

String functions:

Stringstream:

clear() — to clear the stream

str() — to get and set string object whose content is present in stream.

operator << — add a string to the stringstream object.

operator >> — read something from the stringstream object.

Using stringstream we can convert string into int, float or double data type

```
int x = 0;
ss >> x;*/
```

stoi(both for strings and character array) and atoi(only for character array) functions can also be used to convert a string to integer. Similarly atof ..

Using stringstream we can split a string wrt a delimiter

```
/*stringstream check1(line);
string intermediate;
while(getline(check1, intermediate, ' '))
{
    vector.push_back(intermediate);
}
*/
```

String class functions:

c_str returns null terminated char array version of string

```
/* const char* charstr = str.c_str(); */
```

find returns index where pattern is found. If pattern is not there it returns predefined constant npos whose value is -1

```
if (str6.find(str4) != string::npos) {
    cout << "str4 found in str6 at " <<
    str6.find(str4) << " position" << endl;
} else {
    cout << "str4 not found in str6" << endl;
}
*/
```

compare(string_to_compare):- It is used to compare two strings. It returns the difference of second string and first string in integer

find("string"): Searches the string for the first occurrence of the substring specified in arguments. It returns the position of the first occurrence of substring.

find_first_of("string"): Searches the string for the first character that matches any of the characters specified in its arguments. It returns the position of the first character that matches.

find_last_of("string"): Searches the string for the last character that matches any of the characters specified in its arguments. It returns the position of the last character that matches.

rfind("string"): Searches the string for the last occurrence of the substring specified in arguments. It returns the position of the last occurrence of substring

substr: returns the substring of a string. str.substr(3,5) starting from index 3 of length 5

KMP algorithm: //0 based indexing

```
int* pi;
int* compute_pi(string p){
    int m=p.length();
    pi=new int[m];
    pi[0]=-1;
    int k=-1;
    for(int q=1;q<m;q++){
        while(k>-1&& p[q]!=p[k+1])
            k=pi[k];
        if(p[q]==p[k+1])
            k=k+1;
        pi[q]=k;
    }
    return pi;
}
```

```
void kmp(string t,string p){
    int n=t.length();
    int m=p.length();
    pi=compute_pi(p);
    int k=-1;
    for(int i=0;i<n;i++){
        while(k>-1&& t[i]!=p[k+1])
            k=pi[k];
        if(t[i]==p[k+1])
            k=k+1;
        if(k==m-1){
            cout<<i-m+1<<" ";
        }
    }
}
```

```

        k=pi[k];
    }
}
cout<<"\n";
}

next_permutation and prev_permutation //before
calling these array should be sorted
do {
    cout << myints[0] << ' ' << myints[1] << ' ' <<
myints[2] << '\n';
} while (next_permutation(myints,myints+3) );

lower_bound and upper_bound //before calling
these array should be sorted
low=lower_bound (v.begin(), v.end(), 20);
up=upper_bound (v.begin(), v.end(), 20); // they
return iterator not index

int modularExponentiation(int x,int n,int M)
{
    int result=1;
    while(n>0)
    {
        if(n% 2 ==1)
            result=(result * x)%M;
        x=(x*x)%M;
        n=n/2;
    }
    return result;
}

int d, x, y; //d is gcd and Ax+By=d
void extendedEuclid(int A, int B) {
    if(B == 0) {
        d = A;
        x = 1;
        y = 0;
    }
    else {
        extendedEuclid(B, A%B);
        int temp = x;
        x = y;
        y = temp - (A/B)*y;
    }
}

```

```

int modInverse(int A,int M)
{
    return modularExponentiation(A,M-2,M);
}

```

Prime factorisation:

```

#define MAXN 100001
int spf[MAXN];
void sieve()
{
    spf[1] = 1;
    for (int i=2; i<MAXN; i++)
        spf[i] = i;
    for (int i=4; i<MAXN; i+=2)
        spf[i] = 2;
    for (int i=3; i*i<MAXN; i++)
    {
        if (spf[i] == i)
        {
            for (int j=i*i; j<MAXN; j+=i)
                if (spf[j]==j)
                    spf[j] = i;
        }
    }
}
vector<int> getFactorization(int x)
{
    vector<int> ret;
    while (x != 1)
    {
        ret.push_back(spf[x]);
        x = x / spf[x];
    }
    return ret;
}

```

bfs:

```

int main() {
    int n,m,i,u,v;
    cin>>n>>m;
    vector<int> adj[n+1];
    for(i=0;i<m;i++){
        cin>>u>>v;
        adj[u].push_back(v);
        adj[v].push_back(u);
    }
    vector<int> visited(n+1,false);
    visited[1]=true;
}

```

```

queue<int> q;
q.push(1);
while(!q.empty()){
    int x=q.front();
    q.pop();
    for(i=0;i<adj[x].size();i++){
        if(!visited[adj[x][i]]){
            visited[adj[x][i]]=true;
            q.push(adj[x][i]);
        }
    }
}
return 0;
}

```

iterative dfs:

```

void dfs(int v,vector<int> &visited,vector<vector<int> > adj){
    stack<int> s;
    s.push(v);
    while(!s.empty()){
        int x=s.top();
        s.pop();
        if(!visited[x]){
            cout<<x<<" ";
            visited[x]=true;
        }
        for(int i=0;i<adj[x].size();i++){
            if(!visited[adj[x][i]])
                s.push(adj[x][i]);
        }
    }
}

```

```

int main() {
    int n,m,i,u,v;
    cin>>n>>m;
    vector<vector<int> > adj(n+1);
    for(i=0;i<m;i++){
        cin>>u>>v;
        adj[u].push_back(v);
        adj[v].push_back(u);
    }
    vector<int> visited(n+1,false);
    for(i=1;i<=n;i++)
        if(!visited[i])
            dfs(i,visited,adj);
    return 0;
}

```

Kruskals MST:

```

struct edge{
    int u,v,w;
};
bool comp(edge e1,edge e2){
    return (e1.w<e2.w);
}
int find(int x,int pa[]){
    if(pa[x]==x) return x;
    return pa[x]=find(pa[x],pa);
}
int main() {
    int n,m,i,u,v,w;
    cin>>n>>m;
    vector<edge> edges(m);
    for(i=0;i<m;i++){
        cin>>edges[i].u>>edges[i].v>>edges[i].w;
    }
    sort(edges.begin(),edges.end(),comp);
    int pa[n+1],rank[n+1];
    for(i=1;i<=n;i++)
        pa[i]=i,rank[i]=0;
    int j=0,ans=0;
    i=0;
    while(j<n-1){
        struct edge e=edges[i++];
        int px=find(e.u,pa);
        int py=find(e.v,pa);
        if(px!=py){
            ans=ans+e.w;
            j++;
            if(rank[px]<rank[py]) pa[px]=py;
            else if(rank[px]>rank[py]) pa[py]=px;
            else pa[py]=px,rank[px]++;
        }
    }
    cout<<ans<<"\n";
    return 0;
}

```

Prims MST: //vertices are 1,2,3,...

```

typedef pair<int,int> pii;
struct heapnode{
    int v;
    int w;
};

