



Vidyavardhini's College of Engineering and Technology

Department of Artificial Intelligence & Data Science

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Class/Sem:	SE/IV
Experiment No.:	8
Title:	Single Source Shortest Path: Bellman Ford.
Date of Performance:	
Date of Submission:	
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Experiment No: 8

Title: Single Source Shortest Path: Bellman Ford.

Aim: To study and implement Single Source Shortest Path using Dynamic Programming: Bellman Ford

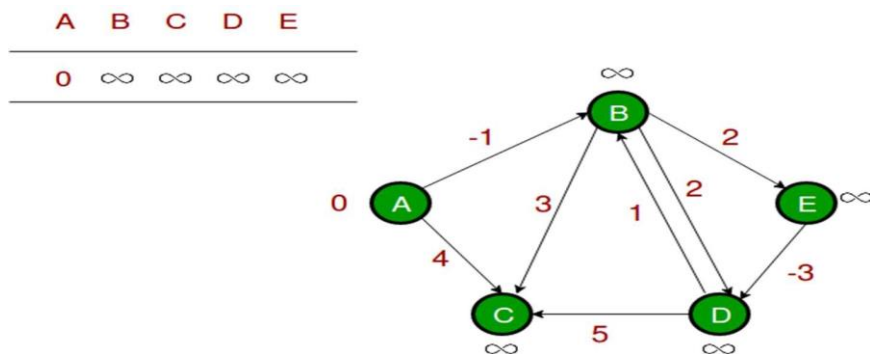
Objective: To introduce Bellman Ford method

Theory:

Given a graph and a source vertex source in graph, find shortest paths from src to all vertices in the given graph. The graph may contain negative weight edges. We have discussed Dijkstra's algorithm for this problem. Dijkstra's algorithm is a Greedy algorithm and time complexity is $O(V \log V)$ (with the use of Fibonacci heap). Dijkstra doesn't work for Graphs with negative weight edges, Bellman-Ford works for such graphs. Bellman-Ford is also simpler than Dijkstra and suites well for distributed systems. But time complexity of Bellman-Ford is $O(VE)$, which is more than Dijkstra.

Example:

Let the given source vertex be 0. Initialize all distances as infinite, except the distance to the source itself. Total number of vertices in the graph is 5, so all edges must be processed 4 times.



Let all edges are processed in the following order: (B, E), (D, B), (B, D), (A, B), (A, C), (D, C), (B, C), (E, D). We get the following distances when all edges are processed the first time. The first row shows initial distances. The second row shows distances when edges (B, E), (D,

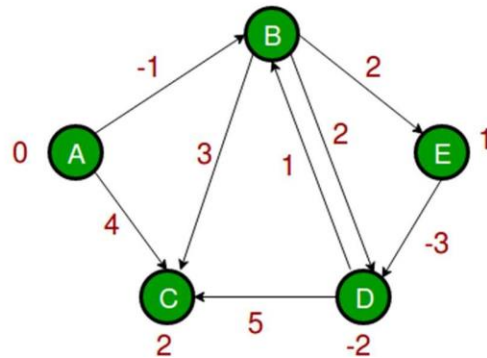


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B), (B, D) and (A, B) are processed. The third row shows distances when (A, C) is processed. The fourth row shows when (D, C), (B, C) and (E, D) are processed.

A	B	C	D	E
0	∞	∞	∞	∞
0	-1	∞	∞	∞
0	-1	4	∞	∞
0	-1	2	∞	∞
0	-1	2	∞	1
0	-1	2	1	1
0	-1	2	-2	1



The second iteration guarantees to give all shortest paths which are at most 2 edges long. The algorithm processes all edges 2 more times. The distances are minimized after the second iteration, so third and fourth iterations don't update the distances.

Handwritten notes showing the execution of the Bellman-Ford algorithm on a graph with 5 nodes (1, 2, 3, 4, 5).

