COL215 Hardware Assignment 3

Submission Deadlines: [PART 1: 26th October 2024]

1 Introduction

The objective of the assignment is: **implementation of AES decryption operation**. The components involved are memory elements (RAM, ROM and registers) and logical unit.

Please note that the diagrams in this document are for illustration purposes and explanation of the problem statement. They do not represent the exact design to be implemented. Design choices can vary across groups and should be carefully explained in the assignment report.

2 Problem Description

Given a cipher text and a key, your task is to perform an AES decryption operation to display plain text on 7-seven display. An overview of the problem is shown in Figure 1.

Figure 1: Overview of task: Decryption



- Input cipher text is of the size in multiples of 128 bits and will be provided in the COE file (8 bit binary unsigned). The input file should be stored in 1-D array format in the block RAM, starting from address 0 (0000₁₆) in row major format.
- Key will be provided via the COE file. All the round keys will be provided in the COE file.

You are allowed to use VHDL modules from previous hardware assignments.

In the Part I of the assignment, the objective will be to design and implement the following modules:

- 1. Memories (RAM/ROM)
- 2. Logical operations in AES decryption

Primary focus will be on designing the individual components. You are not required to connect these modules.

3 Basics of AES Encryption/Decryption

The Advanced Encryption Standard (AES) is a symmetric encryption algorithm that encrypts and decrypts data in blocks of 128 bits using keys of 128, 192, or 256 bits. The AES algorithm consists of several rounds, depending on the key size. Each round includes a series of transformations applied to the data.

The decryption process mirrors the encryption process but with inverse operations. Below is a step-by-step explanation of both encryption and decryption operations. You can refer to the animation AES Rijndael Cipher explained as a Flash animation to understand more about the encryption and decryption process.

3.1 AES Encryption

AES encryption consists of the following steps:

- **Key Expansion**: The encryption key is expanded into an array of key schedule words (round keys), which will be used in the different rounds of encryption.
- Initial Round:
 - AddRoundKey: The state is combined with the round key using a bitwise XOR operation.
- Main Rounds (We are considering 8 rounds):
 - **SubBytes**: A non-linear substitution step where each byte in the state is replaced with its corresponding value from a fixed lookup table S-box (3.2).
 - ShiftRows: This is a transposition step where each row of the state matrix is shifted cyclically by a specific number of positions to the left. The first row remains unchanged, the second row is shifted by one position, the third by two, and the fourth by three positions.
 - This ensures that the columns of the state are mixed and that data from different columns interacts with each other in the following rounds, which improves diffusion across the state.
 - MixColumns: In this step, each column of the state matrix is treated as a polynomial and multiplied by a fixed polynomial over the Galois Field $GF(2^8)$. This operation mixes the bytes within each column, ensuring that the output bytes of a column are linear combinations of the input bytes. This step also increases diffusion by ensuring that even small changes in the input propagate throughout the entire column in subsequent rounds.
 - AddRoundKey: The state is again combined with a round key derived from the main key.
- Final Round (without MixColumns):
 - SubBytes, ShiftRows, AddRoundKey.

The flow of encryption is depicted in Figure 2. Please note that we are using the standard AES-128 protocol with 8 rounds instead of 10.

3.2 AES Decryption

AES decryption reverses the encryption process by applying the inverse operations in the reverse order:

- Key Expansion: The same key expansion process used in encryption is performed.
- Initial Round:
 - AddRoundKey: The state is combined with the round key using a bitwise XOR operation.
- Main Rounds (We are considering 8 rounds):
 - InvShiftRows: This is the inverse of the ShiftRows operation from encryption. Each row of the state is shifted cyclically to the right by a certain number of positions. The first row remains unchanged, the second row is shifted by one position to the right, the third by two, and the fourth by three. This restores the original row arrangement, undoing the transposition from the encryption phase.
 - InvSubBytes: In this step, each byte in the state is replaced by its inverse value from the inverse S-box (3.2). This reverses the non-linear substitution performed in the encryption's SubBytes step, effectively restoring the original byte values before substitution.
 - AddRoundKey: The state is again combined with a round key using a bitwise XOR operation. This step mirrors the encryption process, except the round keys are applied in reverse order.

