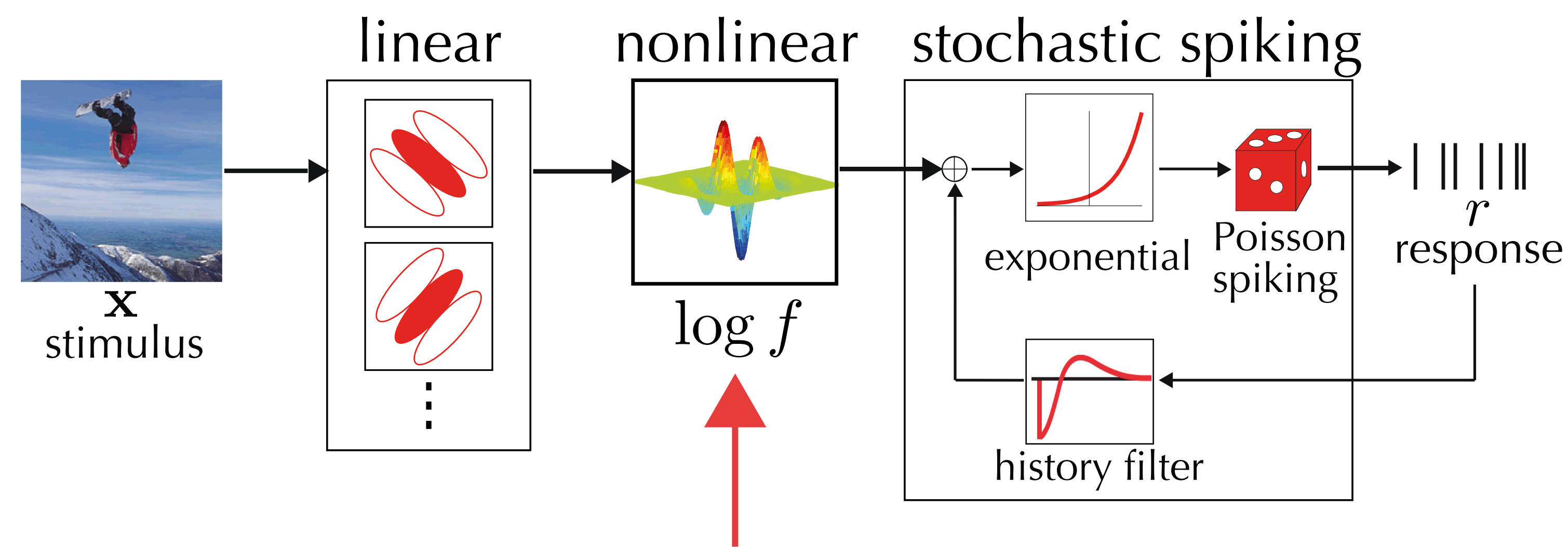


Adaptive Estimation of Nonlinear Response Functions in V1 with Gaussian Processes

Mijung Park¹, Gregory D. Horwitz², and Jonathan W. Pillow³ 1, 3: The University of Texas at Austin, 2: University of Washington.

