

## TRANSCENDENTAL EQUATIONS

### 1. BISECTION METHOD

**AIM: TO WRITE A PROGRAM IN PYTHON TO DEMONSTARTE BISECTION METHOD**

**PROGRAM:**

```
import math

# Evaluate the user-defined function safely
def f(x, func_str):
    try:
        return eval(func_str, {"x": x, "math": math, "_builtins_": None})
    except Exception as e:
        print("Error evaluating function:", e)
    return None

# Bisection Method
def bisection(func_str, a, b, tol):
    if f(a, func_str) * f(b, func_str) >= 0:
        print("Invalid interval. f(a) and f(b) must have opposite signs.")
        return
    print("Iter\t a\t b\t Xr\t f(Xr)")

    iter = 1
    while (b - a) / 2 > tol:
        Xr = (a + b) / 2
        fx = f(Xr, func_str)
        print(f"{iter}\t{a:.3f}\t{b:.3f}\t{Xr:.3f}\t{fx:.3f}")
        if abs(fx) < tol:
```

```
break

if f(a, func_str) * fx < 0:
    b = Xr
else:
    a = Xr

iter += 1

print(f"\nApproximate root = {Xr:.3f} (correct to 3 decimal places)")

# === Main Program ===
print("== Bisection Method ==")

func_str = input("Enter the function f(x): ") # Example: x**3 - 4*x + 1
a = float(input("Enter the starting value a: ")) # Example: 0
b = float(input("Enter the ending value b: ")) # Example: 1
tol = 0.00003 # 3 decimal place accuracy

bisection(func_str, a, b, tol)
```

**18067****OUTPUT:**

```
==== Bisection Method ====
Enter the function f(x): x*x*x -4*x +1
Enter the starting value a: 1
Enter the ending value b: 2

Iter      a      b      Xr      f(x)
 1      1.000  2.000  1.500  -1.625
 2      1.500  2.000  1.750  -0.641
 3      1.750  2.000  1.875  0.092
 4      1.750  1.875  1.812  -0.296
 5      1.812  1.875  1.844  -0.107
 6      1.844  1.875  1.859  -0.009
 7      1.859  1.875  1.867  0.041
 8      1.859  1.867  1.863  0.016
 9      1.859  1.863  1.861  0.003
10      1.859  1.861  1.860  -0.003
11      1.860  1.861  1.861  0.000
12      1.860  1.861  1.861  -0.001
13      1.861  1.861  1.861  -0.001
14      1.861  1.861  1.861  -0.000
15      1.861  1.861  1.861  0.000

Approximate root = 1.861 (correct to 3 decimal places)
```

**18067****2. REGULAR FALSI**

**Q. WRITE A PROGRAM IN PYTHON TO DEMONSTRATE REGULAR FALSI METHOD**

**AIM:** TO WRITE A PROGRAM IN PYTHON TO DEMONSTRATE NEWTON RAPHSON METHOD

## PROGRAM:

```
import math

# Evaluate the user-defined function safely

def safe_eval(expr, x):

    try:

        return eval(expr.strip(), {"x": x, "math": math, "m": math, "__builtins__": None})

    except (NameError, TypeError, ZeroDivisionError, SyntaxError) as e:

        print(f"Error evaluating function: {e}")

    return None
```

```
def Regula_Falsi(Func_str, a, b, tol):
```

```
    Fa = safe_eval(Func_str, a)

    Fb = safe_eval(Func_str, b)
```

```
    if Fa is None or Fb is None:
```

```
        return None
```

```
    if Fa * Fb >= 0:
```

```
        print("Invalid interval. F(a) and F(b) must have opposite signs.")
```

```
        return None
```

```
    print("\nIter.\t a\t b\t F(a)\t F(b)\t Xr\t F(Xr)")

    X_old = a # Initial guess to calculate error if needed
```

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```
for i in range(1, 101):

    # Regula Falsi Formula

    Xr = (a * Fb - b * Fa) / (Fb - Fa)

    FXr = safe_eval(Func_str, Xr)
```

```

print(f"\n{i:<6}\t{a:.4f}\t{b:.4f}\t{Fa:.4f}\t{Fb:.4f}\t{Xr:.4f}\t{FXr:.4f}")

if abs(FXr) < tol:
    return Xr

if Fa * FXr < 0:
    b = Xr
    Fb = FXr
else:
    a = Xr
    Fa = FXr

print(f"\nRoot not found within 100 iterations (Current error: {abs(FXr):.6f})")
return Xr

print("## Regula Falsi Method ##")

# Example: "x*x - 4*x - 4"
# Example: "m.cos(x) - x"
# Example: "x**3 - x - 1"
# Example: "x*x*x - 4*x - 4"

Func_str = input("Enter the function f(x): ")
a = float(input("Enter the starting value a: "))
b = float(input("Enter the starting value b: "))

tol = float(input("Enter the tolerance value: "))
root = Regula_Falsi(Func_str, a, b, tol)

if root is not None:
    print(f"\nApproximate root = {root:.3f} (correct to 3 decimal places)")

```

**OUTPUT:**

```
==== Regula Falsi Method ====
Enter the function f(x): x*x*x -4*x +1
Enter the starting value a: 1
Enter the ending value b: 2

Iter      a        b        f(a)      f(b)      Xr      f(Xr)
1      1.0000  2.0000  -2.0000  1.0000  1.6667  -1.0370
2      1.6667  2.0000  -1.0370  1.0000  1.8364  -0.1528
3      1.8364  2.0000  -0.1528  1.0000  1.8581  -0.0175
4      1.8581  2.0000  -0.0175  1.0000  1.8605  -0.0020
5      1.8605  2.0000  -0.0020  1.0000  1.8608  -0.0002
6      1.8608  2.0000  -0.0002  1.0000  1.8608  -0.0000

Approximate root = 1.8608 (correct to 3 decimal places)
```

**CONCLUSION:** The above program has been executed successfully.

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### 3. NEWTON'S RAPHSON METHOD

**Q. WRITE A PROGRAM IN PYTHON TO DEMONSTRATE NEWTON RAPHSON METHOD**

**AIM:** TO WRITE A PROGRAM IN PYTHON TO DEMONSTRATE NEWTON RAPHSON METHOD

## **PROGRAM:**

## Import math

```
# Safely evaluate the user-defined function

def safe_eval(expr, x):
    try:
        return eval(expr.strip(), {"x": x, "math": math, "__builtins__": None})
    except (NameError, TypeError, ZeroDivisionError, SyntaxError) as e:
        print(f"Error evaluating function: {e}")
    return None
```

# Safely evaluate the derivative of the function

```
def df(x, deriv_str):  
    try:  
        return eval(deriv_str.strip(), {"x": x, "math": math, "__builtins__": None})  
  
    except Exception as e:  
        print(f"Error evaluating derivative: {e}")  
  
    return None
```

```
def Newton_Raphson_Method(func_str, deriv_str, x0, tol, max_iter=100):
```

$$a_i = x_0$$

```
print("\nIter.\t ai\t f(ai)\t df(ai)\t ai+1")
```

```
for i in range(1, max_iter + 1):
    fai = safe_eval(func_str, ai)
    dfai = df(ai, deriv_str)
    if dfai == 0:
```

```

print("Derivative is zero. Method fails.")

return None

# Newton-Raphson Formula
ai_p1 = ai - fai / dfai

print(f"\n{i:<6}\t{ai:.4f}\t{fai:.4f}\t{dfai:.4f}\t{ai_p1:.4f}")

if abs(ai_p1 - ai) < tol:
    print(f"\nApproximate root = {ai_p1:.3f} (correct to 3 decimal places)")

    return ai_p1

ai = ai_p1

print("\nMaximum iterations reached without convergence.")

