500000000001%

Test accuracy: 92.32%

Epoch 105

Training loss: 0.5263967963182853283 Training accuracy: 92.4349999999999% Test accuracy: 91.9400000000001%

Epoch 106

Training loss: 0.5274688864474547382

Training accuracy: 92.365%

Test accuracy: 92.729999999999%

Epoch 107

Training loss: 0.5235953992051184295

Training accuracy: 92.405%

Test accuracy: 92.7%

Epoch 108

Training loss: 0.5175529612526807184
Training accuracy: 92.52000000000001%

Test accuracy: 92.65%

Epoch 109

Training loss: 0.5158665966011020421
Training accuracy: 92.507500000000002%

Test accuracy: 92.85%

Epoch 110

Training loss: 0.51481355013236593 Training accuracy: 92.57750000000001%

Test accuracy: 92.83%

Epoch 111

Training loss: 0.50925440215825335324 Training accuracy: 92.67750000000001%

Test accuracy: 92.72%

Epoch 112

Training loss: 0.50499963713168657606

Training accuracy: 92.695%

Test accuracy: 92.92%

Epoch 113

Training loss: 0.50213016499462745574

Training accuracy: 92.765%

Test accuracy: 92.73000000000002%

Epoch 114

Training loss: 0.49810210946167742847

Training accuracy: 92.7925%

Test accuracy: 92.8200000000001%

Epoch 115

Training loss: 0.49790211655841601942 Training accuracy: 92.8524999999999% Test accuracy: 92.9900000000001%

Epoch 116

Training loss: 0.48859874138618185173 Training accuracy: 92.99500000000002% Test accuracy: 92.449999999999%

Epoch 117

Training loss: 0.48978641375085480393

Training accuracy: 92.95% Test accuracy: 92.84%

Epoch 118

Training loss: 0.48704454981115405631

Training accuracy: 92.89% Test accuracy: 93.16%

Epoch 119

Training loss: 0.484836892365944668

Training accuracy: 93.0575%

Test accuracy: 92.69000000000001%

Epoch 120

Training loss: 0.48621767385332914264

Training accuracy: 92.9225%

Test accuracy: 93.35%

Epoch 121

Training loss: 0.47850526845609744902

Training accuracy: 93.065%

Test accuracy: 93.0%

Epoch 122

Training loss: 0.47659508450624067256 Training accuracy: 93.0799999999998%

Test accuracy: 93.06%

Training loss: 0.47475122446445212868

Training accuracy: 93.16%

Test accuracy: 93.0200000000001%

Epoch 124

Training loss: 0.46808274880120322436 Training accuracy: 93.2400000000001% Test accuracy: 92.87000000000002%

Epoch 125

Training loss: 0.464224337508312318

Training accuracy: 93.32%

Test accuracy: 92.70000000000000%

Epoch 126

Training loss: 0.46988140038887290812 Training accuracy: 93.13500000000002%

Test accuracy: 93.56%

Epoch 127

Training loss: 0.46361561131306186644

Training accuracy: 93.2775%

Test accuracy: 93.21%

Epoch 128

Training loss: 0.45892261712413412377 Training accuracy: 93.33250000000001%

Test accuracy: 93.01%

Epoch 129

Training loss: 0.45826159034971505017 Training accuracy: 93.37750000000001% Test accuracy: 93.01000000000002%

Epoch 130

Training loss: 0.45846006918214342476

Training accuracy: 93.41%

Test accuracy: 93.1499999999999%

Epoch 131

Training loss: 0.45815364481465175616

Training accuracy: 93.3425%

Test accuracy: 93.5399999999999%

Epoch 132

Training loss: 0.45448285490169881536

Training accuracy: 93.3575%

Test accuracy: 93.54%

Epoch 133

Training loss: 0.45174609817699773196

Training accuracy: 93.4075%

Test accuracy: 93.5200000000001%

Epoch 134

Training loss: 0.45057287792781927746
Training accuracy: 93.4424999999998%
Test accuracy: 93.62000000000000%

Epoch 135

Training loss: 0.4439435776773952469

Training accuracy: 93.5325%

Test accuracy: 93.259999999999%

Epoch 136

Training loss: 0.44411678811575270052

Training accuracy: 93.525%

Test accuracy: 93.49%

Epoch 137

Training loss: 0.44324457879588654674
Training accuracy: 93.5424999999999%
Test accuracy: 93.4900000000001%

Epoch 138

Training loss: 0.44324319123878696525

Training accuracy: 93.5275%

Test accuracy: 93.7100000000001%

Epoch 139

Training loss: 0.43987613901745248817

Training accuracy: 93.5825%

Test accuracy: 93.789999999999%

Epoch 140

Training loss: 0.436664713581823304

Training accuracy: 93.625%

Test accuracy: 93.77%

Epoch 141

Training loss: 0.4303227235650945576 Training accuracy: 93.6824999999999%

Test accuracy: 93.64%

Epoch 142

Training loss: 0.432802817843634215 Training accuracy: 93.714999999999% Test accuracy: 93.7100000000001%

Epoch 143

Training loss: 0.4317384451137185207

Training accuracy: 93.665% Test accuracy: 93.91%

Epoch 144

Training loss: 0.43032012582326622176

Training accuracy: 93.815% Test accuracy: 93.42%

Epoch 145

Training loss: 0.42626187542228994367

Training accuracy: 93.735%

Test accuracy: 93.889999999999%

Epoch 146

Training loss: 0.42455500294497585572 Training accuracy: 93.80250000000001%

Test accuracy: 93.72%

Epoch 147

Training loss: 0.42492543858901883044

Training accuracy: 93.8% Test accuracy: 93.98%

Epoch 148

Training loss: 0.41534818677721852632 Training accuracy: 93.9974999999999% Test accuracy: 93.3200000000001%

Epoch 149

Training loss: 0.42087038405811670627 Training accuracy: 93.8874999999999% Test accuracy: 94.0000000000001%

Epoch 150

Training loss: 0.41203653624302735985 Training accuracy: 94.0449999999999%

Test accuracy: 93.38%

Epoch 151

Training loss: 0.41643164182219858093 Training accuracy: 93.9149999999999%

Test accuracy: 94.11%

Training loss: 0.41449397009616625697

Training accuracy: 93.9975%

Test accuracy: 93.899999999999%

Epoch 153

Training loss: 0.41173198523883212108

Training accuracy: 94.0275%

Test accuracy: 94.0%

Epoch 154

Training loss: 0.41026183189993263158 Training accuracy: 94.119999999999%

Test accuracy: 93.89%

Epoch 155

Training loss: 0.4054492057734267452 Training accuracy: 94.104999999999% Test accuracy: 93.799999999998%

Epoch 156

Training loss: 0.40589666704218758153

Training accuracy: 94.1725%

Test accuracy: 93.77%

Epoch 157

Training loss: 0.404836185027750019
Training accuracy: 94.11500000000001%

Test accuracy: 94.22%

Epoch 158

Training loss: 0.402943400746825336

Training accuracy: 94.1525%

Test accuracy: 94.109999999999%

Epoch 159

Training loss: 0.40145288672166645096 Training accuracy: 94.2399999999998%

Test accuracy: 94.0%

Epoch 160

Training loss: 0.40315426738565076397

Training accuracy: 94.16% Test accuracy: 94.38%

Epoch 161

Training loss: 0.39737144454527497956

Training accuracy: 94.3350000000001%

Test accuracy: 94.03%

Epoch 162

Training loss: 0.39719513921885937996

Training accuracy: 94.2425%

Test accuracy: 94.41%

Epoch 163

Training loss: 0.3935560846615894485

Training accuracy: 94.3075%

Test accuracy: 94.1%

Epoch 164

Training loss: 0.39344206609875944522

Training accuracy: 94.3525%

Test accuracy: 94.04%

Epoch 165

Training loss: 0.39207711194504963484 Training accuracy: 94.31250000000001%

Test accuracy: 94.35%

Epoch 166

Training loss: 0.39158693397253236702 Training accuracy: 94.3825000000001% Test accuracy: 94.0500000000001%

Epoch 167

Training loss: 0.3925627827420703906

Training accuracy: 94.38% Test accuracy: 94.45%

Epoch 168

Training loss: 0.39159753003450063319

Training accuracy: 94.3% Test accuracy: 94.77%

Epoch 169

Training loss: 0.3877796217170760142

Training accuracy: 94.39% Test accuracy: 94.53%

Epoch 170

Training loss: 0.38908044454082560282

Training accuracy: 94.3375%

Test accuracy: 94.85%

Training loss: 0.38192892321099931502 Training accuracy: 94.5424999999999% Test accuracy: 94.289999999999%

Epoch 172

Training loss: 0.38199241506695650637 Training accuracy: 94.53500000000001%

Test accuracy: 94.35%

Epoch 173

Training loss: 0.37985634652989393956 Training accuracy: 94.5350000000001% Test accuracy: 94.399999999999%

Epoch 174

Training loss: 0.38163356179768788897 Training accuracy: 94.4974999999999% Test accuracy: 94.5800000000001%

Epoch 175

Training loss: 0.37882859869658468631 Training accuracy: 94.5624999999999% Test accuracy: 94.4899999999998%

Epoch 176

Training loss: 0.36935909014981529018

Training accuracy: 94.7025%

Test accuracy: 94.0200000000001%

Epoch 177

Training loss: 0.37198621856431785004 Training accuracy: 94.6199999999999%

Test accuracy: 94.52%

Epoch 178

Training loss: 0.3778492781379183282

Training accuracy: 94.575% Test accuracy: 94.77%

Epoch 179

Training loss: 0.3782577725950479073

Training accuracy: 94.565%

Test accuracy: 94.9600000000001%

Epoch 180

Training loss: 0.37036794274279403324

Training accuracy: 94.635%

Test accuracy: 94.6899999999998%

Epoch 181

Training loss: 0.36923994361741522622 Training accuracy: 94.68250000000002%

Test accuracy: 94.62%

Epoch 182

Training loss: 0.36914934109819437492

Training accuracy: 94.65% Test accuracy: 94.74%

Epoch 183

Training loss: 0.36384758731292012377 Training accuracy: 94.7924999999999% Test accuracy: 94.2899999999999%

Epoch 184

Training loss: 0.36348437821860411654

Training accuracy: 94.8% Test accuracy: 94.45%

Epoch 185

Training loss: 0.36895496375140135573

Training accuracy: 94.6775%

Test accuracy: 95.08%

Epoch 186

Training loss: 0.36330459705155400798 Training accuracy: 94.7924999999999% Test accuracy: 94.539999999999%

Epoch 187

Training loss: 0.3606536572984903386 Training accuracy: 94.7524999999998% Test accuracy: 94.789999999999%