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#III-11

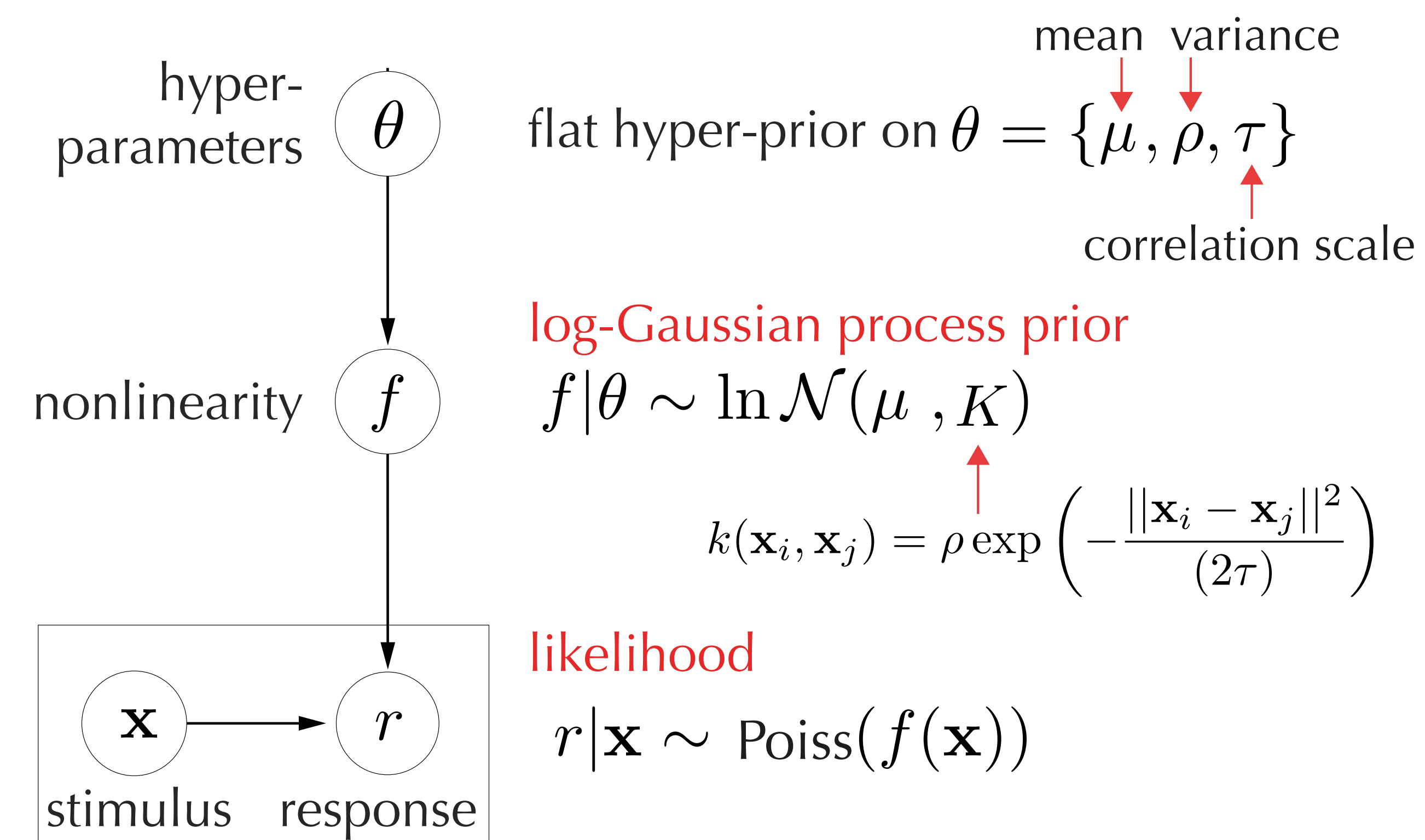
1. Neural characterization problem



Question: how to efficiently learn neural response nonlinearities in closed-loop experiments?

2. logGP-Poisson encoding model

generative model



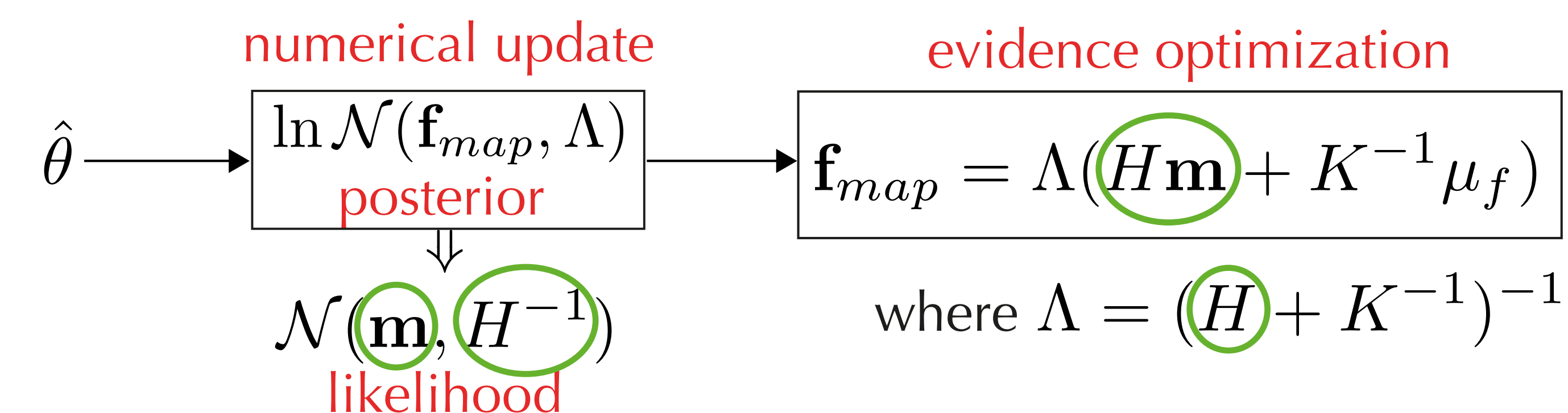
MAP inference: $\mathbf{f}_{\text{map}} = \arg \max_{\mathbf{f}} \log p(\mathbf{f}|\mathbf{r}, \mathbf{X}, \theta)$

setting hyperparameters

- Set θ by maximizing marginal likelihood (Laplace approximation):

