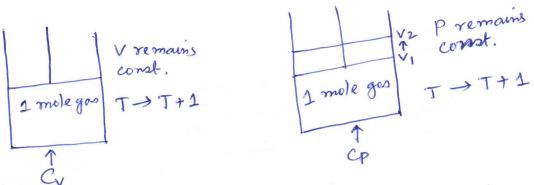
Molar heat capacity of gazes:

Heat capacity (c) of a substance is defined as the amount of heat required to raise the temp. of the substance by one degree. Heat capacity per gram of a substance is called specific heat and per mole is called molar heat capacity.

Thus, Holar heat cofacity = molar mass x specific heat For gases, there are two heat capacities at const. Vol. and at const. Pr. 30, Cv = M x cv and Cp = M x cp, where Cv and Cp are the molar heat capacities at const. Vol. and at const. Pr., respectively. cv and cp are their specific heats.



From the above two schematic descriptions, it is clear that Cp > CV, Since for Cp, some mechanical work is required as additional energy to absorb for lifting the piston from V_1 to V_2 .

Thus, Cp - Cv = Mechanical work $= PdV = P(V_2 - V_1) = PV_2 - PV_1 = R(T+1) - RT$ = R

Thus, Cp - CV = R. This is valid for ideal gas only as PV = RT is taken for 1 mole gas.

Now let us find the expression for CV from the stond-point of the kinehic theory of gas.

Cy = Energy required to increase transtational Kinchic energy tenergy required to increase intramolecular energy of 1 mole gas for 1 degree rise in temperature.

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Increase of translational KE of 1 mole gas for 10 rise in temp. $=\frac{3}{2}R(T+1)-\frac{3}{2}RT=\frac{3}{2}R$

Let the intramolecular energy increase for the gas for 10 rise in temp = x. Then, $\frac{3}{2}R = Translabional contribution$ $<math>C_V = \frac{3}{2}R + x$ x = (Rotational + Vibrational) contribution

The value of ne is calculated from the law of equiportition of energy and this will be discussed later.

Thus, $CP = \frac{5}{2}R + \chi$

The molar heat capacity ration (Poisson ratio),

$$\gamma = \frac{Cp}{CV} = \frac{\frac{5}{2}R + \chi}{\frac{3}{2}R + \chi} = \frac{5 + \chi}{3 + \chi}$$

When expressed in calonie unit. and R = 2 cal mol-1 K-1

For monatomic gas, n=0, $y=\frac{5}{3}=1.66$ For diatomic gas, R = R = 2 cal $mol^{-1} K_j^{-1} \gamma = \frac{7}{5} = 1.4$

For polyatomic gas, $x = \frac{3}{2}R = 3$ cal mol $(K^{-1}; Y = \frac{4}{3} = 1.33)$

For a gas, i can be determined from the measurement of velocity (ov) of sound passing through the gas using the relation, $\gamma = \sqrt{\frac{\gamma_{RT}}{M}}$. The value of γ

thus provides the atomicity (molecular complexity) of the gas.

Internal ang. is entirely kinchic. For monatomic gases (He, Ne, etc.) there is only translational K.E (as no rotation or vibration) is possible for monatomic molecular

* : cannot be derived from Kinchic gas equalsion.

Thus, Kinetic theory fails to theoretically calculate of & Cv values for dialomic and polyatomic gases.

Maxwell's speed distribution:

James clerk Maxwell (1859) formulated speed distribution of particles in idealized gases where the particles more freely inside a stabionary container without interacting with one another. on the basis of probabilistic idea, Maxwell and later Boltzmann formulated the distribution law as This distribution describes how the different speeds are distributed among various group of molecules.

F(c)
$$\rightarrow$$
 Maxwell speed distribution function where $F(c) = \frac{1}{m} \frac{dnc}{dc}$

m = no of molecules per unit volume

dne = " " within the speed range c to (e+de)

$$F(e) = \frac{1}{n} \cdot \frac{dn_c}{de} = \left(\frac{m}{2\pi RT}\right)^{1/2} e^{-\frac{mc^2}{2RT}}$$
 (1-D)

one Dimensional velocity distribution

$$-\frac{me^2}{2\pi RT} \left(2-D\right)$$

$$F(c) = \frac{1}{n} \cdot \frac{dn_c}{dc} = 2\pi \left(\frac{m}{2\pi kT}\right) \cdot c \cdot e^{\frac{-mc^2}{2kT}} (2-D)$$

$$F(c) = \frac{1}{m} \cdot \frac{dn_c}{dc} = 4\pi \left(\frac{m}{2\pi RT}\right)^{3/2} \cdot c^2 \cdot e^{-\frac{mc^2}{2RT}} (3-D)$$

$$F(c) = \frac{1}{m} \cdot \frac{dn_c}{dc} = 4\pi \left(\frac{m}{2\pi RT}\right)^{3/2} \cdot c^2 \cdot e^{-\frac{mc^2}{2RT}} (3-D)$$

m = Molecular mass of the gas; T = Temp. in absolute scale.

It is assumed that the gas molecules remain in complete random and the probability of a molecule to have a definite speed within small range is always finite.

we can also write,
$$F(c) = 4\pi \left(\frac{M}{2\pi RT}\right)^{3/2} c^2 \cdot e^{\frac{Mc^2}{2RT}}$$

Thus, F(c) depends on the nature of the gas which is characterized by molar mass (M) and the temp (T). Thus, F(c) depends on M of the gas. Thus, F(c) of O2 gas mo leader at 300 K is some as

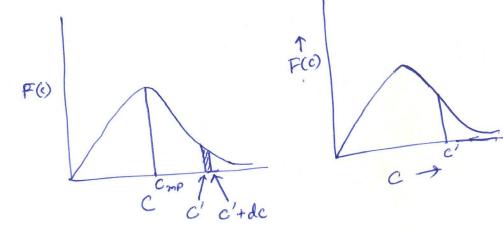
as that of SO2 gas molecules at 600 K as # value is same for both the gases at these temperatures. It means that traction of 02 molecules at 300 K have the same velocity with that of SO2 gas at 600 K. Similarly, F(c) of N2 gas and co gas is some at any temp. as both the gases have same molar mass.