```

```

int hsize;
void swap(heapnode heap[],int x,int y, int index[]){
    index[heap[x].v]=y;
    index[heap[y].v]=x;
    struct heapnode t=heap[x];
    heap[x]=heap[y];
    heap[y]=t;
}
void minheapify(heapnode heap[],int i,int index[] ){
    int sml=i;
    int l=2*i+1;
    int r=2*i+2;
    if(l<hsize&&heap[sml].w>heap[l].w)
        sml=l;
    if(r<hsize&&heap[sml].w>heap[r].w)
        sml=r;
    if(sml!=i){
        swap(heap,sml,i,index);
        minheapify(heap,sml,index);
    }
}
void deletemin(heapnode heap[],int index[]){
    if (hsize == 1)
    {
        hsize--;
        return;
    }
    swap(heap,0,hsize-1,index);
    hsize--;
    minheapify(heap,0,index);
}
void decreasekey(heapnode heap[],int i,int w,int index[]){
    heap[i].w=w;
    while(i!=0&&heap[(i-1)/2].w>heap[i].w){
        swap(heap,(i-1)/2,i,index);
        i=(i-1)/2;
    }
}
int main() {
    int n,m,i,u,v,w;
    cin>>n>>m;
    vector<vector<pii> > adj(n);
    for(i=0;i<m;i++){
        cin>>u>>v>>w;
        u--;v--;
        adj[u].push_back(make_pair(v,w));
        adj[v].push_back(make_pair(u,w));
    }
}

```

```

    }
    vector<int> visited(n,false);
    heapnode heap[n];
    for(i=0;i<n;i++){
        heap[i].v=i;
        heap[i].w=INT_MAX;
    }
    hsize=n;
    heap[0].w=0;
    int index[n];
    for(i=0;i<n;i++){
        index[i]=i;
        int ans=0;
        for(int j=0;j<n;j++){
            u=heap[0].v;
            visited[u]=true;
            ans=ans+heap[0].w;
            deletemin(heap,index);
            for(i=0;i<adj[u].size();i++){
                if(!visited[adj[u][i].first]&&heap[index[adj[u][i].first]].
                w>adj[u][i].second){

                    decreasekey(heap,index[adj[u][i].first],adj[u][i].sec
                    ond,index);
                }
            }
        }
        cout<<ans<<"\n";
        return 0;
    }
}

Dijkstra's shortest path algorithm: //Single
source shortest path algorithm
Works for only positive edge weights same as
prims except
if(!visited[adj[u][i].first]&&heap[index[adj[u][i].first]].
w>adj[u][i].second+dist[u]){

    decreasekey(heap,index[adj[u][i].first],adj[u][i].sec
    ond+dist[u],index);
}

dist array contains shortest path from source for
every other vertex.

```

Bellman ford algorithm: //Single source shortest path algorithm
Works for negative edge weights and returns false if the graph contains negative weight cycles

INITIALIZE SINGLE SOURCE (G,S)

```
for i=1 to |G.V|-1
    for each edge (u,v)
        if(v.d>u.d+w(u,v))
            v.d=u.d+w(u,v)
for each edge (u,v)
    if(v.d>u.d+w(u,v))
        return FALSE;
return TRUE;
```

FLOYD WARSHALL ALGORITHM: //all pairs shortest path problem

```
int dist[n][n];
//initilize dist array with initial weights
for(k=0;k<n;k++){
    for(i=0;i<n;i++){
        for(j=0;j<n;j++){
            if(dist[i][k]+dist[k][j]<dist[i][j])
                dist[i][j]=dist[i][k]+dist[k][j];
        }
    }
}
```

Priority Queue: //min pq

```
struct node{
    int e;
    int p;
};
class compare{
public:
    bool operator() (node a,node b){
        return a.p>b.p;
    }
};
int main() {
    priority_queue<node, vector<node>, compare>
pq;
    int n;
    cin>>n;
    node x;
```

```
for(int i=0;i<n;i++){
    cin>>x.e>>x.p;
    pq.push(x);
}
while(!pq.empty()){
    x=pq.top();pq.pop();
    cout<<x.e<<" "<<x.p<<"\n";
}
return 0;
}
```

PQ Operations:

empty,size,push,pop,top

Queue:

empty,size,push,pop,front,back

Stack:

empty,size,push,pop,top

Vector:

empty,size,push_back,pop_back,begin,end,rbegin,rend,insert,erase,clear,at,front,back

Set:

```
typedef set<int> si;
typedef vector<int> vi;
#define tr(container,it) \
    for \
        (typeof(container.begin())it=container.begin();it!=c \
        ontainer.end();it++)
int main() {
    si s;
    vi v=vi(2,3);
    s.insert(1);
    s.insert(v.begin(),v.end());
    s.insert(9);
    s.insert(6);
    s.insert(8);
    s.erase(2);
    si::iterator it=s.find(8);
    s.erase(it,s.end());
    s.insert(11);
    s.insert(8);
    it=s.lower_bound(8);
    cout<<*it<<"\n";
    it=s.upper_bound(8);
    cout<<*it<<"\n";
```

```

tr(s,it)
cout<<*it<<" ";
cout<<"\n";
return 0;
}

```

Multiset:

```

typedef multiset<int> msi;
int main() {
    msi s;
    vi v=vi(2,3);
    s.insert(1);
    s.insert(v.begin(),v.end());
    v=vi(3,4);
    s.insert(v.begin(),v.end());
    s.insert(9);
    s.insert(6);
    s.insert(8);
    //s.erase(3); multiple elements are erased
    msi::iterator it;
    /*it=s.find(4);//returns an iterator to 1st four
    s.erase(it,s.end()); */
    cout<<s.count(3)<<" "<<s.count(4)<<"\n";
    pair<msi::iterator,msi::iterator> pmsit;
    pmsit=s.equal_range(4);
    s.erase(pmsit.first,pmsit.second);
    tr(s,it)
    cout<<*it<<" ";
    cout<<"\n";
    return 0;
}

```

Map:

```

typedef multimap<int,int> mmii;
typedef map<int,int> mii;
typedef pair<int,int> pii;
int main() {
    mii m;
    m[1]=7;
    m.insert(pii(1,4));
    m.insert(pii(5,7));
    m.insert(make_pair(3,7));
    m.insert(mii::value_type(2,8));
    tr(m,it){
        cout<<(*it).first<<" "<<(*it).second<<"\n";
    }
    //cout<<m.max_size()<<"\n";
    //m.size()

```

```

//m.empty()
mii::iterator it;
it=m.find(7);
if(it!=m.end())
    cout<<(*it).first<<" "<<(*it).second<<"\n";
else
    cout<<"Not found\n";
//m1.swap(m2) where m1 and m2 are maps
of same type
mii m1=m;
cout<<m1.size()<<"\n";
m1.clear();
cout<<m1.size()<<"\n";
m.erase(4);
cout<<m.size()<<"\n";
tr(m,it){
    cout<<(*it).first<<" "<<(*it).second<<"\n";
}
//erase(iterator) erase(iterator first,iterator
last)
return 0;
}

```

Multimap:

```

int main() {
    mmii m;
    m.insert(pii(1,5));
    m.insert(mp(3,7));
    m.insert(mmii::value_type(2,8));
    m.insert(pii(1,2));
    m.insert(pii(3,5));
    m.insert(pii(1,11));
    cout<<m.count(1)<<" "<<m.count(2)<<"
"<<m.count(3)<<"\n";
    pair<mmii::iterator,mmii::iterator> pitit;
    pitit=m.equal_range(3);
    for(mmii::iterator
it=pitit.first;it!=pitit.second;it++)
        cout<<(*it).first<<" "<<(*it).second<<"\n";
    tr(m,it)
    cout<<(*it).first<<" "<<(*it).second<<"\n";
    return 0;
}
////////----priyatam

```

```

//// union find ..written
ll getpar(ll *par,ll u){
    if(par[u]==-1)
        return u;
    else return par[u]=getpar(par,par[u]);
}
void make_union(ll u,ll v,ll *par){
    ll x=getpar(par,u);
    ll y=getpar(par,v);
    par[x]=y;
    return;
}

