# ToyotaCorolla\_regression

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### Input data, choose predictors

```
car.df <- read.csv("ToyotaCorolla.csv") # Read the ToyotaCorolla CSV file</pre>
car.df <- car.df[1:1000, ] # use first 1000 rows of data</pre>
View(car.df)# view the car dataset
t(t(names(car.df)))#names(car.df)holds names of columns in car.df. Transpose
column names of dataset twice to get output.
##
         [,1]
    [1,] "Id"
##
##
   [2,] "Model"
  [3,] "Price"
##
## [4,] "Age_08_04"
## [5,] "Mfg_Month"
## [6,] "Mfg_Year"
## [7,] "KM"
## [8,] "Fuel_Type"
## [9,] "HP"
## [10,] "Met Color"
## [11,] "Color"
## [12,] "Automatic"
## [13,] "CC"
## [14,] "Doors"
## [15,] "Cylinders"
## [16,] "Gears"
## [17,] "Quarterly_Tax"
## [18,] "Weight"
## [19,] "Mfr Guarantee"
## [20,] "BOVAG Guarantee"
## [21,] "Guarantee_Period"
## [22,] "ABS"
## [23,] "Airbag_1"
## [24,] "Airbag 2"
## [25,] "Airco"
## [26,] "Automatic airco"
## [27,] "Boardcomputer"
## [28,] "CD_Player"
## [29,] "Central_Lock"
## [30,] "Powered_Windows"
## [31,] "Power_Steering"
## [32,] "Radio"
## [33,] "Mistlamps"
```

```
## [34,] "Sport_Model"
## [35,] "Backseat_Divider"
## [36,] "Metallic_Rim"
## [37,] "Radio_cassette"
## [38,] "Parking_Assistant"
## [39,] "Tow_Bar"

selected.var <- c(3, 4, 7, 8, 9, 10, 12, 13, 14, 17, 18)# select variables
for regression</pre>
```

###Summary:Data were collected on all previous sales of used Toyota Corollas at the dealership and saved as ToyotaCorolla.csv. The data include the sales price and other information on the car, such as its age, mileage, fuel type, and engine size. There are 39 variables in total. The total number of records in the dataset is 1000 cars (we used the first 1000 cars from the dataset ToyotoCorolla.csv). We are selecting the predictors by reducing the number of variables from 39 to 11

variables("Price", "Age", "KM", "Fuel\_Type", "HP", "Met\_Color", "Automatic", "CC", "Doors", "Quar terly\_tax", "Weight")

#### Partition the data

```
set.seed(1) # set seed for reproducing the partition
train.index <- sample(c(1:1000), 600)#Here we are taking 60% of the data as
training set.Train.index holds 600 index of rows of the 1000
head(train.index)#first several rows of train.index
## [1] 836 679 129 930 509 471
train.df <- car.df[train.index, selected.var]# Assigning sampled 60% of the
data to training set.
valid.df <- car.df[-train.index, selected.var]#Assigning the remaining 40% of</pre>
the data to validation
head(valid.df)#Several first rows of valid.df
                         KM Fuel_Type HP Met_Color Automatic
##
      Price Age 08 04
                                                                 CC Doors
## 2 13750
                   23 72937
                               Diesel 90
                                                   1
                                                             0 2000
                                                                        3
                                                             0 2000
                                                                        3
## 7 16900
                   27 94612
                               Diesel 90
                                                   1
                                                                         3
## 8 18600
                   30 75889
                               Diesel 90
                                                   1
                                                             0 2000
                                                                        3
## 9 21500
                   27 19700
                               Petrol 192
                                                   0
                                                             0 1800
                                                                         3
## 10 12950
                   23 71138
                               Diesel 69
                                                   0
                                                             0 1900
## 12 19950
                   22 43610
                               Petrol 192
                                                   0
                                                             0 1800
                                                                         3
##
      Quarterly_Tax Weight
## 2
                210
                      1165
## 7
                210
                      1245
## 8
                210
                      1245
## 9
                100
                      1185
## 10
                185
                      1105
## 12
                100
                      1185
head(train.df)#several first rows of train.df
```

```
KM Fuel Type HP Met Color Automatic
       Price Age 08 04
                                                                       CC Doors
                                                                               3
## 836
       9750
                     67
                         67762
                                   Petrol 110
                                                        1
                                                                   0 1600
                                                                               5
## 679
       9895
                     68 102494
                                   Petrol 110
                                                        0
                                                                   0 1600
                                                                               5
## 129 17950
                         33740
                                   Petrol 97
                                                        1
                                                                   0 1400
                     17
                                                                               5
## 930 9995
                     57
                         55844
                                   Petrol 86
                                                        1
                                                                   0 1300
                                                                               5
## 509 10500
                     50
                         54465
                                   Petrol 110
                                                        0
                                                                   0 1600
                                                                               5
## 471 10900
                         65471
                                   Petrol 97
                                                        1
                                                                   0 1400
                     50
##
       Quarterly_Tax Weight
## 836
                   85
## 679
                   85
                        1090
## 129
                   85
                        1135
## 930
                   69
                        1045
## 509
                   85
                        1075
## 471
                   85
                        1060
```

###Summary: Here, we are splitting the data set into training ie 60% of the data(600 rows out of 1000) and validating ie 40% of the remaining data(400 rows out of 1000). We have taken the data set for tarining and validating which are selected variables for regression ie Price, Age, KM, Fuel type, HP, Metallic color, Automatic Transmission, CC, Doors, Quarterly Tax, Weight.