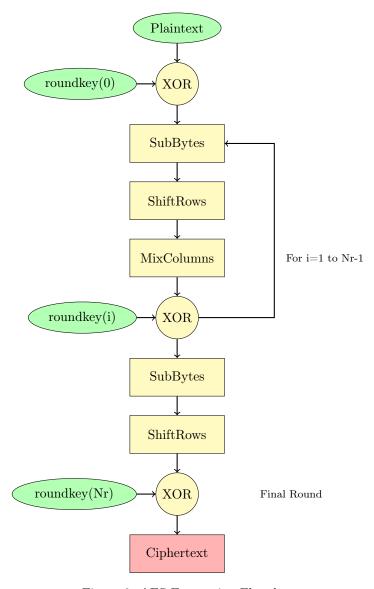


Figure 2: AES Encryption Flowchart

- InvMixColumns: This step reverses the effect of MixColumns. Each column is treated as a polynomial and multiplied by the inverse fixed polynomial in the Galois Field $GF(2^8)$, effectively undoing the mixing operation and restoring the original byte arrangement within each column.
- Final Round (without InvMixColumns):
 - InvShiftRows, InvSubBytes, AddRoundKey.

The flow of decryption is depicted in Figure 3.

```
SBOX = [
    [0x63, 0x7c, 0x77, 0x7b, 0xf2, 0x6b, 0x6f, 0xc5, 0x30, 0x01, 0x67, 0x2b, 0xfe, 0xd7, 0xab, 0x76],
    [0xca, 0x82, 0xc9, 0x7d, 0xfa, 0x59, 0x47, 0xf0, 0xad, 0xd4, 0xa2, 0xaf, 0x9c, 0xa4, 0x72, 0xc0],
    [0xb7, 0xfd, 0x93, 0x26, 0x36, 0x3f, 0xf7, 0xcc, 0x34, 0xa5, 0xe5, 0xf1, 0x71, 0xd8, 0x31, 0x15],
    [0x04, 0xc7, 0x23, 0xc3, 0x18, 0x96, 0x05, 0x9a, 0x07, 0x12, 0x80, 0xe2, 0xeb, 0x27, 0xb2, 0x75],
    [0x09, 0x83, 0x2c, 0x1a, 0x1b, 0x6e, 0x5a, 0xa0, 0x52, 0x3b, 0xd6, 0xb3, 0x29, 0xe3, 0x2f, 0x84],
    [0x53, 0xd1, 0x00, 0xed, 0x20, 0xfc, 0xb1, 0x5b, 0x6a, 0xcb, 0xbe, 0x39, 0x4a, 0x4c, 0x58, 0xcf],
    [0xd0, 0xef, 0xaa, 0xfb, 0x43, 0x4d, 0x33, 0x85, 0x45, 0xf9, 0x02, 0x7f, 0x50, 0x3c, 0x9f, 0xa8],
    [0x51, 0xa3, 0x40, 0x8f, 0x92, 0x9d, 0x38, 0xf5, 0xbc, 0xb6, 0xda, 0x21, 0x10, 0xff, 0xf3, 0xd2],
    [0xcd, 0x0c, 0x13, 0xec, 0x5f, 0x97, 0x44, 0x17, 0xc4, 0xa7, 0x7e, 0x3d, 0x64, 0x5d, 0x19, 0x73],
    [0x60, 0x81, 0x4f, 0xdc, 0x22, 0x2a, 0x90, 0x88, 0x46, 0xee, 0xb8, 0x14, 0xde, 0x5e, 0x0b, 0xdb],
    [0xe0, 0x32, 0x3a, 0x0a, 0x49, 0x06, 0x24, 0x5c, 0xc2, 0xd3, 0xac, 0x62, 0x91, 0x95, 0xe4, 0x79],
    [0xe7, 0xc8, 0x37, 0x6d, 0x8d, 0xd5, 0x4e, 0xa9, 0x6c, 0x56, 0xf4, 0xea, 0x65, 0x7a, 0xae, 0x08],
    [0xba, 0x78, 0x25, 0x2e, 0x1c, 0xa6, 0xb4, 0xc6, 0xe8, 0xdd, 0x74, 0x1f, 0x4b, 0xbd, 0x8b, 0x8a],
    [0x70, 0x3e, 0xb5, 0x66, 0x48, 0x03, 0xf6, 0x0e, 0x61, 0x35, 0x57, 0xb9, 0x86, 0xc1, 0x1d, 0x9e],
    [Oxe1, Oxf8, Ox98, Ox11, Ox69, Oxd9, Ox8e, Ox94, Ox9b, Ox1e, Ox87, Oxe9, Oxce, Ox55, Ox28, Oxdf],
    [0x8c, 0xa1, 0x89, 0x0d, 0xbf, 0xe6, 0x42, 0x68, 0x41, 0x99, 0x2d, 0x0f, 0xb0, 0x54, 0xbb, 0x16]
```

