

COL215 HW Assignment 2 - 4-Digit 7-Segment Display

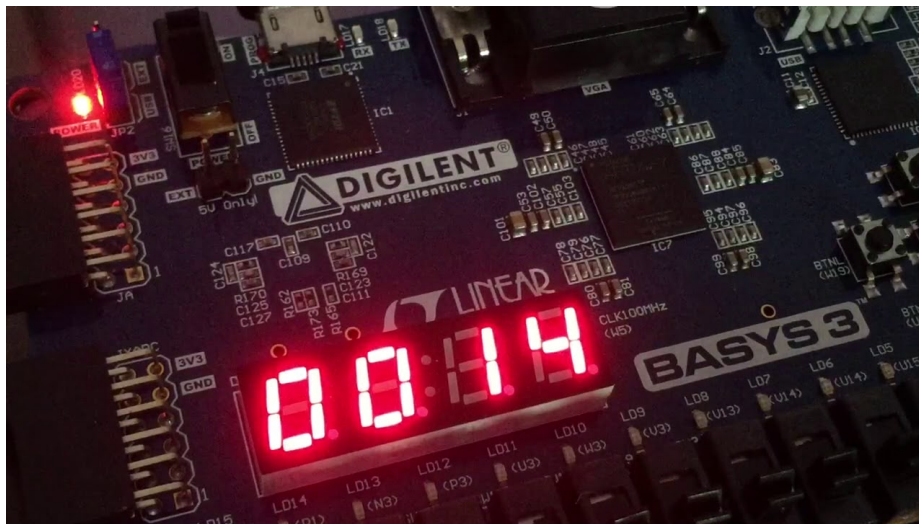
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A	B	C	D	a	b	c	d	e	f	g
0	0	0	0	1	1	1	1	1	1	0
0	0	0	1	0	1	1	0	0	0	0
0	0	1	0	1	1	0	1	1	0	1
0	0	1	1	1	1	1	1	0	0	1
0	1	0	0	0	1	1	0	0	1	1
0	1	0	1	1	0	1	1	0	1	1
0	1	1	0	1	0	1	1	1	1	1
0	1	1	1	1	1	1	0	0	0	0
1	0	0	0	1	1	1	1	1	1	1
1	0	0	1	1	1	1	1	0	1	1

1 Task

Design a combinational circuit that takes a single 4-bit hexadecimal or decimal digit input from the switches and produces a 7-bit output for the seven-segment display of Basys 3 FPGA board. Extend the design to create a circuit that drives all 4 displays for displaying 4 digits together.

2 Overview

2.1 Seven-segment Decoder

2.2 Driving all four LEDs together

3 Design Decisions

3.1 Digits

Since we are implementing a hexadecimal system, we require 16 digits to represent the output. We use the following symbols.



Figure 1: Caption

3.2 Truth Table

Digits & Input Bits					7 Segment Display							Min-Terms: $f(A, B, C, D)$
Digit	A	B	C	D	a	b	c	d	e	f	g	Min-Term Index
0	0	0	0	0	1	1	1	1	1	1	0	m_0
1	0	0	0	1	0	1	1	0	0	0	0	m_1
2	0	0	1	0	1	1	0	1	1	0	1	m_2
3	0	0	1	1	1	1	1	1	0	0	1	m_3
4	0	1	0	0	0	1	1	0	0	1	1	m_4
5	0	1	0	1	1	0	1	1	0	1	1	m_5
6	0	1	1	0	1	0	1	1	1	1	1	m_6
7	0	1	1	1	1	1	1	0	0	0	0	m_7
8	1	0	0	0	1	1	1	1	1	1	1	m_8
9	1	0	0	1	1	1	1	0	0	1	1	m_9
A	1	0	1	0	1	1	1	0	1	1	1	m_{10}
b	1	0	1	1	0	0	1	1	1	1	1	m_{11}
C	1	1	0	0	1	0	0	1	1	1	0	m_{12}
d	1	1	0	1	0	1	1	1	1	0	1	m_{13}
E	1	1	1	0	1	0	0	1	1	1	1	m_{14}
F	1	1	1	1	1	0	0	0	1	1	1	m_{15}

