Session Objectives

- 1. ### What is Regression
- ### Types of Regressions
- ### What is Linear Regression
- ### Applying Linear Regression to Head-Brain Dataset

1. What is Regression

Regression Function: a mathematical relationship enabling us to predict what values of one variable (Y) correspond to given values of another variable (X).

- Y: is referred to as the *dependent variable, the response variable or the predicted variable*.
- X: is referred to as the *independent variable, the explanatory variable or the predictor variable*

Thus Regression analysis is a form of predictive modelling technique which investigates the relationship between a dependent and independent variable.

2. Types of Regressions

- · Linear Regression
- · Logistic Regression
- Polynomial Regression

3. What is Linear Regression?

Linear Regression Theory

The term "linearity" in algebra refers to a linear relationship between two or more variables. If we draw this relationship in a two-dimensional space (between two variables), we get a straight line.

Linear regression performs the task to predict a dependent variable value (y) based on a given independent variable (x). So, this regression technique finds out a linear relationship between x (input) and y(output). Hence, the name is Linear Regression. If we plot the independent variable (x) on the x-axis and dependent variable (y) on the y-axis, linear regression gives us a straight line that best fits the data points, as shown in the figure below.



The equation of the above line is:



Where β_0 is the intercept and β_1 is the slope of the line. So basically, the linear regression algorithm gives us the most optimal value for the intercept and the slope (in two dimensions). The Y_i and X_i variables remain the same, since they are the data features and cannot be changed. The values that we can control are the intercept(β_0) and slope(β_1).

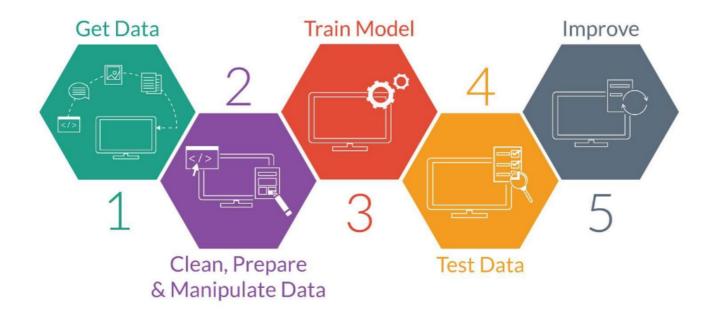
There can be multiple straight lines depending upon the values of intercept and slope. Basically what the linear regression algorithm does is it fits multiple lines on the data points and returns the line that results in the least error.

Linear Regression is one of the most simple yet widely used statistical Machine Learning technique. The linear regression machine learning algorithm tries to map one or more independent variable (features) to a dependent variable (scalar output). In this session, you will be learning about:

- Different types of linear regression in machine learning.
- A bit of statistics/mathematics behind it.
- And what kind of problems you can solve with linear regression.

4. Applying Linear Regression to Head-Brain Dataset

The below steps should be consider while applying any machine learning algorithm



Step 1: Get the Data

In [1]:

```
import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
import seaborn as sns
```

In [2]:

```
brain_df = pd.read_csv('datasets/headbrain.csv')
brain_df.head()
```

Out[2]:

	Gender	Age Range	Head Size(cm^3)	Brain Weight(grams)
0	1	1	4512	1530
1	1	1	3738	1297
2	1	1	4261	1335
3	1	1	3777	1282
4	1	1	4177	1590

Step 2: Clean Prepare and Manipulate Data

In [3]:

```
# Checking dimensionality of the Head Brain DataFrame brain_df.shape
```

Out[3]:

(237, 4)

By above output we can say there are total 237 rows and 4 columns

In [4]:

```
# printing information about Head Brain dataframe
brain_df.info()
```

```
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 237 entries, 0 to 236
Data columns (total 4 columns):
```

Gender 237 non-null int64
Age Range 237 non-null int64
Head Size(cm^3) 237 non-null int64
Brain Weight(grams) 237 non-null int64

dtypes: int64(4)
memory usage: 7.5 KB

In [5]:

```
# Checking for missing data in the Head Brain dataframe
brain_df.isnull().sum()
```

Out[5]:

Gender 0
Age Range 0
Head Size(cm^3) 0
Brain Weight(grams) 0

dtype: int64

By above info we can say that there is no missing data in our dataframe

In [6]:

```
# Checking for any duplicate values in the Head Brain dataframe
brain_df.duplicated().sum()
```

Out[6]:

0

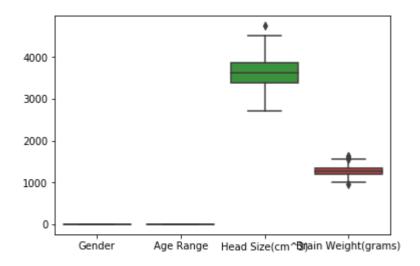
By above info we can say that there are no duplicate values

In [7]:

```
sns.boxplot(data = brain_df)
```

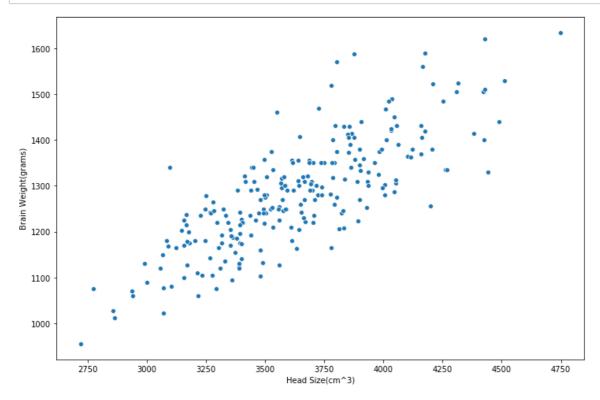
Out[7]:

<matplotlib.axes._subplots.AxesSubplot at 0x24ac2596978>



In [8]:

```
plt.figure(figsize=(12,8))
sns.scatterplot(x=brain_df['Head Size(cm^3)'],y=brain_df['Brain Weight(grams)'])
plt.show()
```



By obseving the above scatter plot Head Size vs Brain Weight are linearly coorelated so we take as the **Head Size as independent variable** and **Brain Weight as dependent variable** or target variable.

Step 3: Train the Model

Method 1: Linear Regression Model using Mathematical

In [9]:

```
X = brain_df['Head Size(cm^3)'].values
Y = brain_df['Brain Weight(grams)'].values
```

$$Y = MX + C$$

We have to find the intercept eta_0 or C and Slope eta_1 or M by using below formula

$$SlopeM = \sum_{i=0}^{len(X)} rac{(X_i - X_{mean}) * (Y_i - Y_{mean})}{(X_i - X_{mean})^2}$$

In [10]:

```
x_mean = X.mean()
y_mean = Y.mean()

n = len(X)
num = 0
den = 0

for i in range(n):
    num += (X[i] - x_mean) * (Y[i] - y_mean)
    den += (X[i] - x_mean) ** 2

M = (num) / (den)
print("Slope M: ",M)

C = y_mean - M * x_mean
print('X_Intercept C: ',C)
```

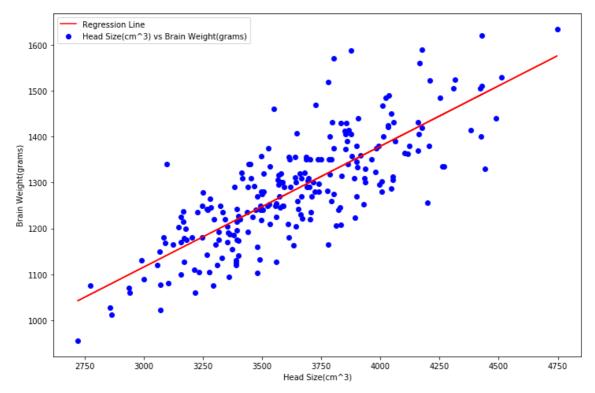
Slope M: 0.26342933948939945 X_Intercept C: 325.57342104944223

In [11]:

```
y_pred = M * X + C # Calculating predicted values
```

In [12]:

```
plt.figure(figsize=(12,8))
plt.scatter(X,Y,label = 'Head Size(cm^3) vs Brain Weight(grams)',color = 'b') # Plottin
g scatter plot
plt.plot(X,y_pred,'r',label='Regression Line') # Plotting the Regressing by using X and
predicted values
plt.xlabel('Head Size(cm^3)')
plt.ylabel('Brain Weight(grams)')
plt.legend()
plt.show()
```



This model is not so bad. But we need to find how good is our model. There are many methods to evaluate models. We will use Root Mean Squared Error and Coefficient of Determination

Calculating Coefficient of Determination (\mathbb{R}^2)

It is the mean of the squared errors and is calculated as:

$$R^2 = \sum_{i=0}^{len(Y)} rac{(Y_{Predicted} - Y_{mean})^2}{(Y_i - Y_{mean})^2}$$

 ${\cal R}^2$ is the total sum of squares and total sum of squares of residuals.

 R^2 Score usually range from 0 to 1. It will also become negative if the model is completely wrong. Now we will find R^2 Score.

In [13]:

```
num = 0
den = 0
for i in range(n):
    y_pred = M * X[i] + C
    num += ((y_pred - y_mean) ** 2)
    den += ((Y[i] - y_mean) ** 2)
R_2 = num/den
print('Coefficient of Determination R^2 is:',R_2)
```

Coefficient of Determination R^2 is: 0.6393117199570001

0.63 is not so bad. So Now we have Sucessfully implemented Simple Linear Regression Model using Ordinary Least Square Method.

Calculating Root Mean Squared Error (RMSE)

Root Mean Squared Error is the square root of sum of all errors divided by number of values, or Mathematically,

$$RMSE = \sum_{i=0}^{len(Y)} \sqrt{rac{\left(Y_{Pred} - Y_{mean}
ight)^2}{len(X)}}$$

Here y_{pred} is the predicted output values.

In [14]:

```
# Calculating Root Mean Squares Error
rmse = 0
for i in range(n):
    y_pred = C + M * X[i]
    rmse += (Y[i] - y_pred) ** 2
rmse = np.sqrt(rmse/n)
print('Root Mean Squares Error is:',rmse)
```

Root Mean Squares Error is: 72.1206213783709

Step 4: Test the Model

```
In [15]:
```

```
test = M * 4512 + C
print('Tested Head size value 4512 using our Linear Regression model is:',test)
print('Actual value for Head size 4512 is:',1530)
```

Tested Head size value 4512 using our Linear Regression model is: 1514.166 6008256125

Actual value for Head size 4512 is: 1530

Step 5: Improve the Model

We can improve our model by using other algorithms we discussing comming sessions

Method 2: Linear Regression Model using Sklearn

In [16]:

```
brain_df = pd.read_csv('datasets/headbrain.csv')
brain_df.head()
```

Out[16]:

	Gender	Age Range	Head Size(cm^3)	Brain Weight(grams)
0	1	1	4512	1530
1	1	1	3738	1297
2	1	1	4261	1335
3	1	1	3777	1282
4	1	1	4177	1590

In [17]:

```
X = brain_df['Head Size(cm^3)'].values
Y = brain_df['Brain Weight(grams)'].values
```

In [18]:

```
from sklearn.linear_model import LinearRegression
from sklearn.metrics import mean_squared_error
```

In [19]:

```
# Cannot use Rank 1 matrix in scikit learn
X = X.reshape((len(X), 1))

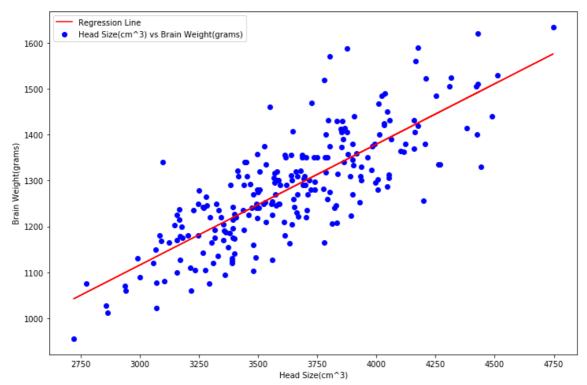
# Creating Model
reg = LinearRegression()

# Fitting training data
reg = reg.fit(X, Y)

# Y Prediction
Y_pred = reg.predict(X)
```

In [20]:

```
plt.figure(figsize=(12,8))
plt.scatter(X,Y,label = 'Head Size(cm^3) vs Brain Weight(grams)',color = 'b') # Plottin
g scatter plot
plt.plot(X,Y_pred,'r',label='Regression Line') # Plotting the Regressing by using X and
predicted values
plt.xlabel('Head Size(cm^3)')
plt.ylabel('Brain Weight(grams)')
plt.legend()
plt.show()
```



In [21]:

```
# Calculating RMSE and R2 Score
mse = mean_squared_error(Y, Y_pred)
rmse = np.sqrt(mse)
print('Root Mean Squares Error is:',np.sqrt(mse))
```

Root Mean Squares Error is: 72.1206213783709

In [22]:

```
r2_score = reg.score(X, Y)
print('Coefficient of Determination R^2 is:',r2_score)
```

Coefficient of Determination R^2 is: 0.639311719957

You can see that this exactly equal to model we built from scratch, but simpler and less code