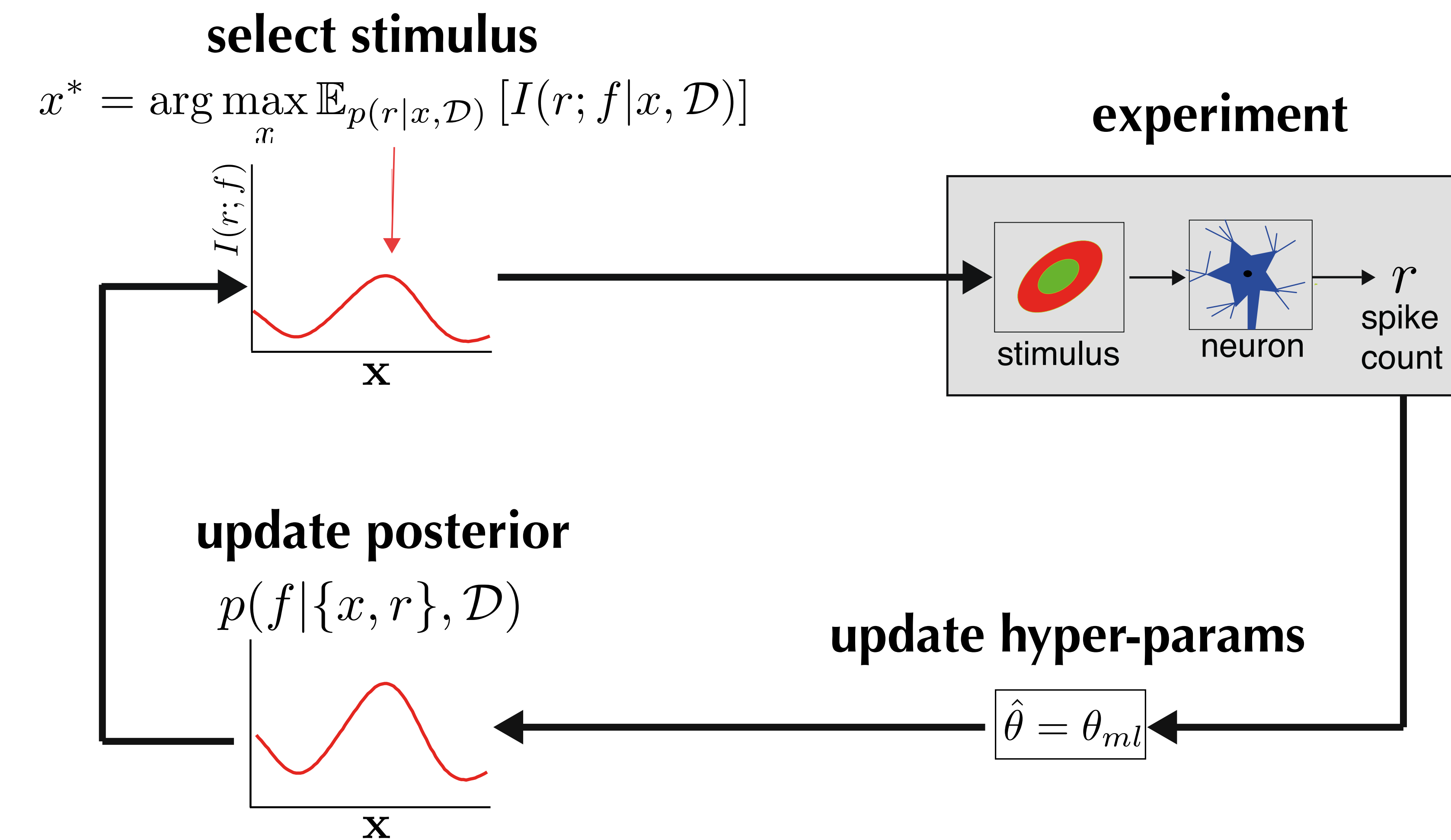
$$p(\mathbf{r}|\theta) = \int p(\mathbf{r}|\mathbf{f})p(\mathbf{f}|\theta)d\mathbf{f} \approx \frac{p(\mathbf{r}|\mathbf{f}_{\text{map}})\ln \mathcal{N}(\mu, \Lambda)}{\ln \mathcal{N}(\mathbf{f}_{\text{map}}, \Lambda)} \left. \vphantom{\frac{p(\mathbf{r}|\mathbf{f}_{\text{map}})\ln \mathcal{N}(\mu, \Lambda)}{\ln \mathcal{N}(\mathbf{f}_{\text{map}}, \Lambda)}} \right\} \begin{array}{l} \text{Poisson likeli.} \\ \text{log-normal} \\ \text{approx. log-normal posterior} \end{array} \text{iterate!}$$

- Numerical update of posterior & evidence for each θ : expensive!



