Deep Residual Networks: ResNet

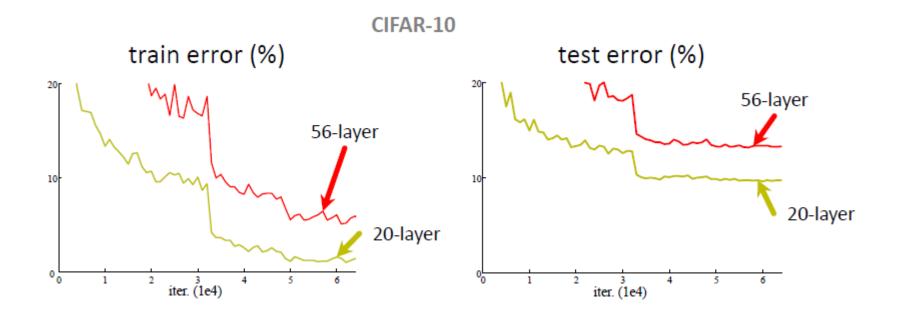
CS8004: Deep Learning and Applications

Deeper Networks

- A deeper network can provide solution to more complex problems.
 - With increasing feature map size.
 - Involving more nonlinearity
- But training a deeper network is much more difficult and a complex problem.
- Why ?
 - Due to exploding /vanishing gradients?
 - Or due to overfitting?

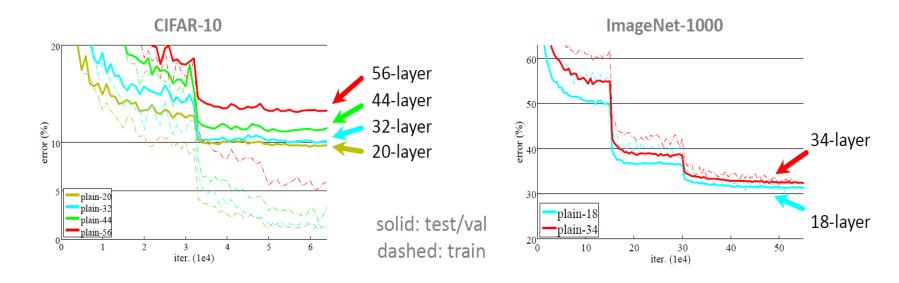
Plain CNN

- Plain nets: A CNN with 3x3 Conv layers
- 56-layer net has higher training error and test error than 20-layers net.



Plain CNN

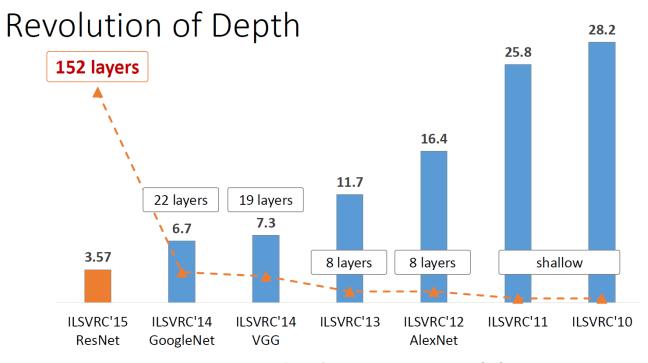
- Very deep plain CNN have higher training error.
- A general phenomenon, observed in many datasets



So, it is not a problem of overfitting!
Then it is vanishing \exploding gradients?

Deep CNN

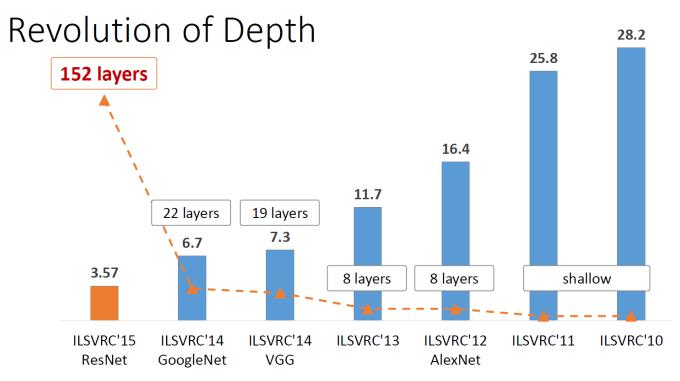
- Solutions: Training relatively less number of layers
 - ReLU for solving gradient vanishing problem
 - Dropout ...