#### Run model

```
car.lm <- lm(Price ~ ., data = train.df)# use lm() to run a linear regression</pre>
of Price on all 11 predictors in the training set. use . after ~ to include
all the remaining columns in train.df as predictors.
options(scipen = 999)
summary(car.lm)
##
## Call:
## lm(formula = Price ~ ., data = train.df)
##
## Residuals:
##
      Min
               1Q
                   Median
                               3Q
                                      Max
          -729.9
##
  -9781.2
                      0.9
                            739.3
                                   6912.9
##
## Coefficients:
##
                      Estimate
                                 Std. Error t value
                                                               Pr(>|t|)
## (Intercept)
                  -4754.379821
                                1661.719608
                                            -2.861
                                                               0.004372
                   -133.271592
                                   4.901960 -27.187 < 0.0000000000000000 ***
## Age 08 04
                                            ## KM
                     -0.020992
                                   0.002304
## Fuel TypeDiesel
                    896.206322
                                 603.164063
                                             1.486
                                                               0.137857
## Fuel_TypePetrol
                   2191.368250
                                 575.629429
                                              3.807
                                                               0.000155 ***
## HP
                                                       0.00000000000317 ***
                     37.257956
                                   5.233283
                                             7.119
## Met_Color
                                 123.395390
                                              0.416
                     51.315188
                                                               0.677664
## Automatic
                     63.567598
                                 262.282017
                                              0.242
                                                               0.808583
## CC
                      0.010747
                                   0.097711
                                              0.110
                                                               0.912456
## Doors
                    -55.700492
                                  63.966255
                                             -0.871
                                                               0.384230
## Quarterly_Tax
                                                        0.00000070465597 ***
                     13.080021
                                   2.608396
                                              5.015
                                   ## Weight
                     16.219638
```

```
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1392 on 588 degrees of freedom
## Multiple R-squared: 0.8703, Adjusted R-squared: 0.8679
## F-statistic: 358.7 on 11 and 588 DF, p-value: < 0.0000000000000022
```

Summary:Residuals is the difference between the actual observed response values and the response values that the model predicted. We can see that the distribution of the residuals do not appear to be strongly symmetrical (-9781.2 to 6912.9 with median at 0.9). That means that the model predicts certain points that fall far away from the actual observed points.

###Coefficients ### Intercept: a negative value for intercept means that the expected value on our dependent variable (Price) will be less than 0 when all independent/predictor variables are set to 0.

###Estimate: The effect of predictor on the response variable value. For instance, for Age\_08\_04, as the age increases, the price drops by -133.271592

###Standard Error: measures the average amount that the coefficient estimates vary from the actual average value of our response variable. For instance, Age\_08\_04 estimate can vary by 4.901960.

###t-value ###t-value far from zero indicates that we can reject the null hypothesis - that is we could declare a relation between Price and Age\_08\_04.

###Pr(>t) ###A small p-value indicates that it is unlikely we will observe a relationship between the predictor (Age\_08\_04) and response variables (Price) due to chance. Typically, a p-value of 5% or less is a good cut-off point.

###t-value far from zero and small Pr(>t), typically less than 5% indicates that we can reject the null hypothesis or declare that there exists a relation between the predictor (e.g., Age\_08\_04) and the response variables (e.g., Price). So, the predictors that have relationship with our response variable Price are: Age\_08\_04, KM, Fuel\_TypePetrol, HP, Quarterly\_Tax, and Weight. Other predictors do not seem to have strong relationship with Price.

###Residual standard error ###measure of the quality of a linear regression fit. The average amount that the response (Price) will deviate from the true regression line. In our case it is 1392.

###Multiple R-squared, Adjusted R-squared ###measure of how well the model is fitting the actual data. Measure of the linear relationship between our predictor variable (e.g., Age\_08\_04) and our response / target variable (Price) ###In our example, the R-squared we get is 0.8703. Or roughly 87% of the variance found in the response variable (Price) can be explained by the predictor variables (e.g., Age\_08\_04).

###F-Statistic is a indicator of whether there is a relationship between our predictor and the response variables. The further the F-statistic is from 1 the better it is. When the number of data points is large, an F-statistic that is only a little bit larger than 1 is already sufficient to reject the null hypothesis (H0: There is no relationship between target variable and predictor variables). In our case it is: 358.7, which indicates that we can reject the null hypothesis.