```

//////////

///fenwick algo gym

///1 indexing

int fen[MAX_N];

//update is adding excess val

```

void update(int p,int val){
    for(int i = p;i <= n;i += i & -i)
        fen[i] += val;
}

```

```

int sum(int p){
    int ans = 0;
    for(int i = p;i != i & -i)
        ans += fen[i];
    return ans;
}

```

//////////dont forget to refer geeks aswell

//////////seg tree

//////////1 indexing;pishty tree;

```

void dfs(long long int x,struct node *tr[],long long cc){
    struct node *temp;
    temp=tr[x];
    ind++;
    fst[x]=ind;
    walk[ind]=x;
    mgc[ind]=cc;
    while(temp!=NULL){
        if(temp->ver!=par[x]){

```

```

        par[temp->ver]=x;
        dfs(temp->ver,tr,temp->mn);

```

```

        }
        temp=temp->next;
    }
}

```

```

ind++;
snd[x]=ind;
walk[ind]=x;
mgc[ind]=cc;
}

```

//////////-----dfs pishty specefic

long long bound[1000005][2],seg[1000005];

```

void buildnew(long long id,long long l,long long r){
    bound[id][0]=l;
    bound[id][1]=r;
    seg[id]=0;
    if(l==r)//////////seg[id]=arr[l];
    return;
    long long mid=(l+r)/2;
    buildnew(2*id,l,mid);
    buildnew(2*id+1,mid+1,r);
    //////////seg[id]=seg[2*id]+seg[2*id+1];or rmq
    respectively;
}

```

```

void update(long long id,long long val,long long tmpin){

```

```

    ///seg[id]+=(val-arr[tmpin]);
    if(bound[id][0]>tmpin||bound[id][1]<tmpin)
        return;
    seg[id]=seg[id]^val;

```

```

    if(bound[id][0]==bound[id][1])
        return;
    update(2*id,val,tmpin);
    update(2*id+1,val,tmpin);

```

```

    }

```

```

long long ans;
long long x,y,l,r,k;
//////////problem specefic;

```

```

long long calculate(long long id,long long l,long
long r){
    if(bound[id][0]>r||bound[id][1]<l)
        return 0;
    if(bound[id][0]>=l&&bound[id][1]<=r){

        return seg[id];
    }

    if(bound[id][0]==bound[id][1])
        return 0;
    return calculate(2*id,l,r)^calculate(2*id+1,l,r);
}

```

//////////

//////////-----algo gym

```

void build(int id = 1,int l = 1,int r = n){
    if(r == l){        //        l + 1 == r
        s[id] = a[l];
        return ;
    }
    int mid = (l+r)/2;
    build(id * 2, l, mid);
    build(id * 2 + 1, mid+1, r);
    s[id] = s[id * 2] + s[id * 2 + 1];
}

```

//So, before reading the queries, we should call build() .

//Modify function :

```

void modify(int p,int x,int id = 1,int l = 1,int r = n){
    s[id] += x - a[p];
    if(r == l){        //        l = r - 1 = p
        a[p] = x;
        return ;
    }
    int mid = (l + r)/2;
    if(p < mid)
        modify(p, x, id * 2, l, mid);

```

```

        else
            modify(p, x, id * 2 + 1, mid+1, r);
    }

```

//(We should call modify(p, x))

//Ask for sum function :

//////////l,r correspond to id

```

int sum(int x,int y,int id = 1,int l = 0,int r = n){
    if(x >= r or l >= y)    return 0;
    if(x <= l && r <= y)    return s[id];
    int mid = (l+r)/2;
    return sum(x, y, id * 2, l, mid) +
        sum(x, y, id * 2 + 1, mid+1, r);
}

```

//////////

///-----**lazypropagation**

```

void upd(int id,int l,int r,int x){//    increase all
members in this interval by x
    lazy[id] += x;
    s[id] += (r - l) * x;
}

```

```

void shift(int id,int l,int r){//pass update information
to the children
    int mid = (l+r)/2;
    upd(id * 2, l, mid, lazy[id]);
    upd(id * 2 + 1, mid+1, r, lazy[id]);
    lazy[id] = 0;// passing is done
}

```

```

void increase(int x,int y,int v,int id = 1,int l = 0,int r
= n){
    if(x > r or l > y)    return ;
    if(x <= l && r <= y){
        upd(id, l, r, v);
        return ;
    }
    shift(id, l, r);
    int mid = (l+r)/2;
    increase(x, y, v, id * 2, l, mid);

```



```

        increase(x, y, v, id*2+1, mid+1, r);
        s[id] = s[id * 2] + s[id * 2 + 1];
    }

    int sum(int x,int y,int id = 1,int l = 0,int r = n){
        if(x >= r or l >= y)    return 0;
        if(x <= l && r <= y)    return s[id];
        shift(id, l, r);
        int mid = (l+r)/2;
        return sum(x, y, id * 2, l, mid) +
               sum(x, y, id * 2 + 1, mid+1, r);
    }

```

//////////

//////////-----dfs

```

    ll visited[1000000];
    void dfs(ll hd){
        ll sz=grph[hd].size();
        ll i;
        visited[hd]=1;

        mn=min(mn,cost[hd]);
        //cout<<mn;

        for(i=0;i<sz;i++){
            if(!visited[grph[hd][i]]){
                dfs(grph[hd][i]);
            }
        }
    }

```

//////////

//////////

//////////-----trie

////as used for sub string xor..nov

```

void make_trie(ll hgt,struct node *hd){
    if(hgt==0){
        return;
    }
    //cout<<hgt<<" ";

```

```

    struct node *tmp;
    tmp=new(node);
    tmp->val=tmp->cnt=0;
    hd->rgt=tmp;
    tmp=new(node);
    tmp->val=tmp->cnt=0;
    hd->lft=tmp;

    make_trie(hgt-1,hd->lft);
    make_trie(hgt-1,hd->rgt);
}

```

```

void insertintotr(ll vl,struct node *hd){
    ll ht=20;//////////

```

```

    while(ht!=0){
        (hd->cnt)++;
        if(vl&(1<<(ht-1))){
            hd=hd->lft;
        }else{
            hd=hd->rgt;
        }
        ht--;
    }

```

```

    hd->val=vl;
    (hd->cnt)++;
}
//////////--end 1 tr

```

//////////-----sparse table for rmq..order nlogn.

```

void process2(int M[MAXN][LOGMAXN], int
A[MAXN], int N)
{
    int i, j;

    //initialize M for the intervals with length 1
    for (i = 0; i < N; i++)
        M[i][0] = i;
    //compute values from smaller to bigger intervals

```

```

for (j = 1; 1 << j <= N; j++)
    for (i = 0; i + (1 << j) - 1 < N; i++)
        if (A[M[i][j - 1]] < A[M[i + (1 << (j - 1))][j - 1]])
            M[i][j] = M[i][j - 1];
        else
            M[i][j] = M[i + (1 << (j - 1))][j - 1];
}

```

//////////

//////////-----**combinatorics**

```

ll pw(ll a, ll b, ll MOD)
{
    if(b==0)
        return 1;
    ll temp = pw(a,b/2,MOD);
    temp = (temp*temp)%MOD;
    if(b%2 == 0)
        return temp;
    else
        return (temp*a)%MOD;
}

ll inv_mod(ll a, ll MOD)
{
    return pw(a,MOD-2,MOD);
}

ll NCR(ll n, ll r, ll MOD)
{
    ll ans = fact[n];
    ans = (ans*inv_mod(fact[r],MOD))%MOD;
    ans = (ans*inv_mod(fact[n-r],MOD))%MOD;
    return ans;
}

