

### ③ Common functions?

$$\frac{d}{dx} F(x) = f(x)$$

$$\Rightarrow \int \underline{f(x)} dx = F(x).$$

$$\bullet \int x^n dx = \frac{x^{n+1}}{n+1} + C, \quad [n \neq -1]$$

$$\frac{d}{dx} x^m = m x^{m-1}$$

$$\Rightarrow \frac{d}{dx} \frac{x^m}{m} = x^{m-1}, \quad m \neq 0$$

$$\Rightarrow \frac{d}{dx} \left( \frac{x^{n+1}}{n+1} \right) = x^n, \quad n \neq -1$$

$$\bullet \int x^{-1} dx = \int \frac{1}{x} dx?$$

$$\frac{d}{dx} \ln x = \frac{1}{x} \Rightarrow \int \frac{1}{x} dx = \boxed{\ln x} + C, \quad x > 0.$$

$x < 0?$   $\nearrow$

$$\rightarrow \int \frac{1}{x} dx = \ln|x| + C$$

$$\int \frac{1}{x} dx, \quad x < 0?$$

$$-x > 0.$$

$$\frac{d}{dx} (\ln(-x)) = \frac{1}{x}.$$

$$\left. \begin{array}{l} \int \frac{1}{x} dx = \ln(-x) + C, \\ x < 0. \end{array} \right\}$$

$$\bullet \int \sin x dx?$$

$$\frac{d}{dx} \sin x = \cos x$$

$$\frac{d}{dx} \cos x = -\sin x$$

$$\frac{d}{dx} \tan x = \sec^2 x$$

$$\int \sin x dx = -\cos x + C$$

$$\int \cos x dx = \sin x + C$$

$$\int \sec^2 x dx = \tan x + C$$

$$\bullet \int e^x dx = e^x + C.$$

$$\frac{d}{dx} e^x = e^x$$