ImageNet Classification top-5 error (%)

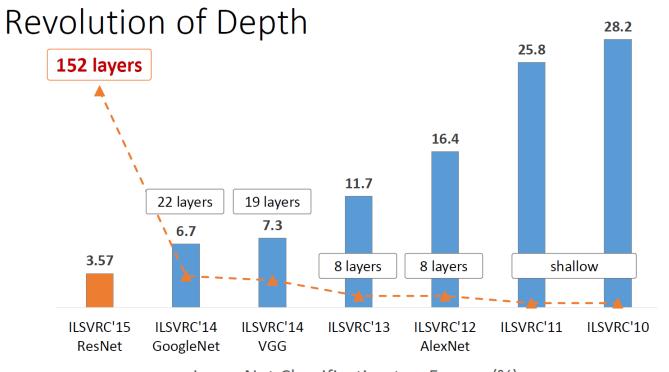
Deep CNN

- Solution: ~ 10 layers
 - Normalized initialization.
 - Intermediate normalization layers.



Deep CNN

- Solution beyond 100 layers
 - Residual network





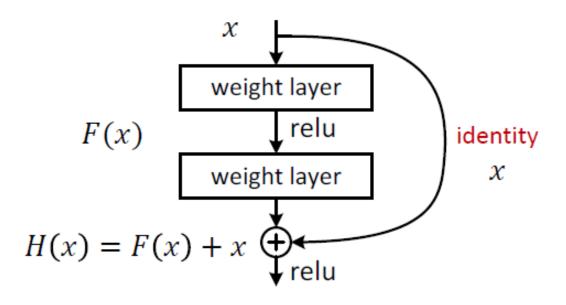
A Deep Residual Learning Framework

- Fit a residual map in place of directly fitting a desired underlying mapping H(x).
- Let the stacked nonlinear layers fit another mapping of the form F(x) := H(x)-x.
- The original mapping is recast into F(x)+x.
- Hypothesis: It is easier to optimize the residual mapping than to optimize the original, unreferenced mapping.
- If an identity mapping were optimal, it would be easier to push the residual to zero than to fit an identity mapping by a stack of nonlinear layers.

A Deep Residual Learning Framework

Think of a shortcut connection.

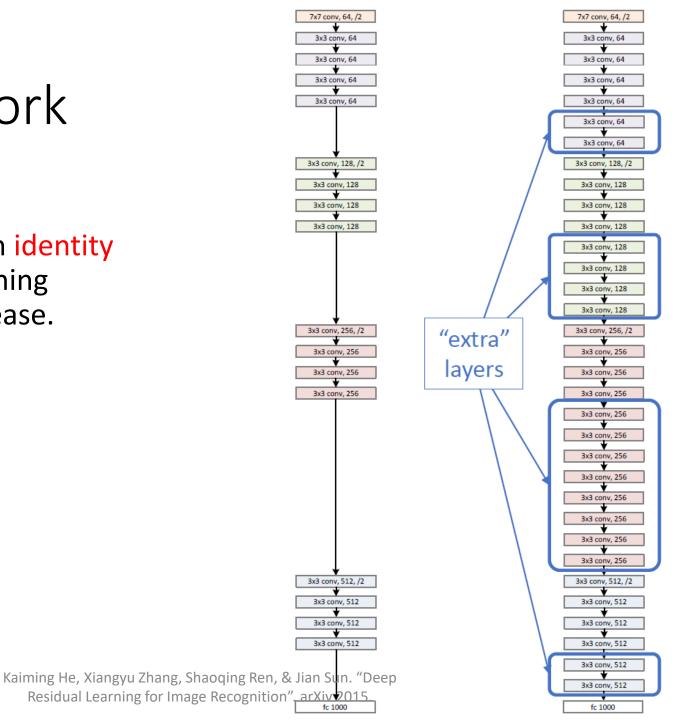
 Identity mappings neither increase the computational complexity nor add extra parameters