```

```

long long Lucas(long long n, long long m, long long p)
{
    if (n==0 && m==0) return 1;

    int ni = n % p;
    int mi = m % p;
    if (mi>ni) return 0;
    if (m==0) return 1;
    return (Lucas(n/p, m/p, p)*NCR(ni, mi, p))%p;
}

```

//////////

////////-----**seive of erosth.**

```

int isprime[10000000], lo[10000000];
long int lim=1000000;
void primegen();

```

```

void primegen()

```

```

{

```

```

    int i,j;
    for(i=0;i<10000000;++i)
    {
        isprime[i]=1;
        lo[i]=i;
    }
    for(i=2;i<=lim;++i)
    {
        if(isprime[i])
        {
            for(j=i;j<lim;j+=i)

```

```

                if(isprime[j])
                {
                    isprime[j]=0;
                }
            }
        }
    }
}

```

```

}

#define ll long long
ll query[1000000];

```

```

void getqryfill(ll *pr, ll *cnt, ll index, ll fact){
    if(index<0){
        query[fact]++;
        return;
    }
    ll times=cnt[index];
    ll fct=1;
    while(times>=0){
        getqryfill(pr, cnt, index-1, fct*fact);
        fct=fct*pr[index];
        times--;
    }
}

```

```

}

void getcal(ll num){
    ll prime[20],count[20],ind=0;
    ll least=lo[num];
    ll prev=prime[0]=least;
    count[0]=0;
    while(least>1){
        if(least==prev){
            count[ind]++;
        }
        else
            ind++,prime[ind]=least,count[ind]=1,prev=least;
        num=num/least;
        least=lo[num];
    }
}

```

```

    getqryfill(prime,count,ind,1);
}

```

////////////////-----end combi.

////////-----algo for lca sq. root decomposition

////////nr is sq. root of height of tree which is to be pre calculated.

////////T[i] is the father of node i in the tree, nr is [sqrt(H)] and L[i] is the level of the node i

```

void dfs(int node, int T[MAXN], int N, int P[MAXN],
int L[MAXN], int nr) {
    int k;
    if (L[node] < nr)
        P[node] = 1;
    else
        if(!(L[node] % nr))
            P[node] = T[node];
        else
            P[node] = P[T[node]];

    for each son k of node
        dfs(k, T, N, P, L, nr);
}

```

```

int LCA(int T[MAXN], int P[MAXN], int L[MAXN],

```

```

int x, int y)
{
    while (P[x] != P[y])
        if (L[x] > L[y])
            x = P[x];
        else
            y = P[y];
}

```

//now they are in the same section, so we trivially compute the LCA

```

while (x != y)
    if (L[x] > L[y])
        x = T[x];
    else
        y = T[y];
return x;
}

```

////////////////

////////-----Another easy solution in $O(N \log N)$, $O(\log N)$

//process_3 using dp in logn

```

void process3(int N, int T[MAXN], int
P[MAXN][LOGMAXN])
{
    int i, j;
}

```

//we initialize every element in P with -1
for (i = 0; i < N; i++)
 for (j = 0; 1 <= j < LOGMAXN; j++)
 P[i][j] = -1;

//the first ancestor of every node i is T[i]
for (i = 0; i < N; i++)
 P[i][0] = T[i];

//bottom up dynamic programming
for (j = 1; j < LOGMAXN; j++)
 for (i = 0; i < N; i++)
 if (P[i][j-1] != -1)
 P[i][j] = P[P[i][j-1]][j-1];
}

////query for logn lca

```

int query(int N, int P[MAXN][LOGMAXN], int
T[MAXN],
int L[MAXN], int p, int q)
{
    int tmp, log, i;

    //if p is situated on a higher level than q then we
    swap them
    if (L[p] < L[q])
        tmp = p, p = q, q = tmp;

    //we compute the value of [log(L[p])
    for (log = 1; 1 << log <= L[p]; log++);
    log--;

    //we find the ancestor of node p situated on the
    same level
    //with q using the values in P
    for (i = log; i >= 0; i--)
        if (L[p] - (1 << i) >= L[q])
            p = P[p][i];

    if (p == q)////////---if p and q are equal it may
    return parent of p(or q) so to overcome that..
        return p;

    //we compute LCA(p, q) using the values in P
    for (i = log; i >= 0; i--)
        if (P[p][i] != -1 && P[p][i] != P[q][i])
            p = P[p][i], q = P[q][i];

    return T[p];
}

```

//////-----in the above algo it is nothing but in last
for loop it executes untill p and q reach to just child
that is if lca is at dist x..it will reach upto x-1;try to
understand that.

//////////

//////////

//////////-----**HEAVY LIGHT DECOMPOSITION**

```

#include <stdio>
#include <vector>
using namespace std;

```

```

#define root 0
#define N 10100
#define LN 14

vector <int> adj[N], costs[N], indexx[N];
int baseArray[N], ptr;
int chainNo, chainInd[N], chainHead[N],
posInBase[N];
int depth[N], pa[LN][N], otherEnd[N], subsize[N];
int st[N*6], qt[N*6];

/*
* make_tree:
* Used to construct the segment tree. It uses the
baseArray for construction
*/
void make_tree(int cur, int s, int e) {
    if(s == e-1) {
        st[cur] = baseArray[s];
        return;
    }
    int c1 = (cur<<1), c2 = c1 | 1, m = (s+e)>>1;
    make_tree(c1, s, m);
    make_tree(c2, m, e);
    st[cur] = st[c1] > st[c2] ? st[c1] : st[c2];
}

/*
* update_tree:
* Point update. Update a single element of the
segment tree.
*/
void update_tree(int cur, int s, int e, int x, int val) {
    if(s > x || e <= x) return;
    if(s == x && s == e-1) {
        st[cur] = val;
        return;
    }
    int c1 = (cur<<1), c2 = c1 | 1, m = (s+e)>>1;
    update_tree(c1, s, m, x, val);
    update_tree(c2, m, e, x, val);
    st[cur] = st[c1] > st[c2] ? st[c1] : st[c2];
}

/*
* query_tree:
* Given S and E, it will return the maximum value

```

```

in the range [S,E)
*/
void query_tree(int cur, int s, int e, int S, int E) {
    if(s >= E || e <= S) {
        qt[cur] = -1;
        return;
    }
    if(s >= S && e <= E) {
        qt[cur] = st[cur];
        return;
    }
    int c1 = (cur<<1), c2 = c1 | 1, m = (s+e)>>1;
    query_tree(c1, s, m, S, E);
    query_tree(c2, m, e, S, E);
    qt[cur] = qt[c1] > qt[c2] ? qt[c1] : qt[c2];
}

```

```

/*
* query_up:
* It takes two nodes u and v, condition is that v is
an ancestor of u
* We query the chain in which u is present till
chain head, then move to next chain up
* We do that way till u and v are in the same
chain, we query for that part of chain and break
*/

```

```

int query_up(int u, int v) {
    if(u == v) return 0; // Trivial
    int uchain, vchain = chainInd[v], ans = -1;
    // uchain and vchain are chain numbers of u
and v
    while(1) {
        uchain = chainInd[u];
        if(uchain == vchain) {
            // Both u and v are in the
same chain, so we need to query from u to v,
update answer and break.
            // We break because we
came from u up till v, we are done
            if(u==v) break;
            query_tree(1, 0, ptr,
posInBase[v]+1, posInBase[u]+1);
            // Above is call to segment
tree query function
            if(qt[1] > ans) ans = qt[1]; //
Update answer
            break;