Epoch 188

Training loss: 0.361612120255389908

Training accuracy: 94.805%

Test accuracy: 94.809999999999%

Epoch 189

Training loss: 0.35718861163897241737 Training accuracy: 94.8874999999999%

Test accuracy: 94.53%

Epoch 190

Training loss: 0.35862918062728819823

Training accuracy: 94.8225%

Test accuracy: 94.85%

Epoch 191

Training loss: 0.35949735031136498877

Training accuracy: 94.8125%

Test accuracy: 94.96%

Epoch 192

Training loss: 0.3563152715485924694

Training accuracy: 94.885%

Test accuracy: 94.649999999999%

Epoch 193

Training loss: 0.35137338075906334616

Training accuracy: 95.005%

Test accuracy: 94.34%

Epoch 194

Training loss: 0.35013641888528973376 Training accuracy: 94.9174999999999%

Test accuracy: 94.67%

Epoch 195

Training loss: 0.34952663293369294828

Training accuracy: 94.9775%

Test accuracy: 94.619999999999%

Epoch 196

Training loss: 0.35045629155387968004

Training accuracy: 94.95%

Test accuracy: 94.8200000000001%

Epoch 197

Training loss: 0.34899207640514613688 Training accuracy: 94.9474999999999%

Test accuracy: 94.85%

Epoch 198

Training loss: 0.34912806308276130186

Training accuracy: 94.975%

Test accuracy: 94.939999999998%

Epoch 199

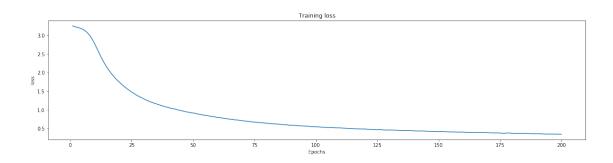
Training loss: 0.34675385339362467304

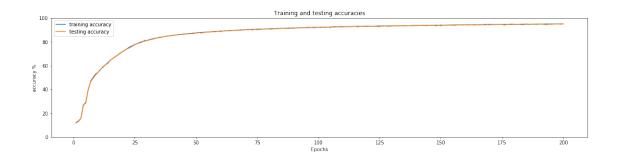
Training accuracy: 95.03% Test accuracy: 94.66%

Training loss: 0.347023505355116699

Training accuracy: 94.9725%

Test accuracy: 94.94%





We can see that the model performs considerably well on the larger dataset of 50000 entries with 95% accuracy. It seems we could get an higher accuracy if we continued for more epochs but considering the enormous time it takes to train the model on the entire data set, we will leave it to this.

Let us now look at the results on the validation data:

```
[10]: print ("Validation accuracy: "+str(net_mnist.

→evaluate_validation_accuracy(validation_data_MNIST))+"%")
```

Validation accuracy: 94.87%

Hence we can see that the Cross Validation has clearly improved the performance.

# 2.3 Part 2

Now we test how well does the PCA data work compared to the normal image data. We'll use the same cost and activation here and play with the parameters of the Stochastic Gradient Descent to see which ones fit the best

# Starting with no hidden layers:

- [2]: training\_data = data\_loader.load\_PCA()
- [3]: net = network.Linear\_Network\_CrossValidation([25,10])
- [4]: net.SGD(training\_data, 200, 10, 0.1)

### Epoch 1

Training loss: 9.22099801657356956

Training accuracy: 46.5%

Test accuracy: 45.0000000000001%

## Epoch 2

Training loss: 5.6972104611961508326 Training accuracy: 64.29166666666666%

Test accuracy: 64.0%

## Epoch 3

Training loss: 4.416983909376654337
Training accuracy: 69.66666666666666
Test accuracy: 73.33333333333334%

### Epoch 4

Training loss: 3.615743826552267308 Training accuracy: 73.8749999999999% Test accuracy: 70.6666666666666%

### Epoch 5

Training loss: 3.099086169043806279 Training accuracy: 76.91666666666666%

Test accuracy: 74.0%

## Epoch 6

Training loss: 2.7268228464475887996 Training accuracy: 78.66666666666666% Test accuracy: 76.83333333333334%

## Epoch 7

Training loss: 2.4652329690654852014 Training accuracy: 79.20833333333334% Test accuracy: 81.333333333333333

## Epoch 8

Training loss: 2.2423227203728069627 Training accuracy: 81.20833333333334% Test accuracy: 81.1666666666667%

Training loss: 2.0902640366876575906

Training accuracy: 81.875%

Test accuracy: 80.5%

### Epoch 10

Training loss: 1.9570741335411768905 Training accuracy: 83.2500000000001% Test accuracy: 81.3333333333334%

### Epoch 11

Training loss: 1.8514596443420896478 Training accuracy: 83.16666666666666%

Test accuracy: 81.5%

## Epoch 12

Training loss: 1.7771641398699509586 Training accuracy: 83.2916666666667% Test accuracy: 82.5000000000001%

#### Epoch 13

Training loss: 1.6865713420050845176 Training accuracy: 83.8749999999999% Test accuracy: 81.3333333333334%

### Epoch 14

Training loss: 1.6438645911290386337

Training accuracy: 84.0%

Test accuracy: 80.6666666666667%

### Epoch 15

Training loss: 1.5931499490888378794 Training accuracy: 84.0416666666666% Test accuracy: 81.1666666666666%

#### Epoch 16

Training loss: 1.5275985931733456518 Training accuracy: 84.2083333333334% Test accuracy: 81.33333333333334%

### Epoch 17

Training loss: 1.5108335397047323175 Training accuracy: 83.45833333333334%

Test accuracy: 83.5%

## Epoch 18

Training loss: 1.4578650939323272563
Training accuracy: 84.583333333333334%

Test accuracy: 81.83333333333334%

Epoch 19

Training loss: 1.4295217681960789051 Training accuracy: 84.33333333333334% Test accuracy: 81.9999999999999

Epoch 20

Training loss: 1.4023068684772099056 Training accuracy: 84.374999999999% Test accuracy: 82.1666666666667%

Epoch 21

Training loss: 1.393550409873582511

Training accuracy: 84.125%

Test accuracy: 83.83333333333334%

Epoch 22

Training loss: 1.3593415094239845594 Training accuracy: 84.58333333333334% Test accuracy: 82.83333333333333%

Epoch 23

Training loss: 1.3367656897410729739
Training accuracy: 84.3750000000001%
Test accuracy: 83.1666666666666%

Epoch 24

Training loss: 1.3303301493884393016 Training accuracy: 84.08333333333333 Test accuracy: 84.1666666666667%

Epoch 25

Training loss: 1.2997867553723576002 Training accuracy: 84.458333333333334%

Test accuracy: 83.5%

Epoch 26

Epoch 27

Training loss: 1.2643420714976450969 Training accuracy: 84.6249999999999% Test accuracy: 82.6666666666666%

Epoch 28

Training loss: 1.2578427745448093097 Training accuracy: 84.666666666666666%

Test accuracy: 84.5%

Epoch 29

Training loss: 1.248363277501828601

Training accuracy: 85.0% Test accuracy: 83.5%

Epoch 30

Training loss: 1.2087526776956383451
Training accuracy: 85.29166666666666%
Test accuracy: 82.66666666666667%

Epoch 31

Training loss: 1.2247311884333820144 Training accuracy: 84.916666666666666%

Test accuracy: 84.0%

Epoch 32

Training loss: 1.2078280365076548693 Training accuracy: 85.1250000000001% Test accuracy: 83.166666666666%

Epoch 33

Training loss: 1.2043542942152072343
Training accuracy: 84.9583333333333333
Test accuracy: 84.5000000000001%

Epoch 34

Training loss: 1.1901402066932745033 Training accuracy: 85.0416666666667% Test accuracy: 83.6666666666666%

Epoch 35

Training loss: 1.1893266877239534126

Training accuracy: 85.125%

Test accuracy: 84.33333333333334%

Epoch 36

Training loss: 1.1753629308617575488
Training accuracy: 85.0000000000001%
Test accuracy: 83.5000000000001%

Epoch 37

Training loss: 1.15785837871610086 Training accuracy: 84.79166666666666%

Test accuracy: 82.5%

Training loss: 1.1566425832193783563

Training accuracy: 84.75% Test accuracy: 84.5%

Epoch 39

Training loss: 1.1495045274817770896

Training accuracy: 85.25%

Test accuracy: 83.83333333333334%

Epoch 40

Training loss: 1.1466338426937817961 Training accuracy: 84.916666666666666%

Test accuracy: 85.0%

Epoch 41

Training loss: 1.131884816837323815 Training accuracy: 85.166666666666666%

Test accuracy: 83.5%

Epoch 42

Training loss: 1.1207454266956132541
Training accuracy: 85.20833333333334%
Test accuracy: 84.6666666666667%

Epoch 43

Training loss: 1.1151955116606021295
Training accuracy: 85.04166666666666%

Test accuracy: 85.0%

Epoch 44

Training loss: 1.1286553414805337821

Training accuracy: 85.0% Test accuracy: 85.5%

Epoch 45

Training loss: 1.1231122970894174319
Training accuracy: 84.70833333333334%
Test accuracy: 86.1666666666667%

Epoch 46

Training loss: 1.1006883708309570318

Training accuracy: 85.25%

Test accuracy: 84.33333333333334%

Epoch 47

Training loss: 1.1063091023874119528

Training accuracy: 85.0%

Test accuracy: 85.83333333333334%

Epoch 48

Training loss: 1.1020724523413657304 Training accuracy: 85.3749999999999% Test accuracy: 83.6666666666666%

Epoch 49

Training loss: 1.1104249716803785487
Training accuracy: 84.75000000000001%

Test accuracy: 86.5%

Epoch 50

Training loss: 1.0818069533600869779 Training accuracy: 84.666666666667% Test accuracy: 84.83333333333334%

Epoch 51

Training loss: 1.0802805427946699336 Training accuracy: 85.45833333333333% Test accuracy: 83.5000000000001%

Epoch 52

Training loss: 1.0781572948084795707 Training accuracy: 85.29166666666667%

Test accuracy: 84.0%

Epoch 53

Training loss: 1.0803223229246038665

Training accuracy: 85.0%

Test accuracy: 85.999999999999%

Epoch 54

Training loss: 1.0777593083232875224

Training accuracy: 85.25%

Test accuracy: 84.1666666666666%

Epoch 55

Training loss: 1.0590637339114498695 Training accuracy: 85.6249999999999% Test accuracy: 83.3333333333333333

Epoch 56

Training loss: 1.0485721456538875736 Training accuracy: 85.54166666666667%

Test accuracy: 82.0%

Training loss: 1.0657101902259506693 Training accuracy: 85.4166666666667% Test accuracy: 84.1666666666666%

Epoch 58

Training loss: 1.0646789183573849475

Training accuracy: 85.0%

Test accuracy: 85.6666666666666%

Epoch 59

Training loss: 1.0700191287991760078 Training accuracy: 84.79166666666667%

Test accuracy: 87.5%

Epoch 60

Training loss: 1.0425749785778933251
Training accuracy: 85.79166666666666%
Test accuracy: 83.33333333333334%

Epoch 61

Training loss: 1.0411661059297303879
Training accuracy: 85.5000000000001%
Test accuracy: 85.3333333333333333

Epoch 62

Training loss: 1.0275679917544947195 Training accuracy: 86.0416666666666% Test accuracy: 82.33333333333334%

Epoch 63

Epoch 64

Training loss: 1.0268900450835347518
Training accuracy: 86.04166666666667%
Test accuracy: 84.16666666666666%

Epoch 65

Training loss: 1.0541205004489146379 Training accuracy: 84.95833333333334% Test accuracy: 86.83333333333334%

Epoch 66

Training loss: 1.0261506166687908975 Training accuracy: 85.91666666666667% Test accuracy: 84.33333333333333333