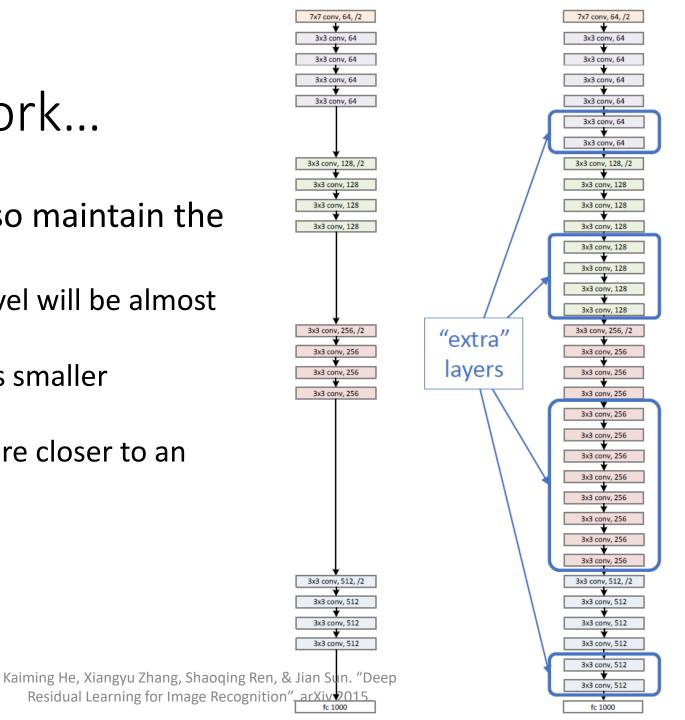
A Deep Residual Learning Framework

- The entire network can still be trained end-to-end using SGD with backpropagation.
- Can be easily implemented using common libraries without modifying the solvers.

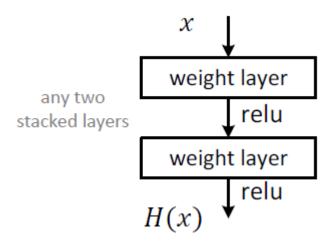
- Naïve solution
 - If extra layers are an identity mapping, then training error does not increase.



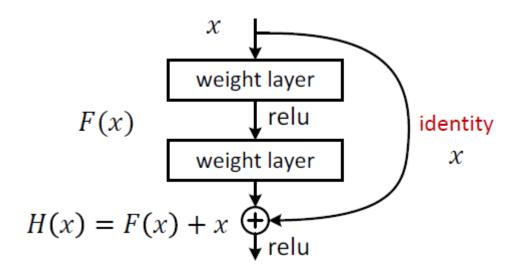
- Deeper networks also maintain the tendency of results.
 - Features in same level will be almost same.
 - Adding layers makes smaller differences.
 - Optimal mappings are closer to an identity map.



- Plain block
 - Difficult to make identity mapping because of multiple non-linear layers



- Residual block
 - If identity were optimal, easy to set weights as 0.
 - If optimal mapping is closer to identity, easier to find small fluctuations.
 - -> Appropriate for treating perturbation as keeping a base information



- Let us see how does the Residual Network (ResNet) work.
- Suppose a^l is the input of the l-th layer.
- Recall the output form of the l-th layer.

•
$$z^{l+1} = W^{l+1}a^l + b^{l+1}$$

Activation :