3. Adaptive stimulus selection

- select stimulus \mathbf{x} that maximizes expected information gain on each trial



- maximizing information = minimizing posterior uncertainty

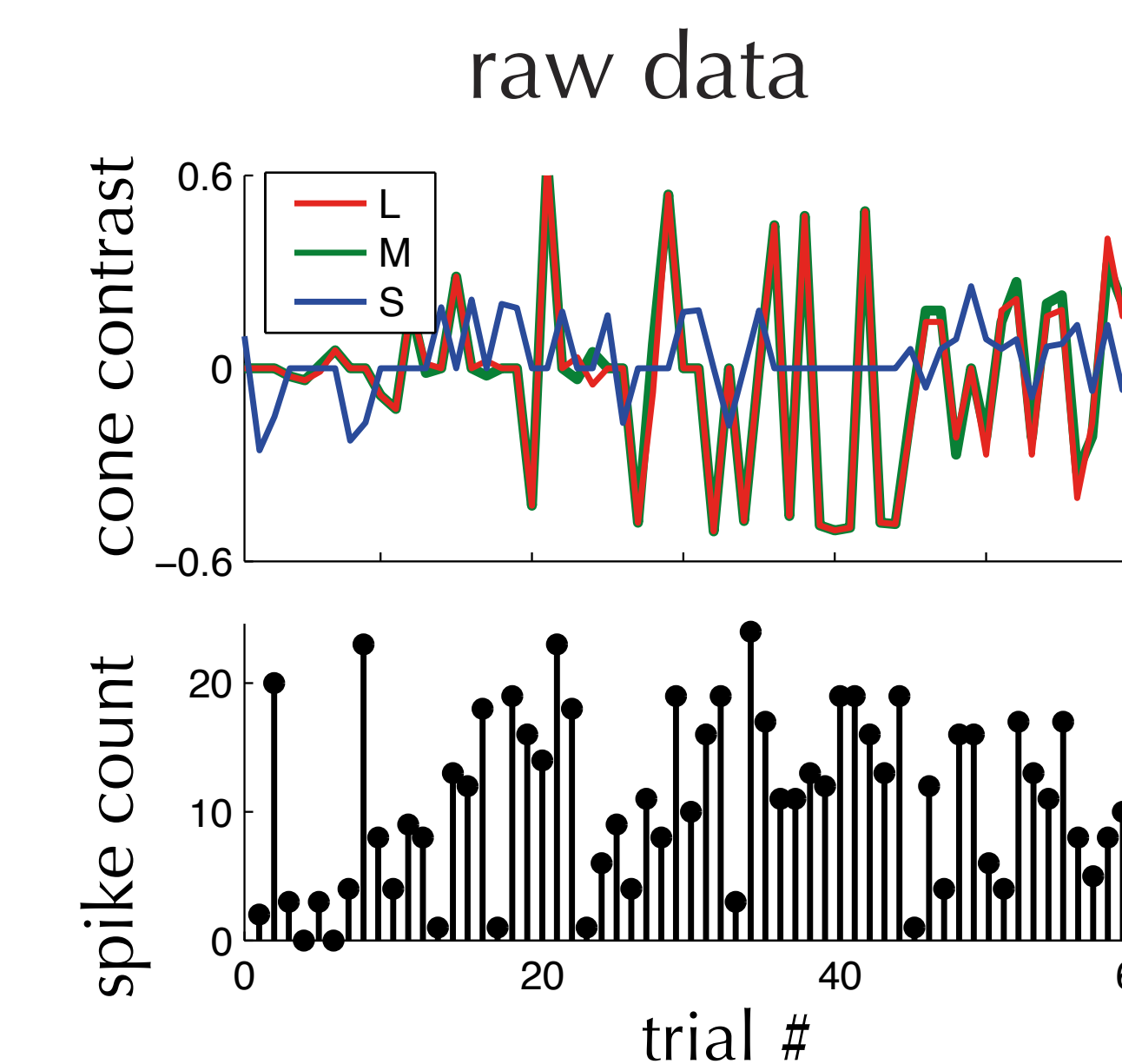
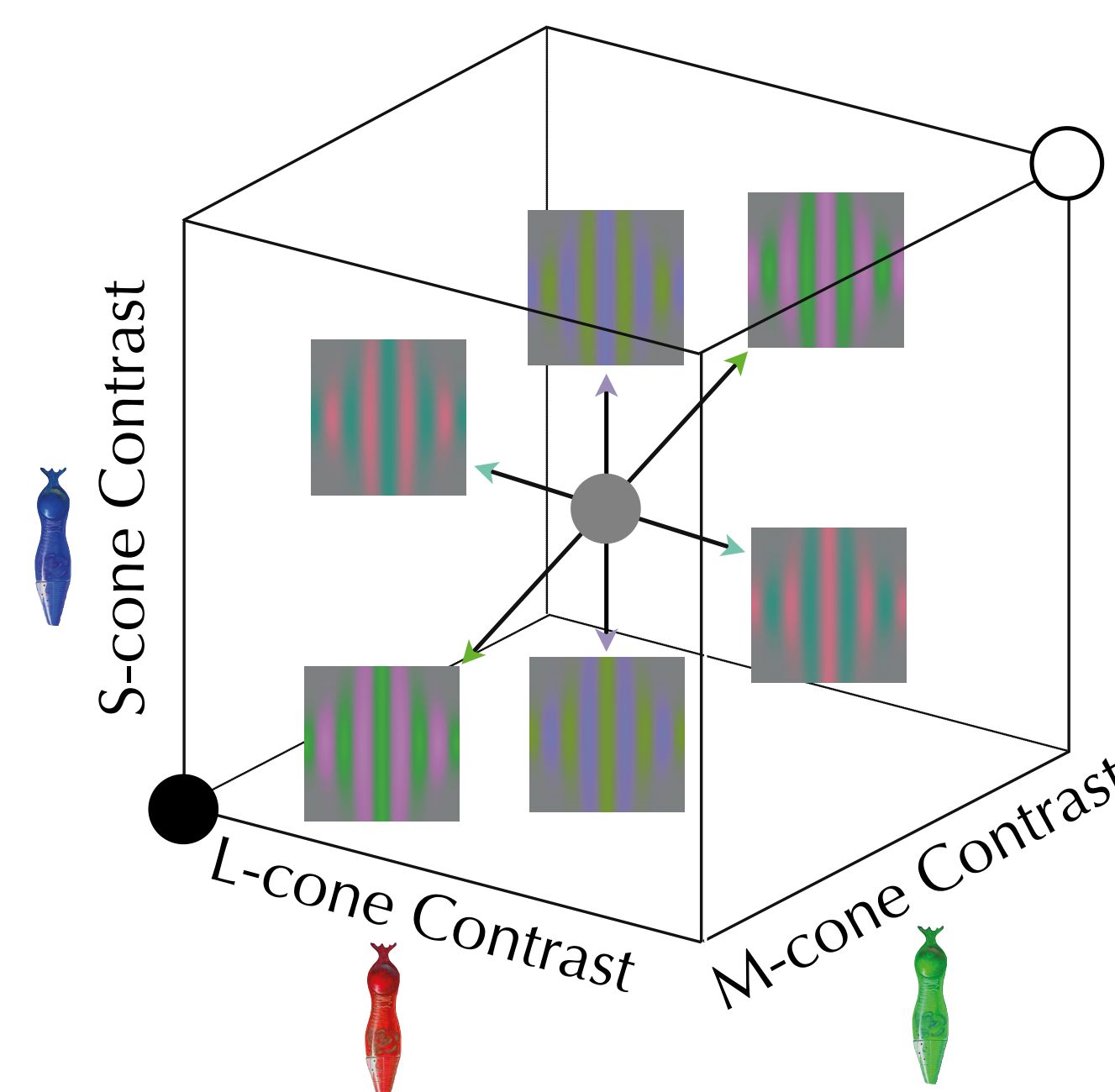
$$\arg \max_x \mathbb{E}_{p(r|x, \mathcal{D})} [I(r; f|x, \mathcal{D})] = \arg \min_x \mathbb{E}_{p(r|x, \mathcal{D})} [H(f|\mathcal{D}, \{x, r\})]$$

$$\text{- reduction in entropy} = \mathbf{f}_{\text{map}}(x) \sigma_p^2(x) e^{\frac{\sigma_p^2(x)}{2}}$$