Epoch 67

Training loss: 1.0349572965866353538

Training accuracy: 85.5%

Test accuracy: 85.333333333333334%

Epoch 68

Training loss: 1.0230714984612415923
Training accuracy: 85.66666666666666
Test accuracy: 84.16666666666667%

Epoch 69

Training loss: 1.0166117901239781439 Training accuracy: 85.874999999999% Test accuracy: 83.3333333333333333

Epoch 70

Training loss: 1.021026728780364924 Training accuracy: 85.79166666666667% Test accuracy: 84.1666666666666%

Epoch 71

Training loss: 1.0259281825614258763
Training accuracy: 85.4999999999999%
Test accuracy: 85.00000000000001%

Epoch 72

Training loss: 1.0116180602894958048

Training accuracy: 85.875%

Test accuracy: 83.6666666666666%

Epoch 73

Training loss: 1.0080787574609261215

Training accuracy: 85.875%

Test accuracy: 83.83333333333334%

Epoch 74

Training loss: 1.0194721232291883708

Training accuracy: 85.5%

Test accuracy: 85.5000000000001%

Epoch 75

Training loss: 1.0048028661834067646 Training accuracy: 85.5833333333334% Test accuracy: 83.3333333333334%

Epoch 76

Training loss: 1.0187854349289774013

Training accuracy: 85.125%

Test accuracy: 86.5%

## Epoch 77

Training loss: 1.0045413021616625495 Training accuracy: 85.91666666666666% Test accuracy: 84.83333333333333%

### Epoch 78

Training loss: 0.9959548748476411365 Training accuracy: 85.8333333333334% Test accuracy: 84.33333333333334%

### Epoch 79

Training loss: 1.0070186709150904116 Training accuracy: 85.45833333333334% Test accuracy: 85.33333333333334%

#### Epoch 80

Training loss: 0.987267135534026435

Training accuracy: 86.125%

Test accuracy: 82.6666666666666%

### Epoch 81

Training loss: 1.0089890770924260621 Training accuracy: 85.5000000000001% Test accuracy: 85.666666666666%

## Epoch 82

Training loss: 0.9950429323735696089 Training accuracy: 85.958333333333333%

Test accuracy: 85.0%

## Epoch 83

Training loss: 0.9976947280861072239 Training accuracy: 85.9166666666666% Test accuracy: 85.5000000000001%

## Epoch 84

Training loss: 0.9936223070099521555 Training accuracy: 86.208333333333334% Test accuracy: 84.1666666666667%

# Epoch 85

Training loss: 0.99902601892256380847 Training accuracy: 85.4583333333333333 Test accuracy: 86.5000000000001%

Training loss: 0.98890967583754411246 Training accuracy: 86.1666666666667% Test accuracy: 85.4999999999999

Epoch 87

Training loss: 0.99209672280889362107

Training accuracy: 85.75% Test accuracy: 84.5%

Epoch 88

Training loss: 0.9953416496848202492

Training accuracy: 85.875%

Test accuracy: 85.83333333333334%

Epoch 89

Epoch 90

Training loss: 0.9941278286603629355 Training accuracy: 85.458333333333334%

Test accuracy: 85.5%

Epoch 91

Training loss: 0.99759560550295738073

Training accuracy: 85.875%

Test accuracy: 85.5%

Epoch 92

Training loss: 0.9942328126805559842

Training accuracy: 85.75% Test accuracy: 86.0%

Epoch 93

Training loss: 0.9649296148785307456 Training accuracy: 86.33333333333334% Test accuracy: 83.66666666666666%

Epoch 94

Training loss: 0.97775143639942753524

Training accuracy: 86.25%

Test accuracy: 85.8333333333333333%

Epoch 95

Training loss: 0.980758190177110446

Epoch 96

Training loss: 0.97627445855370527644
Training accuracy: 86.1250000000001%
Test accuracy: 84.83333333333334%

Epoch 97

Training loss: 0.9694192008438162378 Training accuracy: 86.2499999999999% Test accuracy: 84.6666666666667%

Epoch 98

Training loss: 0.9643773562921801708 Training accuracy: 86.4166666666666% Test accuracy: 83.33333333333333333

Epoch 99

Training loss: 0.97539084866014406883 Training accuracy: 86.08333333333334% Test accuracy: 85.1666666666666%

Epoch 100

Training loss: 0.9671893405417292775 Training accuracy: 85.58333333333334%

Test accuracy: 85.5%

Epoch 101

Training loss: 0.96451305736428271325 Training accuracy: 85.9166666666666% Test accuracy: 86.0000000000001%

Epoch 102

Training loss: 0.96011113968634111083 Training accuracy: 85.91666666666666%

Test accuracy: 85.5%

Epoch 103

Training loss: 0.982912601711349907

Training accuracy: 85.5%

Test accuracy: 87.8333333333333333%

Epoch 104

Training loss: 0.9638803214258042194 Training accuracy: 86.20833333333333 Test accuracy: 84.66666666666667%

Epoch 106

Training loss: 0.95477579559118251834 Training accuracy: 86.58333333333334% Test accuracy: 82.5000000000001%

Epoch 107

Training loss: 0.9508399014948614521 Training accuracy: 86.70833333333334% Test accuracy: 83.66666666666667%

Epoch 108

Training loss: 0.97508097963701102843 Training accuracy: 85.83333333333334% Test accuracy: 85.66666666666666%

Epoch 109

Training loss: 0.97243272116623957773 Training accuracy: 85.7083333333333333 Test accuracy: 85.66666666666667%

Epoch 110

Training loss: 0.9715200685240141046

Training accuracy: 85.875%

Test accuracy: 85.1666666666667%

Epoch 111

Training loss: 0.9606236820461237213 Training accuracy: 85.70833333333333 Test accuracy: 85.33333333333334%

Epoch 112

Training loss: 0.9530854339547007519 Training accuracy: 86.45833333333334% Test accuracy: 84.499999999999%

Epoch 113

Training loss: 0.9573774467594564696

Training accuracy: 85.875%

Test accuracy: 85.6666666666666%

Epoch 114

Training loss: 0.9591036677244270033 Training accuracy: 85.83333333333334% Test accuracy: 85.33333333333333333

Epoch 115

Training loss: 0.96221566654308287756 Training accuracy: 85.83333333333334%

Test accuracy: 85.0%

Epoch 116

Training loss: 0.9620331650043036054 Training accuracy: 85.91666666666667%

Test accuracy: 86.0%

Epoch 117

Training loss: 0.9480083571309839313

Training accuracy: 86.0%

Test accuracy: 85.1666666666666%

Epoch 118

Training loss: 0.95891523401212553366

Training accuracy: 86.25%

Test accuracy: 83.333333333333333333

Epoch 119

Training loss: 0.9549137199912463951 Training accuracy: 86.1666666666667% Test accuracy: 85.33333333333334%

Epoch 120

Training loss: 0.95152916914622130885 Training accuracy: 86.2916666666667% Test accuracy: 85.16666666666666%

Epoch 121

Training loss: 0.9327393379310809832

Training accuracy: 86.625%

Test accuracy: 83.83333333333333333

Epoch 122

Training loss: 0.95170439636192179987 Training accuracy: 86.08333333333334% Test accuracy: 86.16666666666666%

Epoch 123

Training loss: 0.9479719040540984737 Training accuracy: 86.0416666666666% Test accuracy: 85.5000000000001%

Epoch 124

Training loss: 0.9485797780305012789 Training accuracy: 85.70833333333334% Test accuracy: 84.333333333333333

Epoch 125

Training loss: 0.94987166012020494835 Training accuracy: 86.45833333333334% Test accuracy: 84.83333333333334%

Epoch 126

Epoch 127

Training loss: 0.9532671469752907539 Training accuracy: 86.1666666666666% Test accuracy: 85.9999999999999%

Epoch 128

Training loss: 0.94637989040867940855 Training accuracy: 85.95833333333334% Test accuracy: 86.666666666666666%

Epoch 129

Training loss: 0.9536342726793946843 Training accuracy: 86.20833333333333 Test accuracy: 85.666666666666666

Epoch 130

Training loss: 0.94773663383420461747

Training accuracy: 86.125%

Test accuracy: 86.5%

Epoch 131

Training loss: 0.9381800498596907712

Training accuracy: 86.375%

Test accuracy: 85.499999999999%

Epoch 132

Training loss: 0.94838897112323895165 Training accuracy: 86.3749999999999% Test accuracy: 86.33333333333334%

Epoch 133

Training loss: 0.9475479501192993932

Training accuracy: 86.125%

Test accuracy: 86.5%

Training loss: 0.9403978357626282752 Training accuracy: 85.9583333333333333 Test accuracy: 86.99999999999999%

Epoch 135

Training loss: 0.95148697735388235435

Training accuracy: 85.75%

Test accuracy: 86.6666666666667%

Epoch 136

Training loss: 0.92213030598836386275 Training accuracy: 86.5416666666666% Test accuracy: 84.83333333333333%

Epoch 137

Training loss: 0.9483925306492080651 Training accuracy: 86.08333333333334% Test accuracy: 85.83333333333333%

Epoch 138

Training loss: 0.9318572029531691334 Training accuracy: 86.16666666666666% Test accuracy: 84.333333333333333

Epoch 139

Training loss: 0.95558113786210473385

Training accuracy: 85.875%

Test accuracy: 86.83333333333334%

Epoch 140

Training loss: 0.9426267645017579676 Training accuracy: 85.91666666666666% Test accuracy: 87.83333333333334%

Epoch 141

Training loss: 0.949690493423599071 Training accuracy: 86.04166666666667%

Test accuracy: 86.5%

Epoch 142

Epoch 143

Training loss: 0.9323541897388749656

Training accuracy: 86.749999999999%

Test accuracy: 84.5%

Epoch 144

Training loss: 0.9239997508137448849
Training accuracy: 86.5416666666666%
Test accuracy: 84.0000000000001%

Epoch 145

Training loss: 0.93210789341292852786 Training accuracy: 86.083333333333333 Test accuracy: 85.0000000000001%

Epoch 146

Epoch 147

Training loss: 0.92290222671662442187 Training accuracy: 86.7500000000001% Test accuracy: 85.1666666666667%

Epoch 148

Training loss: 0.9564176076051543945 Training accuracy: 85.83333333333334% Test accuracy: 87.66666666666667%

Epoch 149

Training loss: 0.9348165774269013373 Training accuracy: 86.4166666666667% Test accuracy: 85.4999999999999

Epoch 150

Training loss: 0.93596943290919236175 Training accuracy: 86.33333333333334% Test accuracy: 85.5000000000001%

Epoch 151

Training loss: 0.9339130674301683927 Training accuracy: 86.5000000000001% Test accuracy: 85.6666666666667%

Epoch 152

Training loss: 0.93320506152939738454

Training accuracy: 86.375%

Test accuracy: 85.1666666666666%

Training loss: 0.919140210195542701 Training accuracy: 86.70833333333333 Test accuracy: 84.83333333333334%

Epoch 154

Training loss: 0.92703292410881861713 Training accuracy: 86.2499999999999% Test accuracy: 85.6666666666666%

Epoch 155

Training loss: 0.94086879093074386434 Training accuracy: 86.3750000000001% Test accuracy: 85.33333333333334%

Epoch 156

Training loss: 0.95085953024332716234 Training accuracy: 85.6666666666667% Test accuracy: 87.1666666666666%