•
$$a^{l+1} = g(z^{l+1}) = g(W^{l+1}a^l + b^{l+1})$$

•
$$a^{l+2} = g(z^{l+2}) = g(W^{l+2}a^{l+1} + b^{l+2})$$

In ResNet it is modified as

•
$$a^{l+2} = g(z^{l+2} + a^l) = g(W^{l+2}a^{l+1} + b^{l+2} + a^l).$$

- For the sake of simplicity let us assume that there is identity activation function g(x) = x involved between the layers. Also let us take $b^l = 0$ and use W^l in place of W^{lT} for the sake of simplicity.
- In ResNet

$$a^{l+2} = z^{l+2} + a^{l} = W^{l+2} \ a^{l+1} + a^{l}$$

$$a^{l+4} = z^{l+4} + a^{l+2} = W^{l+4} \ a^{l+3} + W^{l+2} \ a^{l+1} + a^{l}$$

$$...$$

$$a^{L} = W^{L} \ a^{L-1} + W^{L-2} \ a^{L-3} + ... + W^{l+2} \ a^{l+1} + a^{l}$$

$$a^{L} = a^{0} + \sum_{j=1}^{L/2} W^{2j} a^{2j-1}$$

Comparison with Plain Network expression.

$$a^{l+1} = W^{l+1} a^l$$

$$a^{l+2} = W^{l+2} a^{l+1} = W^{l+2} W^{l+1} a^l$$

$$\cdots$$

$$a^L = W^L \cdots W^{l+2} W^{l+1} a^l$$

$$ResNet Re$$

$$a^L = \prod_{j=1}^L (W^j) a^0$$

ResNet Recurrence

$$a^{L} = a^{0} + \sum_{j=1}^{L/2} W^{2j} a^{2j-1}$$

• Two main advantages: The feature a^L of a deeper layer can be expressed as the feature a^l of a shallower layer plus a residual term.

$$a^{L} = a^{l} + \sum_{j=l}^{L/2} W^{2j} a^{2j-1}$$

• The feature a^L of a deeper layer is the summation of residual terms plus the initial input term a^0 .

• Imagine a situation when all the weights are zero in the following equation.

$$a^{L} = a^{l} + \sum_{j=l}^{L/2} W^{2j} a^{2j-1}$$

- That means the network has perfectly reconstructed the identity mapping.
- This is the basis of considering residual network to improve training time and performance.

Backward propagation in ResNet:

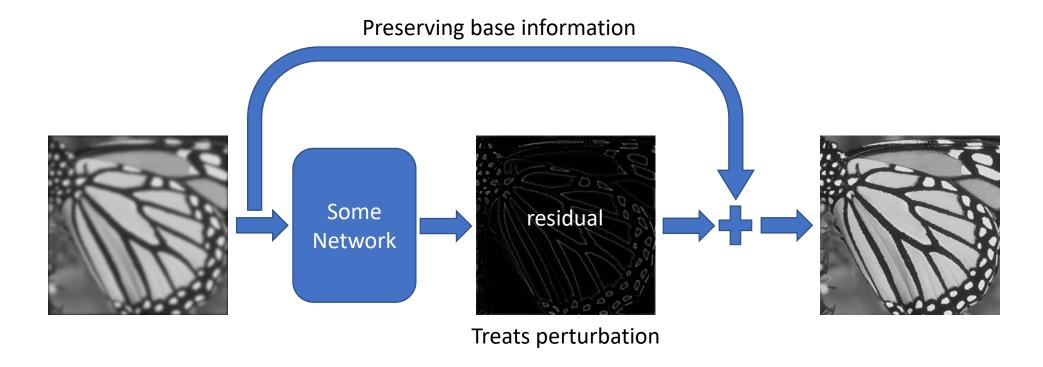
If L is the loss function.

$$\frac{\partial L}{\partial a^l} = \frac{\partial L}{\partial a^L} \cdot \frac{\partial a^L}{\partial a^l}$$

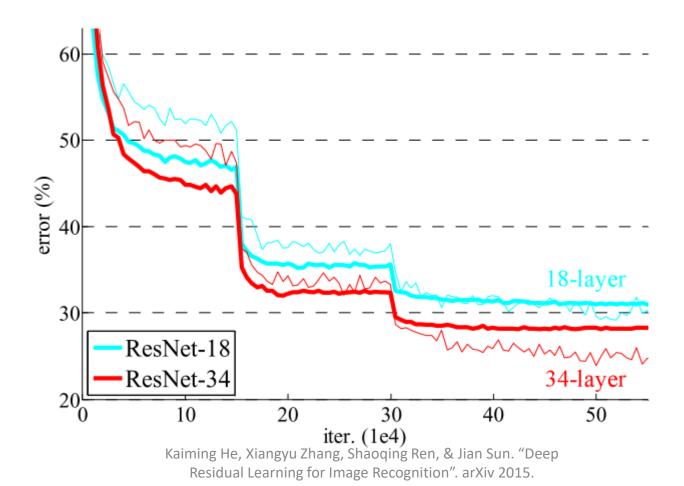
$$\frac{\partial L}{\partial a^L} = \frac{\partial L}{\partial a^L} \left(1 + \frac{\partial}{\partial a^l} \sum_{j=l}^{L/2} W^{2j} a^{2j-1} \right)$$

