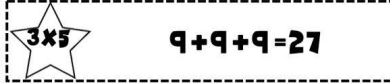
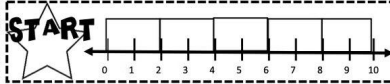
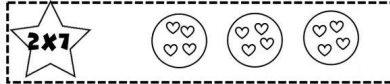
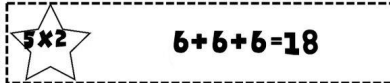
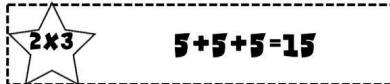
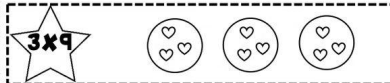
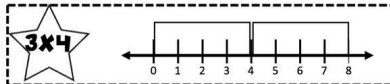


**ARRAYS, NUMBER LINES AND
EQUAL GROUPS**

Cut out each strip below. Glue the start strip in the top rectangle to the left. Then solve the problem on that strip. Next, find the strip with the answer in the star. Glue that one in the next rectangle. Continue until you have arrived at the "finish" strip.



Minimum Replacements to Sort the Array

In this presentation, we'll explore a greedy approach to the problem of sorting an unsorted array by replacing elements with a sum of two elements. We'll discuss the key steps, analyze the time complexity, and explore the limitations of this approach.

The Greedy Approach

The greedy approach to this problem involves repeatedly replacing the largest unsorted element with the sum of two smaller elements. This ensures that the array is sorted in non-decreasing order with the minimum number of operations.

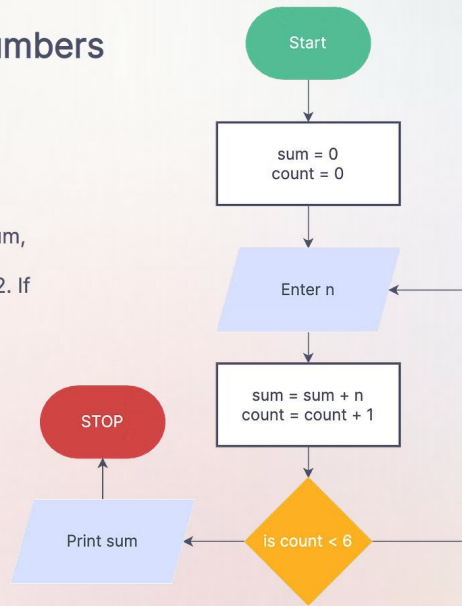
The word "GREEDY" is displayed in a stylized font where each letter is contained within a bright green circle. These circles are connected by a thin, light gray horizontal line, creating a modern, digital aesthetic.

Greedy Algorithms

Key Steps in the Greedy Approach

Find the sum of 6 numbers algorithm

1. Initialize sum = 0 and count = 0
2. Enter n
3. Find sum + n and assign it to sum, then increment count by 1.
4. Is count < 6. If YES, go to step 2. If No, print sum.



1

Identify Largest Unsorted Element

Find the largest element in the unsorted portion of the array.

2

Replace with Sum of Two Elements

Replace the largest unsorted element with the sum of two smaller elements that add up to the original element.

3

Repeat Until Sorted

Continue this process until the array is completely sorted in non-decreasing order.

Example: Sorting [3, 9, 3]

Initial Array

The initial array is [3, 9, 3].

Replace 9 with 3 and 6

The array becomes [3, 3, 6, 3].

Replace 6 with 3 and 3

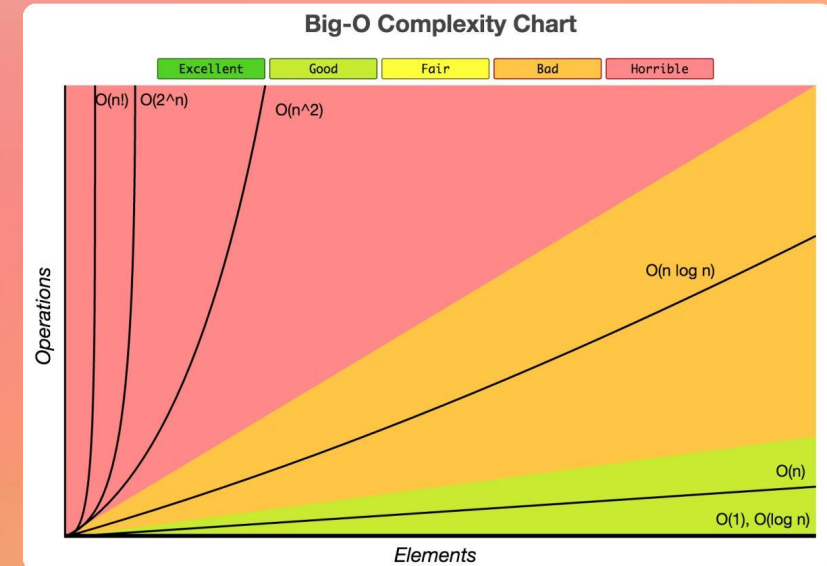
The final sorted array is [3, 3, 3, 3, 3].

Time Complexity Analysis

1 Finding Largest Unsorted Element
 $O(n)$ time, where n is the length of the array.

2 Replacing with Two Elements
 $O(1)$ time for each replacement.

3 Overall Time Complexity
 $O(n^2)$ time, as the algorithm performs n replacements, each taking $O(1)$ time.



Example: Sorting [5, 6, 7]



1

Initial Array

The initial array is [5, 6, 7].

2

Replace 7 with 3 and 4

The array becomes [5, 6, 3, 4].

3

Replace 6 with 3 and 3

The final sorted array is [5, 3, 3, 3, 4].

Disadvantages of Algorithms

Limitations and Edge Cases

Negative Numbers

The greedy approach may not work well with negative numbers, as replacing a negative element with two positive elements may not lead to a sorted array.

Duplicate Elements

If the array contains many duplicate elements, the greedy approach may not be the most efficient solution, as it may require more replacements.

Array with a Single Element

For an array with a single element, the greedy approach is not applicable, as there are no elements to replace.

Conclusion and Future Directions



Summary

The greedy approach to sorting an array by replacing elements with the sum of two elements can be effective in many cases, but has its limitations. Exploring alternative approaches and optimizing the algorithm further could lead to more efficient solutions.



Future Directions

Potential areas for further research include developing dynamic programming or divide-and-conquer solutions, analyzing the performance of the greedy approach on different input distributions, and exploring the tradeoffs between time complexity and the number of replacements required.



THANK YOU