

## Queue Implementation Using Doubly Linked List

### Introduction

A queue is a linear data structure that follows the **FIFO (First In, First Out)** principle. It allows insertion at the back and deletion from the front. However, in this implementation, we use a **doubly linked list** to create a queue that supports additional functionalities like insertion and deletion from both ends, making it a **deque (double-ended queue)**.

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### Class Design

#### 1. Node Class (node)

Each node in the doubly linked list contains:

- An integer value val.
- A pointer next pointing to the next node.
- A pointer prev pointing to the previous node.

#### Code Implementation:

```
class node{
public:
    int val;
    node* next;
    node* prev;
    node(int val){
        this->val = val;
        next = NULL;
        prev = NULL;
    }
};
```

#### 2. Queue Class (queue)

This class maintains:

- f: Pointer to the front node.
- b: Pointer to the back node.
- size: Keeps track of the number of elements.

#### Code Implementation:

```
class queue{
```

```
public:
node* f;
node* b;
int size;

queue(){
    f = NULL;
    b = NULL;
    size = 0;
}
```

---

## Queue Operations

### 1. push\_back(int val) – Insert at the Back

This function inserts a new element at the back of the queue:

- If the queue is empty, both f and b point to the new node.
- Otherwise, the new node is added at the back, and pointers are updated.

```
void push_back(int val){
    if(size == 0){
        node* temp = new node(val);
        f = temp;
        b = temp;
    }
    else{
        node* temp = new node(val);
        b->next = temp;
        temp->prev = b;
        b = temp;
    }
    size++;
}
```

### 2. push\_front(int val) – Insert at the Front

Similar to push\_back, but inserts an element at the front.

```
void push_front(int val){
    if(size == 0){
        node* temp = new node(val);
        f = temp;
        b = temp;
    }
    else{
        node* temp = new node(val);
        f->prev = temp;
        temp->next = f;
        f = temp;
    }
    size++;
}
```

### 3. pop\_back() – Remove from the Back

- If the queue is empty, prints an error message.
- Otherwise, removes the last element and updates b.

```
void pop_back(){
    if(size == 0){
        cout << "QUEUE IS ALREADY EMPTY!";
    }
    else{
        node* temp = b;
        b = b->prev;
        delete temp;
        if (b) b->next = NULL;
        size--;
    }
}
```

### 4. pop\_front() – Remove from the Front

- If the queue is empty, prints an error message.
- Otherwise, removes the front element and updates f.

```
void pop_front(){
    if(size == 0){
        cout << "QUEUE IS ALREADY EMPTY!";
    }
    else{
        node* temp = f;
        f = f->next;
        delete temp;
        if (f) f->prev = NULL;
        size--;
    }
}
```

### 5. front() – Get the Front Element

Prints the front element.

```
void front(){
    cout << f->val << endl;
}
```

### 6. back() – Get the Last Element

Prints the last element.

```
void back(){
    cout << b->val << endl;
}
```

### 7. display() – Print the Queue Elements

Prints all the elements in the queue.

```
void display(){
    node* temp = f;
    while(temp){
        cout << temp->val << " ";
        temp = temp->next;
    }
}
```

```
}  
  
cout << endl;  
  
}
```

### **8. length() – Get the Queue Size**

Prints the current size of the queue.

```
void length(){  
    cout << size << endl;  
}
```

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### **Main Function (main())**

The main() function demonstrates the working of the queue.

```
int main(){  
    queue q;  
    q.push_back(1);  
    q.push_back(2);  
    q.push_back(3);  
    q.display(); // Output: 1 2 3  
  
    q.pop_back();  
    q.display(); // Output: 1 2  
  
    q.push_front(0);  
    q.push_front(-1);  
    q.push_front(-2);  
    q.display(); // Output: -2 -1 0 1 2  
  
    q.pop_front();  
    q.display(); // Output: -1 0 1 2  
  
    q.front(); // Output: -1  
    q.back();  // Output: 2
```

```
q.length(); // Output: 4
```

```
return 0;
```

```
}
```

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### Key Takeaways

1. **Doubly Linked List is used:** Each node has prev and next pointers.
2. **Efficient Insertions and Deletions:** Operations at both ends take  **$O(1)$**  time.
3. **Functionality beyond Standard Queue:** This implementation allows both front and back operations (like a deque).
4. **Memory Management:** Dynamic memory is allocated using new and properly freed using delete.

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### Conclusion

This queue implementation using a doubly linked list provides flexibility with efficient insertion and deletion from both ends. It serves as the foundation for **deque** (double-ended queue), which has multiple applications in scheduling, buffering, and data handling scenarios.