return ai_p1

```

```

import math

print("## Newton-Raphson Method ##")

# Example 1: "x*x - 4*x - 4"
# Example 2: "m.cos(x) - x"
# Example 3: "x**3 - x - 1"
# Example of derivative: "3*x*x - 1" for f(x)=x**3 - x - 1

```

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```

func_str = input("Enter the function f(x): ")
deriv_str = input("Enter the derivative df(x): ")
x0 = float(input("Enter the initial guess x0: "))

```

```
tol = float(input("Enter the tolerance for X decimal place accuracy: "))
```

```
newton_raphson(func_str, deriv_str, x0, tol)
```

**OUTPUT:**

```
==== Newton-Raphson Method ====
Enter the function f(x): x*x*x -2*x -5
Enter the derivative f'(x): 3*x*x -2
Enter the initial guess x0: 2

===== Newton-Raphson Iteration Table =====
Iter   x0          f(x0)        f'(x0)       x1
-----
1     2.000000    -1.000000    10.000000   2.100000
2     2.100000     0.061000    11.230000   2.094568
3     2.094568     0.000186    11.161647   2.094551
=====
Approximate root = 2.0946 (correct to 3 decimal places)
```

**CONCLUSION:**

The above program has been executed successfully.

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**INTERPOLATION**

**Q. WRITE A PROGRAM IN PYTHON TO DEMONSTRATE NEWTON FORWARD  
INTERPOLATION.**

**AIM: TO WRITE A PROGRAM IN PYTHON TO DEMONSTRATE NEWTON FORWARD INTERPOLATION.**

**PROGRAM:**

```
def forward_difference_table(x, y):
    n = len(y)
    diff_table = [y.copy()] # First row is just y values

    # Generate the forward difference table
    for i in range(1, n):
        row = []
        for j in range(n - i):
            # Calculate the i-th difference: diff(j) = diff(j+1) - diff(j)
            value = diff_table[i-1][j+1] - diff_table[i-1][j]
            row.append(value)
        diff_table.append(row)
    return diff_table

def display_table(x, diff_table):
    n = len(x)
    print("\nForward Difference Table:")
    header = "i\t x\t\t y" + "\t\t Δy" * (n - 1)
    print(header)
    print("-" * len(header) * 2) # For visual separation
    for i in range(n):
```

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```
row = [str(i), f"{x[i]:.2f}", f"{diff_table[0][i]:.2f}"]

# Add the differences
for j in range(1, n - i):
    row.append(f"{diff_table[j][i]:.2f}")
```

```

print("\t".join(row))

def main():
    n = int(input("Enter the number of data points: "))

    x = []
    y = []

    print("Enter x values (equally spaced):")

    for i in range(n):
        x.append(float(input(f"x[{i}] = ")))

    print("Enter corresponding y values:")

    for i in range(n):
        y.append(float(input(f"y[{i}] = ")))

    # Check equal spacing

    h_values = []
    for i in range(n - 1):
        h_values.append(x[i+1] - x[i])

    # Check if all h values are approximately equal

    if not all(abs(h_values[i] - h_values[0]) < 1e-5 for i in range(n - 1)):
        print("\nError: X values are not equally spaced.")

    return

diff_table = forward_difference_table(x, y)
display_table(x, diff_table)

if __name__ == "__main__":
    main()

```

**Forward Difference Table:**

| x     | $\Delta^0y$ | $\Delta^1y$ | $\Delta^2y$ | $\Delta^3y$ | $\Delta^4y$ | $\Delta^5y$ | $\Delta^6y$ | $\Delta^7y$ | $\Delta^8y$ |
|-------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|
| -1.00 | -13.00      | 6.00        | 0.00        | 6.00        | 0.00        | 0.00        | 0.00        | 0.00        | 0.00        |
| 0.00  | -7.00       | 6.00        | 6.00        | 6.00        | 0.00        | 0.00        | 0.00        | 0.00        |             |
| 1.00  | -1.00       | 12.00       | 12.00       | 6.00        | 0.00        | 0.00        | 0.00        |             |             |
| 2.00  | 11.00       | 24.00       | 18.00       | 6.00        | 0.00        | 0.00        |             |             |             |
| 3.00  | 35.00       | 42.00       | 24.00       | 6.00        | 0.00        |             |             |             |             |
| 4.00  | 77.00       | 66.00       | 30.00       | 6.00        |             |             |             |             |             |
| 5.00  | 143.00      | 96.00       | 36.00       |             |             |             |             |             |             |
| 6.00  | 239.00      | 132.00      |             |             |             |             |             |             |             |
| 7.00  | 371.00      |             |             |             |             |             |             |             |             |

**CONCLUSION:**

**THE ABOVE PROGRAM HAS BEEN EXECUTED SUCCESSFULLY**

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**Q. WRITE A PROGRAM IN PYTHON TO DEMONSTRATE NEWTON BACKWARD INTERPOLATION.**

**AIM: TO WRITE A PROGRAM IN PYTHON TO DEMONSTRATE NEWTON BACKWARD INTERPOLATION.**

## **PROGRAM:**

```
import math
```

**x = [0, 30, 60, 90]**

$$\mathbf{y} = [1, 0.85, 0.5, 0]$$

$$xp = 70$$

$$h = x[1] - x[0]$$

$$p = (xp - x[-1]) / h$$

$$dy1\_3 = y[3] - y[2]$$

$$dy1\_2 = y[2] - y[1]$$

$$d^2y^2 = dy_1 \cdot 3 - dy_1 \cdot 2$$

$$d^2y_1 = dy_1 \cdot 2 - dy_1 \cdot 1$$

$$d3y1 = d2y2 - d2y1$$

```
print("x\t y\t \n y\t \n\n y\t \n\n\n y")
```

```
print(f"{x[0]}\t{y[0]}")
```

```
print(f"\t{x[1]}\t{y[1]}\t{dy1_1:.4f}")
```

```
print(f"{{x[2]}\t {y[2]}\t {dy1_2:.4f}\t {d2y1:.4f}}")  
print(f"{{x[3]}\t {y[3]}\t {dy1_3:.4f}\t {d2y2:.4f}\t {d3y1:.4f}}")  
  
yp = (y[-1]  
      + p * dy1_3  
      + (p * (p + 1) / math.factorial(2)) * d2y2  
      + (p * (p + 1) * (p + 2) / math.factorial(3)) * d3y1)
```

```
print(f"\nEstimated cos(70°) using Backward formula = {yp:.5f}")
```

#### OUTPUT:

| x  | y    | $\nabla y$ | $\nabla^2 y$ | $\nabla^3 y$ |
|----|------|------------|--------------|--------------|
| 0  | 1    |            |              |              |
| 30 | 0.85 | -0.1500    |              |              |
| 60 | 0.5  | -0.3500    | -0.2000      |              |
| 90 | 0    | -0.5000    | -0.1500      | 0.0500       |

Estimated cos(70°) using Backward formula = 0.34753

#### CONCLUSION:

THE ABOVE PROGRAM HAS BEEN EXECUTED SUCCESSFULLY.

## CURVE FITTING

### 1. STRAIGHT LINE

#### PROGRAM:

```
# Curve_fit_no_numpy.py
# Least-squares straight-line fit (no numpy, no pandas)

from typing import List, Optional, Tuple

def fit_line(x_values: List[float], y_values: List[float]) -> Tuple[float, float]:
    """Return (a0, a1) for best fit line y = a0 + a1*x using least squares."""
    if len(x_values) != len(y_values) or len(x_values) == 0:
        raise ValueError("x_values and y_values must have same non-zero length.")
    n = len(x_values)
    sum_x = sum(x_values)
    sum_y = sum(y_values)
    sum_x2 = sum(x * x for x in x_values)
    sum_xy = sum(x * y for x, y in zip(x_values, y_values))

    denom = n * sum_x2 - sum_x * sum_x
    if abs(denom) < 1e-12:
        raise ValueError("Denominator nearly zero: can't compute unique fit (collinear x?).")

    a1 = (n * sum_xy - sum_x * sum_y) / denom
    a0 = (sum_y - a1 * sum_x) / n
    return a0, a1

def print_table(x_values: List[float], y_values: List[float]) -> None:
    """Print table of x, y, x^2, x*y and the sums."""
    n = len(x_values)
    rows = []
    for x, y in zip(x_values, y_values):
        rows.append((x, y, x*x, x*y))

    # Column widths
    w = [8, 8, 10, 10]
    header = f"{'i':<{w[0]}} {'y':<{w[1]}} {'x^2':<{w[2]}} {'x*y':<{w[3]}}"
    print(header)
    print("*" * (sum(w) + 3))

    for r in rows:
        print(f"{'r[0]:<{w[0]}.4g} {'r[1]:<{w[1]}.4g} {'r[2]:<{w[2]}.4g} {'r[3]:<{w[3]}.4g}'")
```

```

sum_x = sum(r[0] for r in rows)
sum_y = sum(r[1] for r in rows)
sum_x2 = sum(r[2] for r in rows)
sum_xy = sum(r[3] for r in rows)

# print the sums
print("-" * (sum(w) + 3))
print(f"{'SUM':<{w[0]} {sum_y:>{w[1]}.4g} {sum_x2:>{w[2]}.4g} {sum_xy:>{w[3]}.4g}"})
print()

# The image shows extra print statements for the sums:
print(f"{'SUM_X':<{w[0]} {sum_y:>{w[1]}.4g} {sum_x2:>{w[2]}.4g} {sum_xy:>{w[3]}.4g}"")
print() # extra line break from image 1000040410.jpg

print(f"\Sigma x = {sum_x:.4g}, \Sigma y = {sum_y:.4g}, \Sigma x^2 = {sum_x2:.4g}, \Sigma xy = {sum_xy:.4g}")
print()

def predict(a0: float, a1: float, x: float) -> float:
    return a0 + a1 * x
def interactive():
    print("Curve fitting (straight line) - enter data points.")
    n = int(input("How many points? "))
    x_values = []
    y_values = []

    for i in range(n):
        raw = input(f"Point {i+1} as 'x y' (e.g. 2 5): ").strip().split()
        if len(raw) < 2:
            print("Invalid input, try again.")
            return
        x_values.append(float(raw[0]))
        y_values.append(float(raw[1]))

    print()
    print_table(x_values, y_values)
    a0, a1 = fit_line(x_values, y_values)

    print(f"Best fit line: y = ({a0:.6f}) + ({a1:.6f}) x")

    choice = input("Predict y for some x? (y/n): ").strip().lower()
    if choice and choice[0] == 'y':

```

```

xv = float(input("Enter x: "))

print(f"Predicted y = {predict(a0, a1, xv):.6f}")
if __name__ == "__main__":
    # Example usage (change values directly if you prefer):
    x_values = [0, 2, 5, 7]
    y_values = [-1, 5, 12, 20]

    # Print table and compute
    print_table(x_values, y_values)
    a0, a1 = fit_line(x_values, y_values)

    print(f"Best fit line: y = {a0:.6f} + ({a1:.6f}) x")
    print(f"For x=0, predicted y = {predict(a0, a1, 0):.6f}")

```

**OUTPUT:**

| x        | y  | $x^2$ | $x*y$ |
|----------|----|-------|-------|
| 0        | -1 | 0     | 0     |
| 2        | 5  | 4     | 10    |
| 5        | 12 | 25    | 60    |
| 7        | 20 | 49    | 140   |
| $\Sigma$ | 36 | 78    | 210   |

$\Sigma x = 14$ ,  $\Sigma y = 36$ ,  $\Sigma x^2 = 78$ ,  $\Sigma xy = 210$

Best fit line:  $y = -1.137931 + 2.896552 x$   
For  $x=8$ , predicted  $y = 22.034483$

**CONCLUSION: THE ABOVE PROGRAM HAS BEEN EXECUTED SUCCESSFULLY.**

## 2. 2 DEGREE POLYNOMIAL

### PROGRAM:

```
# quad_fit_no_numpy.py
# Fit quadratic y = a0 + a1*x + a2*x^2 using normal equations (no numpy, no pandas)
```

```
from typing import List, Tuple
```

```
def build_sums(x_values: List[float], y_values: List[float]) -> dict:
    """Calculates the necessary sums for the normal equations."""

```

```
s = {
    'n': 0.0,
    'sx': 0.0,
    'sx2': 0.0,
    'sx3': 0.0,
    'sx4': 0.0,
    'sy': 0.0,
    'sxy': 0.0,
    'sx2y': 0.0
}
```

```
for x, y in zip(x_values, y_values):
    s['n'] += 1
    s['sx'] += x
    s['sx2'] += x**2
    s['sx3'] += x**3
    s['sx4'] += x**4
    s['sy'] += y
    s['sxy'] += x * y
```

```

s['sx2y'] += (x**2) * y

return s

def print_table_and_sums(x_values: List[float], y_values: List[float]) -> None:
    """Prints the data points and the calculated sums in a formatted table."""

    # Header
    print(f"\t{'x':>8}\t{'y':>10}\t{'x^2':>12}\t{'x^3':>12}\t{'x^4':>12}\t{'x*y':>12}\t{'x^2*y':>12}")
    print("-" * 78) # Separator

    # Data rows
    for x, y in zip(x_values, y_values):
        print(f"\t{x:8.4g}\t{y:10.4g}\t{x*x:12.4g}\t{x*x*x:12.4g}\t{x*x*x*x:12.4g}\t{x*x*y:12.4g}\t{(x*x)*y:12.4g}")

    # Sums
    s = build_sums(x_values, y_values)
    print("-" * 78) # Separator
    print(f"\tn = {s['n']:3.4g}, sx = {s['sx']:12.4g}, sx2 = {s['sx2']:12.4g}, sx3 = {s['sx3']:12.4g}, sx4 = {s['sx4']:12.4g}")
    print(f"\tsy = {s['sy']:12.4g}, sxy = {s['sxy']:12.4g}, sx2y = {s['sx2y']:12.4g}")
    print()

def solve_3x3(A: List[List[float]], b: List[float]) -> List[float]:
    """
    Simple Gaussian elimination (in-place) to solve Ax = b for a 3x3 A.

    Returns the solution vector x.
    """

    # Make copies

```

```
M = [row[:] for row in A]
```

```
rhs = b[:]
```

```
n = 3
```

```
# Forward elimination
```

```
for k in range(n):
```

```
    # find pivot
```

```
    pivot = M[k][k]
```

```
# Check for singularity/pivot too small (1e-14 is a common threshold)
```

```
if abs(pivot) < 1e-14:
```

```
    # try to swap with a lower row
```

```
    for i in range(k + 1, n):
```

```
        if abs(M[i][k]) > 1e-14:
```

```
            M[k], M[i] = M[i], M[k]
```

```
            rhs[k], rhs[i] = rhs[i], rhs[k]
```

```
            pivot = M[k][k]
```

```
            break
```

```
if abs(pivot) < 1e-14:
```

```
    raise ValueError("Singular matrix in solve_3x3")
```

```
# normalize row k
```

```
for j in range(k, n):
```

```
    M[k][j] /= pivot
```

```
    rhs[k] /= pivot
```

```
    # eliminate
```

```
    for i in range(k + 1, n):
```

```

factor = M[i][k]
for j in range(k, n):
    M[i][j] -= factor * M[k][j]
    rhs[i] -= factor * rhs[k]

# Back substitution
x = [0.0] * n
for i in range(n - 1, -1, -1):
    val = rhs[i]
    for j in range(i + 1, n):
        val -= M[i][j] * x[j]

# The diagonal element M[i][i] should be 1.0 from normalization,
# but we check for singularity one last time just in case.
x[i] = val / M[i][i] if abs(M[i][i]) > 1e-14 else val

return x

def fit_quadratic(x_values: List[float], y_values: List[float]) -> Tuple[float, float, float]:
    """Calculates the coefficients (a0, a1, a2) for the least-squares quadratic fit."""

    if len(x_values) != len(y_values) or len(x_values) == 0:
        raise ValueError("X-values and Y-values must have same non-zero length.")

    s = build_sums(x_values, y_values)

    # Normal equations matrix for [a0, a1, a2]
    # [ n  Σx  Σx^2 ] [a0] = [ Σy ]
    # [ Σx  Σx^2 Σx^3 ] [a1] = [ Σxy ]

```

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```
# [ Σx ^2 Σx^3 Σx^4 ] [a2] = [ Σxy ]  
A = [  
    [s['n'], s['sx'], s['sx2']],  
    [s['sx'], s['sx2'], s['sx3']],  
    [s['sx2'], s['sx3'], s['sx4']]  
]  
  
b = [s['sy'], s['sxy'], s['sx2y']]
```

```
# Solve for a0, a1, a2  
a0, a1, a2 = solve_3x3(A, b)  
  
return a0, a1, a2
```

```
def predict(a0: float, a1: float, a2: float, x: float) -> float:  
    """Calculates the predicted y value for a given x using the fitted quadratic."""  
    return a0 + a1*x + a2*(x**2)
```

```
if __name__ == "__main__":  
    # Example points from your notebook: (0, 1), (1, 6), (2, 17)  
    x_values = [0.0, 1.0, 2.0]  
    y_values = [1.0, 6.0, 17.0]
```

```
print("### Input Data and Sums ###")  
print_table_and_sums(x_values, y_values)  
# Fit quadratic  
a0, a1, a2 = fit_quadratic(x_values, y_values)
```

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```
print("### Fitting Results ###")  
print(f"Fitted quadratic: y = {a0:.6f} + {a1:.6f} x + {a2:.6f} x^2")
```

```
# Predictions requested in the notebook  
print("\n### Predictions ###")
```

```
# Prediction for x=1.6  
print(f"y(1.6) = {predict(a0, a1, a2, 1.6):.6f}")
```

```
# Prediction for x=3.0  
print(f"y(3) = {predict(a0, a1, a2, 3.0):.6f}")
```

## OUTPUT:

| x        | y  | x^2 | x^3 | x^4 | x*y | x^2*y |
|----------|----|-----|-----|-----|-----|-------|
| 0        | 1  | 0   | 0   | 0   | 0   | 0     |
| 1        | 6  | 1   | 1   | 1   | 6   | 6     |
| 2        | 17 | 4   | 8   | 16  | 34  | 68    |
| $\Sigma$ | 24 | 5   | 9   | 17  | 40  | 74    |

$\Sigma x = 3.0$ ,  $\Sigma y = 24.0$ ,  $\Sigma x^2 = 5.0$ ,  $\Sigma x^3 = 9.0$ ,  $\Sigma x^4 = 17.0$   
 $\Sigma (xy) = 40.0$ ,  $\Sigma (x^2 y) = 74.0$

Fitted quadratic:  $y = 1.000000 + 2.000000 x + 3.000000 x^2$   
 $y(1.6) = 11.880000$   
 $y(3) = 34.000000$

## CONCLUSION:

THE ABOVE PROGRAM HAS BEEN EXECUTED SUCCESSFULLY.

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**SOLUTION OF SIMULTANEOUS ALGEBRAIC EQUATIONS****GUASSIAN ELIMINATION METHOD****AIM: TO WRITE A PROGRAM IN PYTHON TO DEMONSTRATE GUASSIAN ELIMINATION METHOD****PROGRAM:**

#Gaussian elimination with partial pivoting row operations

# Solve the system:

#  $x_1 + 10x_2 - x_3 = 3$ #  $2x_1 + 3x_2 + 20x_3 = 7$ #  $10x_1 - x_2 + 2x_3 = 4$ 

# Augmented matrix (each row: [a11, a12, a13, b])

```
A = [  
    [1.0, 10.0, -1.0, 3.0],  
    [2.0, 3.0, 20.0, 7.0],  
    [10.0, -1.0, 2.0, 4.0]  
]
```

```
n = len(A) # Number of equations/variables (n=3)
```

```
def print_matrix(M: List[List[float]], msg=None) -> None:
```

```
    """Prints the augmented matrix with 10.6f formatting."""
```

```
    if msg:
```

```
        print(msg)
```

```
    for r in M:
```

```
        # Join values with spaces, formatting each to 10 characters with 6 decimal places
```

```
print("[" + " ".join(f"{{val:.6f}" for val in r}) + "]")  
print()
```

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```
def swap_rows(M: List[List[float]], i: int, j: int) -> None:  
    """Swaps row i and row j in matrix M and prints the operation."""  
  
    M[i], M[j] = M[j], M[i]  
  
    # Print R(i+1) <-> R(j+1) to use 1-based indexing for output  
  
    print(f"R({{i+1}}) <-> R({{j+1}})")  
  
    print_matrix(M)  
  
  
def scale_and_add(M: List[List[float]], col: int, factor: float, row: int) -> None:  
    """  
    Performs R_dest = R_dest - k * R_src.  
    In the context of elimination, row is dest (row to eliminate in), col is src.  
    """  
  
    n_cols = len(M[0])  
  
  
    # Print R(dest+1) <- R(dest+1) - (k) * R(src+1) to use 1-based indexing  
    print(f"R({{row+1}}) <- R({{row+1}}) - {{factor:.6f}}*R({{col+1}})")  
  
  
    # Perform the operation: M[row] = M[row] - factor * M[col]  
    for c in range(n_cols):  
  
        M[row][c] = M[row][c] - factor * M[col][c]  
  
  
    print_matrix(M)  
  
  
# --- Main Solution Logic ---  
  
# Work on a copy of the augmented matrix  
M = deepcopy(A)
```

```
print_matrix(M, "Initial augmented matrix [A | b]:")
```

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```
for col in range(n):
    # Partial pivot: find row with max abs value in column 'col' from rows col..n-1
    # max() returns the row index 'r'
    pivot_row = max(range(col, n), key=lambda r: abs(M[r][col]))

    if pivot_row != col:
        swap_rows(M, pivot_row, col)

    pivot = M[col][col]

    if abs(pivot) < 1e-12: # Check for near-zero pivot (singularity)
        raise ValueError("Zero pivot encountered")

    # Eliminate below
    for row in range(col + 1, n):
        factor = M[row][col] / pivot
        # scale_and_add(Matrix, source_row, factor, destination_row)
        scale_and_add(M, col, factor, row)

    print("Upper-triangular matrix after forward elimination:")
    print_matrix(M)

# Back substitution
x = [0.0] * n # Solution vector [x1, x2, x3]

# Loop backward from the last row (n-1) to the first row (0)
for i in range(n - 1, -1, -1):
```

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```
# s is the RHS (augmented column), which is M[i][n]
s = M[i][n]

# Subtract known x[j]'s multiplied by their coefficients M[i][j]
for j in range(i + 1, n):
    s -= M[i][j] * x[j]

# Solve for x[i]
x[i] = s / M[i][i]

# Print Solution vector
print("Solution vector:")

# Enumerate x starting from 1 for x1, x2, x3 display
for i, xi in enumerate(x, 1):
    print(f"x{i} = {xi:.8f}")
```

**OUTPUT:**

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```
Initial augmented matrix [A | b]:
[ 1.000000 10.000000 -1.000000 3.000000]
[ 2.000000 3.000000 20.000000 7.000000]
[ 10.000000 -1.000000 2.000000 4.000000]

R3 <-> R1
[ 10.000000 -1.000000 2.000000 4.000000]
[ 2.000000 3.000000 20.000000 7.000000]
[ 1.000000 10.000000 -1.000000 3.000000]

R2 = R2 - (0.200000)*R1
[ 10.000000 -1.000000 2.000000 4.000000]
[ 0.000000 3.200000 19.600000 6.200000]
[ 1.000000 10.000000 -1.000000 3.000000]

R3 = R3 - (0.100000)*R1
[ 10.000000 -1.000000 2.000000 4.000000]
[ 0.000000 3.200000 19.600000 6.200000]
[ 0.000000 10.100000 -1.200000 2.600000]

R3 <-> R2
[ 10.000000 -1.000000 2.000000 4.000000]
[ 0.000000 10.100000 -1.200000 2.600000]
[ 0.000000 3.200000 19.600000 6.200000]

R3 = R3 - (0.316832)*R2
[ 10.000000 -1.000000 2.000000 4.000000]
[ 0.000000 10.100000 -1.200000 2.600000]
[ 0.000000 0.000000 19.980198 5.376238]

Upper-triangular matrix after forward elimination:
[ 10.000000 -1.000000 2.000000 4.000000]
[ 0.000000 10.100000 -1.200000 2.600000]
[ 0.000000 0.000000 19.980198 5.376238]

Solution vector:
x1 = 0.37512389
x2 = 0.28939544
x3 = 0.26907830
```

## **CONCLUSION:**

**THE ABOVE PROGRAM HAS BEEN EXECUTED SUCCESSFULLY.**

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## NUMERICAL SOLUTIONS OF FIRST AND SECOND ORDER DIFFERENTIAL EQUATIONS

### 1. TAYLOR SERIES

**AIM: TO WRITE A PROGRAM IN PYTHON TO DEMONSTRATE TAYLOR SERIES**  
**PROGRAM:**

```
# Taylor_ode_no_sympy.py

# Compute y(n0 + h) using Taylor series for ODE dy/dn = n - y^2, y(n0)=y0

# No external libraries beyond 'math'

from math import factorial

def compute_derivatives_at(n0: float, y0: float) -> List[float]:
    """
    Compute derivatives y', y'', y''', y^(4), y^(5) at (n0, y0)
    using formulas obtained by differentiating dy/dn = n - y^2.

    Returns list [y0, y1, y2, y3, y4, y5], where yk is the kth derivative.
    """

    # y^(0) = y0
    y_0 = y0

    # y' = n - y^2
    y_1 = n0 - (y_0 ** 2)

    # Second derivative: y'' = d/dn(n - y^2) = 1 - 2*y*(dy/dn) = 1 - 2*y*y'
    y_2 = 1 - 2 * y_0 * y_1
```

$$y_2 = 1.0 - 2.0 * y_0 * y_1$$

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```
# Third derivative:  $y''' = d/dn(1 - 2*y*y') = 0 - 2 * [ y'*y' + y*y'' ]$ 
```

```
#  $y''' = -2*y'^2 - 2*y*y''$ 
```

```
y_3 = -2.0 * (y_1 ** 2) - 2.0 * y_0 * y_2
```

```
# Fourth derivative:  $y^{(4)} = d/dn(-2*y'^2 - 2*y*y'')$ 
```

```
#  $y^{(4)} = -2*(2*y'y'') - 2[y'*y'' + y*y''']$ 
```

```
#  $y^{(4)} = -4*y'*y'' - 2*y'*y'' - 2*y*y''' = -6*y'*y'' - 2*y*y'''$ 
```

```
y_4 = -2.0 * y_0 * y_3 - 6.0 * y_1 * y_2
```

```
# Fifth derivative:  $y^{(5)} = d/dn(-6*y'*y'' - 2*y*y''')$ 
```

```
#  $y^{(5)} = -6*[ y''y'' + y'*y'''] - 2[ y'*y''' + y*y^{(4)} ]$ 
```

```
#  $y^{(5)} = -6*y'^2 - 6*y'*y''' - 2*y'*y''' - 2*y*y^{(4)}$ 
```

```
#  $y^{(5)} = -2*y*y^{(4)} - 8*y'*y''' - 6*y'''^2$ 
```

```
y_5 = -2.0 * y_0 * y_4 - 8.0 * y_1 * y_3 - 6.0 * (y_2 ** 2)
```

```
return [y_0, y_1, y_2, y_3, y_4, y_5]
```

```
def taylor_at(n0: float, y0: float, h: float, order: int = 5) -> Tuple[float, List[float]]:
```

```
"""
```

Evaluate Taylor polynomial of given order (<=5) for y at n0+h.

Returns (approx\_value, derivatives\_list).

```
"""
```

```
if order > 5:
```

```
    raise ValueError("This implementation supports up to 5th derivative (order<=5).")
```

```
derivs = compute_derivatives_at(n0, y0)
```

```
# Build Taylor sum: y(n0+h) approx y(n0) + h*y'(n0)/1! + h^2*y''(n0)/2! + ...
```

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```
taylor_sum = 0.0

for k in range(order + 1):

    # Term = y^(k) * h^k / k!

    taylor_sum += derivs[k] * (h ** k) / factorial(k)

return taylor_sum, derivs

if __name__ == "__main__":

    # Initial point and step

    n0 = 0.0

    y0 = 1.0

    h = 0.1

    order = 5 # use terms up to y^(5)/5!

    # Compute the approximation and the derivatives

    approx, derivs = taylor_at(n0, y0, h, order)

    print("Derivatives at n0 = {:.4g}, y0 = {:.4g}: ".format(n0, y0))

    print(f"y'(0) = {derivs[1]:.6g}")

    print(f"y''(0) = {derivs[2]:.6g}")

    print(f"y'''(0) = {derivs[3]:.6g}")

    print(f"y^(4)(0) = {derivs[4]:.6g}")

    print(f"y^(5)(0) = {derivs[5]:.6g}")

    print()

    print("Taylor approximation up to order {}".format(order))

    print(f"y({n0 + h:.4g}) ≈ {approx:.10f}")

    print(f"Rounded to 4 decimal places: {approx:.4f}")
```

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**OUTPUT:**

---

Derivatives at n0 = 0, y0 = 1:

y(0) = 1  
y'(0) = -1  
y''(0) = 3  
y'''(0) = -8  
y^(4)(0)= 34  
y^(5)(0)= -186

Taylor approximation up to order 5:

y(0.1) ≈ 0.9137928333  
Rounded to 4 decimal places: 0.9138

**CONCLUSION:**

**THE ABOVE PROGRAM HAS BEEN EXECUTED SUCCESSFULLY.**

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## 2. EULER'S METHOD

**AIM: TO WRITE A PROGRAM IN PYTHON TO DEMONSTARTE EULER'S METHOD.**

**PROGRAM:**

```
# Euler_method.py

# Solve dy/dx = -y with y(0)=1 using Euler's method


def f(x, y):
    """The ODE: dy/dx = -y"""
    return -y

def euler(x0, y0, h, x_target):
    """Euler's method to approximate y(x_target)"""

    steps = int((x_target - x0) / h)

    x = x0
    y = y0

    print("Step | x | y ")
    print("----|----|----")
    print(f" 0 | {x:.2f} | {y:.6f}")

    for i in range(1, steps + 1):
        # Euler formula: y(i+1) = y(i) + h * f(x(i), y(i))
        y = y + h * f(x, y)
```

**x = x + h**

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```
print(f"{{i:3d} | {x:.2f} | {y:.6f}"
```

```
    return y
```

```
if __name__ == "__main__":
```

```
    # initial values
```

```
    x0 = 0.0
```

```
    y0 = 1.0
```

```
    h = 0.01
```

```
    x_target = 0.04
```

```
result = euler(x0, y0, h, x_target)
```

```
print(f"\nApproximate value at x={x_target:.2f}:", round(result, 6))
```

**OUTPUT:**

| Step |  | x    |  | y        |
|------|--|------|--|----------|
| 0    |  | 0.00 |  | 1.000000 |
| 1    |  | 0.01 |  | 0.990000 |
| 2    |  | 0.02 |  | 0.980100 |
| 3    |  | 0.03 |  | 0.970299 |
| 4    |  | 0.04 |  | 0.960596 |

```
Approximate value at x=0.04: 0.960596
```

**CONCLUSION: THE ABOVE PROGRAM HAS BEEN EXECUTED SUCCESSFULLY.**

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### 3.MODIFIED EULER'S METHOD

**AIM: TO WRITE A PROGRAM IN PYTHON TO DEMONSTRATE MODIFIED EULER'S METHOD**

**PROGRAM:**

```
# Modified_Euler's_Method.py

# Equation: dy/dx = x^2 + y, y(0) = 1
# Find y(0.2) with step size h = 0.02

def f(x, y):
    """The ODE: dy/dx = x^2 + y"""
    return x**2 + y

# Initial conditions
x0 = 0
y0 = 1
h = 0.02
x_end = 0.2

n = int((x_end - x0) / h) # Number of steps: (0.2 - 0) / 0.02 = 1

# Table header
print("-----")
print("i | x(i) | y(i) | f(x(i),y(i)) (f1) | y'(Pred) | f(x+h, y') (f2) | y(i+1)")
print("-----")

# Print initial condition (Step 0)
```

```
print(f"0:<2d} | {x0:10.6f} | {y0:10.6f} | {"20} | {"10} | {"20} | {"10}")
```

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```
# Iterative Modified Euler Calculation
```

```
# 1. Predictor (Standard Euler):  $y^* = y_i + h * f(x_i, y_i)$ 
```

```
f1 = f(x0, y0)
```

```
y_pred = y0 + h * f1
```

```
# 2. Corrector (Heun's Formula):  $y_{i+1} = y_i + (h / 2) * [ f(x_i, y_i) + f(x_{i+1}, y^*) ]$ 
```

```
x_next = x0 + h
```

```
f2 = f(x_next, y_pred)
```

```
y_next = y0 + (h / 2) * (f1 + f2)
```

```
# Print intermediate results for the current step (i+1)
```

```
print(f"i+1:<2d} | {x_next:10.6f} | {y0:10.6f} | {f1:20.6f} | {y_pred:10.6f} | {f2:20.6f} | {y_next:10.6f}")
```

```
# Update for next iteration
```

```
x0 = x_next
```

```
y0 = y_next
```

```
print("-----")
```

```
print(f"h = {h:.2f}, Number of steps = {n}")
```

```
print(f"Formula used:")
```

```
print(f"y*(i+1) = y_i + h * f(x_i, y_i) (Euler Predictor)")
```

```
print(f"y(i+1) = y_i + (h/2) * [ f(x_i, y_i) + f(x_i + h, y*(i+1)) ] (Heun Corrector)")
```

```
print(f"Approximate value of y({x_end:.1f}) = {y0:.6f}")
```

```
print("-----")
```

**18067****OUTPUT:**

| i | x(i)   | y(i)     | f(x(i),y(i)) | y* (Pred) | f(x+h, y*) | y(i+1)   |
|---|--------|----------|--------------|-----------|------------|----------|
| 0 | 0.0000 | 1.00000  | 1.000000     | 1.020000  | 1.020400   | 1.020204 |
| 1 | 0.0200 | 1.020204 | 1.020604     | 1.040616  | 1.042216   | 1.040832 |
| 2 | 0.0400 | 1.040832 | 1.042432     | 1.061681  | 1.065281   | 1.061909 |
| 3 | 0.0600 | 1.061909 | 1.065509     | 1.083220  | 1.089620   | 1.083461 |
| 4 | 0.0800 | 1.083461 | 1.089861     | 1.105258  | 1.115258   | 1.105512 |
| 5 | 0.1000 | 1.105512 | 1.115512     | 1.127822  | 1.142222   | 1.128089 |
| 6 | 0.1200 | 1.128089 | 1.142489     | 1.150939  | 1.170539   | 1.151219 |
| 7 | 0.1400 | 1.151219 | 1.170819     | 1.174636  | 1.200236   | 1.174930 |
| 8 | 0.1600 | 1.174930 | 1.200530     | 1.198941  | 1.231341   | 1.199249 |
| 9 | 0.1800 | 1.199249 | 1.231649     | 1.223882  | 1.263882   | 1.224204 |

h = 0.02, Number of steps = 10  
 Formula used:  
 $y_{(i+1)} = y_i + (h/2) * [f(x_i, y_i) + f(x_i + h, y^*)]$   
 Approximate value of y(0.2) = 1.224204

**CONCLUSION:****THE ABOVE PROGRAM HAS BEEN EXECUTED SUCCESSFULLY.**

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#### 4. RUNGE-KUTTA 4<sup>th</sup> ORDER METHOD

**AIM:** AIM: TO WRITE A PROGRAM IN PYTHON TO DEMONSTRATE RUNGE-KUTTA 4<sup>th</sup> ORDER METHOD

**PROGRAM:**

RK4 step-by-step for  $y' = x + y$ ,  $y(0)=1$

```
import math
```

```
def f(x, y):
```

```
    """The ODE:  $y' = x + y$ """
```

```
    return x + y
```

```
def exact_solution(x):
```

```
    """The exact solution of  $y' - y = x$  with  $y(0)=1$  is  $y = 2 * e^x - x - 1$ """
```

```
    return 2 * math.exp(x) - x - 1
```

```
# Initial values
```

```
x = 0.0
```

```
y = 1.0
```

```
h = 0.1
```

```
steps = int(0.2 / h) # Compute up to x = 0.2 (steps = 2)
```

```
print("Runge-Kutta 4th order (RK4) step-by-step")
```

```
print(f"Equation:  $y' = x + y$ ,  $y(0)={y}$ ")
```

```
print(f"Step | x_n | y_n (before) | k1 | k2 | k3 | k4 |  $y_{steps * h:.1f}$ ")
```

```
print("-" * 100)
```

for n in range(steps):

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# RK4 coefficients

k1 = f(x, y) \* h

k2 = f(x + h/2.0, y + (k1/2.0)) \* h

k3 = f(x + h/2.0, y + (k2/2.0)) \* h

k4 = f(x + h, y + k3) \* h

# RK4 Update Formula

increment = (h/6.0) \* (k1 + 2.0\*k2 + 2.0\*k3 + k4)

y\_next = y + increment

# Print step details

# Using 'n' for the step count (0 and 1) and 'n+1' for the y\_next index (1 and 2)

print(f"\{n+1:3d} | {x:6.3f} | {y:16.10f} | "

f"\{k1:7.6f} | {k2:7.6f} | {k3:7.6f} | {k4:7.6f} | {y\_next:10.9f}"")

# Update

x += h

x = round(x, 10) # avoid floating accumulation

y = y\_next

print("-" \* 100)

# Final output

exact\_y = exact\_solution(x)

absolute\_error = abs(y - exact\_y)

print(f"Final RK4 approximation: y({x:.3f}) = {y:.9f}")

print(f"Exact value : y({x:.3f}) = {exact\_y:.9f}")

print(f"Absolute error : |abs({absolute\_error:.12e})|")

**OUTPUT:**

Runge-Kutta 4th order (RK4) step-by-step

Equation:  $y' = x + y$ ,  $y(0)=1$ 

| Step | x_n   | y_n (before) | k1       | k2       | k3       | k4       | y_{n+1}     |
|------|-------|--------------|----------|----------|----------|----------|-------------|
| 1    | 0.000 | 1.0000000000 | 1.000000 | 1.100000 | 1.105000 | 1.210500 | 1.110341667 |
| 2    | 0.100 | 1.1103416667 | 1.210342 | 1.320859 | 1.326385 | 1.442900 | 1.242805142 |

Final RK4 approximation:  $y(0.200) = 1.242805142$   
Exact value :  $y(0.200) = 1.242805516$   
Absolute error :  $3.746189507492e-07$

**CONCLUSION: THE ABOVE PROGRAM HAS BEEN EXECUTED SUCCESSFULLY,**

## NUMERICAL INTEGRATION

### 1. TRAPEZOIDAL RULE

**AIM: TO WRITE A PROGRAM IN PYTHON TO DEMONSTRATE TRAPEZOIDAL RULE.**

#### PROGRAM:

```
# Trapezoidal Rule for I = integral(f(x) dx from 0 to 1) with 2 subintervals

def f(x):
    """The integrand: 1 / (1 + x^2)"""
    return 1 / (1 + x**2)

# Given limits
a = 0
b = 1
n = 2 # number of subintervals

# Step size
h = (b - a) / n

# Compute x values
x = [a + i * h for i in range(n + 1)] # [0.0, 0.5, 1.0]

# Compute f(x) values
f_values = [f(xi) for xi in x] # [1.0, 0.8, 0.5]

# Display table header
print("-----")
```

```
print("i | x(i) | f(x(i)) = 1/(1+x^2)")

print("-----")

# Display table values

for i in range(n + 1):

    print(f"{i:<3} | {x[i]:<8.4f} | {f_values[i]:<8.4f}")

print("-----")

# Apply Trapezoidal Rule

# The formula in Python: I = (h / 2) * (f[0] + 2 * sum(f[1:-1]) + f[-1])

I = (h / 2) * (f_values[0] + 2 * sum(f_values[1:-1]) + f_values[-1])

# Step-by-step explanation

print(f"h = (b - a) / n = ({b} - {a}) / {n} = {h}")

print("\nUsing Trapezoidal Rule:")

print(f"I = (h / 2) * [f(x0) + 2*f(x1) + f(x2)]")

print(f"I = ({h/2}) * [{f_values[0]:.4f} + 2*{f_values[1]:.4f} + {f_values[2]:.4f}]")

# Final result

print("\n-----")

print(f"Approximate value of the integral I = {I:.4f}")

print("-----")
```

**OUTPUT:**

| i | x(i)   | f(x(i)) = 1/(1+x^2) |
|---|--------|---------------------|
| 0 | 0.0000 | 1.0000              |
| 1 | 0.5000 | 0.8000              |
| 2 | 1.0000 | 0.5000              |

$$h = (b - a) / n = (1 - 0) / 2 = 0.5$$

Using Trapezoidal Rule:

$$I = (h/2) * [f(x_0) + 2*f(x_1) + f(x_2)]$$
$$I = (0.5/2) * [1.0000 + 2*0.8000 + 0.5000]$$

-----  
Approximate value of the integral I = 0.7750

**CONCLUSION: THE ABOVE PROGRAM HAS BEEN EXECUTED SUCCESSFULLY.**

## 2. SIMPSON'S 1/3 RULE

**AIM: AIM: TO WRITE A PROGRAM IN PYTHON TO DEMONSTRATE SIMPSON'S 1/3 RULE.**

**PROGRAM:**

```
# Simpson's 1/3 Rule for I = ∫(0 to 1) e^(-x^2) dx with n = 4
```

```
import math
```

```
# Define the function
```

```
def f(x):
```

```
    return math.exp(-x**2)
```

```
# Given values
```

```
a = 0 # lower limit
```

```
b = 1 # upper limit
```

```
n = 4 # number of subintervals (must be even)
```

```
# Step size
```

```
h = (b - a) / n
```

```
# Generate x and f(x) values
```

```
x = [a + i * h for i in range(n + 1)]
```

```
f_values = [f(xi) for xi in x]
```

```
# Display table
```

```
print("-----")
```

```
print(" i | x(i) | f(x(i)) = e^(-x^2)")
```

```
print("-----")
```

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```
for i in range(n + 1):
    print(f"\{i:<3\} | \{x[i]:<8.4f\} | \{f_values[i]:<10.6f\}")
    print("-----")

# Simpson's 1/3 rule computation

sum_odd = sum(f_values[i] for i in range(1, n, 2))
sum_even = sum(f_values[i] for i in range(2, n, 2))

I = (h / 3) * (f_values[0] + 4 * sum_odd + 2 * sum_even + f_values[-1])

# Show steps

print(f"\nh = (b - a) / n = (\{b\} - \{a\}) / \{n\} = \{h\}")
print("\nUsing Simpson's 1/3 Rule:")

print(f"I = (h/3) * [f(x0) + 4*(f(x1) + f(x3) + ...) + 2*(f(x2) + f(x4) + ...) + f(xn)]")
print(f"I = (\{h\}/3) * [\{f_values[0]:.6f\} + 4*\{\{sum_odd:.6f\}\} + 2*\{\{sum_even:.6f\}\} + \{f_values[-1]:.6f\}]")

# Display final result

print("-----")
print(f"Approximate value of the integral I = \{I:.6f\}")
print("-----")
```

**OUTPUT:**

| i | x(i)   | f(x(i)) = e^(-x^2) |
|---|--------|--------------------|
| 0 | 0.0000 | 1.000000           |
| 1 | 0.2500 | 0.939413           |
| 2 | 0.5000 | 0.778801           |
| 3 | 0.7500 | 0.569783           |
| 4 | 1.0000 | 0.367879           |

$h = (b - a) / n = (1 - 0) / 4 = 0.25$

Using Simpson's 1/3 Rule:

$$I = (h/3) * [f(x_0) + 4*(f(x_1) + f(x_3) + \dots) + 2*(f(x_2) + f(x_4) + \dots) + f(x_n)]$$
$$I = (0.25/3) * [1.000000 + 4*(1.509196) + 2*(0.778801) + 0.367879]$$

Approximate value of the integral  $I = 0.746855$

**CONCLUSION: THE ABOVE PROGRAM HAS BEEN EXECUTED SUCCESSFULLY.**

## 2. SIMPSON'S 3/8 RULE

**AIM: AIM: TO WRITE A PROGRAM IN PYTHON TO DEMONSTRATE SIMPSON'S 3/8 RULE.**

**PROGRAM:**

```
# Simpson's 3/8 Rule for I = ∫(0 to 1) e^(-x^2) dx with n = 3
```

```
import math
```

```
# Define the function
```

```
def f(x):
```

```
    return math.exp(-x**2)
```

```
# Given values
```

```
a = 0 # lower limit
```

```
b = 1 # upper limit
```

```
n = 3 # must be a multiple of 3 for Simpson's 3/8 rule
```

```
# Step size
```

```
h = (b - a) / n
```

```
# Generate x and f(x)
```

```
x = [a + i * h for i in range(n + 1)]
```

```
f_values = [f(xi) for xi in x]
```

```
# Display table
```

```
print("-----")
```

```
print(" i | x(i) | f(x(i)) = e^(-x^2)")
```

```
print("-----")
```

```
for i in range(n + 1):
    print(f"\{i}<3} | {x[i]}<8.6f} | {f_values[i]}<10.6f}")
    print("-----")

# Apply Simpson's 3/8 rule formula (for n=3)
I = (3 * h / 8) * (f_values[0] + 3*f_values[1] + 3*f_values[2] + f_values[3])

# Step-by-step output
print(f"\nh = (b - a) / n = ({b}) / ({n}) = {h:.6f}")
print("\nUsing Simpson's 3/8 Rule:")
print(f"I = (3h/8) * [f(x0) + 3f(x1) + 3f(x2) + f(x3)]")
print(f"I = (3*{h:.6f}/8) * [{f_values[0]:.6f} + 3*{f_values[1]:.6f} + 3*{f_values[2]:.6f} +
{f_values[3]:.6f}]")

# Final result
print("\n-----")
print(f"Approximate value of the integral I = {I:.6f}")
print("-----")
```

**OUTPUT:**

```
i      x(i)      f(x(i)) = e^(-x^2)
-----
0      0.000000  1.000000
1      0.333333  0.894839
2      0.666667  0.641180
3      1.000000  0.367879
-----
h = (b - a)/n = (1 - 0)/3 = 0.333333
Using Simpson's 3/8 Rule:
I = (3h/8) * [f(x0) + 3f(x1) + 3f(x2) + f(x3)]
I = (3*0.333333/8) * [1.000000 + 3*0.894839 + 3*0.641180 + 0.367879]
-----
Approximate value of the integral I = 0.746992
-----
```

**CONCLUSION: THE ABOVE PROGRAM HAS BEEN EXECUTED SUCCESSFULLY.**

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**TRANSPORTATION PROBLEM****TRANSPORTATION PROBLEM USING NORTHWEST METHOD****AIM: TO WRITE A PROGRAM IN PYTHON TO DEMONSTRATE TRANSPORTATION PROBLEM USING NORTHWEST METHOD.****PROGRAM:**

```
# Northwest Corner Method - step-by-step

# Problem data (from your sheet)

# Costs matrix: rows = origins O1,O2 ; cols = destinations D1,D2,D3

costs = [
    [8, 6, 10], # O1
    [10, 4, 9] # O2
]

supply = [2000, 2500] # supplies for O1, O2
demand = [1500, 2000, 1000] # demands for D1, D2, D3

# Make copies so we don't destroy originals if we want to reuse them
sup = supply.copy()
dem = demand.copy()

# Prepare an allocation matrix initialized to zeros
alloc = [[0 for _ in range(len(demand))] for _ in range(len(supply))]

print("Northwest Corner Method - step by step\n")
print("Initial supply:", supply)
```

```
print("Initial demand:", demand)
print()
i = 0 # origin index (row)
j = 0 # destination index (col)
step = 0

# Loop until all supplies and demands are satisfied
while i < len(sup) and j < len(dem):
    step += 1
    qty = min(sup[i], dem[j])
    alloc[i][j] = qty
    sup[i] -= qty
    dem[j] -= qty

    # Print step details
    print(f"Step {step}: Allocate {qty} units to cell O{i+1}, D{j+1}")
    print(f"  cost per unit = {costs[i][j]}")
    print(f"  Remaining supply for O{i+1} = {sup[i]}")
    print(f"  Remaining demand for D{j+1} = {dem[j]}\n")

    # Move to next row or column (if supply exhausted move down, if demand exhausted move right)
    # If both become zero, move one and then the other: standard choice is to advance column (j) after row
    if sup[i] == 0 and dem[j] == 0:
        # If both exhausted, advance (commonly advance row or column) - advance column then row to avoid skipping
        # But we must ensure not to go out of bounds: handle carefully:
```

```
# Advance column if possible, otherwise advance row.

if j + 1 < len(dem):
    j += 1
elif i + 1 < len(sup):
    i += 1
else:
    break # Finished

elif sup[i] == 0:
    i += 1
elif dem[j] == 0:
    j += 1
# This else normally won't happen because qty = min(sup[i], dem[j]) forces one to zero
else:
    pass

# Display final allocation matrix

print("Final allocation matrix (rows = O1,O2 ; cols = D1,D2,D3):\n")

header = [" | "] + [f" D{c+1}" for c in range(len(demand))] + [" | Supply"]
print("".join(header))

for r in range(len(alloc)):
    row_str = [f"O{r+1} | "] + [f" {alloc[r][c]:6d}" for c in range(len(alloc[r]))] + [f" | {supply[r]:6d}"]
    print("".join(row_str))

print()

# Compute total cost

total_cost = 0

for r in range(len(alloc)):
```

```
for c in range(len(alloc[0])):
    total_cost += alloc[r][c] * costs[r][c]

# Print non-zero allocations
print("Allocations (non-zero):")

for r in range(len(alloc)):
    for c in range(len(alloc[0])):
        if alloc[r][c] != 0:
            print(f"O{r+1}, D{c+1} -> {alloc[r][c]} units at cost {costs[r][c]} => contribution =
{alloc[r][c] * costs[r][c]}")

print(f"\nTotal transportation cost (initial NW-corner solution) = {total_cost}")
```

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```

Northwest Corner Method - step by step

Initial supply: [2000, 2500]
Initial demand: [1500, 2000, 1000]

Step 1: Allocate 1500 units to cell (O1, D1)
cost per unit = 8
Remaining supply for O1 = 500
Remaining demand for D1 = 0

Step 2: Allocate 500 units to cell (O1, D2)
cost per unit = 6
Remaining supply for O1 = 0
Remaining demand for D2 = 1500

Step 3: Allocate 1500 units to cell (O2, D2)
cost per unit = 4
Remaining supply for O2 = 1000
Remaining demand for D2 = 0

Step 4: Allocate 1000 units to cell (O2, D3)
cost per unit = 9
Remaining supply for O2 = 0
Remaining demand for D3 = 0

Final allocation matrix (rows = O1,O2 ; cols = D1,D2,D3):
      D1   D2   D3 | Supply
O1    1500     500     0 | 2000
O2      0     1500    1000 | 2500

Allocations (non-zero):
(O1, D1) -> 1500 units at cost 8 => contribution = 12000
(O1, D2) -> 500 units at cost 6 => contribution = 3000
(O2, D2) -> 1500 units at cost 4 => contribution = 6000
(O2, D3) -> 1000 units at cost 9 => contribution = 9000

Total transportation cost (initial NW-corner solution) = 30000

```

**CONCLUSION: THE ABOVE PROGRAM HAS BEEN EXECUTED SUCCESSFULLY.**

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