```

```

        }
        query_tree(1, 0, ptr,
posInBase[chainHead[uchain]], posInBase[u]+1);
        // Above is call to segment tree
query function. We do from chainHead of u till u.
That is the whole chain from
        // start till head. We then update the
answer
        if(qt[1] > ans) ans = qt[1];
        u = chainHead[uchain]; // move u to
u's chainHead
        u = pa[0][u]; //Then move to its
parent, that means we changed chains
    }
    return ans;
}

```

```

/*
* LCA:
* Takes two nodes u, v and returns Lowest
Common Ancestor of u, v
*/
int LCA(int u, int v) {
    if(depth[u] < depth[v]) swap(u,v);
    int diff = depth[u] - depth[v];
    for(int i=0; i<LN; i++) if( (diff>>i)&1 ) u =
pa[i][u];
    if(u == v) return u;
    for(int i=LN-1; i>=0; i--) if(pa[i][u] != pa[i][v])
    {
        u = pa[i][u];
        v = pa[i][v];
    }
    return pa[0][u];
}

```

```

void query(int u, int v) {
    /*
    * We have a query from u to v, we break it
into two queries, u to LCA(u,v) and LCA(u,v) to v
    */
    int lca = LCA(u, v);
    int ans = query_up(u, lca); // One part of
path
    int temp = query_up(v, lca); // another part
of path
    if(temp > ans) ans = temp; // take the
maximum of both paths

```

```

        printf("%d\n", ans);
    }

/*
 * change:
 * We just need to find its position in segment tree
and update it
 */
void change(int i, int val) {
    int u = otherEnd[i];
    update_tree(1, 0, ptr, posInBase[u], val);
}

/*
 * Actual HL-Decomposition part
 * Initially all entries of chainHead[] are set to -1.
 * So when ever a new chain is started, chain
head is correctly assigned.
 * As we add a new node to chain, we will note its
position in the baseArray.
 * In the first for loop we find the child node which
has maximum sub-tree size.
 * The following if condition is failed for leaf nodes.
 * When the if condition passes, we expand the
chain to special child.
 * In the second for loop we recursively call the
function on all normal nodes.
 * chainNo++ ensures that we are creating a new
chain for each normal child.
 */
/////HLD
void HLD(int curNode, int cost, int prev) {
    if(chainHead[chainNo] == -1) {
        chainHead[chainNo] = curNode; //
Assign chain head
    }
    chainInd[curNode] = chainNo;
    posInBase[curNode] = ptr; // Position of this
node in baseArray which we will use in Segtree
    baseArray[ptr++] = cost;

    int sc = -1, ncost;
    // Loop to find special child
    for(int i=0; i<adj[curNode].size(); i++)
if(adj[curNode][i] != prev) {
        if(sc == -1 || subsz[sc] <
subsz[adj[curNode][i]]) {
            sc = adj[curNode][i];

```

```

        ncost = costs[curNode][i];
    }
}

if(sc != -1) {
    // Expand the chain
    HLD(sc, ncost, curNode);
}

for(int i=0; i<adj[curNode].size(); i++)
if(adj[curNode][i] != prev) {
    if(sc != adj[curNode][i]) {
        // New chains at each normal
node
        chainNo++;
        HLD(adj[curNode][i],
costs[curNode][i], curNode);
    }
}

/*
 * dfs used to set parent of a node, depth of a
node, subtree size of a node
 */
void dfs(int cur, int prev, int _depth=0) {
    pa[0][cur] = prev;
    depth[cur] = _depth;
    subsz[cur] = 1;
    for(int i=0; i<adj[cur].size(); i++)
        if(adj[cur][i] != prev) {
            otherEnd[indexx[cur][i]] =
adj[cur][i];
            dfs(adj[cur][i], cur, _depth+1);
            subsz[adj[cur][i]] +=
subsz[cur];
        }
}

int main() {
    int t;
    scanf("%d ", &t);
    while(t--) {
        ptr = 0;
        int n;
        scanf("%d", &n);
        // Cleaning step, new test case

```

```

for(int i=0; i<n; i++) {
    adj[i].clear();
    costs[i].clear();
    indexx[i].clear();
    chainHead[i] = -1;
    for(int j=0; j<LN; j++) pa[j][i] =
-1;
}
for(int i=1; i<n; i++) {
    int u, v, c;
    scanf("%d %d %d", &u, &v,
&c);
    u--; v--;
    adj[u].push_back(v);
    costs[u].push_back(c);
    indexx[u].push_back(i-1);
    adj[v].push_back(u);
    costs[v].push_back(c);
    indexx[v].push_back(i-1);
}

chainNo = 0;
dfs(root, -1); // We set up subsize,
depth and parent for each node
HLD(root, -1, -1); // We decomposed
the tree and created baseArray
make_tree(1, 0, ptr); // We use
baseArray and construct the needed segment tree

// Below Dynamic programming code
is for LCA.
for(int i=1; i<LN; i++)
    for(int j=0; j<n; j++)
        if(pa[i-1][j] != -1)
            pa[i][j] =
pa[i-1][pa[i-1][j]];

while(1) {
    char s[100];
    scanf("%s", s);
    if(s[0]=='D') {
        break;
    }
    int a, b;
    scanf("%d %d", &a, &b);
    if(s[0]=='Q') {
        query(a-1, b-1);
    } else {
change(a-1, b);
}
}
}
}
}
}

//////////END HEAVY LIGHT DEC.

//////////-----sos dp brute force

for(int mask = 0; mask < (1<<N); ++mask){
    for(int i = 0; i < (1<<N); ++i){
        if((mask&i) == i){
            F[mask] += A[i];
        }
    }
}

//order=(4^n);

//-----Suboptimal Solution

// iterate over all the masks
for (int mask = 0; mask < (1<<n); mask++){
    F[mask] = A[0];
    // iterate over all the subsets of the mask
    for(int i = mask; i > 0; i = (i-1) & mask){
        F[mask] += A[i];
    }
}

//order--3^n;

///-----sos dp solution
//iterative version
for(int mask = 0; mask < (1<<N); ++mask){
    dp[mask][-1] = A[mask];    //handle base
case separately (leaf states)
    for(int i = 0; i < N; ++i){
        if(mask & (1<<i))
            dp[mask][i] = dp[mask][i-1] +
dp[mask^(1<<i)][i-1];
        else
            dp[mask][i] = dp[mask][i-1];
    }
    F[mask] = dp[mask][N-1];
}

```

```

}

//memory optimized, super easy to code.
for(int i = 0; i < (1<<N); ++i)
    F[i] = A[i];
for(int i = 0; i < N; ++i) for(int mask = 0; mask <
(1<<N); ++mask){
    if(mask & (1<<i))
        F[mask] += F[mask^(1<<i)];
}
//-----order n*(2^n);

```

/////prbv old doc

GRAPHS

*No Eulerian Path <=> No of Odd Degree Vertices

>=2

*Eulerian Circuit No odd degree vertex

*Maximal Independent Set = Total_Nodes - Minimal_Vertex_Cover

*Directed Graph is Eulerian(having E.Cycle) iff in_degree=out_degree(of all vertices) and all vertices with non 0 degree belong to a single SCC

*Maximum Bipartite Matching = Minimal Vertex Cover (Konigs Theorem)

MAXIMAL BIPARTITE MATCHING

```
#define MAXN 100010 //Maximum Nodes
```

```
#define MAXM 150000 //Maximum Edges
```

```
int n1, n2, edges, last[MAXN];
```

```
int previous[MAXM], head[MAXM];
```

```
int matching[MAXN], dist[MAXN], Q[MAXN];
```

```
bool used[MAXN], vis[MAXN];
```

```
void init(int a, int b) {
```

```
    n1 = a;
```

```
    n2 = b;
```

```
    edges = 0;
```

```
    fill(last, last + n1, -1);
```

```
}
```