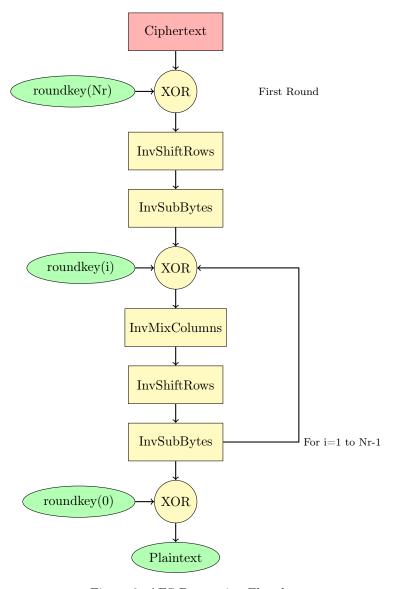


Figure 3: AES Decryption Flowchart

```
INV\_SBOX = [
    [0x52, 0x09, 0x6a, 0xd5, 0x30, 0x36, 0xa5, 0x38, 0xbf, 0x40, 0xa3, 0x9e, 0x81, 0xf3, 0xd7, 0xfb],
    [0x7c, 0xe3, 0x39, 0x82, 0x9b, 0x2f, 0xff, 0x87, 0x34, 0x8e, 0x43, 0x44, 0xc4, 0xde, 0xe9, 0xcb],
    [0x54, 0x7b, 0x94, 0x32, 0xa6, 0xc2, 0x23, 0x3d, 0xee, 0x4c, 0x95, 0x0b, 0x42, 0xfa, 0xc3, 0x4e],
    [0x08, 0x2e, 0xa1, 0x66, 0x28, 0xd9, 0x24, 0xb2, 0x76, 0x5b, 0xa2, 0x49, 0x6d, 0x8b, 0xd1, 0x25],
    [0x72, 0xf8, 0xf6, 0x64, 0x86, 0x88, 0x98, 0x16, 0x44, 0x44, 0x5c, 0xcc, 0x5d, 0x65, 0xb6, 0x92],
    [0x6c, 0x70, 0x48, 0x50, 0xfd, 0xed, 0xb9, 0xda, 0x5e, 0x15, 0x46, 0x57, 0xa7, 0x8d, 0x9d, 0x84],
    [0x90, 0xd8, 0xab, 0x00, 0x8c, 0xbc, 0xd3, 0x0a, 0xf7, 0xe4, 0x58, 0x05, 0xb8, 0xb3, 0x45, 0x06],
    [0xd0, 0x2c, 0x1e, 0x8f, 0xca, 0x3f, 0x0f, 0x02, 0xc1, 0xaf, 0xbd, 0x03, 0x01, 0x13, 0x8a, 0x6b],
    [0x3a, 0x91, 0x11, 0x41, 0x4f, 0x67, 0xdc, 0xea, 0x97, 0xf2, 0xcf, 0xce, 0xf0, 0xb4, 0xe6, 0x73],
    [0x96, 0xac, 0x74, 0x22, 0xe7, 0xad, 0x35, 0x85, 0xe2, 0xf9, 0x37, 0xe8, 0x1c, 0x75, 0xdf, 0x6e],
    [0x47, 0xf1, 0x1a, 0x71, 0x1d, 0x29, 0xc5, 0x89, 0x6f, 0xb7, 0x62, 0x0e, 0xaa, 0x18, 0xbe, 0x1b],
    [Oxfc, Ox56, Ox3e, Ox4b, Oxc6, Oxd2, Ox79, Ox20, Ox9a, Oxdb, Oxc0, Oxfe, Ox78, Oxcd, Ox5a, Oxf4],
    [0x1f, 0xdd, 0xa8, 0x33, 0x88, 0x07, 0xc7, 0x31, 0xb1, 0x12, 0x10, 0x59, 0x27, 0x80, 0xec, 0x5f],
    [0x60, 0x51, 0x7f, 0xa9, 0x19, 0xb5, 0x4a, 0x0d, 0x2d, 0xe5, 0x7a, 0x9f, 0x93, 0xc9, 0x9c, 0xef],
    [0xa0, 0xe0, 0x3b, 0x4d, 0xae, 0x2a, 0xf5, 0xb0, 0xc8, 0xeb, 0xbb, 0x3c, 0x83, 0x53, 0x99, 0x61],
    [0x17, 0x2b, 0x04, 0x7e, 0xba, 0x77, 0xd6, 0x26, 0xe1, 0x69, 0x14, 0x63, 0x55, 0x21, 0x0c, 0x7d]
]
```

