

# Problem Summary Leetcode: 169

We are given an array `nums` of size `n`.

- **Majority element** = The element that appears **more than  $\lfloor n/2 \rfloor$  times**.
- We are guaranteed that such an element always exists.

Example:

- `nums = [3,2,3]` → Majority = 3
- `nums = [2,2,1,1,2,2]` → Majority = 2

## Code You Wrote

```
class Solution {
public:
    int majorityElement(vector<int>& nums) {
        sort(nums.begin(), nums.end());
        return nums[((nums.size())/2)];
    }
};
```

## Logic of This Code

### 1. Sorting Step:

- First, we sort the array.
- Example: `[2,2,1,1,2,2]` → After sorting → `[1,1,2,2,2,2]`.

### 2. Middle Element Trick:

- Since the majority element appears more than  $\lfloor n/2 \rfloor$  times, after sorting, **it will always occupy the middle index**.

- Example:  $n = 7$ , so  $n/2 = 3$ . The element at index 3 (0-based indexing) is guaranteed to be the majority.
- Sorted array: `[1,1,1,2,2,2,2]` → element at index 3 = 2.

### 3. Return It:

- Just return `nums[n/2]`.

✅ That's why this works perfectly.

## Time & Space Complexity

- Sorting takes  $O(n \log n)$  time.
- Space complexity depends on sorting algorithm (in C++ STL sort =  $O(\log n)$  stack space).
- Not the best for the **follow-up** (which asks  $O(n)$  time and  $O(1)$  space).

## Follow-up: Optimal Solution (Moore's Voting Algorithm)

There is a better approach called **Moore's Voting Algorithm**:

```
class Solution {
public:
    int majorityElement(vector<int>& nums) {
        int candidate = 0, count = 0;
        for(int num : nums){
            if(count == 0) candidate = num;
            count += (num == candidate) ? 1 : -1;
        }
        return candidate;
    }
};
```

## Logic of Moore's Algorithm

- If we take pairs of **different elements** and cancel them out, the **majority element** will always remain in the end.
  - Works in  **$O(n)$  time** and  **$O(1)$  space**.
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## Explanatory Notes (for revision)

- **Majority element** = appears more than  $n/2$  times.
  - **Sorting Trick**: Majority always at middle index after sorting  $\rightarrow$  `nums[n/2]` . ( $O(n \log n)$ )
  - **Optimal Method (Moore's Voting)**: Cancel out different pairs  $\rightarrow$  candidate left is majority. ( $O(n)$ ,  $O(1)$ )
  - **Guarantee**: Majority element always exists in given array (so no need for extra check).
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