

### ③ Common functions?

$$\frac{d}{dx} F(x) = f(x)$$

$$\Rightarrow \int f(x) dx = F(x).$$

- $\int x^n dx = \frac{x^{n+1}}{n+1} + C, \quad [n \neq -1]$

$$\frac{d}{dx} x^m = m x^{m-1}$$

$$\Rightarrow \frac{d}{dx} \frac{x^m}{m} = x^{m-1}, \quad [m \neq 0]$$

$$\Rightarrow \frac{d}{dx} \left( \frac{x^{n+1}}{n+1} \right) = x^n, \quad [n \neq -1]$$

- $\int x^1 dx = \int \frac{1}{x} dx ?$

$$\frac{d}{dx} \ln x = \frac{1}{x} \Rightarrow \int \frac{1}{x} dx = \boxed{\ln x + C}, \quad x > 0.$$

$x < 0 ?$

$$\int \frac{1}{x} dx, \quad x < 0 ?$$

$$\frac{d}{dx} (\ln(-x)) = \frac{1}{x}.$$

$$\left\{ \begin{array}{l} \int \frac{1}{x} dx = \ln(-x) + C', \\ x < 0. \end{array} \right.$$

- $\int \sin x dx ?$

$$\left. \begin{array}{l} \frac{d}{dx} \sin x = \cos x \\ \frac{d}{dx} \cos x = -\sin x \\ \frac{d}{dx} \tan x = \sec^2 x \end{array} \right\} \left. \begin{array}{l} \int \sin x dx = -\cos x + C \\ \int \cos x dx = \sin x + C' \\ \int \sec^2 x dx = \tan x + C'' \end{array} \right.$$

- $\int e^x dx = e^x + C.$

$$\frac{d}{dx} e^x = e^x$$