3.2.1 Illustration of Decryption process

Following Figure 4 show the last round in decryption process, that is $InvMixColumns \rightarrow InvShiftRows \rightarrow InvSubBytes \rightarrow XOR$. The figure 4 shows the State and the corresponding operation involved. Kindly note, multiplication in the InvMixColumns is a $GF(2^8)$ (Not a decimal operation). We present an example for the steps

0E	0B	0D	09	
09	0E	0B	0D	
0D	09	0E	0B	
0B	0D	09	0E	

8B	0C	68	DA
42	70	43	4E
6D	30	00	D7
D5	1F	8A	EE

63	F9	5B	6F
A2	AA	12	63
67	63	6A	23
D7	63	82	82

(a) InvMixColumns operation

63	F9	5B	6F
A2	AA	12	63
67	63	6A	23
D7	63	82	82

 ${\bf InvRowShift}$

63	F9	5B	6F
63	A2	AA	12
6A	23	67	63
63	82	82	D7

(b) InvRowShift operation

63	F9	5B	6F
63	A2	AA	12
6A	23	67	63
63	82	82	D7

InvSubbytes

00	69	57	06
00	1A	62	39
58	32	0A	00
00	11	11	0D

(c) InvSubbytes operation

54	49	36	65
68	73	42	4B
31	41	79	65
73	31	74	79

 \oplus

00	69	57	06
00	1A	62	39
58	32	0A	00
00	11	11	0D

(d) XOR operation

Figure 4: Illustration to perform various operations in decryption

• First operation is **InvMixColumns**. It reverses the mixing of bytes performed during the encryption's MixColumns step.

The transformation uses Galois Field arithmetic in $GF(2^8)$, a finite field that allows operations on bytes (8-bit values). In $GF(2^8)$, bytes are treated as polynomials of degree less than 8, and multiplication is defined arithmetic modulo a specific irreducible polynomial, $x^8 + x^4 + x^3 + x + 1$. It is used in AES because it ensures that small changes in the input propagate through the entire ciphertext, providing strong diffusion.

In the InvMixColumns step, each column in the state matrix is transformed by multiplying each byte by a set of fixed constants: 0x0e, 0x0b, 0x0d, and 0x09, all in the Galois Field. These constants are derived from the inverse matrix of the MixColumns operation. (The multiplicative inverses of the constants 0x02, 0x03, and 0x01.)