- This efficiently eliminates the gradient descent problem .
 - Any backpropagation ensures that the information $\frac{\partial L}{\partial a^L}$ directly back propagates to the l-th layer.

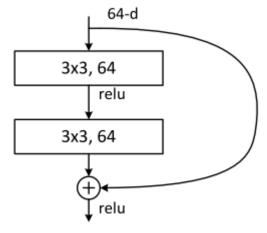
• Difference between an original image and a changed image.



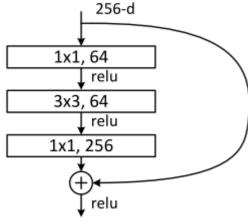
Deeper ResNets have lower training error



- Residual block
 - Very simple
 - Parameter-free



A naïve residual block



"bottleneck" residual block (for ResNet-50/101/152)

- Shortcuts connections
 - Identity shortcuts : $x^{l+1} = F(x^l, \{W_{l+1}\}) + x^l$
 - Projection shortcuts : $x^{l+1} = F(x^l, \{W_{l+1}\}) + W_s x^l$
- Why projection shortcuts?
 - To match the dimension of the output $F(x, \{W_{l+1}\})$ from the residual weight layers.
 - For example if $F(x, \{W_{l+1}\})$ is of dimension 256 and initial x is of dimension 128. Then W_s projects x to make it a vector of dimension 256.
 - Hence W_s is of dimension 256×128 .

Identity Mapping in ResNet

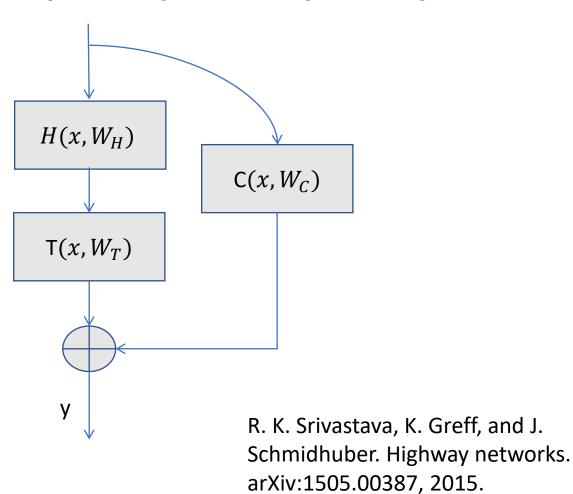
Identity shortcuts are defined by

•
$$x^{l+1} = F(x^l, \{W_{l+1}\}) + x^l$$

- Performance of ResNet with other shortcuts is also studied by He et al. (2016) where x is replaced by h(x).
- Such shortcut connections are defined by
 - $x^{l+1} = F(x^l, \{W_{l+1}\}) + h(x^l)$
 - $y^{l+1} = f(x^{l+1})$
- It is reported that identity skip connections (shortcuts) achieves the fastest error reduction and lowest training loss among all variants (scaling, gating) convolutions.
- Other choices lead to higher training loss and error.
- These experiments suggest that keeping a "clean" information path is helpful for easing optimization.

