

## Assignment Answers:

### 1. Types of Data (Qualitative and Quantitative):

- **Qualitative Data** (Categorical): Describes qualities or characteristics.
  - *Nominal*: No natural order. Example: Gender (Male, Female), Blood Type (A, B, AB, O).
  - *Ordinal*: Ordered categories. Example: Satisfaction (Poor, Fair, Good, Excellent).
- **Quantitative Data** (Numerical): Represents measurable quantities.
  - *Interval*: Numeric scale without true zero. Example: Temperature in Celsius.
  - *Ratio*: Numeric scale with true zero. Example: Height, Weight, Age.

### 2. Measures of Central Tendency:

- **Mean (Average)**: Useful when data is symmetric and has no outliers.
  - *Formula*:  $\text{Mean} = \sum x / n$
- **Median**: Middle value; best for skewed data or outliers.
- **Mode**: Most frequent value; useful for categorical or repeated values.

### 3. Dispersion (Spread of Data):

- **Range**: Difference between highest and lowest values.
- **Variance**: Measures average squared deviation from mean.
  - *Population Variance*:  $\sigma^2 = \sum (x - \mu)^2 / N$
  - *Sample Variance*:  $s^2 = \sum (x - \bar{x})^2 / (n - 1)$
- **Standard Deviation**: Square root of variance; shows average deviation.

### 4. Box Plot and Data Distribution:

- Shows five-number summary: Minimum, Q1, Median (Q2), Q3, Maximum.
- Detects skewness, spread, and outliers.
- *Outlier Detection*:  $Q1 - 1.5 \times IQR$  and  $Q3 + 1.5 \times IQR$ .

### 5. Importance of Random Sampling:

- Removes selection bias.
- Ensures equal probability of selection.
- Helps make reliable population inferences.

### 6. Skewness and Its Interpretation:

- **Positive Skew**: Right tail longer; Mean > Median.
- **Negative Skew**: Left tail longer; Mean < Median.
- Affects mean and spread; important for selecting correct statistical tools.

### 7. Interquartile Range (IQR) and Outliers:

- $IQR = Q3 - Q1$
- Measures middle 50% spread of data.
- Used to detect outliers via lower and upper fences.

### 8. Binomial Distribution Conditions:

- Fixed number of trials.

- Two outcomes: Success or Failure.
- Trials are independent.
- Constant probability of success.
- *Formula:*  $P(X = k) = C(n, k) \times p^k \times (1 - p)^{(n - k)}$

9. **Normal Distribution & Empirical Rule:**

- Bell-shaped, symmetric curve.
- Mean = Median = Mode.
- *Empirical Rule:*
  - 68% within 1 standard deviation
  - 95% within 2 standard deviations
  - 99.7% within 3 standard deviations

10. **Poisson Process Example:**

- Models random events over time (fixed average rate  $\lambda$ ).
- Example: 5 phone calls per hour
- *Find  $P(X = 3)$ :*  $P(X = 3) = (e^{-5} \times 5^3) / 3! \approx 0.1404$

11. **Random Variables:**

- **Discrete:** Countable values (e.g., number of heads).
- **Continuous:** Any value within a range (e.g., height).

12. **Covariance and Correlation Example:**

- Dataset:

Student	Hours Studied (X)	Exam Score (Y)
A	2	65
B	4	70
C	6	80
D	8	90

- Mean of X = 5, Mean of Y = 76.25
- Covariance = 54.7
- Correlation ( $r$ ) = 0.98 → Strong Positive Relationship
- *Interpretation:* As study time increases, exam scores also increase significantly.