MixColumns uses the matrix:

$$\begin{bmatrix} 02 & 03 & 01 & 01 \\ 01 & 02 & 03 & 01 \\ 01 & 01 & 02 & 03 \\ 03 & 01 & 01 & 02 \\ \end{bmatrix}$$

The $\bf Inverse\ MixColumns$ undoes the diffusion using the inverse matrix:

$$\begin{bmatrix} 0e & 0b & 0d & 09 \\ 09 & 0e & 0b & 0d \\ 0d & 09 & 0e & 0b \\ 0b & 0d & 09 & 0e \end{bmatrix}$$

The transformation for each byte is as follows, here c_0 , c_1 , c_2 , and c_3 represent the four bytes of a single column in the state:

- For the first byte of the column:

$$col[0] = xtimes_0e(c_0) \oplus xtimes_0b(c_1) \oplus xtimes_0d(c_2) \oplus xtimes_0g(c_3)$$

where each term represents multiplication by the respective constant in $GF(2^8)$, and \oplus represents bitwise XOR.

- For the second byte of the column:

$$col[1] = xtimes_09(c_0) \oplus xtimes_0e(c_1) \oplus xtimes_0b(c_2) \oplus xtimes_0d(c_3)$$

- Similarly, for col[2] and col[3], the bytes are transformed using Galois Field multiplication.

Each function (e.g., xtimes_0e, xtimes_0b) represents multiplication by a fixed constant in the Galois Field $GF(2^8)$. (Note that each of the xtimes_ab operations return the output modulo $x^8 + x^4 + x^3 + x + 1$ hence we do not need to XOR the result with $0x1B \equiv 00011011$ which is the hex representation of our polynomial as a byte (1) 0001 1011. For example:

- xtimes_0e(c_0): Multiplies the byte c_0 by 0x0e in $GF(2^8)$. This multiplication is done using shifts and XOR operations, not normal integer/decimal multiplication.
- xtimes_09(c_3): Multiplies the byte c_3 by 0x09 in the same manner.

In hardware, multiplication in $GF(2^8)$ is not the same as normal integer multiplication. Instead, it is implemented using a series of shift and XOR operations. Each constant multiplication (e.g., by 0x0e, 0x0b) can be implemented using a series of bitwise operations. For instance:

- Multiply by 0x02: Shift the byte left by one bit. If the highest bit in result is set, XOR it with 0x1B.
- Multiply by 0x03: Shift the byte left by one bit, then XOR the original byte with the shifted result. Again, if the highest bit is set, XOR it with 0x1B. (Alternatively, first compute the multiplication by 0x02 and then XOR with the original byte.)
- Multiply by other constants: Perform additional shifts and XORs.

Hardware implementations would use combinational logic (gates) to achieve this.

We present an example for the steps for Multiplication by 0x09. Multiplying by 0x09 in $GF(2^8)$ is broken down as follows:

$$0x09 = 0x08 \oplus 0x01 = x^3 + 1$$

This means multiplying a byte by 0x09 is equivalent to multiplying the byte by 0x08 (which is the same as shifting it left by 3 bits modulo our polynomial) and then XORing the result with the original byte.

- Multiply by 0x02: Shift the byte left by one bit. If the highest bit in result is set, XOR (modulo) it with 0x1B.

- Multiply by 0x04: Shift the result of 0x02 multiplication left by one bit. If the highest bit in result is set, XOR it with 0x1B.
- Multiply by 0x08: Shift the result of 0x04 multiplication left by one bit. If the highest bit is set, XOR it with 0x1B.
- Multiply by 0x09: First, compute multiplication by 0x08 (shift left by 3 as in previous step), then XOR with the original byte. The XOR operation does not suffer from overflow, so we return.
- Second operation is rotating the elements in the given row. As seen in Figure 4a, no elements are shifted in row 1. Then in row 2, the first element is shifted by one place. In row 3, two elements are shifted and in row 4 three elements are left shifted.
- Further, in inverse sub bytes operation, each element is replaced by value determined using INV_SBOX (3.2). Like INV_SBOX(0x63) is 0x00, that is value at 6th row and 3rd column. Similarly, INV_SBOX(0xF9) is 0x69: value at F row and 9th column.
- The last operation is bitwise XOR with the 0th round key. The final state is the recovered plaintext which can be converted using ASCII table to actual text (**This is a secret key**). Refer to following link: ASCII Table