//u->Node of left side, v->Right Side

```
void addEdge(int u, int v) {
```

```
    head[edges] = v;
```

```
    previous[edges] = last[u];
```

```
    last[u] = edges++;
```

```
}
```

```
void bfs() {
```

```
    fill(dist, dist + n1, -1);
```

```
    int sizeQ = 0;
```

```
    for (int u = 0; u < n1; ++u) {
```

```
        if (!used[u]) {
```

```
            Q[sizeQ++] = u;
```

```
            dist[u] = 0;
```

```
        }
```

```
    }
```

```
    for (int i = 0; i < sizeQ; i++) {
```

```
        int u1 = Q[i];
```

```
        for (int e = last[u1]; e >= 0; e =
```

```
            previous[e]) {
```

```
            int u2 = matching[head[e]];
```

```
            if (u2 >= 0 && dist[u2] < 0) {
```

```
                dist[u2] = dist[u1] + 1;
```

```
                Q[sizeQ++] = u2;
```

```
            }
```

```
        }
```

```
    }
```

```
    }
```

```
bool dfs(int u1) {
```

```
    vis[u1] = true;
```

```
    for (int e = last[u1]; e >= 0; e = previous[e]) {
```

```
        int v = head[e];
```

```
        int u2 = matching[v];
```

```
        if (u2 < 0 || !vis[u2] && dist[u2] ==
```

```
            dist[u1] + 1 && dfs(u2)) {
```

```
            matching[v] = u1;
```

```
            used[u1] = true;
```

```
            return true;
```

```
        }
```

```
    }
```

```
    return false;
```

```
}
```

```
int maxMatching() {
```

```
    fill(used, used + n1, false);
```

```
    fill(matching, matching + n2, -1);
```

```
    for (int res = 0;;) {
```

```
        bfs();
```

```
        fill(vis, vis + n1, false);
```

```
        int f = 0;
```

```
        for (int u = 0; u < n1; ++u)
```

```
            if (!used[u] && dfs(u))
```

```
                ++f;
```

```
        if (!f)
```

```
            return res;
```

```
        res += f;
```

```
    }
```

//FIRST init() then addEdges then, maxMatching

BRIDGES

```
void getBridges(int u){
low[u]=dt[u]=tim++;
visited[u]=1;
for(auto i=G[u].begin();i!=G[u].end();i++){
    int v=*i;
    if(!visited[v]){
        P[v]=u;
        getBridges(v);
        low[u]=min(low[v],low[u]);
        if(low[v]>dt[u]){
            if(u!=v)
                B.pb(pii(min(u,v),max(u,v))); //BRIDGE
        }
    }
    else{
        if(v!=P[u])
            low[u]=min(low[u],dt[v]);
    }
}
}
```

Articulation Point:

(1) u is root of DFS tree and has two or more children. (2) If u is not root and low value of one of its child is more than discovery value of u. if(parent[u] != NIL && low[v] >= dt[u]) ap[u] = true;

DINIC'S MAXFLOW

```
const long long maxnodes = 5005;
long long capacity[maxnodes][maxnodes];
long long nodes = maxnodes, src, dest;
long long dist[maxnodes], q[maxnodes],
work[maxnodes];
struct Edge {
    long long to, rev;
    long long f, cap;
};

vector<Edge> g[maxnodes];
// Adds bidirectional edge
// if unidirectional is needed, make cap=0 in Edge b
void addEdge(long long s, long long t, long long cap){
    Edge a = {t, g[t].size(), 0, cap};
    Edge b = {s, g[s].size(), 0, cap};
    g[s].push_back(a);
    g[t].push_back(b);
}
```

```

}
bool dinic_bfs() {
    fill(dist, dist + nodes, -1);
    dist[src] = 0;
    long long qt = 0;
    q[qt++] = src;
    for (long long qh = 0; qh < qt; qh++) {
        long long u = q[qh];
        for (long long j = 0; j < (long long) g[u].size(); j++) {
            Edge &e = g[u][j];
            long long v = e.to;
            if (dist[v] < 0 && e.f < e.cap) {
                dist[v] = dist[u] + 1;
                q[qt++] = v;
            }
        }
    }
    return dist[dest] >= 0;
}

long long dinic_dfs(long long u, long long f) {
    if (u == dest)
        return f;
    for (long long &i = work[u]; i < (long long) g[u].size(); i++) {
        Edge &e = g[u][i];
        if (e.cap <= e.f) continue;
        long long v = e.to;
        if (dist[v] == dist[u] + 1) {
            long long df = dinic_dfs(v, min(f, e.cap - e.f));
            if (df > 0) {
                e.f += df;
                g[v][e.rev].f -= df;
                return df;
            }
        }
    }
    return 0;
}

long long maxFlow(long long _src, long long _dest) {
    src = _src;
    dest = _dest;
    long long result = 0;
    while (dinic_bfs()) {
        fill(work, work + nodes, 0);
        while (long long delta = dinic_dfs(src,
```

```

INT_MAX))
result += delta;
}
return result;
}
int main()
{
cin>>nodes;
while(nodes!=0)
{
long long s,t,m;
//cin>>s>>t>>m;
cin>>m;
s=0;t=nodes-1;
//s-- ;t-- ;//if nodes are from 0 to n-1
for(long long i=0;i<nodes;i++)
for(long long j=0;j<nodes;j++)
capacity[i][j]=0;

while(m-- )
{
long long u,v,c;
cin>>u>>v>>c;
u-- ;v-- ; //if nodes are from 0 to n-1
capacity[u][v]+=c;
}
for(long long i=0;i<nodes;i++) g[i].clear();
for (long long i = 0; i < nodes; i++)
for (long long j = 0; j < nodes; j++)
if (capacity[i][j] != 0)
addEdge(i, j, capacity[i][j]);
cout<<endl; maxFlow(s, t) <<endl; endl;
//cin>>nodes;
nodes=0;

}
}

```

8	7 3 6
1 8	3 6 8
15	5 6 5
1 2	6 7
10	15
1 3 5	5 8
1 4	10
15	6 8
2 5 9	10
2 6	7 8
15	10

2 3 4	
3 4 4	
4 7	
16	

==>30 undirectional, 28 directional

STRONGLY CONNECTED COMPONENT

```

#define MAX 100001
#define pb push_back
using namespace std;
vector<int> V[MAX];
vector<int> InV[MAX];
int visited[MAX]={0};
stack<int> S;
void dfs(int u){
    visited[u]=1;
    for(unsigned i=0;i<V[u].size();i++){
        int v=V[u][i];
        if(!visited[v]){
            dfs(v);
        }
    }
    S.push(u);
}
int P[MAX];
int Rank[MAX]={0};
int find(int i){
    if(P[i]==i)
        return i;
    else{
        P[i]=find(P[i]);
        return P[i];
    }
}
void Union(int a,int b){
    int u=find(a),v=find(b);
    if(u!=v){
        if(Rank[u]<Rank[v]){
            P[u]=P[v];
        }
        else{
            P[v]=P[u];
            if(Rank[u]==Rank[v])
                Rank[u]++;
        }
    }
}