3.3 Minimizing the Combinational Logic using K-Maps

3.3.1 Segment a

$f(A, B, C, D)$

		C, D			
		00	01	11	10
A, B	00	1	0	1	1
	01	0	1	1	1
	11	1	0	1	1
	10	1	1	0	1

The reduced formula for segment a using the mentioned K-Map reduction is as following :

$$f(A, B, C, D) = A'B'D' + A'BD + AC'D' + AB'C' + A'C + BC + CD'$$

3.3.2 Segment b

$f(A, B, C, D)$

		C, D			
		00	01	11	10
A, B	00	1	1	1	1
	01	1	0	1	0
	11	0	1	0	0
	10	1	1	0	1

The reduced formula for segment b using the mentioned K-Map reduction is as following :

$$f(A, B, C, D) = A'C'D' + A'CD + AC'D + AB'C' + A'B'$$

3.3.3 Segment c

$f(A, B, C, D)$

		C, D			
		00	01	11	10
A, B	00	1	1	1	0
	01	1	1	1	1
	11	0	1	0	0
	10	1	1	1	1

The reduced formula for segment c using the mentioned K-Map reduction is as following :

$$f(A, B, C, D) = A'CD + A'C' + A'B + C'D + AB'$$

3.3.4 Segment d

$f(A, B, C, D)$

		C, D			
		00	01	11	10
A, B	00	⁰ 1	¹ 0	⁵ 1	⁴ 1
	01	² 0	³ 1	⁷ 0	⁶ 1
	11	¹⁰ 1	¹¹ 1	¹⁵ 0	¹⁴ 1
	10	⁸ 1	⁹ 0	¹³ 1	¹² 0

The reduced formula for segment d using the mentioned K-Map reduction is as following :

$$f(A, B, C, D) = A'B'D' + B'CD + BC'D + BCD' + A'C'D'$$

3.3.5 Segment e

$f(A, B, C, D)$

		C, D			
		00	01	11	10
A, B	00	⁰ 1	¹ 0	⁵ 0	⁴ 1
	01	² 0	³ 0	⁷ 0	⁶ 1
	11	¹⁰ 1	¹¹ 1	¹⁵ 1	¹⁴ 1
	10	⁸ 1	⁹ 0	¹³ 1	¹² 1

The reduced formula for segment e using the mentioned K-Map reduction is as following :

$$f(A, B, C, D) = B'C'D' + AB + CD' + AC$$

3.3.6 Segment f

$f(A, B, C, D)$

		C, D			
		00	01	11	10
A, B	00	⁰ 1	¹ 0	⁵ 0	⁴ 0
	01	² 1	³ 1	⁷ 0	⁶ 1
	11	¹⁰ 1	¹¹ 0	¹⁵ 1	¹⁴ 1
	10	⁸ 1	⁹ 1	¹³ 1	¹² 1

The reduced formula for segment f using the mentioned K-Map reduction is as following :

$$f(A, B, C, D) = A'BC' + BCD' + AB' + AC + C'D'$$

3.3.7 Segment g

$f(A, B, C, D)$

		C, D			
		00	01	11	10
A, B	00	⁰ 0	¹ 0	⁵ 1	⁴ 1
	01	² 1	³ 1	⁷ 0	⁶ 1
	11	¹⁰ 0	¹¹ 1	¹⁵ 1	¹⁴ 1
	10	⁸ 1	⁹ 1	¹³ 1	¹² 1

The reduced formula for segment g using the mentioned K-Map reduction is as following :

$$f(A, B, C, D) = A'B'C + A'BC'$$

$$CD' + AB' + AD$$