3.3 Components of the Decryption unit

The design consists of three parts, (i) Memory, (ii) Compute unit, and (iii) Controller. In this part, we will focus on implementing part (i) and (ii). The controller the reading/writing from the ROM/RAM and logical operations in the Compute unit. The Compute unit consists of components such as arithmetic units, multiplexers and other logical units. For the given design, some alternative designs are shown in Figure 5 - (i) One controller to control both memory read/write and compute unit. (ii) Two separate controllers: control1 for memory operations and control2 for the compute unit, with a synchronization/interaction between the two controllers.

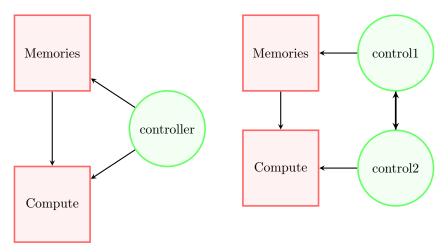


Figure 5: Alternative designs

The overall design would consist of the following:

- 1. Dedicated units to perform various round operations. Like multiplexer, gate array and Multiplier block for $GF(2^8)$ (MAC): to perform element wise multiplication to get one output value.
- 2. A Read-Write Memory (RWM, more popularly known as RAM or Random-Access Memory) Use this memory to store the output.
- 3. A Read-Only Memory (ROM) Use this memory to store the input text and key.

All the components are described in the Figure 7, and the block diagram for MAC $GF(2^8)$ block is expanded in Figure 6. For the four operations described in section 3.2.1, you will design four separate blocks which constitute the compute unit.

- 1. Design Multiplier to implement $GF(2^8)$ multiplication
- 2. Use MUXes to implement InvRowShift operation.
- 3. Use one of the memories to implement look up table for InvSubByte operation.

4. Use gate array to implement XOR operation.

You have to define appropriate control signals and the size of input/output ports.

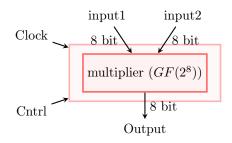


Figure 6: MAC $GF(2^8)$ unit

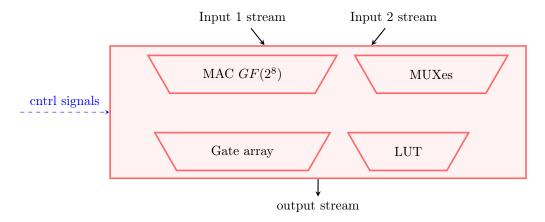


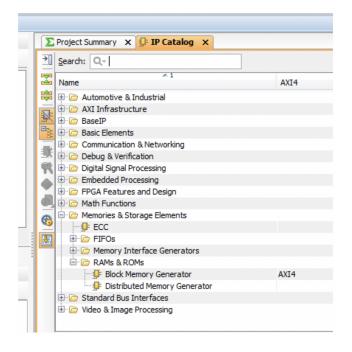
Figure 7: Details of Compute units

3.4 Memories in Vivado

We would be using Vivado's memory generator to design program and data memories. Instructions are as follows:

- In Vivado, go to the Project Manager window on the left side of the screen which looks like the screen-shot shown on right.
- Open IP catalog. You can also open IP Catalog through a drop down menu after clicking on Window in the main menu on the top of the screen. "IP" (Intellectual Property) refers to pre-designed modules available for use. The IP catalog lists various IPs category-wise.
- Select the category Memories & Storage Elements and sub-category RAMs & ROMs, as shown below.

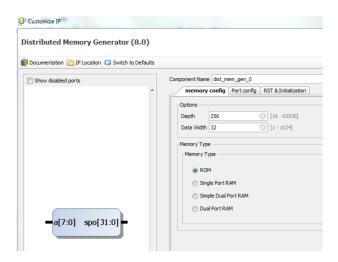




• Now choose **Distributed Memory Generator** or **Block Memory Generator**, to create a ROM / RAM as per your design requirement. This generator creates memory modules of specified sizes using LUTs of FPGA. The reason for using the Distributed Memory Generator here is that **Block Memory Generator** creates a memory with an address register since they use FPGA BRAMs, and are mostly preferred when we want large on-chip memories.