posterior variance of $\log f$

4. Experimental setup

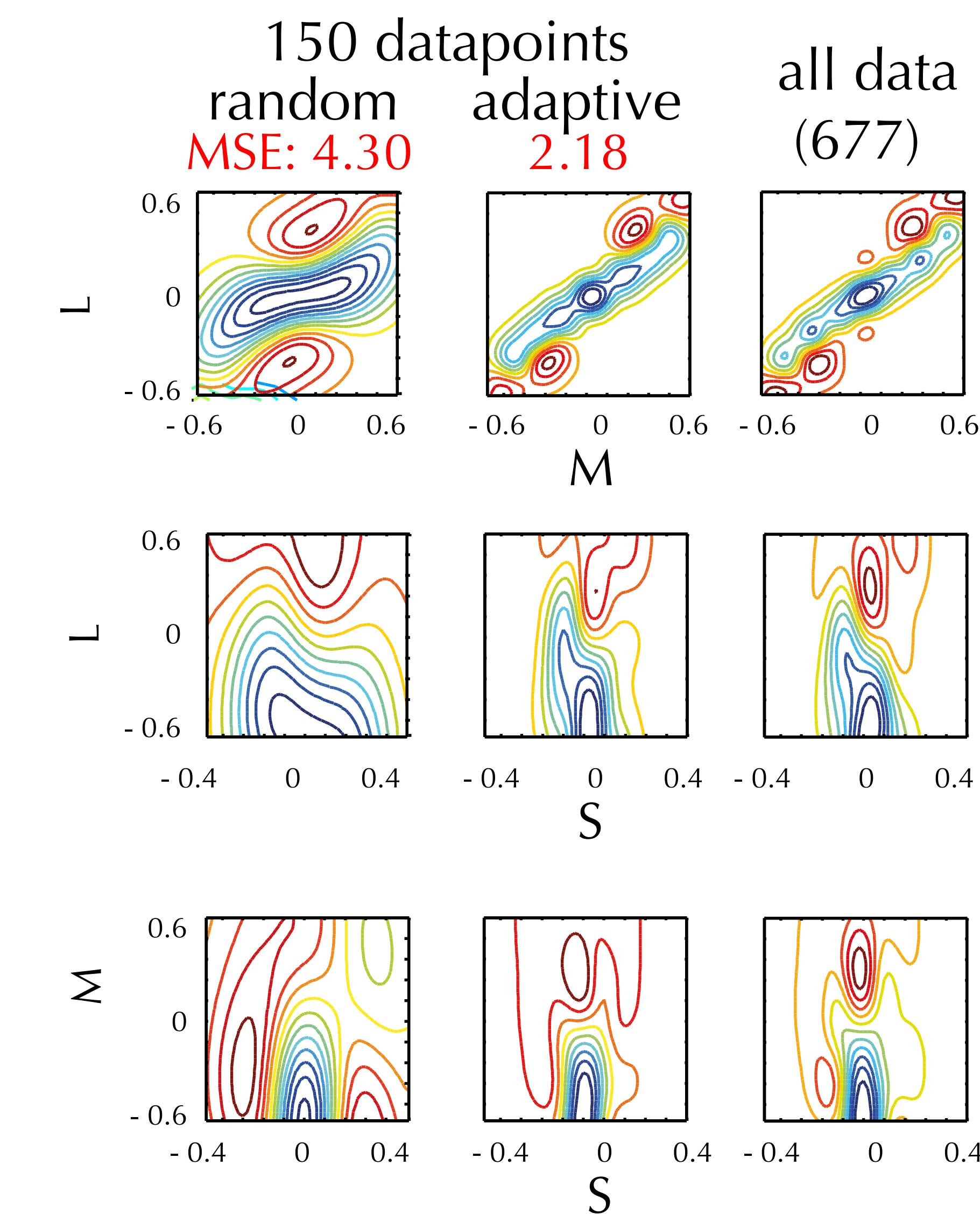
- color-tuned neurons in macaque V1
- spectrally-modulated Gabor stimuli