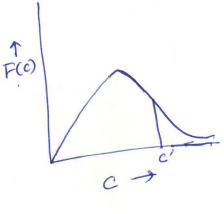
Salient features of Maxwell's distribution curve: -

It is possible to calculate F(e) of a particular gas at a given temp. with different speeds ranging from small value to high value. The calculated values can be but in a table and then it can be projected in a Figure, F(c) vs. C.

For O2 gas 300 K

Speed	function
0	0
9	F (4)
62	F(C2)
Cz	F (C3)
Cy	F (Cy)
	3





Various conclusions can be drawn from the F(c) vs. C curve.

- 1) The curve initially rises in parabolic form with increasing Speed, reaches a maxima and then falls off exponentially.
- The fraction total no. of molecules within a certain speed range c' to (c'+dc) is given by the area of the shaded region: F(c') x de. Total area of the curve is unity, i.e., traction of molecules that have speed o to ∞ is one.

3 Maximum fraction of the molecules have a common speed, it is called most probable speed (Cmp).

⊕ F(c) contains two factors: one is exponential term, e² 2kT
 and the other is non-exponential term, e². Thus, with increase of c, the exponential term decreases the value of F(c) while the non-exponential term increases the value of F(c). So, the net effect on F(c) depends on the relative magnitude of these two factors. At low cone c, the non-exponential term dominates term dominates while at high c, exponential term dominates. Thus, the value of F(c) Starts from zero at c=0,
 Thus, the value of F(c) Starts from zero at c=0,
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 Thus, the value of F(c) starts from zero at c=0,
 Thus, the value of F(c) starts finally decreases
 increases, then attains maximum and finally decreases
 toward asymptotic value with increase of c. The value of F(c)
 again becomes zero at c→∞

(5) when c=0, F(c)=0. It means that there is no molecule that have zero speed i.e. no molecule is at rest at any temp., all molecules are moving in the gaseous phase.

Effect of temp. on the distribution: -

1 F(c) contains two factors which are dependent on T, one is exponential term, e-mc²/2RT and the other is non-exponential term, (m/2TRT) 3/2. So distribution curve varies when the temp. of the gas is increased.

The most-probable speed is Cmp(T₁) Cmp(T₃)
increased with rise in terms. However the fraction of molecules having most-proble speed is decreased.

Thus, if T₂ > T, then The F(Cmp) at T₂ < F(Cmp) at T₁

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3) The fraction of molecules having speed close to Comp is also large as the curve is flat at higher T.

- (a) when T +, the curve becomes more and more flat.

 when T → ∞, the curve lies on the C-axis indicating that
 the speed distribution is totally uniform. All the molecules
 that same speed and in fact distribution is lost.
- (5) 9t T+, the curve becomes narrow.

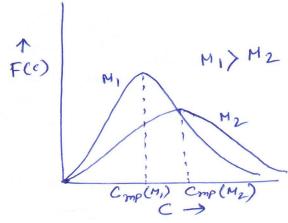
 When T→ OK, the curve lies on the F(c)-axis.

 All the molecules have speed zero and So again distribution is lost.
- 6) The total area in both the cases of T₁ and T₂ is 8 some and it is unity.

Effect of molar mass on distribution: -

The molar mass (M) and temp (T) remain in the expression of F(c) as (M). So, the effect of M is just the opposite to that of T.

The curve for the gas of lower molar mass (such as He) is



Wider than the gas of heavier molar mass (Such as Argon).

Kinetic energy distribution from Maxwell's speed distribution:

$$\frac{1}{n} \frac{dn_c}{dc} = 4\pi \left(\frac{m}{2\pi kT}\right)^{3/2} c^2 e^{-mc^2/2kT}$$

Kinetic energy, & = \frac{1}{2} me^2 = de = \frac{1}{2} \cdot 2mc \cdot dc

$$=) dc = \frac{d\varepsilon}{mc} = \frac{d\varepsilon}{m\sqrt{\frac{2\varepsilon}{m}}} = \frac{d\varepsilon}{(2m\varepsilon)^{1/2}}$$

Substituting de and c2 in the equip.

$$\frac{1}{m} \frac{dn_e}{d\epsilon} = 4\pi \left(\frac{m}{2\pi kT}\right)^{3/2} \frac{2\epsilon}{m} \cdot e^{-m \cdot \frac{2\epsilon}{m}/2kT}$$

$$\Rightarrow \frac{1}{m} \frac{dn_{\epsilon}}{d\epsilon} = 4\pi \left(\frac{m}{2\pi kT}\right)^{3/2} \left(2m\epsilon\right)^{-1/2} \left(\frac{2\epsilon}{m}\right) e^{-\frac{\epsilon}{kT}}$$

$$\Rightarrow F(\epsilon) = \frac{1}{n} \cdot \frac{dn_{\epsilon}}{d\epsilon} = 2\pi \left(\frac{1}{\pi \kappa T}\right)^{3/2} \epsilon^{1/2} e^{-\epsilon/\kappa T}$$

the molecular mass of the gas.

This means that KE distribution only depends on T but does not depend on the nature of the gas.

