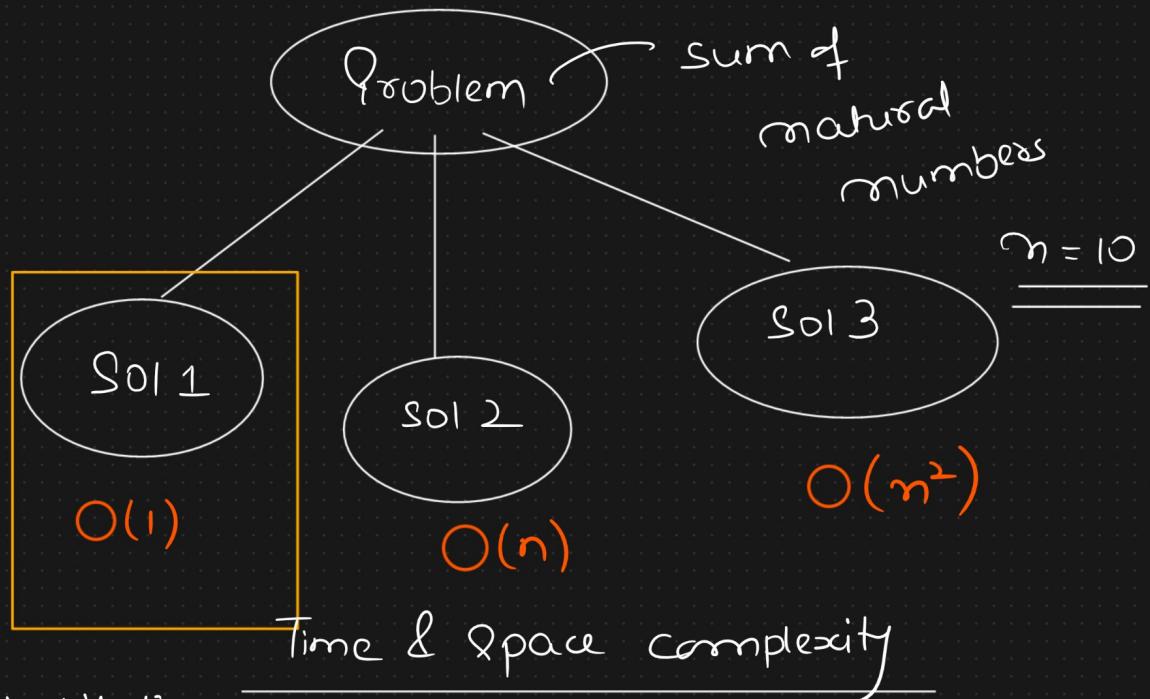
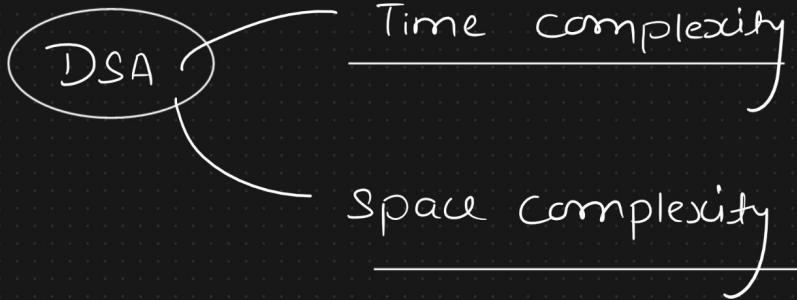


Week-1 DSA



- (1) Substitution
- (2) Recurrence Tree
- (3) Master's Theorem

→ very less

Recurrence Relation

Sum of natural numbers

Approach 1

$\sim O(n)$

int sum=0;

for ($i = 0$ to 10) {

 sum += i;

} return sum;

$n = 10$

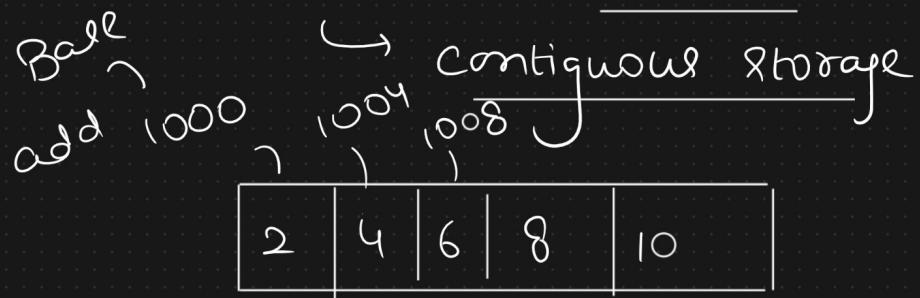
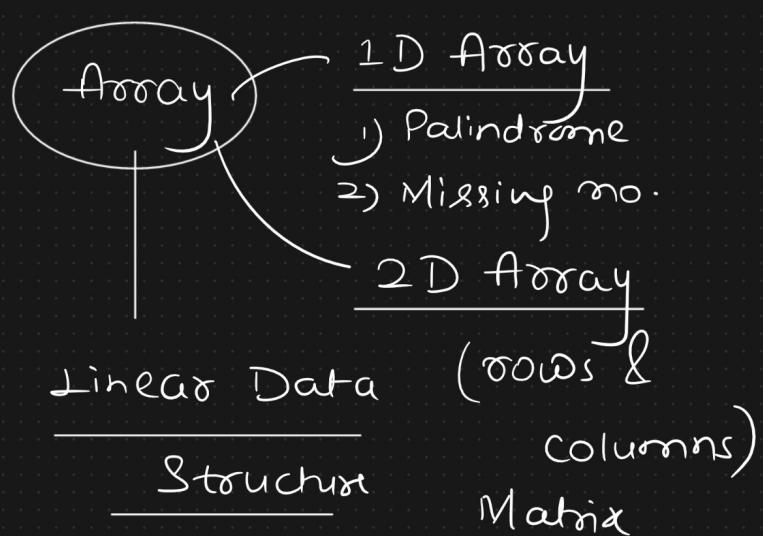
Approach 2

$\sim O(1)$

$$\frac{n(n+1)}{2} = \text{sum}$$

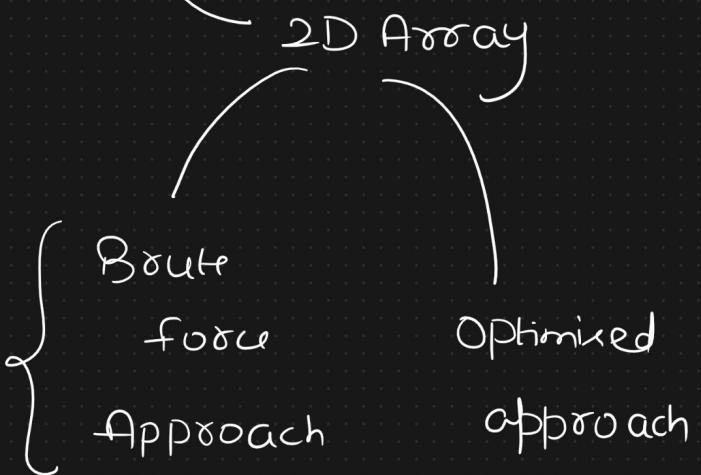
return sum;

- 3) Reversal
- 4) Duplicate



↳ Rotation of Matrix

↳ Prefix sum ↳ 1D Array



{ Binary Search
 $\underline{\underline{O(\log_2 n)}}$ } Logarithmic time complexity

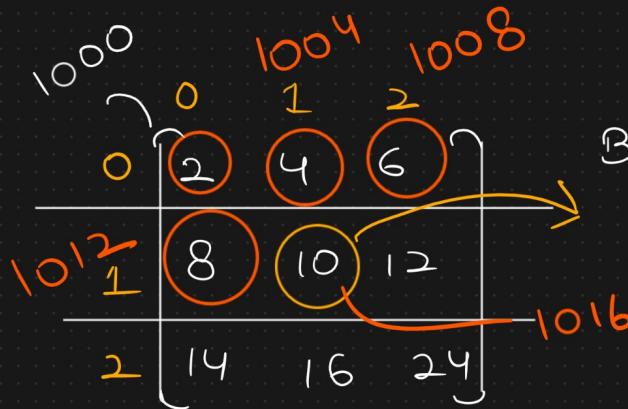
$$nR = 3$$

$$nC = 3$$

$$2B_d = 0$$

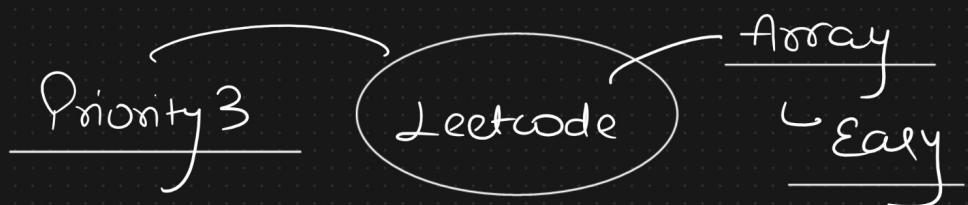
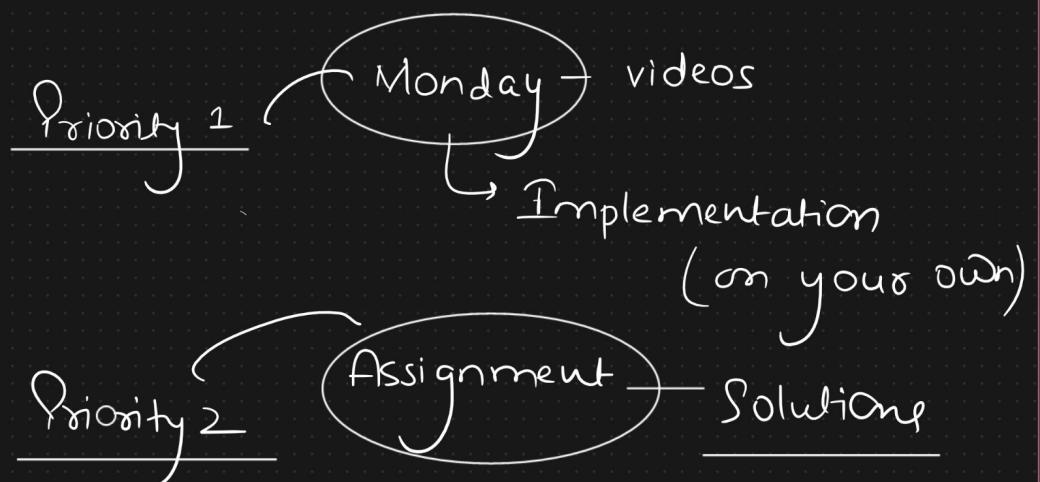
$$2B_c = 0$$

Row major form
 Row major form



$$1000 + \left(\frac{(1-0)*3}{3} + \frac{(1-0)}{1} \right) * 4$$

$$1000 + (4*4) = 1016$$



GP Series

$$O(4n) = O(n)$$

Common ratio

$$r > 1$$

$$r < 1$$

Sum of GP
series

$$\left(1 + mc - c \right) \quad O(n)$$

90% clockwise

Input matrix

$$\begin{matrix} 0 & 1 & 2 \\ 0 & \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix} \\ 1 & \\ 2 & \end{matrix} \quad \begin{matrix} \text{Output} \\ \begin{bmatrix} 7 & 4 & 1 \\ 8 & 5 & 2 \\ 9 & 6 & 3 \end{bmatrix} \end{matrix}$$

Step 1 → transpose

$$\left\{ \begin{array}{l} l_1 = 0 \\ k_1 = 2 \end{array} \right.$$
$$\begin{matrix} 0 & 1 & 2 \\ 0 & \begin{bmatrix} 1 & 4 & 7 \\ 8 & 5 & 8 \\ 3 & 6 & 9 \end{bmatrix} \\ 1 & \\ 2 & \end{matrix} \rightarrow \begin{matrix} 0 & 1 & 2 \\ 0 & \begin{bmatrix} 1 & 4 & 1 \\ 8 & 5 & 2 \\ 9 & 6 & 3 \end{bmatrix} \\ 1 & \\ 2 & \end{matrix}$$

$i = 0 \quad i = 1 \quad i = 2$

Map ($\alpha_{\sigma(i)}(l_i), \alpha_{\sigma(i)}(k_i)$)

$$\left\{ \begin{array}{l} l_i = 1 \\ k_i = 1 \end{array} \right.$$

$$0 \begin{pmatrix} 1 & 2 & 3 & 4 \\ 5 & 6 & 7 & 8 \end{pmatrix}_{2 \times 4}$$

$$\begin{pmatrix} 5 & 1 \\ 6 & 2 \\ 7 & 3 \\ 8 & 4 \end{pmatrix}_{4 \times 2} \quad \text{final output}$$

$l_i \quad q_i$

final result

$0 \begin{pmatrix} 5 & 5 \\ 6 & 6 \\ 7 & 7 \\ 8 & 8 \end{pmatrix}$

$l_i = 1$ while ($l_i < q_i$)

$l_i = 0$ $\left\{ \begin{array}{l} \text{swap} \\ \text{arr}(i)(l_i) \\ \text{arr}(i)(q_i) \end{array} \right.$

$$l_i = l_i + 1$$

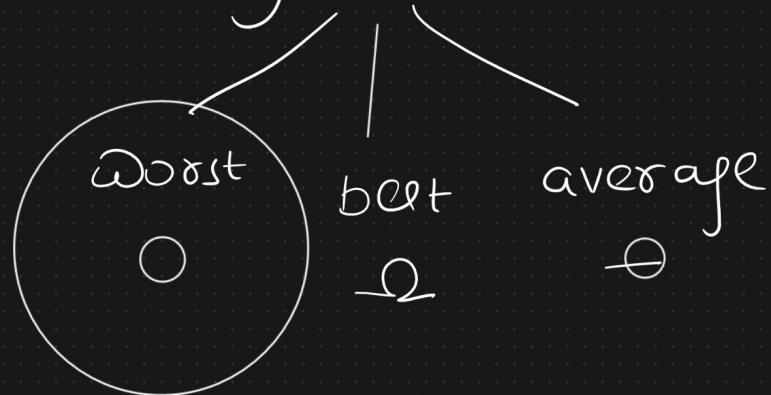
$$q_i = q_i - 1$$

transpose

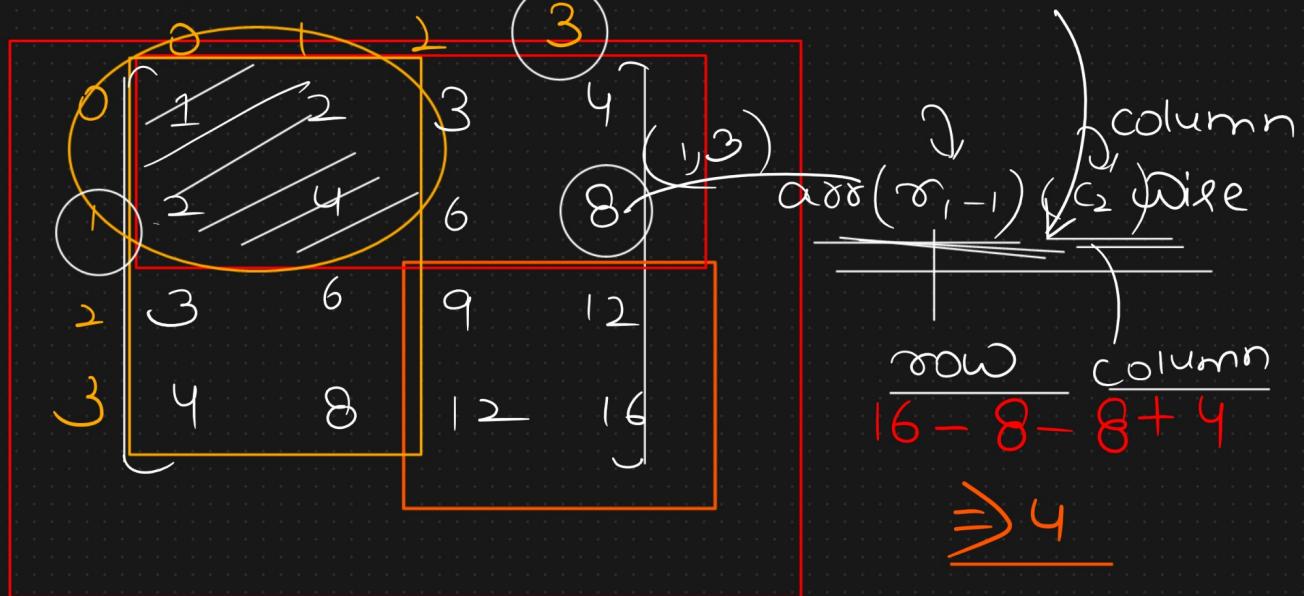
$\begin{pmatrix} 1 & 2 & 3 & 4 \\ 5 & 6 & 7 & 8 \end{pmatrix} \rightarrow \begin{pmatrix} 1 & 5 \\ 2 & 6 \\ 3 & 7 \\ 4 & 8 \end{pmatrix}$

$$\begin{bmatrix} 1 & 2 & 3 & 4 \\ 5 & 6 & 7 & 8 \end{bmatrix} \xrightarrow{\text{Transpose}} \begin{bmatrix} 1 & 5 \\ 2 & 6 \\ 3 & 7 \\ 4 & 8 \end{bmatrix}$$

Asymptotic Notations



$$\begin{array}{c}
 \begin{array}{ccccc}
 & 0 & 1 & 2 & 3 \\
 \begin{array}{c} 0 \\ 1 \\ 2 \\ 3 \end{array} & \left\{ \begin{array}{ccccc} 1 & \frac{1}{1} & 1 & 1 \\ 1 & 1 & 1 & \textcircled{1} \\ 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & \textcircled{1} \end{array} \right\} & \xrightarrow{\quad} & \left\{ \begin{array}{ccccc} 1 & \frac{1}{2} & \frac{2}{3} & \frac{3}{4} \\ 1 & 2 & 3 & 4 \\ 1 & 2 & 3 & 4 \\ 1 & 2 & 3 & 4 \end{array} \right\}
 \end{array}
 \end{array}$$



$$k_1 = 2 \quad c_1 = 2$$

$$k_2 = 3 \quad c_2 = 3$$

