SETER

Namet

Student University Roll No.:

Prod Pages:

School of Engineering

Second Sessional Examination, Even Semester (AS: 2022-23)

B. Tech: All Branch

[Year: First] [Semester: II]

Course Title: Differential Equations and Fourier Analysis

lysis Max Marks: 60

Course Code: BAS3201

Time: 3hrs

Instr	uctions if any: Read the question Carefully.		
Q.N.	SECTION 'A' 1. Attempt all parts of the following:	CO	Marks
a)	Find the order and degree of the differential equation $\left(\frac{d^2y}{dx^2}\right)^2 = \left[1 + \left(\frac{dy}{dx}\right)^2\right]^3$	1,	1
b)	Find the particular integral of $\frac{d^2y}{dx^2} + y = sinx$	3	1
c)	Find the values of α and β for which $3x^2 = \alpha P_2(x) + \beta P_0(x).$	7	1
d)	Show that $x = 1$ is a singular point of $(x - 1)\frac{d^2y}{dx^2} + x\frac{dy}{dx} + 2y = 0.$	7	1
e)	Write Dirichlet's conditions for a Fourier series.	8	1
f)	Find the constant term if the function $f(x) = x$ is expanded in Fourier series defined in $(-1, 1)$.	8	1
g)	Form the partial differential equation from $z = (x + a)(y + b)$ by eliminating the arbitrary constants a and b .	11	1
h)	Classify the partial differential equation $\frac{\partial^2 u}{\partial t^2} = c^2 \frac{\partial^2 u}{\partial x^2}$	12	1
SECTION 'B' Q.N.2. Attempt any two parts of the following:		СО	Marks
2)	Apply method of variation of parameters to solve $\frac{d^2y}{dx^2} - 3\frac{dy}{dx} + 2y = \frac{e^x}{1 + e^x}$	6	6
b)	Find the power series solution of $(1 - x^2) \frac{d^2y}{dx^2} - 2x \frac{dy}{dx} + 2y = 0 \text{ about } x = 0.$	7	- 5
c)	Given that $f(x) = x + x^2$ for $-\pi < x < \pi$, Find the Fourier series expansion of $f(x)$. Deduce that $\pi^2 - 1 + \frac{1}{\pi^2} + \frac{1}{\pi^2} + \frac{1}{\pi^2} + \dots$	8	6
<u>d)</u>	6 2 2 3 4 4 Find the remperature in a bar of length 2 whose ends kept at zero and		

	The state of the s		
	lateral surface is the equal of the initial temperature is $\left[sin(\frac{nx}{2}) + 3sin(\frac{-x}{2})\right]$	10	
	SECTION 'C'	w	Marke
Q.N	3. Attempt any two parts of the following:		
a)	Solve $(3x+2)^2 \frac{d^2y}{dx^2} - (3x+2) \frac{dy}{dx} - 12y = 6x$	#	
b)_	Solve $(D^2 - 4D + 3)y = 2xe^{3x}$	3	5
c)	Solve the simultaneous differential equations $\frac{dx}{dt} = 3x + 8y$		
	$\frac{dt}{dy} = -x - 3y \text{ with } x(0) = 6 \text{ and } y(0) \Rightarrow -2$	4	+ 5
Q.N	.4. Attempt any two parts of the following:		
a)	Prove that $xf'_n = nf_n - xf_{n+1}$	7	5
b)	Prove that $\int_{-1}^{1} [P_n(x)]^2 dx = \frac{2}{2n+1}$	7	5
c)	Prove that $I_{1/2}(x) = \sqrt{\frac{2}{n x}} \sin x$	7	5
Q.N	.5. Attempt any two parts of the following:		
a)	Find the half Range Fourier size series of $f(x) = \begin{cases} x & 0 < x < 2 \\ (4-x), & 2 < x < 4 \end{cases}$	8	5
b)	Expand the function $f(x) = x \cos x$, as a Fourier series in the interval $-\pi < x < \pi$.	9	5
	The state of the s	-	-
c)	Find the half Range Fourier cosine series of $f(x) = \begin{cases} x & 0 < x < \frac{\pi}{2} \\ (\pi - x), & \frac{\pi}{2} < x < \pi \end{cases}$	*	5
c)	$f(x) = \begin{cases} x & , & 0 < x < \frac{\pi}{2} \\ (\pi - x), & \frac{\pi}{2} < x < \pi \end{cases}$ (6. Attempt any two parts of the following:		5
c)	$f(x) = \begin{cases} x , & 0 < x < \frac{\pi}{2} \\ (\pi - x), & \frac{\pi}{2} < x < \pi \end{cases}$ i.6. Attempt any two parts of the following:	3	14.5
c) Q.5	$f(x) = \begin{cases} x , & 0 < x < \frac{\pi}{2} \\ (\pi - x), & \frac{\pi}{2} < x < \pi \end{cases}$	3	