

509. Fibonacci Number

LeetCode



Fibonacci using Memoization (Top-Down DP)



Problem

Compute the $n\text{-th}$ Fibonacci number using **recursion with memoization** to avoid redundant calculations.



Approach — Recursive + DP (Top-Down)

We use a dp array to **store already computed results**, so that each Fibonacci value is computed only once.



Code

```
class Solution {
public:
    int fibo(int n, vector<int>& dp) {
        if (n <= 1) return n; // Base case: F(0)=0, F(1)=1
        if (dp[n - 1] != -1) return dp[n - 1]; // If already computed, return it

        // Store result before returning
        return dp[n - 1] = fibo(n - 1, dp) + fibo(n - 2, dp);
    }

    int fib(int n) {
        vector<int> dp(n, -1); // Initialize DP array of size n with -1
        return fibo(n, dp); // Compute F(n)
    }
};
```

Key Points

- **Base Case:**

`fibo(0) = 0 , fibo(1) = 1`

- **Recurrence Relation:**

`fibo(n) = fibo(n-1) + fibo(n-2)`

- **Memoization:**

- Store results in `dp` to prevent recomputation
 - Use `dp[n-1]` because vector size = `n` (indices `0` to `n-1`)

Time Complexity

| $O(n)$ — each Fibonacci number is computed once.

Space Complexity

| $O(n)$ — for the recursion stack + dp array.

Example

For `n = 5` :

```
fibo(5)
  → fibo(4) + fibo(3)
  → (fibo(3) + fibo(2)) + (fibo(2) + fibo(1))
  → ...
Result = 5
```