Epoch 157

Training loss: 0.9468469458793463968 Training accuracy: 86.04166666666667%

Test accuracy: 87.0%

Epoch 158

Training loss: 0.94237196246204010477

Training accuracy: 86.125%

Test accuracy: 86.833333333333333333

Epoch 159

Training loss: 0.9297184877123993287

Training accuracy: 86.5%

Test accuracy: 85.1666666666666%

Epoch 160

Epoch 161

Training loss: 0.91467708801819335243
Training accuracy: 86.50000000000001%

Test accuracy: 85.0%

Epoch 162

Training loss: 0.9312914627904353087

Training accuracy: 86.0%

Test accuracy: 86.0000000000001%

Epoch 163

Training loss: 0.9329994720909179408

Training accuracy: 86.25%

Test accuracy: 84.6666666666667%

Epoch 164

Training loss: 0.9070743203536967148 Training accuracy: 86.58333333333334%

Test accuracy: 84.5%

Epoch 165

Training loss: 0.92750206907822564087 Training accuracy: 86.04166666666666%

Test accuracy: 87.0%

Epoch 166

Training loss: 0.9314286658320047433

Training accuracy: 86.125%

Test accuracy: 86.5%

Epoch 167

Training loss: 0.9072719704957024541 Training accuracy: 86.83333333333334% Test accuracy: 84.166666666666%

Epoch 168

Training loss: 0.92819261146233053865 Training accuracy: 86.1249999999999%

Test accuracy: 87.0%

Epoch 169

Training loss: 0.91111359618094969504 Training accuracy: 87.08333333333333%

Test accuracy: 83.0%

Epoch 170

Training loss: 0.9205717767795343373

Training accuracy: 86.375%

Test accuracy: 85.333333333333333333

Epoch 171

Training loss: 0.91284131819120961345 Training accuracy: 86.5416666666666% Test accuracy: 84.3333333333334%

Epoch 172

Training loss: 0.9034718972975628766

Training accuracy: 86.375%

Test accuracy: 85.0%

## Epoch 173

## Epoch 174

Training loss: 0.9163946539407847977 Training accuracy: 86.958333333333334% Test accuracy: 84.0000000000001%

### Epoch 175

Training loss: 0.93817536546166749084

Training accuracy: 86.0%

Test accuracy: 87.6666666666666%

#### Epoch 176

Training loss: 0.92294329129082237705 Training accuracy: 86.4583333333333333 Test accuracy: 85.16666666666667%

#### Epoch 177

Training loss: 0.92206947596340459216 Training accuracy: 86.83333333333334% Test accuracy: 84.33333333333334%

## Epoch 178

Training loss: 0.9445396987415937035

Training accuracy: 85.625%

Test accuracy: 87.8333333333333333%

## Epoch 179

Training loss: 0.9225894754227977433 Training accuracy: 86.66666666666666% Test accuracy: 84.1666666666666%

## Epoch 180

Training loss: 0.9300007719836669897 Training accuracy: 86.08333333333334% Test accuracy: 86.83333333333334%

# Epoch 181

Training loss: 0.91691251941907935517

Training accuracy: 86.5%

Test accuracy: 85.1666666666666%

Training loss: 0.90995940583365245754 Training accuracy: 86.79166666666666% Test accuracy: 83.66666666666667%

Epoch 183

Training loss: 0.9402954934432730443 Training accuracy: 85.95833333333334% Test accuracy: 87.66666666666666%

Epoch 184

Epoch 185

Training loss: 0.92376679380484247084 Training accuracy: 86.16666666666666% Test accuracy: 86.333333333333333

Epoch 186

Training loss: 0.91151696468287896747 Training accuracy: 86.6249999999999% Test accuracy: 84.499999999999%

Epoch 187

Training loss: 0.9239680807201916695 Training accuracy: 86.0416666666666% Test accuracy: 86.666666666666%

Epoch 188

Training loss: 0.9155973874335843458 Training accuracy: 86.33333333333334% Test accuracy: 86.1666666666667%

Epoch 189

Training loss: 0.92769020484144148624 Training accuracy: 85.8749999999999%

Test accuracy: 87.0%

Epoch 190

Training loss: 0.9288258499646736957 Training accuracy: 86.16666666666666%

Test accuracy: 86.0%

Epoch 191

Training loss: 0.9207505904042493449

Training accuracy: 86.58333333333334% Test accuracy: 85.33333333333334%

Epoch 192

Training loss: 0.92456407869531978565 Training accuracy: 86.1666666666667% Test accuracy: 87.0000000000001%

Epoch 193

Training loss: 0.9079855519680257943 Training accuracy: 86.66666666666667%

Test accuracy: 85.5%

Epoch 194

Training loss: 0.91731855525541156624 Training accuracy: 86.33333333333334% Test accuracy: 86.3333333333334%

Epoch 195

Training loss: 0.9089417328397642065

Training accuracy: 86.625%

Test accuracy: 84.33333333333333333%

Epoch 196

Training loss: 0.9057281808393979813 Training accuracy: 86.95833333333333%

Test accuracy: 84.5%

Epoch 197

Epoch 198

Training loss: 0.9128849809650571227 Training accuracy: 86.8749999999999%

Test accuracy: 85.0%

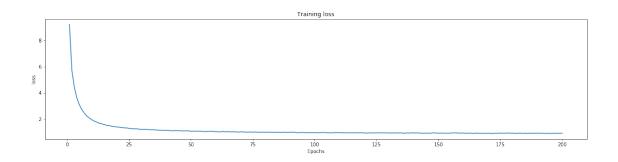
Epoch 199

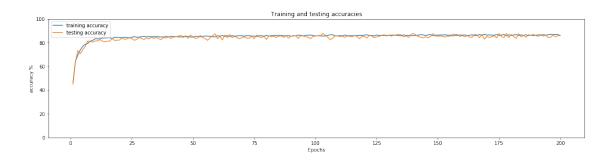
Training loss: 0.9224974515088569001 Training accuracy: 86.7916666666666% Test accuracy: 85.833333333333333

Epoch 200

Training loss: 0.9262812921787709626

Training accuracy: 86.0% Test accuracy: 86.0%





Now adding a hidden layer with 15 neurons:

[5]: net = network.Linear\_Network\_CrossValidation([25,15,10])

[6]: net.SGD(training\_data, 200, 10, 0.1)

## Epoch 1

Training loss: 4.792071241986174617

Training accuracy: 14.0%

Test accuracy: 14.166666666666666%

## Epoch 2

Training loss: 3.3346337310360963358 Training accuracy: 33.04166666666667%

Test accuracy: 33.5%

## Epoch 3

Training loss: 3.024566060762295849
Training accuracy: 44.791666666666664%

Test accuracy: 45.8333333333333333%

## Epoch 4

Training loss: 2.861589116469465267

Training accuracy: 51.75%

Test accuracy: 49.6666666666667%

Training loss: 2.755135437759301802

Training accuracy: 55.25%

Test accuracy: 57.8333333333333336%

#### Epoch 6

Training loss: 2.6496530787622441599

Training accuracy: 59.375%

Test accuracy: 57.8333333333333336%

#### Epoch 7

Training loss: 2.5734595082181430433

Training accuracy: 61.75%

Test accuracy: 64.999999999999%

## Epoch 8

Training loss: 2.4751802065387753368 Training accuracy: 65.70833333333333% Test accuracy: 61.6666666666667%

#### Epoch 9

Training loss: 2.4047869776722956285

Training accuracy: 66.875%

Test accuracy: 66.1666666666666%

### Epoch 10

Training loss: 2.337064684430916995 Training accuracy: 69.5416666666666%

Test accuracy: 67.0%

## Epoch 11

Training loss: 2.2634988026305364562 Training accuracy: 71.3750000000001% Test accuracy: 68.166666666666%

## Epoch 12

Training loss: 2.2044487360756696262 Training accuracy: 72.5416666666667% Test accuracy: 70.333333333333333

### Epoch 13

Training loss: 2.1526844679981901808 Training accuracy: 73.2916666666666% Test accuracy: 73.999999999999%

## Epoch 14

Training loss: 2.0966026309364424907

Training accuracy: 74.25%

Test accuracy: 74.66666666666667%

Epoch 15

Training loss: 2.0494970646965249214
Training accuracy: 75.16666666666666
Test accuracy: 76.83333333333334%

Epoch 16

Training loss: 1.9914875619643344253 Training accuracy: 76.7916666666666% Test accuracy: 73.999999999999%

Epoch 17

Training loss: 1.9422051684254647482 Training accuracy: 76.83333333333334% Test accuracy: 77.1666666666667%

Epoch 18

Training loss: 1.8955869939104049791 Training accuracy: 77.7916666666667% Test accuracy: 76.8333333333333333

Epoch 19

Epoch 20

Training loss: 1.8381849444997990589 Training accuracy: 78.41666666666667%

Test accuracy: 81.5%

Epoch 21

Training loss: 1.8003039329544767915

Training accuracy: 79.25%

Test accuracy: 81.1666666666667%

Epoch 22

Training loss: 1.759474149049852692 Training accuracy: 79.79166666666666% Test accuracy: 81.66666666666667%

Epoch 23

Training loss: 1.7287966115834145813 Training accuracy: 80.45833333333333%

Test accuracy: 81.0%

Training loss: 1.6986172921309353453 Training accuracy: 81.33333333333334%

Test accuracy: 80.5%

Epoch 25

Training loss: 1.664123405648994153 Training accuracy: 81.958333333333334%

Test accuracy: 80.0%

Epoch 26

Training loss: 1.6397804306801896705 Training accuracy: 81.91666666666666% Test accuracy: 80.83333333333333%

Epoch 27

Training loss: 1.6170875797548805396

Training accuracy: 82.125%

Test accuracy: 81.5%

Epoch 28

Training loss: 1.5896991525325337858
Training accuracy: 82.3750000000001%
Test accuracy: 82.166666666666%

Epoch 29

Training loss: 1.5642606610991159054

Training accuracy: 83.25% Test accuracy: 80.0%

Epoch 30

Training loss: 1.5455033895480043297 Training accuracy: 82.58333333333334%

Test accuracy: 83.5%

Epoch 31

Training loss: 1.5125636832502982036 Training accuracy: 83.20833333333333 Test accuracy: 81.83333333333334%

Epoch 32

Training loss: 1.4874199918974025626 Training accuracy: 83.7916666666667% Test accuracy: 80.33333333333334%

Epoch 33

Training loss: 1.4943063733399869675

Training accuracy: 82.125%

Test accuracy: 86.0%

Epoch 34

Training loss: 1.4753324177960314486 Training accuracy: 82.8333333333334% Test accuracy: 84.8333333333334%

Epoch 35

Training loss: 1.4457634506661197761
Training accuracy: 83.6250000000001%
Test accuracy: 83.33333333333334%

Epoch 36

Training loss: 1.4265547282899436502 Training accuracy: 83.6666666666667% Test accuracy: 84.5000000000001%

Epoch 37

Training loss: 1.4211053928843640298 Training accuracy: 83.95833333333334%

Test accuracy: 83.5%

Epoch 38

Training loss: 1.3952727323563335106 Training accuracy: 84.2916666666667% Test accuracy: 84.333333333333333

Epoch 39

Training loss: 1.3818687002725903815

Training accuracy: 84.625%

Test accuracy: 83.0%

Epoch 40

Training loss: 1.3673264963782815201 Training accuracy: 84.45833333333334% Test accuracy: 84.33333333333334%

