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## Multiple-Choice Questions (MCQs)

**1. (Theoretical) Question:** According to the slides, what is the definition of a "stationary policy"?

- a) A policy that specifies a fixed sequence of actions, regardless of the state.
- b) A policy that is a function of both the current state and the time step.
- c) A policy that specifies what the agent should do as a function of only the current state.
- d) A policy that always tells the agent to stay in its current state.

✓ **Correct Answer:** (c) **Explanation:** Slide 17 explicitly defines a stationary policy as one that is a function of the state. A non-stationary policy is a function of the state and the time.

Here are 5 multiple-choice questions (2 numerical, 3 theoretical) and 2 numerical short-answer questions based on your request.

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**2. (Numerical) Question:** In the 3×4 grid world (diagram on slide 10), the robot is in state s14 and tries to move 'right'. What is the probability that the robot stays in state s14?

	1	2	3	4
1	Start			
2		X		-1
3				+1

- a) 0.1
- b) 0.8
- c) 0.9
- d) 1.0

✓ **Correct Answer:** (c) **Explanation:** The transition model (slide 9) states an action has a 0.8 probability of its intended effect, 0.1 of a 90-deg left turn, and 0.1 of a 90-deg right turn.

- **Intended ('right'):** Bumps the wall, stays in s14 (Prob: 0.8).
- **90-deg left ('up'):** Bumps the wall, stays in s14 (Prob: 0.1).
- **90-deg right ('down'):** Moves to s24 (Prob: 0.1).
- The total probability of staying in s14 is  $0.8+0.1=0.9$ .

	1	2	3	4
1	Start			
2		X		-1
3				+1

**3. (Theoretical) Question:** The Policy Iteration algorithm is described as alternating between two main steps. What are these two steps?

- a) Value Iteration and Policy Improvement
- b) Policy Evaluation and Policy Improvement
- c) Synchronous Updates and Asynchronous Updates
- d) Bellman Equations and Q-Value Calculation

✓ **Correct Answer:** (b) **Explanation:** The slides state that Policy Iteration alternates between two steps: (1) **Policy Evaluation**, to calculate the utility  $V_{\pi}(s)$  for the current policy, and (2) **Policy Improvement**, to calculate a new policy  $\pi_{i+1}$  using those utilities .

**4. (Numerical) Question:** In the Value Iteration example for the 3×4 grid, the algorithm starts with  $V_0(s)=0$  for all non-goal states (see  $V_0$  table on slide 43). Given  $\gamma=1$  and  $R(s)=-0.04$  for non-goals, what is the value of  $V_1(s_{33})$ ?

- a) -0.04    b) 0.80    c) 0.76    d) 1.00

✓ **Correct Answer:** (c)    **Explanation:** The update rule is  $V_{i+1}(s) \leftarrow R(s) + \gamma \max_a \sum_{s'} P(s'|s,a) V_i(s')$ . For  $V_1(s_{33})$ :

- $R(s_{33})=-0.04$ .
- The best action 'a' from  $s_{33}$  is 'right', which has a 0.8 probability of reaching  $s_{34}$  (value  $V_0(s_{34})=+1$ ).
- The max expected utility from  $V_0$  is  $\approx (0.8 \times V_0(s_{34})) = 0.8 \times 1 = 0.8$ .
- Therefore,  $V_1(s_{33}) = -0.04 + (1 \times 0.8) = 0.76$ .

**5. (Theoretical) Question:** Why does the optimal policy for the 3×4 grid world (slide 19) depend on the value of  $R(s)$  for non-goal states?

When  $R(s) < -1.6284$ ,  
what does the optimal policy look like?

	1	2	3	4
1	Start			
2		X		-1
3				+1

- a) Because  $R(s)$  determines the location of the wall at  $s_{22}$ .
- b) Because the agent's policy must balance the "cost of living" (the reward  $R(s)$  for each step) against the final reward at a goal state.
- c) Because the transition probabilities  $P(s'|s,a)$  change when  $R(s)$  changes.
- d) Because a positive  $R(s)$  makes the discount factor  $\gamma$  negative.