Similar Architecture – Highway Net

$$\mathbf{y} = H(\mathbf{x}, \mathbf{W_H}) \cdot T(\mathbf{x}, \mathbf{W_T}) + \mathbf{x} \cdot C(\mathbf{x}, \mathbf{W_C}).$$



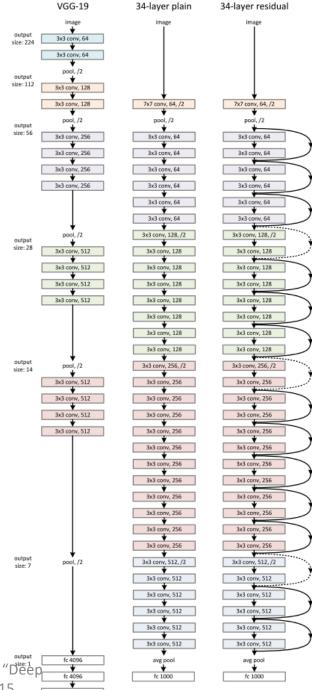
Highway Net vs. ResNet

- C and T are data dependent
- Both the gates have parameters.
- When a gated shortcut is "closed" the layers in highway networks represent non-residual functions.
- High-2 way networks have not demonstrated accuracy gains with depth of over 100 layers.

R. K. Srivastava, K. Greff, and J. Schmidhuber. Highway networks. arXiv:1505.00387, 2015.

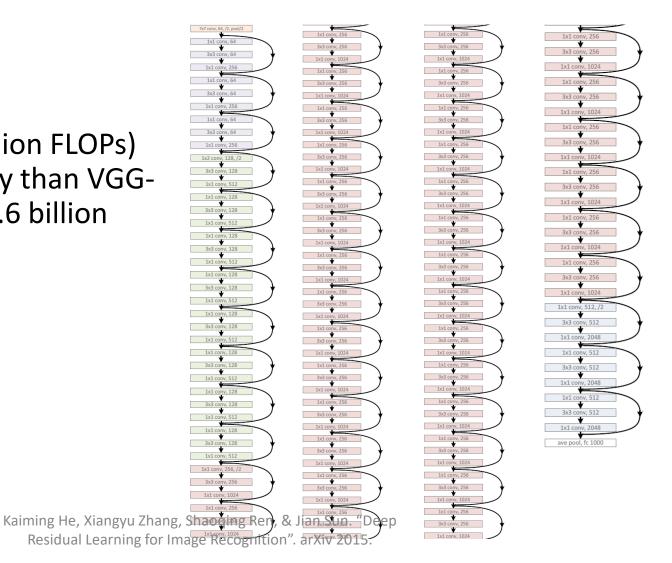
ResNet Design

- Basic design (VGG-style)
 - All 3x3 conv (almost)
 - Spatial size/2 => #filters x2
 - Batch normalization
 - Simple design, just deep
- Other remarks
 - No max pooling (almost).
 - No hidden fully connected layers.
 - No dropout.



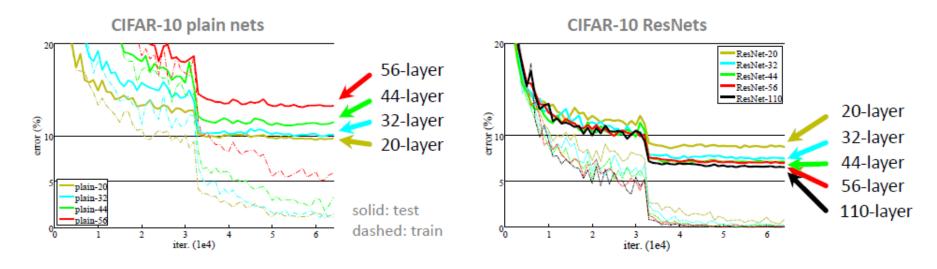
Network Design

- ResNet-152
 - Use bottlenecks.
 - ResNet-152(11.3 billion FLOPs)
 has lower complexity than VGG16/19 nets (15.3/19.6 billion
 FLOPs).



Results

- Deep Resnets can be trained without difficulties.
- Deeper ResNets have lower training error, and also lower test error.