Epoch 41

Training loss: 1.3510860143272757518
Training accuracy: 84.41666666666667%

Test accuracy: 85.5%

Epoch 42

Training loss: 1.3412508966567629617 Training accuracy: 84.58333333333334% Test accuracy: 84.6666666666667%

Epoch 43

Training loss: 1.3354592836216542951

Training accuracy: 85.25% Test accuracy: 83.0%

Epoch 44

Training loss: 1.3117213611373053009 Training accuracy: 85.3333333333333%

Test accuracy: 84.0%

Epoch 45

Epoch 46

Training loss: 1.2807342935883394653

Training accuracy: 85.0%

Test accuracy: 85.333333333333334%

Epoch 47

Training loss: 1.2832940053815598599 Training accuracy: 85.20833333333333%

Test accuracy: 85.5%

Epoch 48

Training loss: 1.2733372223314146567 Training accuracy: 84.91666666666667% Test accuracy: 86.1666666666666%

Epoch 49

Training loss: 1.2611978321538024588
Training accuracy: 85.16666666666666%

Test accuracy: 85.0%

Epoch 50

Training loss: 1.2498402836722762714
Training accuracy: 85.166666666666666%

Test accuracy: 85.5%

Epoch 51

Training loss: 1.2443737628992837575 Training accuracy: 85.2499999999999% Test accuracy: 85.833333333333333

Epoch 52

Training loss: 1.2285847576162392171
Training accuracy: 85.29166666666667%

Test accuracy: 86.0%

Training loss: 1.2180203783985894354
Training accuracy: 85.1666666666667%
Test accuracy: 87.3333333333333333

Epoch 54

Epoch 55

Training loss: 1.2013132219519657333
Training accuracy: 85.83333333333333333
Test accuracy: 85.166666666666666%

Epoch 56

Training loss: 1.1865733613617536035 Training accuracy: 85.8750000000001% Test accuracy: 85.0000000000001%

Epoch 57

Training loss: 1.1835710885031180698 Training accuracy: 85.58333333333334% Test accuracy: 86.83333333333333%

Epoch 58

Training loss: 1.1806409032128290632 Training accuracy: 85.58333333333334% Test accuracy: 87.5000000000001%

Epoch 59

Training loss: 1.1526536949425053005 Training accuracy: 86.499999999999%

Test accuracy: 84.0%

Epoch 60

Training loss: 1.1425263001911997493

Training accuracy: 86.75%

Test accuracy: 83.1666666666667%

Epoch 61

Training loss: 1.1426443532326102506 Training accuracy: 85.91666666666666% Test accuracy: 86.3333333333333333

Epoch 62

Training loss: 1.1402445093914412693

Training accuracy: 86.29166666666666% Test accuracy: 85.83333333333334%

Epoch 63

Training loss: 1.1205126387494043933 Training accuracy: 86.75000000000001% Test accuracy: 83.33333333333334%

Epoch 64

Training loss: 1.130712958249890276 Training accuracy: 85.95833333333333 Test accuracy: 86.833333333333333

Epoch 65

Training loss: 1.1133509697931886723 Training accuracy: 86.20833333333333% Test accuracy: 85.66666666666667%

Epoch 66

Training loss: 1.110849579724731241

Training accuracy: 86.125%

Test accuracy: 87.0000000000001%

Epoch 67

Training loss: 1.1086111833887634714
Training accuracy: 86.00000000000001%

Test accuracy: 87.0%

Epoch 68

Training loss: 1.0782887914912924358
Training accuracy: 86.6666666666667%
Test accuracy: 84.5000000000001%

Epoch 69

Training loss: 1.0784938539304441548

Training accuracy: 86.625%

Test accuracy: 85.1666666666667%

Epoch 70

Training loss: 1.0753656220372738554
Training accuracy: 86.4166666666666%
Test accuracy: 85.8333333333333333

Epoch 71

Training loss: 1.0869640692904350286 Training accuracy: 86.33333333333334%

Test accuracy: 87.0%

Training loss: 1.0583872441487163007 Training accuracy: 87.08333333333333 Test accuracy: 83.83333333333334%

Epoch 73

Training loss: 1.0583546080816946487 Training accuracy: 86.29166666666667%

Test accuracy: 86.5%

Epoch 74

Training loss: 1.073400021566969035 Training accuracy: 86.0416666666666% Test accuracy: 88.1666666666666%

Epoch 75

Epoch 76

Epoch 77

Training loss: 1.0442352536381456231 Training accuracy: 86.749999999999% Test accuracy: 87.3333333333333333

Epoch 78

Training loss: 1.0485822954776624642

Training accuracy: 86.5%

Test accuracy: 87.3333333333333333%

Epoch 79

Training loss: 1.0394737214361774839

Training accuracy: 86.875%

Test accuracy: 87.5%

Epoch 80

Training loss: 1.0266713662968041834 Training accuracy: 86.70833333333334%

Test accuracy: 87.0%

Epoch 81

Training loss: 1.0088097129781432113
Training accuracy: 87.2500000000001%

Test accuracy: 85.5%

Epoch 82

Training loss: 1.0030700666534626408 Training accuracy: 87.2500000000001%

Test accuracy: 85.5%

Epoch 83

Training loss: 1.0251100498694718426 Training accuracy: 86.58333333333334% Test accuracy: 88.6666666666667%

Epoch 84

Epoch 85

Training loss: 0.9916018921327679249

Training accuracy: 87.125%

Test accuracy: 86.0000000000001%

Epoch 86

Training loss: 0.986182765179135335
Training accuracy: 87.04166666666667%
Test accuracy: 86.1666666666666%

Epoch 87

Epoch 88

Training loss: 0.9903955685781764636 Training accuracy: 87.20833333333333% Test accuracy: 86.1666666666667%

Epoch 89

Training loss: 0.98822047562277363285 Training accuracy: 87.3749999999999% Test accuracy: 86.1666666666667%

Epoch 90

Training loss: 0.97857988628633842007 Training accuracy: 87.4166666666667% Test accuracy: 85.833333333333333

Training loss: 0.96252298184761960555 Training accuracy: 87.58333333333334% Test accuracy: 84.83333333333334%

Epoch 92

Training loss: 0.97859248811936812914 Training accuracy: 86.70833333333334%

Test accuracy: 88.0%

Epoch 93

Training loss: 0.9846400518195798965 Training accuracy: 86.83333333333334% Test accuracy: 87.99999999999999

Epoch 94

Training loss: 0.9522857693034275841 Training accuracy: 87.749999999999% Test accuracy: 84.8333333333334%

Epoch 95

Training loss: 0.9708674870452022016 Training accuracy: 87.08333333333334% Test accuracy: 87.1666666666666%

Epoch 96

Training loss: 0.9538011084673532119 Training accuracy: 87.2916666666666% Test accuracy: 85.6666666666666%

Epoch 97

Training loss: 0.9620743374461834331 Training accuracy: 86.5416666666666% Test accuracy: 89.6666666666666%

Epoch 98

Training loss: 0.9489315993769272317 Training accuracy: 87.2916666666666% Test accuracy: 87.1666666666666%

Epoch 99

Training loss: 0.95448517119208038895

Training accuracy: 87.0%

Test accuracy: 87.33333333333334%

Epoch 100

Training loss: 0.9412384954137370943 Training accuracy: 87.4583333333334% Test accuracy: 86.3333333333334%

Training loss: 0.93590102581430667376 Training accuracy: 87.58333333333334%

Test accuracy: 86.5%

Epoch 102

Training loss: 0.9255851255313546605

Training accuracy: 87.875%

Test accuracy: 85.1666666666667%

Epoch 103

Training loss: 0.93184329146338837677 Training accuracy: 87.33333333333334%

Test accuracy: 87.0%

Epoch 104

Training loss: 0.9354958174191041429 Training accuracy: 87.16666666666666% Test accuracy: 87.6666666666666%

Epoch 105

Training loss: 0.9254144451295545146 Training accuracy: 87.3749999999999% Test accuracy: 87.33333333333334%

Epoch 106

Training loss: 0.93826832295926048354 Training accuracy: 86.8750000000001% Test accuracy: 89.499999999999%

Epoch 107

Training loss: 0.92281230631242051356 Training accuracy: 87.5416666666666% Test accuracy: 87.0000000000001%

Epoch 108

Training loss: 0.92344866489474711907

Training accuracy: 87.5%

Test accuracy: 87.1666666666667%

Epoch 109

Training loss: 0.9160526559781779713
Training accuracy: 87.4166666666667%
Test accuracy: 88.1666666666667%

Epoch 110

Training loss: 0.9087690082938462748

Training accuracy: 87.91666666666666% Test accuracy: 86.333333333333333

Epoch 111

Epoch 112

Training loss: 0.898667110554932874

Training accuracy: 88.25%

Test accuracy: 84.83333333333334%

Epoch 113

Training loss: 0.8961106107936043808

Training accuracy: 87.875%

Test accuracy: 86.83333333333333333%

Epoch 114

Training loss: 0.9124922442581743497

Training accuracy: 87.25%

Test accuracy: 89.499999999999%

Epoch 115

Training loss: 0.90399932135205304806 Training accuracy: 87.6666666666667% Test accuracy: 88.333333333333333

Epoch 116

Training loss: 0.89135088281432103255 Training accuracy: 88.20833333333333 Test accuracy: 86.33333333333334%

Epoch 117

Epoch 118

Training loss: 0.8933366739458444653

Training accuracy: 87.625%

Test accuracy: 88.0%

Epoch 119

Training loss: 0.8870837975972320764
Training accuracy: 87.8749999999999%
Test accuracy: 87.66666666666667%

Training loss: 0.8894478913205205831

Training accuracy: 87.5%

Test accuracy: 88.1666666666666%

Epoch 121

Epoch 122

Training loss: 0.88436532299397705635

Training accuracy: 87.75%

Test accuracy: 88.6666666666666%

Epoch 123

Training loss: 0.87278278124390786723 Training accuracy: 88.0833333333334% Test accuracy: 86.8333333333334%

Epoch 124

Training loss: 0.86954010660260297146 Training accuracy: 88.0000000000001% Test accuracy: 86.83333333333334%

Epoch 125

Training loss: 0.8570596032470416318 Training accuracy: 88.33333333333334% Test accuracy: 86.1666666666667%

Epoch 126

Training loss: 0.84869443862327666504 Training accuracy: 88.5000000000001% Test accuracy: 85.333333333333333

Epoch 127

Training loss: 0.8597267919683197739

Training accuracy: 88.5%

Test accuracy: 85.833333333333334%

Epoch 128

Training loss: 0.86634196055481387433 Training accuracy: 88.0416666666667% Test accuracy: 86.6666666666667%

Epoch 129

Training loss: 0.8614274878274532961 Training accuracy: 87.666666666666666% Test accuracy: 88.1666666666666%

Epoch 130

Training loss: 0.8675033232795675226

Training accuracy: 88.0%

Test accuracy: 88.0000000000001%

Epoch 131

Epoch 132

Epoch 133

Training loss: 0.85488098176505648997 Training accuracy: 88.2916666666666% Test accuracy: 87.66666666666667%

Epoch 134

Training loss: 0.8485277062289370063 Training accuracy: 88.2083333333333% Test accuracy: 87.33333333333334%

