

NUMBER SYSTEM

Expt. No. Class 1.

Page No. 1
Date 15/02/2015

AIM:

Q:1 CHOOSE YOUR BASE B/W 3 AND 13. AND WRITE 20
→ 50 NUMBERS.

⇒ Let's take Base as 9

0	10	20	30	40	50	60
1	11	21	31	41	51	61
2	12	22	32	42	52	62
3	13	23	33	43	53	63
4	14	24	34	44	54	64
5	15	25	35	45	<u>55</u>	65
6	16	26	36	46	56	66
7	17	27	37	47	57	67
8	18	28	38	48	58	68

Q:2:→ ADD AND SUBTRACT SINGLE AND MULTIPLE DIGIT
IN YOUR NUMBER SYSTEM.

⇒ ADDITION.

3	6	1	3	7
+5	+4	+0	+8	+9
<hr/>	<hr/>	<hr/>	<hr/>	<hr/>
8	11	1	12	17

$\begin{array}{r} 24 \\ 31 \\ \hline 55_9 \end{array}$	$\begin{array}{l} \rightarrow 2 \times 9 + 4 \times 9 = 22_{10} \\ \rightarrow 3 \times 9 + 1 \times 9 = 28_{10} \\ \hline 50_{10} \end{array}$	$\begin{array}{r} 5 \\ 9 \overline{) 50} \\ \underline{45} \\ 5 \end{array}$
--	---	--

Expt. No. _____
AIM: _____

$$\begin{array}{r} 10 \\ 33 \\ + 99 \\ \hline 132 \end{array}$$

$$\begin{array}{r} 33 \\ + 99 \\ \hline 153 \end{array}$$

$$\begin{aligned} 33 &\Rightarrow 3 \times 9 + 3 \times 9^0 \\ &= 27 + 3 \\ &= 30_{10} \end{aligned}$$

$$\begin{aligned} 99 &\Rightarrow 9 \times 11 \\ &= 99_{10} \end{aligned}$$

$$30 + 99 = 129_{10}$$

$$\begin{array}{r} 14 \\ 9 \overline{) 129} \\ \underline{9} \\ 39 \\ \underline{36} \\ 3 \end{array}$$

$$\begin{array}{r} 1 \\ 9 \overline{) 14} \\ \underline{9} \\ 5 \end{array}$$

$$\rightarrow 9 \overline{) 1} \Rightarrow 1$$

$$33 + 99 = 153$$

$$\begin{array}{r} 66 \\ + 48 \\ \hline 125 \end{array}$$

$$\begin{aligned} 66 &\Rightarrow 6 \times 9^1 + 6 \times 9^0 \\ &= 54 + 6 \\ &= 60 \end{aligned}$$

$$\begin{aligned} 48 &\Rightarrow 4 \times 9^1 + 8 \times 9^0 \\ &= 36 + 8 \\ &= 44 \end{aligned}$$

$$60 + 44 = 104$$

convert to base 9

$$\begin{array}{r} 11 \\ 9 \overline{) 104} \\ \underline{9} \\ 14 \\ \underline{9} \\ (5) \end{array}$$

$$\begin{array}{r} 1 \\ 9 \overline{) 11} \\ \underline{9} \\ (2) \end{array}$$

$$9 \overline{) 1} = 1 \quad \therefore = 125$$

AIM:

SUBTRACTION

$$\begin{array}{r} 5 \\ -3 \\ \hline 2 \end{array}$$

$$\begin{array}{r} 3 \\ -1 \\ \hline 2 \end{array}$$

$$\begin{array}{r} 9 \\ -5 \\ \hline 4 \end{array}$$

$$\begin{array}{r} 33 \\ -21 \\ \hline 12 \end{array}$$

$$\begin{array}{r} 98 \\ -97 \\ \hline 01 \end{array}$$

$$\begin{array}{r} 2^{10} \\ 83 \\ -25 \\ \hline 08 \end{array}$$

Q3:- PREPARE A TABLE OF SINGLE DIGIT MULTIPLICATION IN YOUR NUMBER SYSTEM

	0	1	2	3	4	5	6	7	8
0	0	0	0	0	0	0	0	0	0
1	0	1	2	3	4	5	6	7	8
2	0	2	4	6	8	11	13	15	17
3	0	3	6	10	13	16	20	23	26
4	0	4	8	13	17	22	26	31	35
5	0	5	11	16	22	27	33	38	44
6	0	6	13	20	26	33	40	46	53
7	0	7	15	23	31	38	46	54	62
8	0	8	17	26	35	44	53	62	71

AIM :

