# **Document Ranking Approaches for Query Relevance**

# 1. Introduction

In information retrieval, accurately ranking documents based on user queries is essential to deliver relevant information efficiently.

In this report, we compare three models applied for ranking: the `all-MiniLM-L6-v2` model, Latent Semantic Indexing (LSI),

and a probabilistic model with iterative refinement. We examine each model's approach, formulas, and impact on results.

#### 2.A all-MiniLM-L6-v2 Model

Model: all-MiniLM-L6-v2

Definition: A transformer-based language model that generates embeddings for text.

It captures semantic similarities in high-dimensional space. Each document and query are encoded into

vectors.

Purpose: Embeddings represent the text in a way that captures context and meaning, allowing cosine

similarity to rank documents.

Application: Documents are ranked based on cosine similarity between the encoded document and query

vectors.

#### 2.B Latent Semantic Indexing (LSI)

Model: Latent Semantic Indexing (LSI)

Definition: A dimensionality reduction technique using Singular Value Decomposition (SVD)

to capture latent relationships between terms and documents.

Formula: SVD decomposes the TF-IDF matrix (A) into  $(A = U \times V^T)$ , where:

- \( U \): Left singular vectors (document-topic relationships)
- \( \Sigma \): Singular values (importance of each topic)
- \( V^T \): Right singular vectors (topic-term relationships)

Purpose: Reduces the vocabulary space by retaining only the top singular values, capturing the most significant patterns.

Application: Documents and queries are transformed into a lower-dimensional space, with similarity measured in this latent space.

# 2.C Probabilistic Model with Iterative Refinement

Model: Probabilistic Model with Iterative Refinement

Definition: A ranking model that uses probabilities

to weigh the relevance of terms based on their occurrence in relevant and non-relevant documents.

#### Relevance Formula:

- $(P(t_i | R) = \frac{V_i + 0.5}{V + 1})$
- $(P(t_i | NR) = \frac{n_i V_i + 0.5}{N V + 1})$

Purpose: Iteratively refines term relevance by updating probabilities based on a selected subset of ranked documents.

Application: For each query, calculates similarity using a weighted log-odds formula. Updates probabilities to enhance accuracy with each query.

# 3. Comparison of Methods

Model	Characteristics	Pros	Cons
	I		
all-MiniLM-L	_6-v2   Transformer-base	ed embeddings capturing semar	ntics   Captures deep context,
adaptable for	similarity ranking   Requires GI	PU for speed, embeddings can be	high-dimensional
LSI	Latent space, reduces noi	se   Captures term de	ependencies, effective for large
corpora   Sen	sitive to parameter choice, may	lose term specificity	
Probabilistic	Model   Iterative probability-	based relevance scoring   Dyna	amically improves with queries,
considers rele	evance   Computationally intens	sive, sensitive to initial scores	

#### 4. Influence on Results

Influence on Results:

- \*\*all-MiniLM-L6-v2\*\*: Provides embeddings that capture semantic relationships in context, allowing for more accurate similarity rankings in high-dimensional space.

However, embeddings are computationally intensive and best suited for GPU environments.

- \*\*LSI\*\*: Reduces dimensionality by capturing latent topics, improving results when terms are not direct matches but semantically related.

May introduce noise if too many dimensions are retained.

- \*\*Probabilistic Model\*\*: Adapts dynamically, refining accuracy over time as relevance probabilities are adjusted based on feedback from prior queries.

This model is advantageous in evolving search scenarios but requires additional computation.

# 5. Conclusion

Each model offers unique strengths: all-MiniLM-L6-v2 is best for capturing deep semantic similarity, LSI aids in capturing

latent meaning, and the probabilistic model provides a dynamically refined ranking approach. Combining these methods may yield optimal relevance and adaptability in complex and evolving corpora.