Epoch 135

Training loss: 0.85430917042471805987 Training accuracy: 88.20833333333334% Test accuracy: 87.66666666666667%

Epoch 136

Epoch 137

Training loss: 0.8421445363747444247 Training accuracy: 88.2916666666666% Test accuracy: 87.8333333333333333

Epoch 138

Training loss: 0.84943022814370667287 Training accuracy: 87.9583333333333333 Test accuracy: 89.166666666666666%

Training loss: 0.8349318309690698501 Training accuracy: 88.29166666666667% Test accuracy: 87.33333333333334%

Epoch 140

Training loss: 0.8438952523635520031

Training accuracy: 88.0%

Test accuracy: 88.6666666666667%

Epoch 141

Training loss: 0.85058200704388999566

Training accuracy: 87.625%

Test accuracy: 89.999999999999%

Epoch 142

Training loss: 0.8473580652430164179 Training accuracy: 87.95833333333334%

Test accuracy: 89.0%

Epoch 143

Training loss: 0.8288904536445277127 Training accuracy: 88.2916666666666% Test accuracy: 88.33333333333333

Epoch 144

Training loss: 0.84502554239888817776 Training accuracy: 88.20833333333333% Test accuracy: 88.6666666666666%

Epoch 145

Training loss: 0.8249704041738632288 Training accuracy: 88.7083333333334% Test accuracy: 86.8333333333334%

Epoch 146

Training loss: 0.8101243845468566538 Training accuracy: 88.8749999999999%

Test accuracy: 85.5%

Epoch 147

Training loss: 0.830451180332476665 Training accuracy: 88.1666666666667% Test accuracy: 88.83333333333334%

Epoch 148

Training loss: 0.8144032512335116481 Training accuracy: 88.5416666666667% Test accuracy: 87.333333333333333

Training loss: 0.8432930815210359316 Training accuracy: 87.87500000000001%

Test accuracy: 90.5%

Epoch 150

Training loss: 0.825801178390405318

Training accuracy: 88.375%

Test accuracy: 88.5%

Epoch 151

Epoch 152

Training loss: 0.8285413194550985597 Training accuracy: 88.70833333333333% Test accuracy: 88.166666666666%

Epoch 153

Training loss: 0.8334283435540793537 Training accuracy: 88.1666666666666% Test accuracy: 89.999999999999%

Epoch 154

Epoch 155

Training loss: 0.80758688123256104613

Training accuracy: 88.625%

Test accuracy: 88.3333333333333333%

Epoch 156

Training loss: 0.8152647293477368018 Training accuracy: 88.6666666666667% Test accuracy: 88.1666666666666%

Epoch 157

Training loss: 0.8045939084748499149

Training accuracy: 88.875%

Test accuracy: 86.333333333333334%

Epoch 158

Training loss: 0.80871380920139343095

Training accuracy: 88.4166666666667% Test accuracy: 89.0000000000001%

Epoch 159

Training loss: 0.80862215258834086297 Training accuracy: 88.54166666666667%

Test accuracy: 88.5%

Epoch 160

Training loss: 0.81109737952508566435 Training accuracy: 88.58333333333334%

Test accuracy: 88.5%

Epoch 161

Epoch 162

Training loss: 0.7887270445608660589 Training accuracy: 89.16666666666666% Test accuracy: 86.1666666666666%

Epoch 163

Training loss: 0.81079918934649637744 Training accuracy: 88.4166666666666%

Test accuracy: 90.0%

Epoch 164

Training loss: 0.804321835729747886

Training accuracy: 88.75%

Test accuracy: 88.499999999999%

Epoch 165

Training loss: 0.80519862423734845074

Training accuracy: 88.625%

Test accuracy: 89.16666666666667%

Epoch 166

Training loss: 0.79150341498594873225 Training accuracy: 88.83333333333334% Test accuracy: 88.16666666666666%

Epoch 167

Training loss: 0.8054933571248680998

Training accuracy: 88.75%

Test accuracy: 88.83333333333334%

Training loss: 0.8004371378537407327 Training accuracy: 88.749999999999% Test accuracy: 88.83333333333334%

Epoch 169

Training loss: 0.79403213159163128445 Training accuracy: 88.5416666666666% Test accuracy: 89.333333333333333

Epoch 170

Training loss: 0.8198124009414503929 Training accuracy: 88.4166666666667% Test accuracy: 90.833333333333333

Epoch 171

Training loss: 0.79965938213617195106 Training accuracy: 88.70833333333334% Test accuracy: 89.33333333333333%

Epoch 172

Training loss: 0.7935774878280064536 Training accuracy: 89.16666666666667%

Test accuracy: 88.0%

Epoch 173

Training loss: 0.79964979396792001617 Training accuracy: 88.66666666666666% Test accuracy: 89.66666666666666%

Epoch 174

Training loss: 0.7962230692132322766

Training accuracy: 88.875%

Test accuracy: 89.0%

Epoch 175

Training loss: 0.7759182197727546255 Training accuracy: 88.95833333333333%

Test accuracy: 88.5%

Epoch 176

Training loss: 0.7839940889231773586 Training accuracy: 89.0416666666666% Test accuracy: 88.1666666666667%

Epoch 177

Training loss: 0.7790762599926182088

Training accuracy: 88.875%

Test accuracy: 88.5%

Epoch 178

Training loss: 0.7954524776762061021

Training accuracy: 88.75%

Test accuracy: 89.6666666666666%

Epoch 179

Training loss: 0.7894512102378247983

Training accuracy: 89.25%

Test accuracy: 88.33333333333334%

Epoch 180

Training loss: 0.7803963148911486146

Training accuracy: 88.75%

Test accuracy: 89.5%

Epoch 181

Training loss: 0.7864668859977220898

Training accuracy: 88.625%

Test accuracy: 90.33333333333334%

Epoch 182

Training loss: 0.78957837613564864484 Training accuracy: 88.7499999999999% Test accuracy: 89.83333333333334%

Epoch 183

Epoch 184

Training loss: 0.77078406289936850167 Training accuracy: 88.91666666666666% Test accuracy: 88.9999999999999%

Epoch 185

Training loss: 0.78671820398724182034 Training accuracy: 88.458333333333333 Test accuracy: 90.6666666666666666

Epoch 186

Training loss: 0.7707891080309591755
Training accuracy: 89.0000000000001%
Test accuracy: 88.66666666666666

Training loss: 0.75172239125461242417 Training accuracy: 89.33333333333334% Test accuracy: 87.666666666666666%

#### Epoch 188

Training loss: 0.77231962397597780896 Training accuracy: 88.7916666666667% Test accuracy: 89.499999999999%

# Epoch 189

Training loss: 0.7669693061633796559 Training accuracy: 89.1666666666666% Test accuracy: 88.3333333333333333

## Epoch 190

Training loss: 0.76702278147236339814 Training accuracy: 89.20833333333334% Test accuracy: 88.16666666666666%

#### Epoch 191

Training loss: 0.7727409459974207853 Training accuracy: 89.08333333333334% Test accuracy: 89.1666666666667%

## Epoch 192

Training loss: 0.7540243424422010283 Training accuracy: 89.20833333333333%

Test accuracy: 88.5%

## Epoch 193

## Epoch 194

Training loss: 0.7833166390186084041 Training accuracy: 88.2083333333334% Test accuracy: 91.9999999999999

# Epoch 195

Training loss: 0.75936802310676597687 Training accuracy: 89.04166666666666%

Test accuracy: 89.0%

# Epoch 196

Training loss: 0.77347086182156473777 Training accuracy: 88.7083333333333%

Test accuracy: 90.0%

Training loss: 0.7599821046214927405 Training accuracy: 88.95833333333334%

Test accuracy: 89.0%

Epoch 198

Training loss: 0.7664173272979356108

Training accuracy: 89.0%

Test accuracy: 89.8333333333333333%

Epoch 199

Training loss: 0.7583545119896498101

Training accuracy: 89.25%

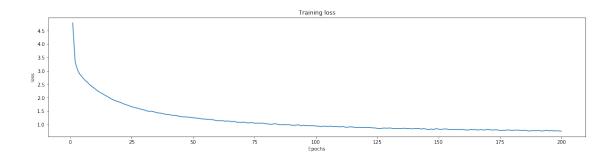
Test accuracy: 88.1666666666667%

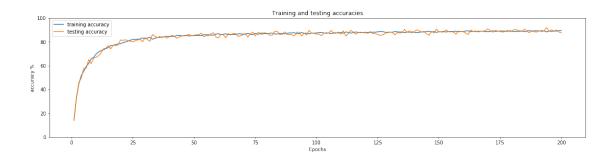
Epoch 200

Training loss: 0.7491805327490448665

Training accuracy: 89.5%

Test accuracy: 87.50000000000001%





Here we see a slight increase in the accuracy reaching upto 90%

Finally let's try 2 hidden layers with 15 and 15 neurons in each respectively. We'll keep a regularization parameter to prevent overfitting.

# [7]: net = network.Linear\_Network\_CrossValidation([25,15,15,10])

# [8]: net.SGD(training\_data, 200, 10, 0.1, lmbda=1.0)

## Epoch 1

Training loss: 4.4850064782964885078 Training accuracy: 9.91666666666668% Test accuracy: 8.4999999999998%

# Epoch 2

Training loss: 3.356805739666318296 Training accuracy: 14.66666666666668%

Test accuracy: 16.5%

#### Epoch 3

Training loss: 3.2432002048708097601 Training accuracy: 19.04166666666664% Test accuracy: 19.49999999999999%

# Epoch 4

Training loss: 3.216742481772191744

Training accuracy: 18.708333333333332%

Test accuracy: 19.8333333333333333

# Epoch 5

Training loss: 3.2048485018208617062
Training accuracy: 22.3333333333333336%
Test accuracy: 22.49999999999996%

## Epoch 6

Training loss: 3.1970616176103365687 Training accuracy: 23.458333333333336% Test accuracy: 22.333333333333336%

### Epoch 7

Training loss: 3.1887496605536887408

Training accuracy: 22.375%

Test accuracy: 22.8333333333333332%

# Epoch 8

Training loss: 3.1825580041979554334
Training accuracy: 23.208333333333336%
Test accuracy: 22.4999999999996%

### Epoch 9

Training loss: 3.170211927743147328
Training accuracy: 27.0833333333333336%

Epoch 10

Training loss: 3.160177211390351139
Training accuracy: 23.833333333333336%
Test accuracy: 21.3333333333333336%

Epoch 11

Training loss: 3.1545633996040141993 Training accuracy: 30.4583333333333336%

Test accuracy: 30.0%

Epoch 12

Training loss: 3.1468754136148765752
Training accuracy: 31.1666666666668%
Test accuracy: 30.83333333333333333

Epoch 13

Training loss: 3.138705717917055301 Training accuracy: 32.29166666666664% Test accuracy: 33.3333333333333336%

Epoch 14

Training loss: 3.1260554735067432575
Training accuracy: 34.54166666666667%
Test accuracy: 34.833333333333333

Epoch 15

Training loss: 3.1148095681350496632 Training accuracy: 35.2916666666667% Test accuracy: 37.6666666666667%