```

```

    }
    }
}
void dfs2(int u,int &m){
    visited[u]=0;
    m=min(m,u);
    for(unsigned i=0;i<lnV[u].size();i++){
        if(visited[lnV[u][i]]){
            Union(u,lnV[u][i]);
            dfs2(lnV[u][i],m);
            m=min(m,lnV[u][i]);
        }
    }
}
int main(){
    int n,m;
    cin>>n>>m;
    for(int i=0;i<m;i++){
        int a,b;
        cin>>a>>b;
        V[a].pb(b);
        lnV[b].pb(a);
    }
    for(int i=0;i<n;i++){
        P[i]=i;
        if(!visited[i])
            dfs(i);
    }
    int M[MAX]={0};
    while(!S.empty()){
        int v=S.top();
        S.pop();
        int m;
        if(visited[v]){
            m=v;
            dfs2(v,m);
            M[find(v)]=m;
        }
    }
    //Prints the minimum valued vertex in the
    SCC of
    i
    for(int i=0;i<n;i++)

    cout<<M[find(i)]<<endl;
}

```

DIJKSTRA's Shortest Path

```

typedef pair<int, int> pii;
typedef vector<vector<pii> > Graph;
//prio has the distance
void dijkstra(Graph &g, int s, vector<int> &prio,
vector<int> &pred) {
    int n = g.size();
    prio.assign(n, INT_MAX);
    prio[s] = 0;
    pred.assign(n, -1);
    priority_queue<pii, vector<pii>, greater<pii> >
q;
    q.push(make_pair(0, s));

    while (!q.empty()) {
        int d = q.top().first;
        int u = q.top().second;
        q.pop();
        if (d != prio[u])
            continue;
        for (int i = 0; i < (int) g[u].size(); i++) {
            int v = g[u][i].first;
            int nprio = prio[u] + g[u][i].second;
            if (prio[v] > nprio) {
                prio[v] = nprio;
                pred[v] = u;
                q.push(make_pair(nprio, v));
            }
        }
    }
}
//~ Graph g(n+1);
//~ addEdge(a,b,cost) =>
g[a].push_back(pii(b,cost))

```

EULER TOTIENT

```

int phi(int n) {
    int result = n;
    for(int i = 2; i * i <= n; ++i)
        if(n % i == 0) {
            while(n % i == 0)
                n /= i;
            result -= result / i;
        }
    if(n > 1)

```

```

        result -= result / n;
    return result;
}

long long factMOD(int n, int MOD)
{
    long long res = 1;
    while (n > 0)
    {
        for (int i=2, m=n%MOD; i<=m; i++)
            res = (res * i) % MOD;
        if ((n/=MOD)%2 > 0)
            res = MOD - res;
    }
    return res;
}

// ----- pollard rho brent factorization -----

```

```

def brent(N):
    if N%2==0:
        return 2
    y,c,m = random.randint(1, N-1),random.randint(1,
N-1),random.randint(1, N-1)
    g,r,q = 1,1,1
    while g==1:
        x = y
        for i in range(r):
            y = ((y*y)%N+c)%N
        k = 0
        while (k<r and g==1):
            ys = y
            for i in range(min(m,r-k)):
                y = ((y*y)%N+c)%N
                q = q*(abs(x-y))%N
            g = gcd(q,N)
            k = k + m
        r = r*2
    if g==N:
        while True:
            ys = ((ys*ys)%N+c)%N
            g = gcd(abs(x-ys),N)
            if g>1:
                break

```

```

    return g

// ----- miller rabin primality test -----
def modulo(a,b,c):
    x = 1
    y = a
    while b>0:
        if b%2==1:
            x = (x*y)%c
        y = (y*y)%c
        b = b/2
    return x%c

def millerRabin(N,iteration):
    if N<2:
        return False
    if N!=2 and N%2==0:
        return False

    d=N-1
    while d%2==0:
        d = d/2

    for i in range(iteration):
        a = random.randint(1, N-1)
        temp = d
        x = modulo(a,temp,N)
        while (temp!=N-1 and x!=1 and x!=N-1):
            x = (x*x)%N
            temp = temp*2

        if (x!=N-1 and temp%2==0):
            return False

    return True

// ----- Z algo for string matching in linear time
bool zAlgorithm(string pattern, string target)
{
    string s = pattern + '$' + target ;
    int n = s.length();
    vector<int> z(n,0);

```

```

int goal = pattern.length();
int r = 0, l = 0, i;
for (int k = 1; k < n; k++)
{
    if (k > r)
    {
        for (i = k; i < n && s[i] == s[i - k]; i++);
        if (i > k)
        {
            z[k] = i - k;
            l = k;
            r = i - 1;
        }
    }
    else
    {
        int kt = k - l, b = r - k + 1;
        if (z[kt] > b)
        {
            for (i = r + 1; i < n && s[i] == s[i - k]; i++);
            z[k] = i - k;
            l = k;
            r = i - 1;
        }
    }
    if (z[k] == goal)
        return true;
}
return false;
}

```

// Sieve of Eratosthenes with linear time work

```

const int N = 10000000;
int lp[N + 1];
vector<int> pr;

for (int i = 2; i <= N; ++i) {
    if (lp[i] == 0) {
        lp[i] = i;
        pr.push_back(i);
    }
    for (int j = 0; j < (int)pr.size() && pr[j] <= lp[i] &&
i * pr[j] <= N; ++j)

```

```

        lp[i * pr[j]] = pr[j];
    }
}

```

MATRICES

```

typedef vector<int> vi;
typedef vector<vi> vvi;
const int mod = 100000007;
vvi matrixUnit(int n) {
    vvi res(n, vi(n));
    for (int i = 0; i < n; i++)
        res[i][i] = 1;
    return res;
}

```

MATRIX MULTIPLICATION

```

vvi matrixMul(const vvi &a, const vvi &b) {
    int n = a.size();
    int m = a[0].size();
    int k = b[0].size();
    vvi res(n, vi(k));
    for (int i = 0; i < n; i++)
        for (int j = 0; j < k; j++)
            for (int p = 0; p < m; p++)
                res[i][j] = (res[i][j] + (long long) a[i][p] * b[p][j]) % mod;
    return res;
}

vvi matrixPow(const vvi &a, int p) {
    if (p == 0)
        return matrixUnit(a.size());
    if (p & 1)
        return matrixMul(a, matrixPow(a, p - 1));
    return matrixPow(matrixMul(a, a), p / 2);
}

```

KMP

* Terminologies Used

* T ==> Input string (the long one)

* P ==> Pattern to be matched

* P^k ==> $P[1...k]$

* $=]$ ==> Suffix ($A =]$ B means A is a suffix of B. eg: cd =] abcd)

* $pi[q] = \max\{k : k < q \text{ \&\& } P^k =] P^q\}$

*/

vector<char> T;

vector<char> P;

```

vector<long long> pi;
void compute_pi(long long m)
{
    //P[1.....m] is the Pattern to be matched
    //pi[1....m] will be the new array
    pi.clear();
    pi.push_back(0); //pi[0]=0;
    pi.push_back(0); //pi[1]=0;
    long long k=0;
    for(long long q=2;q<=m;q++)
    {
        while((k>0) && (P[k+1]!=P[q]))
            k=pi[k];
        if(P[k+1]==P[q]) k++;
        pi.push_back(k);
    }
}

void match(long long m) // Add a newline at the end
of T to determine termination
{
    //T[0....(n-1)] is the input string
    //P[1....m] is the pattern to be matched
    //Compute_pi() should be called for P
    int q=0;
    char x;
    int i=0;
    x=T[i];
    while(x!='\n')
    {
        i++;
        while((q>0) && (P[q+1]!=x))
            q=pi[q];
        if(P[q+1]==x) q++;
        if(q==m) {
            cout << "Match at " << i-m << endl; q=pi[q];
            x=T[i];
            //cout<<x;
        }
    }
}

int main()
{
    long long m;
    while(cin>>m)
    {