## Make predictions on a hold-out set

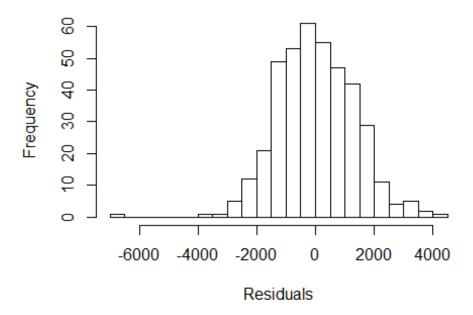
```
library(forecast)
## Registered S3 method overwritten by 'xts':
                from
##
     method
##
     as.zoo.xts zoo
## Registered S3 method overwritten by 'quantmod':
##
     method
                       from
##
     as.zoo.data.frame zoo
## Registered S3 methods overwritten by 'forecast':
##
     method
                        from
##
     fitted.fracdiff
                        fracdiff
##
     residuals.fracdiff fracdiff
# use predict() to make predictions on a new set.
car.lm.pred <- predict(car.lm, valid.df)# predicting the price of validation</pre>
data using the linear regression model.car.lm.pred is an array of 400 price
predictions.
options(scipen=999, digits = 0)
some.residuals <- valid.df$Price[1:20] - car.lm.pred[1:20]#computing the</pre>
diffrence between the validation dataset price and predicted prices for the
first 20 prices .
data.frame("Predicted" = car.lm.pred[1:20], "Actual" = valid.df$Price[1:20],
           "Residual" = some.residuals)# creating a table with 3 columns
showing Predicted, Actual and Residual prices and the table contains 20 rows.
##
      Predicted Actual Residual
## 2
          16447 13750
                          -2697
## 7
          16757 16900
                            143
## 8
          16750 18600
                           1850
          20959 21500
## 9
                            541
                          -1400
## 10
          14350 12950
          21124 19950
                          -1174
## 12
          20964 19600
## 13
                          -1364
## 14
          20408 21500
                           1092
          16817 17950
## 18
                           1133
## 21
          15053 15950
                            897
          15800 15950
## 23
                            150
## 24
          16307 16950
                            643
## 26
          16786 15950
                           -836
## 30
          16484 17950
                           1466
```

```
## 32
          16233 15750
                           -483
## 34
          15752 14950
                           -802
          15485 15750
## 36
                            265
## 38
          16629 14950
                          -1679
## 46
          18069 19000
                            931
## 47
          17441 17950
                            509
options(scipen=999, digits = 3)
# use accuracy() to compute common accuracy measures.
accuracy(car.lm.pred, valid.df$Price)
##
              ME RMSE MAE
                             MPE MAPE
## Test set 19.6 1325 1049 -0.75 9.35
```

###Summary: Here, we have created 3 columns showing the predicted, Actual and residual prices and the table contains 20 rows. The function accuracy gives us multiple measures of accuracy of the model fit. ##Mean error(ME) 19.6 is an informal term that usually refers to the average of all errors in a set. ### The Root Mean Square Error(RMSE)value is 1325.The RMSE is the square root of the variance of the residuals. It indicates the absolute fit of the model to the data-how close the observed data points are to the model's predicted values. The RMSE will always be larger or equal to the MAE. The value of MAE is 1049. We can interpret that the average diffrence between the predicted and the actual price is 276. The greater difference between them, the greater the variance in the individual errors. ###Mean Absolute Error(MAE) value is 1049. It is the absolute average of the difference between predicted and actual values of price in the test. ###Mean Percentage Error(MPE)is -0.75.It is average value of percentage errors by which predicted values differ from actual values. A negetive value here indicates that the predicted values are less than the actual values. ###Mean Absolute Percentage Error(MAPE) value is 9.35.It is a measure to validate predicted values. MAPE states that our model's predictions are, on average, 9.35% off from actual value.

#### ###Histogram of residuals

```
library(forecast)
car.lm.pred <- predict(car.lm, valid.df)# predicting the price of validation
data using the linear regression model.car.lm.pred is an array of 400 price
predictions.
all.residuals <- valid.df$Price - car.lm.pred #computing the diffrence
between the validation data price and price predictions.
length(all.residuals[which(all.residuals > -2000 & all.residuals <
2000)])/400#length of all residual values that are greater than -2000 and all
residual values less than 2000.
## [1] 0.892
hist(all.residuals, breaks = 25, xlab = "Residuals", main = "")</pre>
```



###0.892...... ###Summary:The Histogram of the Residual can be used to check whether the variance is normally distributed. Here, the histogram shows that the residurals are normally distributed, however it is negetively left skewed and also has outliers.

```
Run an exhaustive search for the best model
# use regsubsets() in package leaps to run an exhaustive search.
# unlike with lm, categorical predictors must be turned into dummies
manually.
# create dummies for fuel type
train.df <- car.df[train.index, selected.var]# Assigning sampled 60% of the
data to training set.
valid.df <- car.df[-train.index, selected.var]##Assigning the remaining 40%</pre>
of the data to validation
train.index <- sample(c(1:1000), 600)#Here we are taking 60% of the data as
training set. Train. index holds 600 index of rows of the 1000
train.df <- car.df[train.index, selected.var]# Assigning sampled 60% of the
data to training set.
dim(train.df)##dimension of training data set.contains 600 rows and 11
columns.
## [1] 600 11
Fuel_Type1 <- as.data.frame(model.matrix(~ 0 + Fuel_Type, data=train.df))#</pre>
Fuel_Type1 is a table with 600 rows and three newly created columns. Here,
```

Fuel Type column is split into three columns: Fuel TypeCNG, Fuel TypeDiesel,

```
and Fuel_TypePetrol. The values for these columns are 0 or 1, indicating
whether the original column had CNG, Disel, or Petrol.
# replace Fuel_Type column with 2 dummies
train.df <- cbind(train.df[,-4], Fuel_Type1[,])# Fuel_Type column is removed</pre>
and three new Fuel_Type1 columns are inserted into train.df. train.df now
contains 13 columns.
head(train.df)
       Price Age 08 04
                           KM HP Met Color Automatic
                                                          CC Doors Quarterly Tax
## 979 8745
                     65 45681 110
                                                     0 1600
                                                                 3
                                           0
                                                                               69
## 209 11450
                     41 84312 110
                                                     0 1600
                                                                 5
                                                                               85
                                           0
## 148 24500
                     13 19988 110
                                           1
                                                     0 1600
                                                                 5
                                                                               85
## 704 10500
                                                     0 1600
                                                                 5
                     65 93428 110
                                           1
                                                                               85
                                                                 5
## 501 9700
                     51 57645 110
                                           0
                                                     0 1600
                                                                               85
                                                                 3
## 343 14950
                     42 29640 110
                                           0
                                                                               85
       Weight Fuel_TypeCNG Fuel_TypeDiesel Fuel_TypePetrol
##
## 979
         1050
                          0
## 209
         1080
                          0
                                                            1
                                           0
## 148
         1130
                          0
                                           0
                                                            1
## 704
         1075
                          0
                                           0
                                                            1
## 501
         1080
                          0
                                           0
                                                            1
## 343
                          0
                                           0
                                                            1
         1055
Fuel_Type2 <- as.data.frame(model.matrix(~ 0 + Fuel_Type, data=valid.df))#</pre>
Similar to Fuel_Type1, but for the valid.df.
# replace Fuel_Type column with 2 dummies
valid.df <- cbind(valid.df[,-4], Fuel Type2[,])# Replaced Fuel Type column</pre>
with three new columns from Fuel_Type2. Now valid.df has 13 columns.
head(valid.df)
##
      Price Age_08_04
                              HP Met_Color Automatic
                                                         CC Doors Quarterly_Tax
                          ΚM
## 2 13750
                    23 72937
                                                    0 2000
                                                                3
                              90
                                          1
                                                                             210
## 7 16900
                                                    0 2000
                                                                3
                    27 94612
                              90
                                          1
                                                                             210
## 8 18600
                    30 75889
                                          1
                                                    0 2000
                                                                3
                                                                             210
                              90
## 9 21500
                   27 19700 192
                                          0
                                                    0 1800
                                                                3
                                                                             100
## 10 12950
                   23 71138 69
                                          0
                                                    0 1900
                                                                3
                                                                             185
                    22 43610 192
## 12 19950
                                          0
                                                    0 1800
                                                                3
                                                                             100
##
      Weight Fuel_TypeCNG Fuel_TypeDiesel Fuel_TypePetrol
## 2
        1165
                         0
                                          1
## 7
        1245
                         0
                                          1
                                                           0
## 8
                         0
        1245
                                          1
                                                           0
                         0
## 9
        1185
                                          0
                                                           1
## 10
                         0
                                          1
                                                           0
        1105
## 12
        1185
                                                           1
dim(valid.df)
## [1] 400 13
#install.packages("leaps")
library(leaps)
```

```
search <- regsubsets(Price ~ ., data = train.df, nbest = 1, nvmax =</pre>
dim(train.df)[2],
                     method = "exhaustive") # search is a list of 28 models
## Warning in leaps.setup(x, y, wt = wt, nbest = nbest, nvmax = nvmax,
## force.in = force.in, : 1 linear dependencies found
## Warning in leaps.setup(x, y, wt = wt, nbest = nbest, nvmax = nvmax,
## force.in = force.in, : nvmax reduced to 11
sum <- summary(search)# regsubsets helps with variable selection. We have 12</pre>
variables and summary provides their importance across 11 models.
# show modeLs
sum$which # provides which variables (or predictors) are included
(TRUE/FALSE) in the models (there are 11 models)
##
      (Intercept) Age 08 04
                                      HP Met Color Automatic
                                ΚM
                                                                 CC Doors
## 1
             TRUE
                       TRUE FALSE FALSE
                                             FALSE
                                                        FALSE FALSE FALSE
## 2
             TRUE
                       TRUE FALSE FALSE
                                             FALSE
                                                        FALSE FALSE FALSE
## 3
             TRUE
                       TRUE FALSE FALSE
                                             FALSE
                                                        FALSE FALSE
## 4
             TRUE
                       TRUE
                             TRUE FALSE
                                             FALSE
                                                        FALSE FALSE
## 5
             TRUE
                       TRUE
                              TRUE FALSE
                                             FALSE
                                                        FALSE FALSE
                                                                     TRUE
             TRUE
                       TRUE
                              TRUE FALSE
                                                        FALSE FALSE
## 6
                                             FALSE
                                                                     TRUE
## 7
             TRUE
                       TRUE
                             TRUE FALSE
                                             FALSE
                                                        TRUE FALSE
                                                                     TRUE
                       TRUE
                             TRUE
                                                         TRUE FALSE
## 8
             TRUE
                                   TRUE
                                             FALSE
                                                                     TRUE
## 9
                       TRUE
                             TRUE
             TRUE
                                   TRUE
                                             FALSE
                                                         TRUE
                                                               TRUE
                                                                     TRUE
             TRUE
                       TRUE
                             TRUE
                                   TRUE
                                                         TRUE
                                                               TRUE
## 10
                                             FALSE
                                                                     TRUE
## 11
             TRUE
                       TRUE
                             TRUE
                                   TRUE
                                              TRUE
                                                         TRUE TRUE
                                                                     TRUE
##
      Quarterly_Tax Weight Fuel_TypeCNG Fuel_TypeDiesel Fuel_TypePetrol
## 1
              FALSE FALSE
                                   FALSE
                                                   FALSE
                                                                    FALSE
## 2
                      TRUE
                                   FALSE
                                                   FALSE
                                                                    FALSE
              FALSE
                      TRUE
## 3
              FALSE
                                   FALSE
                                                   FALSE
                                                                     TRUE
## 4
              FALSE
                      TRUE
                                   FALSE
                                                   FALSE
                                                                     TRUE
## 5
                                                                     TRUE
              FALSE
                      TRUE
                                   FALSE
                                                   FALSE
## 6
               TRUE
                      TRUE
                                   FALSE
                                                   FALSE
                                                                     TRUE
## 7
               TRUE
                      TRUE
                                   FALSE
                                                   FALSE
                                                                     TRUE
## 8
               TRUE
                      TRUE
                                                                     TRUE
                                   FALSE
                                                   FALSE
## 9
               TRUE
                      TRUE
                                   FALSE
                                                   FALSE
                                                                     TRUE
## 10
               TRUE
                      TRUE
                                    TRUE
                                                   FALSE
                                                                     TRUE
## 11
               TRUE
                      TRUE
                                    TRUE
                                                                    FALSE
                                                    TRUE
# show metrics
sum$rsq # the r-squared metric for all the 11 models
## [1] 0.749 0.812 0.875 0.885 0.890 0.891 0.893 0.894 0.895 0.896 0.896
sum$adjr2 # adjusted r-squared metric for all the 11 models
## [1] 0.748 0.812 0.874 0.884 0.889 0.890 0.892 0.892 0.893 0.894 0.894
sum$cp # mallow's cp metric for all the 11 models
```

Summary: The exhaustive search using regsubsets showed inclusion of predictors across 11 models. We are looking for predictors that are not included for most of the models to deem them unimportant. For instance, Fuel\_TypeCNG is only included in one model. CC and Met\_Color are other such predictors. Whereas, some predictors like Age\_08\_04 is included in all the models. Finally, rsq, adjr2, and cp metrics are shown.

# use step() to run stepwise regression, backward selection.

```
head(valid.df)#first 6 rows of validation data set.
      Price Age 08 04
                          KM HP Met Color Automatic
                                                         CC Doors Ouarterly Tax
##
                                                                             210
## 2
      13750
                    23 72937
                                                    0 2000
                                                                3
                              90
                                          1
## 7 16900
                   27 94612
                              90
                                          1
                                                    0 2000
                                                                3
                                                                             210
## 8 18600
                   30 75889
                                          1
                                                    0 2000
                                                                3
                              90
                                                                             210
## 9 21500
                   27 19700 192
                                                    0 1800
                                                                3
                                                                             100
## 10 12950
                   23 71138 69
                                                                3
                                                    0 1900
                                                                             185
                                                                3
## 12 19950
                   22 43610 192
                                          0
                                                    0 1800
                                                                             100
      Weight Fuel_TypeCNG Fuel_TypeDiesel Fuel_TypePetrol
##
## 2
                         0
                                          1
        1165
## 7
        1245
                         0
                                          1
                                                           0
                         0
## 8
        1245
                                          1
                                                           0
## 9
        1185
                         0
                                          0
                                                           1
        1105
                                          1
## 10
                                                           0
## 12
        1185
                         0
head(train.df)# first 6 rows of training data set.
       Price Age_08_04
                           KM HP Met_Color Automatic
                                                          CC Doors Quarterly Tax
## 979 8745
                                                                 3
                     65 45681 110
                                           0
                                                     0 1600
                                                                               69
## 209 11450
                     41 84312 110
                                           0
                                                      0 1600
                                                                 5
                                                                               85
                                                                 5
## 148 24500
                     13 19988 110
                                           1
                                                     0 1600
                                                                               85
                                                                 5
## 704 10500
                     65 93428 110
                                           1
                                                     0 1600
                                                                               85
                                           0
                                                      0 1600
                                                                 5
                                                                               85
## 501 9700
                     51 57645 110
                     42 29640 110
                                                                 3
## 343 14950
                                           0
                                                     0 1600
                                                                               85
       Weight Fuel_TypeCNG Fuel_TypeDiesel Fuel_TypePetrol
##
## 979
         1050
                          0
                                           0
                                                            1
## 209
         1080
                          0
                                           0
                                                            1
## 148
         1130
                          0
                                           0
                                                            1
## 704
         1075
                          0
                                                            1
## 501
         1080
                          0
                                                            1
## 343
                                                            1
         1055
```

car.lm <-  $lm(Price \sim ., data = train.df)$ # use lm() to run a linear regression of Price on all 11 predictors in the training set. use . after  $\sim$  to include all the remaining columns in train.df as predictors.

```
car.lm.step <- step(car.lm, direction = "backward")#computing backward</pre>
selection on the linear regression model car.lm using step command.
## Start: AIC=8541
## Price ~ Age 08 04 + KM + HP + Met Color + Automatic + CC + Doors +
       Quarterly_Tax + Weight + Fuel_TypeCNG + Fuel_TypeDiesel +
##
       Fuel TypePetrol
##
##
## Step: AIC=8541
## Price ~ Age 08 04 + KM + HP + Met Color + Automatic + CC + Doors +
##
       Quarterly_Tax + Weight + Fuel_TypeCNG + Fuel_TypeDiesel
##
##
                     Df Sum of Sq
                                        RSS AIC
## - Met_Color
                          2266092 878937940 8540
## <none>
                                   876671847 8541
## - Automatic
                    1
                          8366413 885038261 8545
## - CC
                     1 14321587 890993434 8549
## - Fuel_TypeDiesel 1 14811707 891483554 8549
## - Quarterly_Tax
                     1 15756166 892428014 8550
## - HP
                     1 18363944 895035791 8551
## - Doors
                     1 25213122 901884970 8556
## - Fuel_TypeCNG
                     1 54031878 930703726 8575
## - KM
                     1 68220130 944891977 8584
                     1 389146231 1265818078 8759
## - Weight
## - Age 08 04
                     1 758018466 1634690313 8913
##
## Step: AIC=8540
## Price ~ Age 08 04 + KM + HP + Automatic + CC + Doors + Quarterly Tax +
##
       Weight + Fuel_TypeCNG + Fuel_TypeDiesel
##
                     Df Sum of Sq
##
                                        RSS AIC
## <none>
                                   878937940 8540
## - Automatic
                     1
                         8574722 887512662 8544
## - CC
                     1 13626991 892564931 8548
## - Fuel_TypeDiesel 1 14991775 893929715 8549
## - Quarterly_Tax
                     1 15326578 894264518 8549
## - HP
                     1 18229552 897167491 8551
## - Doors
                     1 24564771 903502711 8555
## - Fuel_TypeCNG
                     1 53685703 932623643 8574
## - KM
                     1 68369633 947307572 8583
## - Weight
                     1 388073155 1267011095 8758
## - Age 08 04
                     1 775312160 1654250100 8918
summary(car.lm.step) # Which variables did it drop?##
Met_color,Fuel_typePetrol got dropped.
##
## Call:
## lm(formula = Price ~ Age 08 04 + KM + HP + Automatic + CC + Doors +
```

```
##
      Quarterly Tax + Weight + Fuel TypeCNG + Fuel TypeDiesel,
##
      data = train.df)
##
## Residuals:
##
     Min
             1Q Median
                           3Q
                                Max
   -3944
                  -120
                                6034
##
           -833
                          740
##
## Coefficients:
                                 Std. Error t value
                                                               Pr(>|t|)
##
                      Estimate
## (Intercept)
                  -20308.35538
                                 2279.27485
                                             4.77395 -22.79 < 0.0000000000000000 ***
## Age_08_04
                    -108.81655
                                    0.00226
                                            -6.77
                                                         0.00000000031 ***
## KM
                      -0.01530
## HP
                      28.24247
                                    8.08046
                                              3.50
                                                                0.00051 ***
## Automatic
                    -614.56814
                                  256.37842
                                             -2.40
                                                                0.01684 *
## CC
                                    0.77199
                                             -3.02
                      -2.33286
                                                                0.00262 **
## Doors
                    -241.72075
                                  59.57706
                                             -4.06
                                                         0.000056338057 ***
## Quarterly_Tax
                       8.29217
                                    2.58742
                                              3.20
                                                                0.00142 **
## Weight
                                    2.28423
                                             36.83627
## Fuel TypeCNG
                   -3332.89616
                                 555.66612
                                             -6.00
                                                         0.000000003487 ***
## Fuel_TypeDiesel -2146.48096
                                 677.20783
                                             -3.17
                                                                0.00161 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1220 on 589 degrees of freedom
## Multiple R-squared: 0.896, Adjusted R-squared: 0.894
## F-statistic: 505 on 10 and 589 DF, p-value: <0.00000000000000002
car.lm.step.pred <- predict(car.lm.step, valid.df)# predicting the price of</pre>
validation data using the linear stepwise regression model.car.lm.step .
accuracy(car.lm.step.pred, valid.df$Price)##accuracy of the predicting price
of validation data using actual validation price
##
              ME RMSE MAE
                             MPE MAPE
## Test set -4.92 1350 1017 -1.19 9.09
```

Summary: Backward selection (or backward elimination), which starts with all predictors in the model (full model), iteratively removes the least contributive predictors, and stops when you have a model where all predictors are statistically significant. Accordingly, least contributive predictors Fuel\_typePetrol,Met\_color were removed .The mean error(ME) is -25.5. The Root mean square error(RMSE) is 1362 and the Mean absolute error(MAE) is 1019.The diffrence between RMSE and MAE is 343.The greater difference between them, the greater the variance in the individual errors.Mean percentage error is -1.42. And the Mean absolute percentage error is 9.13.

#### **Forward selection**

```
car.lm <- lm(Price ~ ., data = train.df)#use Lm() to run a Linear regression</pre>
of Price on all 11 predictors in the training set. use . after ~ to include
all the remaining columns in train.df as predictors.
car.lm.step <- step(car.lm, direction = "forward")#computing Forward</pre>
selection on the linear regression model car.lm using step command
## Start: AIC=8541
## Price ~ Age 08 04 + KM + HP + Met Color + Automatic + CC + Doors +
      Quarterly_Tax + Weight + Fuel_TypeCNG + Fuel_TypeDiesel +
##
##
      Fuel_TypePetrol
summary(car.lm.step) #
##
## Call:
## lm(formula = Price ~ Age 08 04 + KM + HP + Met Color + Automatic +
      CC + Doors + Quarterly_Tax + Weight + Fuel_TypeCNG + Fuel_TypeDiesel +
##
##
      Fuel_TypePetrol, data = train.df)
##
## Residuals:
##
     Min
             1Q Median
                           3Q
                                 Max
##
   -3844
           -834
                   -80
                          740
                                6014
##
## Coefficients: (1 not defined because of singularities)
                      Estimate
                                 Std. Error t value
                                                               Pr(>|t|)
                                              ## (Intercept)
                  -20399.20522
                                 2279.46102
                                    4.79841 -22.55 < 0.0000000000000000 ***
## Age_08_04
                    -108.19499
                                             -6.76
                                                         0.000000000032 ***
## KM
                      -0.01529
                                    0.00226
                                                                0.00048 ***
## HP
                      28.34798
                                    8.07735
                                               3.51
## Met Color
                     132.93914
                                  107.83107
                                               1.23
                                                                0.21813
                                              -2.37
## Automatic
                    -607.22139
                                  256.33462
                                                                0.01817 *
## CC
                                              -3.10
                                                                0.00203 **
                      -2.39701
                                    0.77340
## Doors
                                   59.61602
                                              -4.11
                                                          0.000044757491 ***
                    -245.15818
## Quarterly Tax
                                    2.58816
                                               3.25
                                                                0.00122 **
                       8.41368
## Weight
                      36.89526
                                    2.28373
                                              ## Fuel_TypeCNG
                   -3344.06956
                                  555.49498
                                             -6.02
                                                         0.000000003072 ***
```

```
## Fuel_TypeDiesel -2133.79761 676.98732 -3.15 0.00170 **

## Fuel_TypePetrol NA NA NA NA NA

## ---

## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1

##

## Residual standard error: 1220 on 588 degrees of freedom

## Multiple R-squared: 0.896, Adjusted R-squared: 0.894

## F-statistic: 460 on 11 and 588 DF, p-value: <0.000000000000000000
```

###Summary:Forward selection,which starts with no predictors in the model, iteratively adds the most contributive predictors, and stops when the improvement is no longer statistically significant.so, here the most contributive predictors are  $Age_08_04$ , KM , HP , Met\_Color , Automatic ,CC, Doors, Quarterly\_Tax, Weight, Fuel\_TypeCNG, Fuel\_TypeDiesel, Fuel TypePetrol.