Epoch 16

Training loss: 3.0997341956324029333

Training accuracy: 34.25%

Test accuracy: 26.8333333333333332%

Epoch 17

Training loss: 3.0928784680679185012

Training accuracy: 33.75%

Test accuracy: 32.5%

Epoch 18

Training loss: 3.0811709984576454067
Training accuracy: 35.458333333333336%
Test accuracy: 35.83333333333336%

Training loss: 3.067233034350844062 Training accuracy: 35.7083333333333% Test accuracy: 34.66666666666667%

Epoch 20

Training loss: 3.0557381413786215698 Training accuracy: 36.83333333333333%

Test accuracy: 39.5%

Epoch 21

Training loss: 3.0392835509045703535 Training accuracy: 39.20833333333333%

Test accuracy: 36.5%

Epoch 22

Training loss: 3.024857649851178058
Training accuracy: 39.16666666666667%

Test accuracy: 39.5%

Epoch 23

Training loss: 3.0095757197702931425
Training accuracy: 39.3333333333333336%
Test accuracy: 38.66666666666667%

Epoch 24

Epoch 25

Training loss: 2.973875056258342664 Training accuracy: 41.29166666666664% Test accuracy: 40.0000000000001%

Epoch 26

Training loss: 2.9609351706824136642

Training accuracy: 41.625%

Test accuracy: 43.6666666666667%

Epoch 27

Epoch 28

Training loss: 2.9211061901704385986 Training accuracy: 42.458333333333336% Test accuracy: 39.66666666666664%

Training loss: 2.9053420813347378279 Training accuracy: 41.999999999999% Test accuracy: 40.1666666666667%

#### Epoch 30

Training loss: 2.8872881228682418546 Training accuracy: 41.0000000000001% Test accuracy: 43.6666666666667%

#### Epoch 31

# Epoch 32

Training loss: 2.8441363051991943155 Training accuracy: 43.54166666666667%

Test accuracy: 42.5%

#### Epoch 33

Training loss: 2.8330324357810255972 Training accuracy: 43.95833333333333%

Test accuracy: 48.0%

## Epoch 34

Training loss: 2.8056650006215426841 Training accuracy: 46.2500000000001% Test accuracy: 45.83333333333336%

## Epoch 35

# Epoch 36

## Epoch 37

Training loss: 2.7413646196354858639 Training accuracy: 46.999999999999%

Test accuracy: 46.5%

# Epoch 38

Training loss: 2.7271742149533882565

Training accuracy: 47.208333333333333%

Test accuracy: 51.5%

Epoch 39

Training loss: 2.7001558407477445482

Training accuracy: 48.125%

Test accuracy: 46.0%

Epoch 40

Training loss: 2.6861866865012374993

Training accuracy: 49.0%

Test accuracy: 50.33333333333333333%

Epoch 41

Training loss: 2.6583238320076925628
Training accuracy: 50.0833333333333336%

Test accuracy: 48.83333333333333333%

Epoch 42

Training loss: 2.6317074658853856822 Training accuracy: 51.0416666666667% Test accuracy: 46.833333333333336%

Epoch 43

Training loss: 2.6138176654526768892 Training accuracy: 50.416666666666664%

Test accuracy: 49.83333333333333333

Epoch 44

Epoch 45

Training loss: 2.5793089454023069506

Training accuracy: 52.5%

Test accuracy: 51.833333333333336%

Epoch 46

Training loss: 2.5632994127822610584

Training accuracy: 52.125%

Test accuracy: 53.33333333333333336%

Epoch 47

Training loss: 2.5347167003372911306

Training accuracy: 52.25%

Test accuracy: 50.6666666666667%

Training loss: 2.5081880780601504175

Training accuracy: 53.125%

Test accuracy: 50.6666666666667%

Epoch 49

Training loss: 2.5019774462264822306

Training accuracy: 52.625%

Test accuracy: 55.3333333333333336%

Epoch 50

Training loss: 2.4764848894662325287 Training accuracy: 54.041666666666664%

Test accuracy: 53.5%

Epoch 51

Training loss: 2.452226904106796056 Training accuracy: 55.4583333333333%

Test accuracy: 53.0%

Epoch 52

Training loss: 2.4271786882900317133 Training accuracy: 55.8333333333333336% Test accuracy: 53.16666666666664%

Epoch 53

Training loss: 2.4087328773039589653 Training accuracy: 56.958333333333333 Test accuracy: 54.833333333333336%

Epoch 54

Training loss: 2.3978986053310927494

Training accuracy: 56.625%

Test accuracy: 58.0%

Epoch 55

Training loss: 2.3741816651786440753
Training accuracy: 57.79166666666664%
Test accuracy: 57.66666666666664%

Epoch 56

Training loss: 2.3542260355808065624

Training accuracy: 58.625%

Test accuracy: 56.1666666666667%

Epoch 57

Training loss: 2.335589776492270719
Training accuracy: 59.791666666666664%

Test accuracy: 56.333333333333333333

Epoch 58

Training loss: 2.3231360258998368397

Training accuracy: 59.125%

Test accuracy: 59.833333333333336%

Epoch 59

Training loss: 2.3041447095744746758 Training accuracy: 60.208333333333333 Test accuracy: 59.333333333333336%

Epoch 60

Training loss: 2.2830765835297399668
Training accuracy: 60.125000000000014%

Test accuracy: 62.0%

Epoch 61

Training loss: 2.2635407150988852269 Training accuracy: 61.708333333333333%

Test accuracy: 61.16666666666667%

Epoch 62

Training loss: 2.243757019773092045
Training accuracy: 62.5416666666667%
Test accuracy: 61.66666666666664%

Epoch 63

Training loss: 2.2319958972046281365 Training accuracy: 62.7083333333333% Test accuracy: 64.83333333333333%

Epoch 64

Training loss: 2.2069541656405040695 Training accuracy: 63.9583333333333336% Test accuracy: 63.16666666666664%

Epoch 65

Training loss: 2.1899232454828515661

Training accuracy: 64.0%

Test accuracy: 64.6666666666666%

Epoch 66

Training loss: 2.1752786555805750444
Training accuracy: 64.708333333333334%

Test accuracy: 64.5%

Training loss: 2.1423056912061856105 Training accuracy: 65.124999999999% Test accuracy: 63.33333333333333

Epoch 68

Epoch 69

Training loss: 2.1057280311128920547 Training accuracy: 66.70833333333334% Test accuracy: 62.6666666666664%

Epoch 70

Training loss: 2.0927274522981452404 Training accuracy: 66.4166666666667% Test accuracy: 66.833333333333333

Epoch 71

Training loss: 2.0839770262945515422
Training accuracy: 66.2916666666666%
Test accuracy: 68.0000000000001%

Epoch 72

Epoch 73

Training loss: 2.0608752314827123479

Training accuracy: 67.25%

Test accuracy: 70.66666666666667%

Epoch 74

Training loss: 2.0311699091818183954
Training accuracy: 68.37500000000001%

Test accuracy: 69.5%

Epoch 75

Training loss: 2.0246517738084845745

Training accuracy: 68.75% Test accuracy: 71.0%

Epoch 76

Training loss: 1.9988725003135568018 Training accuracy: 69.5416666666667% Test accuracy: 69.6666666666666%

Epoch 78

Training loss: 1.9519214609644449316 Training accuracy: 70.91666666666666% Test accuracy: 67.16666666666666%

Epoch 79

Training loss: 1.9502124920417778286

Training accuracy: 70.5%

Test accuracy: 70.1666666666666%

Epoch 80

Training loss: 1.9353559834261043355 Training accuracy: 70.7499999999999% Test accuracy: 72.83333333333333%

Epoch 81

Training loss: 1.9086712622242026586 Training accuracy: 71.916666666666667%

Test accuracy: 69.5%

Epoch 82

Training loss: 1.8981191522404278106 Training accuracy: 72.58333333333334% Test accuracy: 70.333333333333333

Epoch 83

Training loss: 1.8881939145386377953

Training accuracy: 72.625%

Test accuracy: 72.0%

Epoch 84

Training loss: 1.8706959282181593679 Training accuracy: 72.70833333333334% Test accuracy: 71.1666666666667%

Epoch 85

Training loss: 1.8461974074922937936 Training accuracy: 73.7916666666666% Test accuracy: 69.33333333333334%

Epoch 86

Training loss: 1.8439941128404285996

Training accuracy: 73.458333333333334%

Test accuracy: 73.5%

Epoch 87

Training loss: 1.8333436000222114443 Training accuracy: 73.83333333333334%

Test accuracy: 74.5%

Epoch 88

Epoch 89

Training loss: 1.8105139833816417727 Training accuracy: 73.1666666666667% Test accuracy: 78.6666666666667%

Epoch 90

Training loss: 1.792401468222083781
Training accuracy: 74.458333333333334%

Test accuracy: 75.5%

Epoch 91

Training loss: 1.7810047174499233268

Training accuracy: 74.625%

Test accuracy: 75.33333333333333333

Epoch 92

Training loss: 1.765299902122823938
Training accuracy: 74.3750000000001%
Test accuracy: 75.999999999999%

Epoch 93

Training loss: 1.7498873781278681779 Training accuracy: 75.41666666666667%

Test accuracy: 73.0%

Epoch 94

Training loss: 1.726827081529860334 Training accuracy: 75.45833333333333%

Test accuracy: 75.0%

Epoch 95

Training loss: 1.7295224553217010096 Training accuracy: 75.2916666666667% Test accuracy: 75.6666666666667%

Training loss: 1.7246548127522062297 Training accuracy: 75.7083333333333333 Test accuracy: 77.66666666666666%

Epoch 97

Training loss: 1.7032964189077534928

Training accuracy: 75.875%

Test accuracy: 76.1666666666666%

Epoch 98

Training loss: 1.6995911223933147227 Training accuracy: 76.2916666666666% Test accuracy: 76.499999999999%

Epoch 99

Training loss: 1.6651640978227772287 Training accuracy: 76.79166666666666%

Test accuracy: 75.5%

Epoch 100

Training loss: 1.6808723451918177181 Training accuracy: 76.499999999999% Test accuracy: 78.166666666666%

Epoch 101

Training loss: 1.6429320071485863347 Training accuracy: 77.0416666666666% Test accuracy: 76.1666666666667%

Epoch 102

Training loss: 1.6394109113463755749 Training accuracy: 77.4166666666666% Test accuracy: 75.499999999999%

Epoch 103

Training loss: 1.6277586155694477767

Training accuracy: 77.75%

Test accuracy: 74.3333333333333333%

Epoch 104

Training loss: 1.6283481274764727302 Training accuracy: 77.54166666666666% Test accuracy: 77.66666666666666%

Epoch 105

Training loss: 1.6203712566662611195
Training accuracy: 77.75000000000001%

Test accuracy: 78.1666666666667%

Epoch 106

Training loss: 1.6044070173546441207 Training accuracy: 78.5416666666667% Test accuracy: 76.3333333333333333

Epoch 107

Training loss: 1.5839484847893517887 Training accuracy: 79.0416666666667% Test accuracy: 75.333333333333333

Epoch 108

Training loss: 1.5782264454868773425

Training accuracy: 78.75%

Test accuracy: 77.83333333333334%

Epoch 109

Training loss: 1.5807373960647599396 Training accuracy: 78.6666666666667% Test accuracy: 78.33333333333334%