✓ **Correct Answer:** (b)    **Explanation:** The optimal policy is a trade-off. When  $R(s)$  is very negative (e.g., "painful,"  $R(s) < -1.6284$ ), the agent wants to exit *fast*, even to the -1 goal. When  $R(s)$  is only slightly negative (e.g., "slightly dreary"), the agent is willing to take a *safer*, longer path to get the +1 goal.

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Q.1

In the 3×4 grid world, the Value Iteration algorithm is applied with  $\gamma=1$  and  $R(s)=-0.04$  for non-goal states. You are given the initial values  $V_0(s)$  from the table on **slide 43**, where all non-goal states are 0,  $V_0(s_{24})=-1$ , and  $V_0(s_{34})=+1$ .

**Calculate the value  $V_1(s_{23})$ .**

	1	2	3	4
1	0	0	0	0
2	0	X	0	-1
3	0	0	0	+1

**Answer:** We use the Value Iteration update rule shown on **slide 42** and **slide 44**:  
 $V_1(s_{23}) = R(s_{23}) + \gamma \max_a \sum P(s' | s_{23}, a) V_0(s')$  Given  $R(s_{23}) = -0.04$  and  $\gamma = 1$ . We must check the expected utility for all 4 actions using the  $V_0$  values:

1. **Action 'up':**  $0.8 \times V_0(s_{13}) + 0.1 \times V_0(s_{22} \rightarrow s_{23}) + 0.1 \times V_0(s_{24})$   
 $= (0.8 \times 0) + (0.1 \times 0) + (0.1 \times -1) = -0.1$

2. **Action 'down':**  $0.8 \times V_0(s_{33}) + 0.1 \times V_0(s_{22} \rightarrow s_{23}) + 0.1 \times V_0(s_{24})$   
 $= (0.8 \times 0) + (0.1 \times 0) + (0.1 \times -1) = -0.1$

3. **Action 'left':**  $0.8 \times V_0(s_{22} \rightarrow s_{23}) + 0.1 \times V_0(s_{33}) + 0.1 \times V_0(s_{13})$   
 $= (0.8 \times 0) + (0.1 \times 0) + (0.1 \times 0) = 0$

4. **Action 'right':**  $0.8 \times V_0(s_{24}) + 0.1 \times V_0(s_{33}) + 0.1 \times V_0(s_{13})$   
 $= (0.8 \times -1) + (0.1 \times 0) + (0.1 \times 0) = -0.8$

The max of these outcomes is 0.  $V_1(s_{23}) = -0.04 + (1 \times 0) = -0.04$ .

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## Question 2

In the 2x2 grid Policy Iteration example (diagram on **slide 61**), the values after Policy Evaluation are  $V(s_{11})=0.75$ ,  $V(s_{21})=-0.85$ ,  $V(s_{12})=+1$ , and  $V(s_{22})=-1$ . The transition model is 0.8 for the intended direction, 0.1 for a 90-degree left turn, and 0.1 for a 90-degree right turn.

**Calculate the expected utility (Q-value) for  $Q(s_{11}, \text{right})$  during the Policy Improvement step.**

A hand-drawn diagram of a 2x2 grid. The columns are labeled 1 and 2 at the top. The rows are labeled 1 and 2 on the left. The cells contain the following values: top-left is 0.75, top-right is +1, bottom-left is -0.85, and bottom-right is -1.

	1	2
1	0.75	+1
2	-0.85	-1

**Answer:** We calculate the Q-value as the sum of (probability  $\times$  utility) for all possible outcomes, as shown on **slide 61**:  $Q(s_{11}, \text{right}) = P(s' | s_{11}, \text{right}) V(s')$

1. **Intended ('right'):** Moves to  $s_{12}$ . Probability = 0.8. Utility =  $0.8 \times V(s_{12}) = 0.8 \times (+1) = 0.8$
2. **90-deg left ('up'):** Bumps wall, stays in  $s_{11}$ . Probability = 0.1. Utility =  $0.1 \times V(s_{11}) = 0.1 \times (0.75) = 0.075$
3. **90-deg right ('down'):** Moves to  $s_{21}$ . Probability = 0.1. Utility =  $0.1 \times V(s_{21}) = 0.1 \times (-0.85) = -0.085$

**Total Q-value:**  $0.8 + 0.075 - 0.085 = 0.79$ .