#### #Stepwise

```
# use step() to run stepwise regression.
car.lm <- lm(Price ~ ., data = train.df)#use Lm() to run a linear regression
of Price on all 11 predictors in the training set. use . after \sim to include
all the remaining columns in train.df as predictors.
car.lm.step <- step(car.lm, direction = "both")#computing Forward selection</pre>
and backward selection on the linear regression model car.lm using step
command.
## Start: AIC=8541
## Price ~ Age_08_04 + KM + HP + Met_Color + Automatic + CC + Doors +
##
       Quarterly_Tax + Weight + Fuel_TypeCNG + Fuel_TypeDiesel +
##
       Fuel_TypePetrol
##
##
## Step: AIC=8541
## Price ~ Age 08 04 + KM + HP + Met Color + Automatic + CC + Doors +
       Quarterly_Tax + Weight + Fuel_TypeCNG + Fuel_TypeDiesel
##
##
                     Df Sum of Sq
##
                                         RSS AIC
## - Met Color
                          2266092 878937940 8540
## <none>
                                   876671847 8541
## - Automatic
                      1
                          8366413 885038261 8545
## - CC
                      1 14321587 890993434 8549
## - Fuel_TypeDiesel 1 14811707 891483554 8549
## - Quarterly_Tax
                      1 15756166 892428014 8550
## - HP
                      1 18363944 895035791 8551
## - Doors
                      1 25213122 901884970 8556
## - Fuel_TypeCNG
                      1 54031878 930703726 8575
## - KM
                      1 68220130 944891977 8584
## - Weight
                      1 389146231 1265818078 8759
## - Age 08 04
                      1 758018466 1634690313 8913
##
## Step: AIC=8540
```

```
## Price ~ Age 08 04 + KM + HP + Automatic + CC + Doors + Quarterly Tax +
      Weight + Fuel_TypeCNG + Fuel_TypeDiesel
##
##
##
                    Df Sum of Sq
                                       RSS AIC
## <none>
                                  878937940 8540
## + Met Color
                     1
                         2266092 876671847 8541
## - Automatic
                         8574722 887512662 8544
                     1
## - CC
                     1
                        13626991 892564931 8548
## - Fuel_TypeDiesel 1
                       14991775 893929715 8549
## - Quarterly_Tax
                     1 15326578 894264518 8549
## - HP
                     1 18229552 897167491 8551
## - Doors
                     1 24564771 903502711 8555
## - Fuel_TypeCNG
                     1 53685703 932623643 8574
## - KM
                     1 68369633 947307572 8583
## - Weight
                     1 388073155 1267011095 8758
                     1 775312160 1654250100 8918
## - Age_08_04
summary(car.lm.step) #which variables were added/dropped?
##
## Call:
## lm(formula = Price ~ Age 08 04 + KM + HP + Automatic + CC + Doors +
      Quarterly_Tax + Weight + Fuel_TypeCNG + Fuel_TypeDiesel,
      data = train.df)
##
##
## Residuals:
##
     Min
             1Q Median
                           3Q
                                 Max
##
   -3944
           -833
                          740
                                6034
                  -120
##
## Coefficients:
##
                      Estimate
                                 Std. Error t value
                                                               Pr(>|t|)
## (Intercept)
                  -20308.35538
                                 2279.27485
                                             -108.81655
                                    4.77395 -22.79 < 0.00000000000000000 ***
## Age 08 04
## KM
                      -0.01530
                                    0.00226
                                             -6.77
                                                         0.000000000031 ***
                                              3.50
                                                                0.00051 ***
## HP
                      28.24247
                                    8.08046
## Automatic
                                             -2.40
                    -614.56814
                                  256.37842
                                                                0.01684 *
## CC
                      -2.33286
                                    0.77199
                                             -3.02
                                                                0.00262 **
                                             -4.06
                                                         0.000056338057 ***
## Doors
                    -241.72075
                                   59.57706
## Quarterly Tax
                                    2.58742
                                             3.20
                                                                0.00142 **
                       8.29217
                                    2.28423
                                             ## Weight
                      36.83627
## Fuel_TypeCNG
                   -3332.89616
                                  555.66612
                                             -6.00
                                                         0.000000003487 ***
                                             -3.17
## Fuel TypeDiesel -2146.48096
                                  677.20783
                                                                0.00161 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1220 on 589 degrees of freedom
## Multiple R-squared: 0.896, Adjusted R-squared: 0.894
## F-statistic: 505 on 10 and 589 DF, p-value: <0.0000000000000000
```

car.lm.step.pred <- predict(car.lm.step, valid.df)# predicting the price of validation data using the linear stepwise regression model.car.lm.step. accuracy(car.lm.step.pred, valid.df\$Price)##accuracy of the predicting price of validation data using actual validation price

```
## ME RMSE MAE MPE MAPE
## Test set -4.92 1350 1017 -1.19 9.09
```

###Summary:which is a combination of forward and backward selections. You start with no predictors, then sequentially add the most contributive predictors (like forward selection). After adding each new variable, remove any variables that no longer provide an improvement in the model fit (like backward selection). Age\_08\_04, KM, HP,Doors,Quarterly\_Tax,Weight,Fuel\_TypeCNG, Fuel\_TypeDiesel,CC,Automatic are the contributive predictors. Fuel\_typePetrol,Met\_color are the least contributive predictors which were dropped. The mean error(ME) is -25.5. The Root mean square error(RMSE) is 1362 and the Mean absolute error(MAE) is 1019. The diffrence between RMSE and MAE is 343. The greater difference between them, the greater the variance in the individual errors. Mean percentage error is -1.42. And the Mean absolute percentage error is 9.13.