

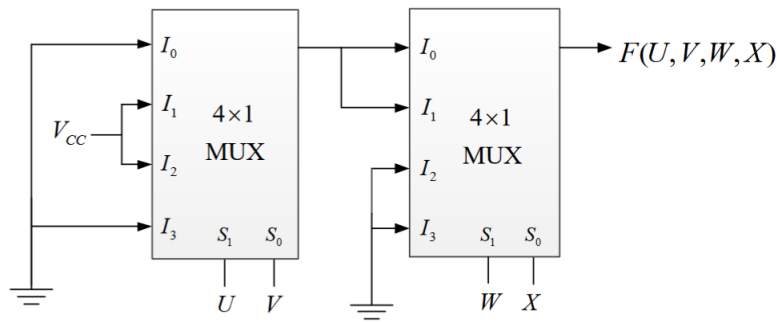
# Digital Logic Design Assignment 9 - EC2018-31

Priyansh Agrahari

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## 1 Question:

A four-variable Boolean function is realized using 4x1 multiplexers as shown in the figure:



The minimized expression for  $F(U, V, W, X)$  is

- (A)  $(U V + \overline{U} \overline{V}) \overline{W}$
- (B)  $(U V + \overline{U} \overline{V}) (\overline{W} \overline{X} + \overline{W} X)$
- (C)  $(U \overline{V} + \overline{U} V) \overline{W}$
- (D)  $(U \overline{V} + \overline{U} V) (\overline{W} \overline{X} + \overline{W} X)$

## 2 Solution:

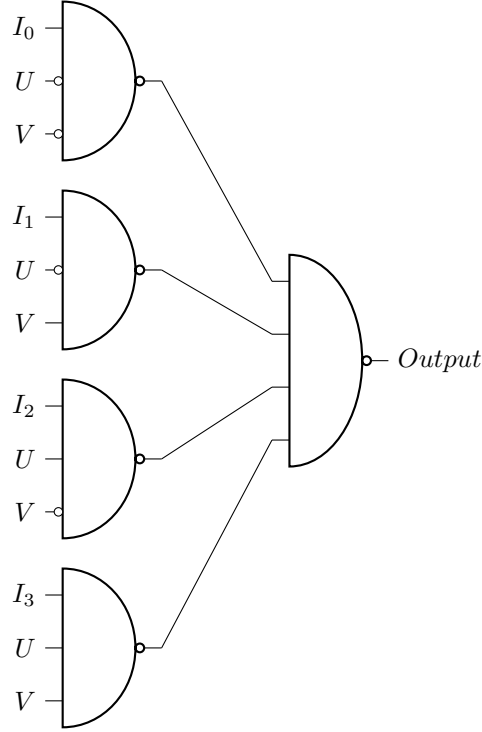


Figure 1: *Logic circuit equivalent of 4x1 MUX used to solve this problem*

Since we have  $I_0$  and  $I_3$  grounded, we can take their boolean equivalents to be 0. Then, we get the following equation:

$$Output = \overline{(U + \bar{V})(\bar{U} + V)} \quad (1)$$

which can be further simplified (using de Morgan's law) to obtain:

$$Output = U\bar{V} + \bar{U}V \quad (2)$$

Moving further, the same logic can be used to obtain the result of the second MUX. Since in this case,  $I_2$  and  $I_3$  are grounded; hence by taking their boolean equivalents to be 0, we get the following equation from the second MUX:

$$F = \overline{\overline{(Output.\bar{W}.X)}.(Output.\bar{W}.X)} \quad (3)$$

simplifying, we get:

$$F = Output.\bar{W}.\bar{X} + Output.\bar{W}.X \quad (4)$$

after placing the value of *Output* from eq.(2), and performing a few more manipulations, we get:

$$F = (U\bar{V} + \bar{U}V)\bar{W}(X + \bar{X}) \quad (5)$$

Since  $X + \bar{X} = 1$ , we finally get the desired equation:

$$F = (U\bar{V} + \bar{U}V)\bar{W} \quad (6)$$

Hence, the answer the given question is (C).

### 3 Truth Table

$U$	$V$	$W$	$X$	$F$	Term
0	0	0	0	0	-
0	0	0	1	0	-
0	0	1	0	0	-
0	0	1	1	0	-
0	1	0	0	1	$\bar{U} V \bar{W} \bar{X}$
0	1	0	1	1	$\bar{U} V \bar{W} X$
0	1	1	0	0	-
0	1	1	1	0	-
1	0	0	0	1	$U \bar{V} \bar{W} \bar{X}$
1	0	0	1	1	$U \bar{V} \bar{W} X$
1	0	1	0	0	-
1	0	1	1	0	-
1	1	0	0	0	-
1	1	0	1	0	-
1	1	1	0	0	-
1	1	1	1	0	-

Table 1: Truth Table for eq.(6)

#### 4 K-map for the function F(U,V,W,X)

		UV			
		00	01	11	10
WX	00	0	1	0	1
	01	0	1	0	1
	11	0	0	0	0
	10	0	0	0	0

The expression obtained using the K-map is the same as the one obtained earlier in eq.(6). Alternatively, we can also make a K-map for obtaining the POS expression:

		UV			
		00	01	11	10
WX	00	0	1	0	1
	01	0	1	0	1
	11	0	0	0	0
	10	0	0	0	0

The POS expression hence obtained is:

$$F = (U + V)(\bar{U} + \bar{V})\bar{W} \quad (7)$$

## 5 C implementation to verify Table 1

### 5.1 C code:

```
1 #include <stdio.h>
2 int main(void)
3 {
4     unsigned char U = 0x00, V = 0x01, W = 0x00, X = 0x00;
5     unsigned char F, one = 0x01;
6
7     F = (~W) & ( (U & (~V)) | ((~U) & V) );
8     printf("Using SOP form: F = %x\n", (F & one));
9
10    F = (U | V) & ((~U) | (~V)) & (~W);
11    printf("Using POS form: F = %x\n", (F & one));
12 }
```

### 5.2 Output:

```
1 Using SOP form: F = 1
2 Using POS form: F = 1
```

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