Q:4 MULTIPLY MULTIPLE DIGIT IN YOUR NUMBER SYSTEM

$$\begin{array}{r} 8 \\ \times 8 \\ \hline 71 \end{array}$$

$$\begin{array}{r} 23 \\ \times 25 \\ \hline 586 \end{array}$$

$$\begin{aligned} 23 &\Rightarrow 2 \times 9_{10} + 3 \\ &\Rightarrow 18 + 3 \\ &\Rightarrow 21 \end{aligned}$$

$$\begin{aligned} 25 &\Rightarrow 2 \times 9_{10} + 5 \\ &= 18 + 5 \\ &= 23 \end{aligned}$$

$$23 \times 21 \Rightarrow 483_{10}$$

convert to base 9

$$\begin{array}{r} 53 \\ 9 \overline{) 483} \\ \underline{45} \\ 33 \\ \underline{27} \\ 6 \end{array}$$

$$\begin{array}{r} 53 \\ 9 \overline{) 53} \\ \underline{45} \\ 8 \end{array}$$

$$15869$$

AIM:

Q.5 WRITE 1, 10, 20, 30, 50 AND 100 FROM YOUR BASE TO BASE 10

$$1 \rightarrow 1$$

$$10 \rightarrow 19$$

$$20 \rightarrow 18$$

$$30 \rightarrow 27$$

$$50 \rightarrow 45$$

$$100 \rightarrow 81$$

Q.6 WRITE A STRATEGY TO CONVERT BASE 7 TO BASE 10 IN PLAN ENGLISH OR PSEUDO CODE OR CODE

\Rightarrow STEP 1: TAKE NUMBER.

STEP 2: DIVIDE THAT NUMBER BY 10 TO GET WHOLE NUMBER, AND GET THE REMINDER ADDED

e.g. 21

$$\Rightarrow 2 \times 7_{10} + 7_{10}$$

$$\Rightarrow 14 + 1$$

$$\Rightarrow 15$$

STEP 3:- MULTIPLY BY 7 OF WHOLE NUMBER AND ADD REMINDER IN IT.

Example : 154_7

$$15 \times 7_{10} + 4$$

$$\Rightarrow 7 \times 7_{10} + 1 + 4$$

\Rightarrow

AIM:

EXAMPLE : 154

$$\begin{aligned} 154 &= (1 \times 7^2) + (5 \times 7^1) + (4 \times 7^0) \\ &= 49 + 35 + 4 \\ &= 88 \end{aligned}$$

$$\begin{aligned} 1324 &= (1 \times 7^3) + (3 \times 7^2) + (2 \times 7^1) + (4 \times 7^0) \\ &= 1 \times 7 \times 7 \times 7 + 3 \times 7 \times 7 + 2 \times 7 + 4 \\ &= 343 + 147 + 14 + 4 \\ &= 508 \end{aligned}$$

CODE:-

FUNCTION / METHOD TO CONVERT BASE 7 TO
BASE 10 (JAVA)

```
public int ConvertToBaseTen (String Number) {  
    int baseTenNum = 0;  
    int lengthOfNumber = number.length();  
  
    for (i = 0; i < length; i++) {  
  
        char digitChar = number.charAt (length-1-i);  
        int digit = Character.getNumericValue  
                                (digitChar);  
        baseTenNum += digit * Math.Pow (7, i);  
    }  
    return baseTenNum;  
}
```

Call this method in your class and pass
Number as String to get the o/p

AIM:

Q: 2 Write a Strategy to convert Base N to Base M

⇒ Convert Base N to Base 10 first and then Base 10 to Base M so that calculation will be easy.

Here, First will take for loop for converting base N to base 10 same like above question which was base 7 to 10
 $\text{int baseN} = 7, \text{baseM} = 8$

```
for (i = 0; i < length; i++) {
```

```
    char digitChar = number.charAt(length - 1 - i)
```

```
    int digit = Character.getNumericValue
```

```
        (digitChar);
```

```
    baseTenNum = digit * Math.pow(baseN, i)
```

⇒ Here baseTenNum is now base 10 Number.

↳ Iterate it through while loop for base M

```
StringBuilder S = new StringBuilder
```

```
while (baseTenNum > 0)
```

```
{
```

```
    int r = baseTenNum % baseM;
```

```
    S.insert(0, Integer.toString(r, baseM));
```

```
    baseTenNum /= baseM;
```

```
}
```

```
return S.toString()
```


AIM:

Q:8 In base 10 How many 5 digit numbers will come

$$9 \times 10 \times 10 \times 10 \times 10 \\ = 90,000$$

Q:9 Algorithm or Strategy to find \log_{10}

Use brute force algorithm.

While (Math.Pow(10, value) < provided value)
{

Value = Value + 0.00001 (or more
smaller no.)

}