Epoch 110

Training loss: 1.5827687259254224922

Training accuracy: 78.375%

Test accuracy: 79.999999999999%

Epoch 111

Training loss: 1.5682899960488519013 Training accuracy: 78.2916666666666% Test accuracy: 81.33333333333334%

Epoch 112

Training loss: 1.5349081594944330439 Training accuracy: 79.70833333333334% Test accuracy: 76.1666666666667%

Epoch 113

Epoch 114

Training loss: 1.5281130021398682932 Training accuracy: 79.04166666666667%

Test accuracy: 79.0%

Training loss: 1.522334181367994055

Training accuracy: 79.125%

Test accuracy: 79.8333333333333333%

Epoch 116

Training loss: 1.5117069466936084875 Training accuracy: 78.8750000000001% Test accuracy: 81.6666666666667%

Epoch 117

Epoch 118

Training loss: 1.498418350903087802 Training accuracy: 79.54166666666666% Test accuracy: 81.66666666666667%

Epoch 119

Training loss: 1.4842821763492565848 Training accuracy: 80.4166666666667% Test accuracy: 79.33333333333334%

Epoch 120

Training loss: 1.4834437734570311832 Training accuracy: 79.9166666666667% Test accuracy: 81.83333333333334%

Epoch 121

Epoch 122

Epoch 123

Training loss: 1.4521998225408930161

Training accuracy: 80.5%

Test accuracy: 81.6666666666666%

Epoch 124

Training loss: 1.4330439050394409963

Training accuracy: 81.125%

Test accuracy: 80.33333333333334%

Training loss: 1.4178019349950530134

Training accuracy: 81.25% Test accuracy: 81.0%

Epoch 126

Training loss: 1.4063413248700011705

Training accuracy: 81.875%

Test accuracy: 78.333333333333333333

Epoch 127

Training loss: 1.4171777733106056664
Training accuracy: 81.66666666666667%

Test accuracy: 81.0%

Epoch 128

Training loss: 1.4024362252603030789 Training accuracy: 82.04166666666667%

Test accuracy: 80.5%

Epoch 129

Training loss: 1.3828547646318187213 Training accuracy: 81.8749999999999%

Test accuracy: 80.0%

Epoch 130

Training loss: 1.3835596830702955788
Training accuracy: 81.5000000000001%

Test accuracy: 82.5%

Epoch 131

Training loss: 1.3752081231646720192 Training accuracy: 82.29166666666667%

Test accuracy: 80.5%

Epoch 132

Training loss: 1.3814652758042693465 Training accuracy: 82.04166666666666% Test accuracy: 82.66666666666667%

Epoch 133

Training loss: 1.3622488750226002483

Training accuracy: 82.25%

Test accuracy: 82.1666666666667%

Epoch 134

Training loss: 1.3708993073272228599

Epoch 135

Training loss: 1.3451353839415193901

Training accuracy: 82.875%

Test accuracy: 80.5%

Epoch 136

Epoch 137

Training loss: 1.3385968511041070021 Training accuracy: 83.08333333333334%

Test accuracy: 82.5%

Epoch 138

Training loss: 1.3337758253238553851
Training accuracy: 83.04166666666666%
Test accuracy: 82.333333333333334%

Epoch 139

Training loss: 1.3259104316468697047 Training accuracy: 82.9166666666667% Test accuracy: 84.0000000000001%

Epoch 140

Training loss: 1.3087905092210158444 Training accuracy: 83.66666666666667%

Test accuracy: 81.0%

Epoch 141

Training loss: 1.319660184317914443

Training accuracy: 82.625%

Test accuracy: 86.499999999999%

Epoch 142

Training loss: 1.3064673179315585598

Training accuracy: 83.125%

Test accuracy: 83.6666666666667%

Epoch 143

Training loss: 1.2809365515009170014
Training accuracy: 83.70833333333333333
Test accuracy: 81.66666666666667%

Training loss: 1.2872712545188807299
Training accuracy: 83.5000000000001%
Test accuracy: 82.6666666666667%

Epoch 145

Epoch 146

Training loss: 1.2721159298840193667 Training accuracy: 83.874999999999% Test accuracy: 82.33333333333334%

Epoch 147

Training loss: 1.2859210391615178577

Training accuracy: 83.25%

Test accuracy: 84.833333333333334%

Epoch 148

Epoch 149

Training loss: 1.2413955859140263797 Training accuracy: 84.16666666666666% Test accuracy: 82.16666666666667%

Epoch 150

Epoch 151

Training loss: 1.2405623698211687882 Training accuracy: 84.4166666666666% Test accuracy: 82.83333333333334%

Epoch 152

Training loss: 1.2444146140355801715

Training accuracy: 84.0%

Test accuracy: 83.83333333333334%

Epoch 153

Training loss: 1.2325377299862857082 Training accuracy: 84.20833333333334% Test accuracy: 83.6666666666667%

Epoch 154

Training loss: 1.22127167598089548
Training accuracy: 84.83333333333334%
Test accuracy: 82.1666666666666%

Epoch 155

Training loss: 1.2237970114797168009 Training accuracy: 84.16666666666666%

Test accuracy: 85.0%

Epoch 156

Training loss: 1.2202835807130927578 Training accuracy: 84.04166666666666% Test accuracy: 85.3333333333333333

Epoch 157

Training loss: 1.2075148067370243655 Training accuracy: 84.54166666666666%

Test accuracy: 83.5%

Epoch 158

Training loss: 1.1986431462950857805 Training accuracy: 84.3749999999999% Test accuracy: 84.166666666666%

Epoch 159

Training loss: 1.2031189737939484987

Training accuracy: 84.875%

Test accuracy: 83.83333333333334%

Epoch 160

Training loss: 1.2032240720395311271
Training accuracy: 84.29166666666666%
Test accuracy: 85.333333333333334%

Epoch 161

Training loss: 1.1894628091619322769

Training accuracy: 84.375%

Test accuracy: 85.1666666666666%

Epoch 162

Training loss: 1.1763866716792061334
Training accuracy: 84.458333333333333
Test accuracy: 84.833333333333333

Training loss: 1.1822431818465281286 Training accuracy: 84.91666666666667% Test accuracy: 83.33333333333334%

Epoch 164

Training loss: 1.1836099314217062288
Training accuracy: 84.08333333333334%

Test accuracy: 86.5%

Epoch 165

Training loss: 1.1737219363981122391 Training accuracy: 85.0416666666666% Test accuracy: 83.6666666666666%

Epoch 166

Training loss: 1.1658452517535298158 Training accuracy: 84.8749999999999%

Test accuracy: 84.0%

Epoch 167

Training loss: 1.1553331757552881924

Training accuracy: 85.0%

Test accuracy: 84.499999999999%

Epoch 168

Training loss: 1.1557910241415638655 Training accuracy: 85.04166666666666%

Test accuracy: 84.0%

Epoch 169

Training loss: 1.1301753500787422925 Training accuracy: 85.999999999999% Test accuracy: 80.499999999999%

Epoch 170

Training loss: 1.1343607785122263982

Training accuracy: 85.0%

Test accuracy: 83.83333333333334%

Epoch 171

Training loss: 1.1510424740460766448
Training accuracy: 84.79166666666667%

Test accuracy: 85.5%

Epoch 172

Training loss: 1.1247047363009302611 Training accuracy: 85.5416666666666% Test accuracy: 83.499999999999%

#### Epoch 174

Training loss: 1.1237967223888397194
Training accuracy: 85.2916666666667%
Test accuracy: 84.83333333333334%

#### Epoch 175

Training loss: 1.1147545116480842052

Training accuracy: 85.625%

Test accuracy: 83.1666666666666%

# Epoch 176

Training loss: 1.1047748684328695884 Training accuracy: 85.45833333333334% Test accuracy: 84.9999999999999

#### Epoch 177

Training loss: 1.1130921121547114152
Training accuracy: 85.16666666666666
Test accuracy: 86.0000000000001%

# Epoch 178

## Epoch 179

Training loss: 1.1086664133032136249 Training accuracy: 85.3749999999999% Test accuracy: 85.666666666666%

#### Epoch 180

Training loss: 1.1016285063092241905 Training accuracy: 85.7916666666667% Test accuracy: 84.83333333333334%

## Epoch 181

Training loss: 1.0970076731483456799 Training accuracy: 85.41666666666666%

Test accuracy: 86.0%

# Epoch 182

Training loss: 1.0886376006681835261

Epoch 183

Training loss: 1.076965967019693096 Training accuracy: 86.0000000000001% Test accuracy: 83.83333333333334%

Epoch 184

Training loss: 1.0791030542458641371 Training accuracy: 85.79166666666667%

Test accuracy: 84.5%

Epoch 185

Training loss: 1.086553503845163421

Training accuracy: 85.5%

Test accuracy: 86.333333333333334%

Epoch 186

Training loss: 1.0757990159937518747
Training accuracy: 86.00000000000001%

Test accuracy: 85.5%

Epoch 187

Training loss: 1.0621987199240161012 Training accuracy: 86.166666666666666%

Test accuracy: 84.5%

Epoch 188

Training loss: 1.0637489190452939322

Training accuracy: 86.5%

Test accuracy: 84.499999999999%

Epoch 189

Training loss: 1.0705150586464930026 Training accuracy: 85.1666666666667% Test accuracy: 88.83333333333334%

Epoch 190

Training loss: 1.0476088977868649868

Training accuracy: 86.25%

Test accuracy: 84.6666666666666%

Epoch 191

Training loss: 1.0530836098361415143
Training accuracy: 86.166666666666666
Test accuracy: 85.66666666666667%

Training loss: 1.0334311235185067992 Training accuracy: 86.7499999999999% Test accuracy: 84.0000000000001%

Epoch 193

Training loss: 1.0476885268063559933 Training accuracy: 85.7916666666666% Test accuracy: 86.83333333333334%

Epoch 194

Training loss: 1.0500284734024286511 Training accuracy: 86.04166666666667%

Test accuracy: 87.0%

Epoch 195

Training loss: 1.0287267488290544034 Training accuracy: 86.0416666666666% Test accuracy: 86.83333333333334%

Epoch 196

Training loss: 1.0452435175130006009 Training accuracy: 86.16666666666666% Test accuracy: 86.6666666666666%

Epoch 197

Training loss: 1.0254561796901198003 Training accuracy: 86.5416666666666% Test accuracy: 86.3333333333333333

Epoch 198

Training loss: 1.018080162968010525 Training accuracy: 86.9166666666667% Test accuracy: 84.4999999999999

Epoch 199

Training loss: 1.0215660936076044658
Training accuracy: 86.87500000000001%

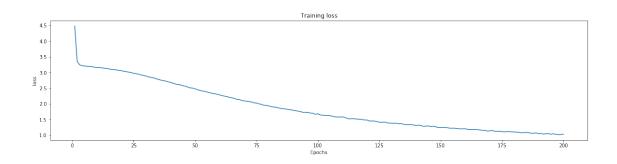
Test accuracy: 85.0%

Epoch 200

Training loss: 1.0314826435002884537

Training accuracy: 85.875%

Test accuracy: 88.33333333333333333





We still don't get a result as good as the original images.

This might be because when reducing the dimensionality of the image, we may lose some spatial information of the image. This will make it tough for the neural network to learn some key spatial differences that separates one digit from another.

2.4 With this we end the 1st report. In the next report, we'll train a CNN using PyTorch to train on the entire MNIST dataset

[]: