

Beta-reduction in the lambda-calculus is defined by substitution:

$$(\lambda v.E) x \longrightarrow_{\beta} E[x/v] \quad (1)$$

$$(\lambda vw.E) x \longrightarrow_{\beta} \lambda w.(E[x/v]) \quad (2)$$

where  $x$  may be any lambda term (variable, function or application). E.g.:

$$\begin{aligned} & (\lambda xy.(y (x x y))) (\lambda xy.(y (x x y))) \\ & \longrightarrow_{\beta} \lambda y.(y ((\lambda xy.(y (x x y))) (\lambda xy.(y (x x y))) y)) \quad (3) \end{aligned}$$