



# LeetCode 378 – Kth Smallest Element in a Sorted Matrix



Approach Used: Max-Heap of Size **k**



## Problem Statement (Simplified):

Matrix ke har row aur column ascending sorted hai.

Hume **k-th** smallest value nikaalni hai.

**Tera code max-heap se kar raha hai.**



## Code Used:

```
class Solution {
public:
    int kthSmallest(vector<vector<int>>& matrix, int k) {
        priority_queue<int> pq; // Max-heap

        for(int i = 0; i < matrix.size(); i++) {
            for(int j = 0; j < matrix.size(); j++) {
                pq.push(matrix[i][j]);    // Push element
                if(pq.size() > k) pq.pop(); // Pop max if size > k
            }
        }

        return pq.top(); // Return k-th smallest
    }
};
```

## Logic Behind Each Step:

Step	Code Line	Explanation
1	<code>priority_queue&lt;int&gt; pq;</code>	Max-heap banayi jisme top pe <b>largest</b> value hoti hai.
2	Loop on <code>i</code> and <code>j</code>	Matrix ke har element ko access kar raha hai nested loop se.
3	<code>pq.push(matrix[i][j]);</code>	Har element ko heap me insert kar raha hai.
4	<code>if(pq.size() &gt; k) pq.pop();</code>	Agar size <code>k</code> se bada ho jaye toh sabse bada element (top) hata deta hai.
5	<code>return pq.top();</code>	Heap me ab sirf <code>k</code> smallest elements hain. Top = <code>k-th</code> smallest.

## Dry Run (Example):


### Input:

```
matrix = [  
  [1, 5, 9],  
  [10,11,13],  
  [12,13,15]  
], k = 8
```

### Process:

- Har element heap me gaya
- Heap size `k` se zyada hone par sabse bada element pop hota raha
- End me heap me 8 chhote elements bache
- Top = 8th smallest = `13`

## Time & Space Complexity:





Type	Complexity	Reason
 Time	<code>O(n<sup>2</sup> log k)</code>	<code>n<sup>2</sup></code> elements, each heap op is <code>log k</code>

 Space

$O(k)$

Max heap size  $k$  hi rakha

## ← END Summary:

-  Simple & intuitive
-  Solves problem correctly
-  Not optimal for very large  $n$
-  **Perfect for first try / brute-force level**