



LeetCode 118 – Pascal's Triangle



Problem Overview

Given an integer numRows, generate the first numRows of **Pascal's Triangle**.

Each number in Pascal's Triangle is the sum of the two numbers directly above it. The triangle starts with 1 at the top and continues with each row having one more element than the previous.



Intuition

Pascal's Triangle has the following properties:

- The **first and last** elements of each row are always **1**.
 - Every **inner element** at position j in row i is the **sum** of the elements at positions $j-1$ and j from the previous row ($i-1$).
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Solution Explanation (C++)

◆ 1. Initialization

```
vector<vector<int>>> v;  
  
for(int i = 0; i < numRows; i++) {  
    vector<int> a(i + 1); // Create a row with (i+1) elements  
    v.push_back(a);      // Add it to the triangle  
}
```

- ✓ Creates a 2D vector v , where each row has $i + 1$ elements
 - ✓ This sets up the structure of the triangle
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◆ 2. Filling the Triangle

```
for(int i = 0; i < numRows; i++) {  
    for(int j = 0; j <= i; j++) {  
        if(j == 0 || j == i) {  
            v[i][j] = 1; // First and last elements are always 1  
        } else {  
            v[i][j] = v[i-1][j-1] + v[i-1][j]; // Inner elements  
        }  
    }  
}
```

```
}  
}
```

- ♦ **Edge cases** ($j == 0$ || $j == i$) are filled with 1
 - ♦ **Other elements** are calculated by summing two numbers from the row above
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3. Example Output for numRows = 5

```
1  
1 1  
1 2 1  
1 3 3 1  
1 4 6 4 1
```

Each row has one more element than the previous and follows the Pascal's Triangle rule.





Time & Space Complexity

Complexity Explanation

Time $O(n^2)$ – Each element is computed once

Space $O(n^2)$ – All rows are stored in a 2D vector

Key Takeaways

-  Pascal's Triangle builds naturally from top to bottom
 -  First and last elements of each row are **always 1**
 -  Inner elements are the **sum of two above elements**
 -  Very efficient solution using dynamic programming principles
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Would you like a **Python version** or a **visual diagram** to go along with it too?