The distributed RAMs are faster and more efficient because they use the LUTs in contrast to FPGA BRAMs.

The Distributed Memory Generator opens a window with three tabs. In the **memory config tab**, specify memory size and type. The screen-shot shown below is for a ROM with 256 words, each of size 32 bits.



• In the **RST** & **Initialization** tab, specify name of the file that defines the ROM contents. A sample file named *sample.coe* is available on moodle.

Now instead of passing the inputs from the test bench or using "force value" construct, please initialize the inputs using a *coe* file and pass input to the DUT by connecting it to the memory module.

Once you synthesize and implement your design, you will see a change in the number of LUTs used in your design.

3.4.1 Test bench for generated memory block

Use the following test bench to simulate the memory IP block in vivado. The test bench is an illustration of how to import the generated memory block into your VHDL design file.

```
LIBRARY ieee;
USE ieee.std_logic_1164.ALL;
use ieee.numeric_std.all;
ENTITY tb_ROM_block IS
END tb_ROM_block;
ARCHITECTURE behavior OF tb_ROM_block IS
    COMPONENT blk_mem_gen_0
    PORT(
        clka : IN STD_LOGIC;
        addra : IN STD_LOGIC_VECTOR(13 DOWNTO 0);
        douta : OUT STD_LOGIC_VECTOR(7 DOWNTO 0)
    END COMPONENT;
  --Inputs
   signal clock : std_logic := '0';
  signal rdaddress : std_logic_vector(13 downto 0) := (others => '0');
  --Outputs
  signal data : std_logic_vector(7 downto 0) := (others => '0');
   -- Clock period definitions
  constant clock_period : time := 10 ns;
   signal i: integer;
BEGIN
 -- Read image in VHDL
  uut: blk_mem_gen_0 PORT MAP (
          clka => clock,
          douta => data,
          addra => rdaddress
        );
   -- Clock process definitions
   clock_process :process
  begin
      clock <= '0';
      wait for clock_period/2;
      clock <= '1';
      wait for clock_period/2;
   end process;
   -- Stimulus process
   stim_proc: process
  begin
      for i in 0 to 16383 loop
        rdaddress <= std_logic_vector(to_unsigned(i, 14));</pre>
      wait for 20 ns;
      end loop;
      wait;
   end process;
END;
```

4 Displaying the plaintext

To display the final text, you will be using the seven segment display of the basys 3 board. You are allowed to reuse the VHDL code from HW2 assignment. The following points should be kept in mind:

- After the final round, you need to convert the hexa-decimal value to the corresponding character using ASCII Table.
- We will restrict the characters to be displayed in the range 0-F. For any out of the range character display a default value "-" as shown in Figure 8. Plaintext will contain blank space as well.

- No case sensitivity that is display capital F and small f as F on the display.
- Only four character can be displayed at a time, your code should ensure that text keep scrolling across the display in cyclic manner.



Figure 8: Output for out of range character

5 Submission and Demo Instructions

Since this assignment will span over multiple weeks, your progress in each week will be evaluated as described below.

- 1. Make sure that you have a working system first before optimizing it. Another golden rule: Always ensure that a simulation is working correctly before testing on the FPGA board.
- 2. PART 1. Week 1-2 (14th October 26th October 2024): Design and test compute unit, memory unit for decryption operation.
- 3. You are required to submit a zip file containing the following via gradescope:
 - VHDL files for all the designed modules (Four operations and display unit).
 - Simulated waveforms with test cases of each subcomponent and complete design.
 - A short report (1-2 pages) explaining your approach. Include block diagram depicting the modules. And short summary about functionality of each module.

6 Resources references

- IEEE document: https://ieeexplore.ieee.org/document/8938196
- Basys 3 board reference manual: https://digilent.com/reference/_media/basys3:basys3_rm.pdf
- Online VHDL simulator: https://www.edaplayground.com/x/A4