Initial graph structure (from image):

- Node 1: source, distance 0
- Node 2: distance 3
- Node 3: distance 6
- Node 4: distance 2
- Node 5: distance 0

Iteration 1: Relax edge $\langle 5, 2 \rangle$ & $\langle 5, 4 \rangle$

V	1	2	3	4	5
d[V]	0	3	6	2	0
p[V]	1	5	1	5	-

Iteration 2: Relax edge $\langle 2, 1 \rangle$ $\langle 4, 2 \rangle$ $\langle 4, 3 \rangle$

V	1	2	3	4	5
d[V]	0	3	3	2	0
p[V]	1	5	4	5	-

Iteration 3: Relax edge $\langle 2, 1 \rangle$

V	1	2	3	4	5
d[V]	0	3	3	2	0
p[V]	1	5	4	5	-

Iteration 4: No edge relaxed

Final shortest path:

```

graph LR
    1((1)) -- 3 --> 2((2))
    2 -- 1 --> 4((4))
    4 -- 1 --> 3((3))
    4 -- 2 --> 5((5))
  
```

eg. shortest path to 1: $\{5, 4, 2, 1\}$



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Algorithm:

```
function Bellman_Ford(list vertices, list edges, vertex source, distance[], parent[])
```

```
for each vertex v in vertices
```

```
    distance[v] = INFINITY
```

```
    parent[v] = NULL
```

```
distance[source] = 0
```

```
for i = 1 to V-1
```

```
    for each edge (u, v) with weight w
```

```
        if (distance[u] + w) is less than distance[v]
```

```
            distance[v] = distance[u] + w
```

```
            parent[v] = u
```

```
for each edge (u, v) with weight w
```

```
    if (distance[u] + w) is less than distance[v]
```

```
        return "Graph contains a negative-weight cycle"
```

```
return distance[], parent[]
```

Output:

Shortest path from source (5)

Vertex 5 -> cost=0 parent=0

Vertex 1-> cost=6 parent=2

Vertex 2-> cost=3 parent=4

Vertex 3-> cost =3 parent =4

Vertex 4-> cost =2 paren=5



Implementation:

```
#include <stdio.h>

#include <limits.h>

#define MAX_VERTICES 100

struct Edge {
    int source, destination, weight;
};

struct Graph {
    int vertices, edges;
    struct Edge edge[MAX_VERTICES];
};

void initGraph(struct Graph *graph, int vertices, int edges) {
    graph->vertices = vertices;
    graph->edges = edges;
}

void bellmanFord(struct Graph *graph, int source) {
    int distance[MAX_VERTICES];
    int i, j;
    for (i = 0; i < graph->vertices; i++) {
        distance[i] = INT_MAX;
    }
    distance[source] = 0; // Distance from source to itself is 0
```



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```
for (i = 1; i <= graph->vertices - 1; i++) {
    for (j = 0; j < graph->edges; j++) {
        int u = graph->edge[j].source;
        int v = graph->edge[j].destination;
        int weight = graph->edge[j].weight;
        if (distance[u] != INT_MAX && distance[u] + weight < distance[v]) {
            distance[v] = distance[u] + weight;
        }
    }
}

for (i = 0; i < graph->edges; i++) {
    int u = graph->edge[i].source;
    int v = graph->edge[i].destination;
    int weight = graph->edge[i].weight;
    if (distance[u] != INT_MAX && distance[u] + weight < distance[v]) {
        printf("Graph contains negative weight cycle\n");
        return;
    }
}

printf("Vertex Distance from Source\n");
for (i = 0; i < graph->vertices; i++) {
    printf("%d \t\t %d\n", i, distance[i]);
}
}
```



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```
int main() {  
    struct Graph graph;  
    int vertices, edges, source;  
    printf("Enter number of vertices and edges: ");  
    scanf("%d %d", &vertices, &edges);  
    initGraph(&graph, vertices, edges);  
    printf("Enter source vertex: ");  
    scanf("%d", &source);  
    printf("Enter edges (source destination weight):\n");  
    for (int i = 0; i < edges; i++) {  
        scanf("%d %d %d", &graph.edge[i].source, &graph.edge[i].destination,  
&graph.edge[i].weight);  
    }  
    bellmanFord(&graph, source);  
    return 0;  
}
```

Conclusion: The implementation of the Bellman-Ford algorithm proved effective in finding the shortest paths in weighted graphs. Through rigorous testing and analysis, the algorithm demonstrated its reliability and efficiency in solving the single-source shortest path problem, offering valuable insights for real-world applications in network routing and optimization.