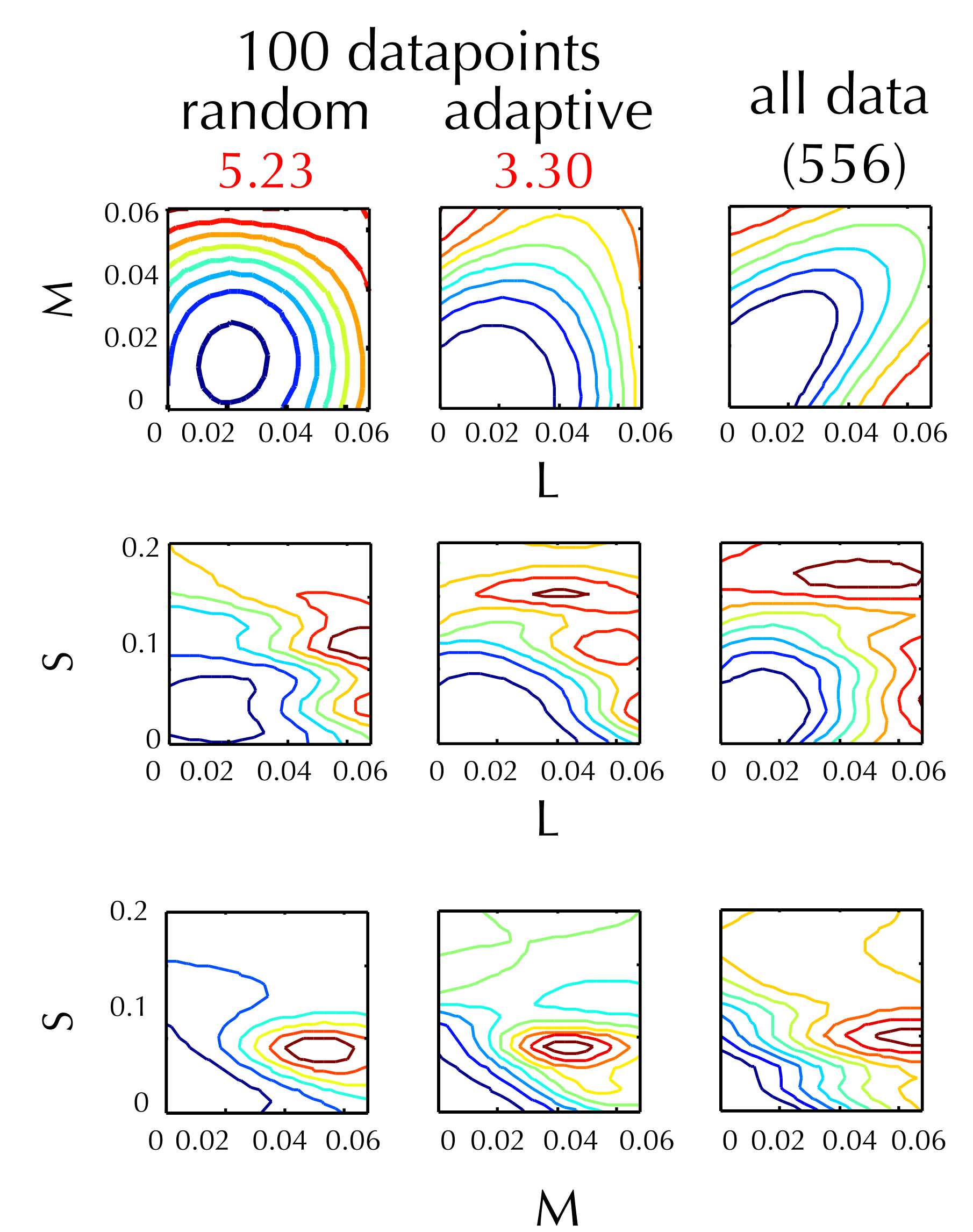
5. Results

- 2D slices of 3D nonlinearity

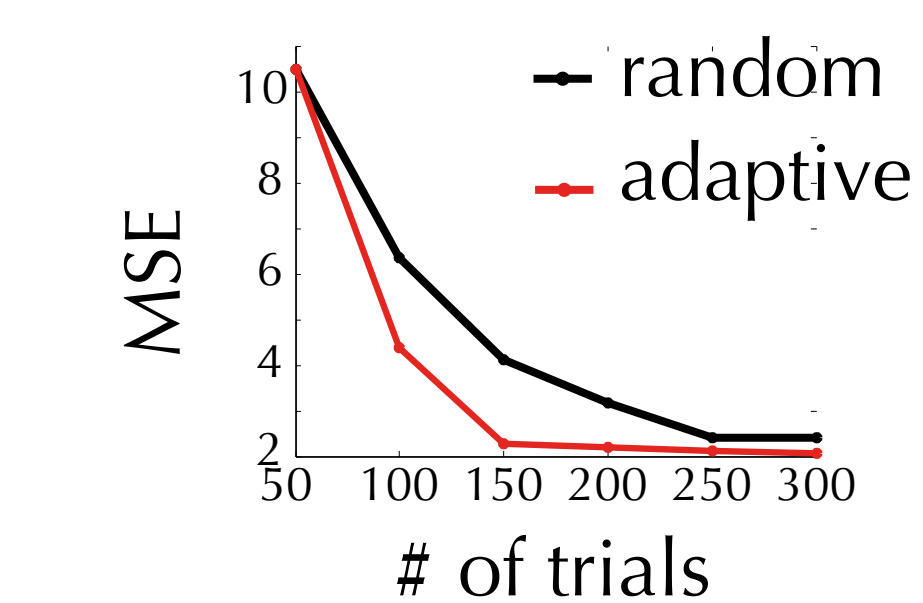
Cell1 :