```

```

        P.clear();
        char x;
        scanf("%c",&x);
        P.push_back('a'); //Pushing junk
                                at P[0]
        for(long long i=0;i<m;i++)
        {
            scanf("%c",&x);
            //cout<<x;
            P.push_back(x);
        }
        scanf("%c",&x);
        scanf("%c",&x);
        T.clear();
        while(x!='\n')
        {
            T.push_back(x);
            scanf("%c",&x);
        }
        T.push_back(x);
        compute_pi(m);
        match(m);
    }
}

```

KRUSKAL's MST

```

#define pii pair<int,int>
vector<pii> E;
vector<pii> Edges;
vector<int> P;
vector<int> R;
int find(int i){
    if(P[i]==i)
        return i;
    else
        return (P[i]=find(P[i]));
}

int main(){
    cout.sync_with_stdio(0);
    cin.tie(0);
    int n,m;
    cin>>n>>m;
    for(int i=0;i<m;i++){
        int a,b,c;
        cin>>a>>b>>c;
    }
}

```

```

    E.push_back(pii(c,i));
    Edges.push_back(pii(a,b));
}
sort(E.begin(),E.end());
R.assign(n+1,0);
for(int i=0;i<=n;i++){
    P.push_back(i);
    int e=0;
    long long cost=0;
    for(int i=0;e<n-1;i++){
        int a=E[i].second;
        int u=Edges[a].first;
        int v=Edges[a].second;
        if(find(u)!=find(v)){
            e++;
            u=P[u],v=P[v];
            cost+=E[i].first;
            if(R[u]<R[v])
                P[u]=P[v];
            else{
                P[v]=P[u];
                if(R[v]==R[u])
                    R[u]++;
            }
        }
    }
}
cout<<cost<<'\n';
}

```

FLOYD WARSHALL

```

for(i=1;i<=n;i++)
    for(j=1;j<=n;j++)
        mat[i][j]=INT_MAX;
while(m--)
{
    int a,b,x;
    cin>>a>>b>>x;
    mat[a][b]=x;
}
for(i=1;i<=n;i++)
    mat[i][i]=0;

for(i=1;i<=n;i++)
    for(j=1;j<=n;j++)

```

```

        for(k=1;k<=n;k++)
            mat[i][j]=min(mat[i][j],mat[i][k]+mat[k][j]);

```

//mat[a][b] => distance between A & B

Longest Increasing Subsequence

```

int main()
{
    int n, num;
    vector<int> v;
    cin >> n;
    while (n--){
        cin >> num;
        if (v.size() == 0 || num > v.back())
            v.push_back(num);
        else *lower_bound(v.begin(), v.end(), num) =
num;
        //for(unsigned int i=0;i<v.size();i++)
        //cout<<v[i]<<' ';cout<<endl;
    }
    cout << v.size();
}

```

KD TREES

```

typedef pair<int, int> pii;
typedef vector<pii> vpii;

```

```

const int maxn = 100000;
int tx[maxn];
int ty[maxn];
bool divX[maxn];

```

```

bool cmpX(const pii &a, const pii &b) {
    return a.first < b.first;
}

```

```

bool cmpY(const pii &a, const pii &b) {
    return a.second < b.second;
}

```

```

void buildTree(int left, int right, pii
points[]) {
    if (left >= right)
        return;
    int mid = (left + right) >> 1;

```

```

//sort(points + left, points + right + 1,
divX ? cmpX : cmpY);
int minx = INT_MAX;
int maxx = INT_MIN;
int miny = INT_MAX;
int maxy = INT_MIN;
for (int i = left; i < right; i++) {
    checkmin(minx, points[i].first);
    checkmax(maxx, points[i].first);
    checkmin(miny, points[i].second);
    checkmax(maxy, points[i].second);
}
divX[mid] = (maxx - minx) >= (maxy -
miny);
nth_element(points + left, points +
mid, points + right, divX[mid] ? cmpX :
cmpY);

```

```

tx[mid] = points[mid].first;
ty[mid] = points[mid].second;

```

```

if (left + 1 == right)
    return;
buildTree(left, mid, points);
buildTree(mid + 1, right, points);
}

```

```

long long closestDist;
int closestNode;

```

```

void findNearestNeighbour(int left, int
right, int x, int y) {
    if (left >= right)
        return;
    int mid = (left + right) >> 1;
    int dx = x - tx[mid];
    int dy = y - ty[mid];
    long long d = dx * (long long) dx + dy
* (long long) dy;
    if (closestDist > d && d) {
        closestDist = d;
        closestNode = mid;
    }
}

```

```

}
if (left + 1 == right)
    return;

int delta = divX[mid] ? dx : dy;
long long delta2 = delta * (long long)
delta;
int l1 = left;
int r1 = mid;
int l2 = mid + 1;
int r2 = right;
if (delta > 0)
    swap(l1, l2), swap(r1, r2);

findNearestNeighbour(l1, r1, x, y);
if (delta2 < closestDist)
    findNearestNeighbour(l2, r2, x, y);
}

```

```

int findNearestNeighbour(int n, int x,
int y) {
    closestDist = LLONG_MAX;
    findNearestNeighbour(0, n, x, y);
    return closestNode;
}

```

```

int main() {
    vpil p;
    p.push_back(make_pair(0, 2));
    p.push_back(make_pair(0, 3));
    p.push_back(make_pair(-1, 0));

    p.resize(unique(p.begin(), p.end()) -
p.begin());

    int n = p.size();
    buildTree(1, 0, n - 1, &(vpil(p)[0]));
    int res = findNearestNeighbour(n, 0,
0);

    cout << p[res].first << " " <<
p[res].second << endl;
}

```



```

    return 0;
}

```

PRIMS

```

typedef pair<int, int> pii;
typedef vector<vector<pii> > Graph;

long long prim(Graph &g, vector<int> &
pred) {
    int n = g.size();
    pred.assign(n, -1);
    vector<bool> vis(n);
    vector<int> prio(n, INT_MAX);
    prio[0] = 0;
    priority_queue<pii, vector<pii>, great
er<pii> > q;
    q.push(make_pair(0, 0));
    long long res = 0;

    while (!q.empty()) {
        int d = q.top().first;
        int u = q.top().second;
        q.pop();
        if (vis[u])
            continue;
        vis[u] = true;
        res += d;
        for (int i = 0; i < (int) g[u].size(); i++)
        {
            int v = g[u][i].first;
            if (vis[v])
                continue;
            int nprio = g[u][i].second;
            if (prio[v] > nprio) {
                prio[v] = nprio;
                pred[v] = u;
                q.push(make_pair(nprio, v));
            }
        }
    }
    return res;
}

```

CONVEX HULL

```

typedef pair<double, double> point;
bool cw(const point &a, const point &b,
const point &c) {
    return (b.first - a.first) * (c.second - a.
second) - (b.second - a.second) * (c.first
- a.first) < 0;
}
vector<point> convexHull(vector<point
> p) {
    int n = p.size();
    if (n <= 1)
        return p;
    int k = 0;
    sort(p.begin(), p.end());
    vector<point> q(n * 2);
    for (int i = 0; i < n; q[k++] = p[i++])
        for (; k >= 2 && !cw(q[k - 2], q[k - 1]
, p[i]); --k)
            ;
    for (int i = n - 2, t = k; i >= 0; q[k++] = p
[i--])
        for (; k > t && !cw(q[k - 2], q[k - 1],
p[i]); --k)
            ;
    q.resize(k - 1 - (q[0] == q[1]));
    return q;
}

int main() {
    vector<point> points(4);
    points[0] = point(0, 0);
    points[1] = point(3, 0);
    points[2] = point(0, 3);
    points[3] = point(1, 1);
    vector<point> hull = convexHull(point
s);
    cout << (3 == hull.size()) << endl;
}

```