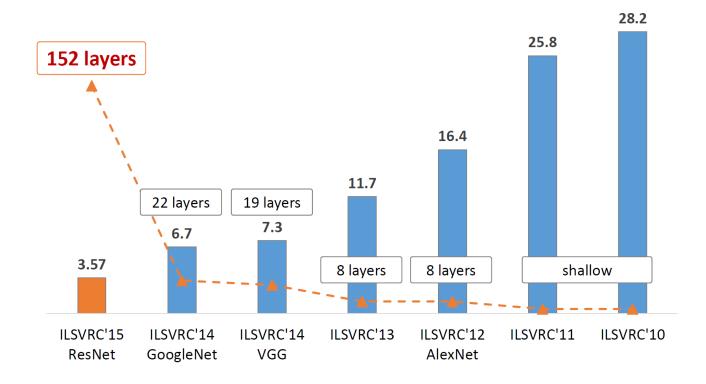


Results

- 1st places in all five main tracks in "ILSVRC & COCO 2015 Competitions"
 - ImageNet Classification
 - ImageNet Detection
 - ImageNet Localization
 - COCO Detection
 - COCO Segmentation

Quantitative Results

ImageNet Classification



Result

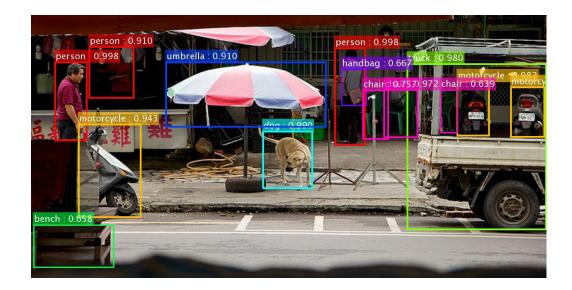
• Performances increase absolutely.

task	2nd-place winner	MSRA	margin (relative)
ImageNet Localization (top-5 error)	12.0	9.0	27%
ImageNet Detection (mAP@.5)	53.6 abs 6 8.5 %	better!	16%
COCO Detection (mAP@.5:.95)	33.5	37.3	11%
COCO Segmentation (mAP@.5:.95)	25.1	28.2	12%

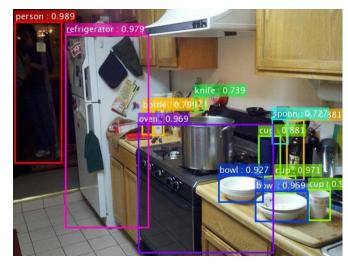
- Based on ResNet-101
- Existing techniques can use residual networks or features from it

Qualitative Result

- Object detection
 - Faster R-CNN + ResNet



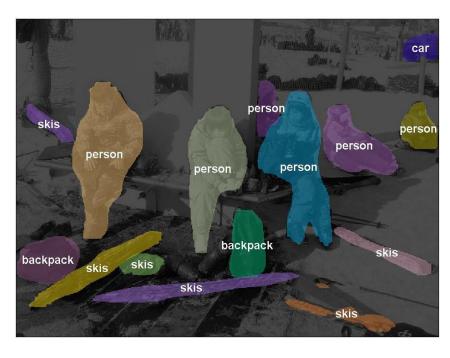
80 Object Categories More than 300,000 images



Qualitative Results

MS COCO –Instance Segmentation





Qualitative Results

ImageNet - Classification, **Localization & Detection**

200 object classes 1000 object classes

456,567 images DET **CLS-LOC** 1,431,167 images







Strawberry



Backpack



Bathing cap

Traffic light



Racket



http://image-net.org/challenges/LSVRC/

Further Deep Residual Network

 1202 layer network was also explored, but with the dataset mentioned in previous slides, its test set error was showing increase in error as compared to 110 layer network.

Probably due to overfitting.

Data set size was not sufficient to train such a high sized network.

Conclusion

- ResNet training is simple and computationally convenient.
- Accuracy improved.

- New versions
 - Wide ResNet
 - ResNext

Reference

- Kaiming He, Xiangyu Zhang, Shaoqing Ren, & Jian Sun. "Deep Residual Learning for Image Recognition". arXiv 2015.
- Slides of Deep Residual Learning @ ILSVRC & COCO 2015 competitions
- Slides of Hyeonwoo Noh, Pohang University of Science and Technology on ResNet.