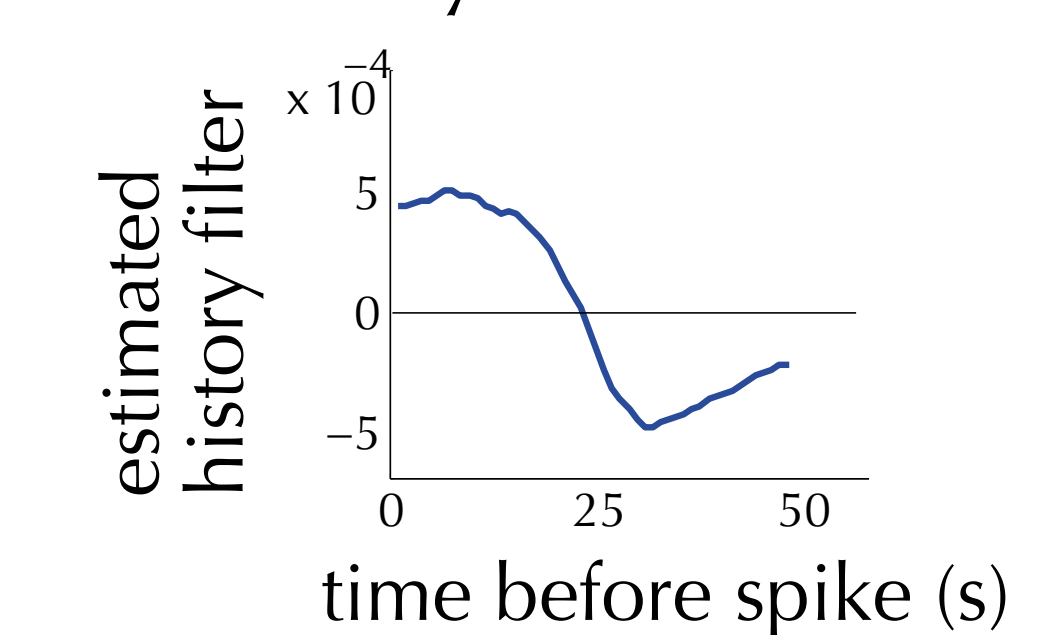
Cell2 :



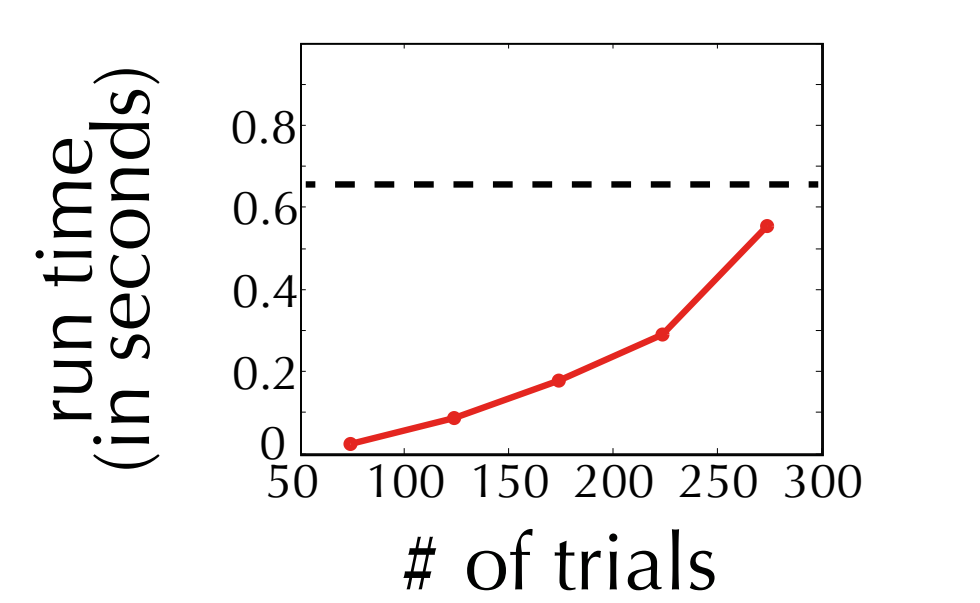
• MSE



• history effect



• run time



6. Conclusions

- flexible logGP-Poisson model for neural nonlinearities
- optimal design based on mutual information
- rapid learning of nonlinearities in closed-loop experiments

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