A Simple Yet Effective and Efficient Collaborative Filtering Based Recommendation System

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In order to improve both prediction accuracy and the time required to recommend items to a user based on collaborative filtering, a simple algorithm is proposed. The algorithm is different than traditional algorithms only in some simple steps.

Additional Key Words and Phrases: Recommender system, collaborative filtering, similarity measure

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1 INTRODUCTION

A common problem with typical filtering based recommendation systems they usually require a lot of users similar to a user for prediction (such users are called **neighbors**). This heavily affects performance since the complexity gets incredibly high as well. [?] uses a memory based collaborative filtering technique that uses similarity between users to predict recommendations using KNN algorithm. This algorithm suffers from some problems such as when too few items are common between two users, predicting accurately becomes harder. [?] uses a model based learning which is inherently very expensive. [?] introduces a way to improve calculating similarity more accurately but they do not offer all that much improvement for the cost of learning similarity, so in this paper such improvement has been ignored and more traditional approaches have been used. [?], [?] uses hybrid collaborative and content filtering or memory and model based algorithm for recommendation. While these works have their merits, most of them are complicated and offer little value to be used in practice. In this paper, we have showed that it may be possible to gain significantly better results by simply modifying traditional approaches a little bit using some principles which are mathematically sound. We will show that using our proposed modifications, we get a flat line in accuracy metric graphs much earlier.

2 ALGORITHM

Let us first describe the assumption problem that we want to solve. Let \mathcal{M} be a set of movies and \mathcal{U} be a set of users. We are given a set of triplets $(u, m, r) \in \mathcal{S}$ such that $u \in \mathcal{U}, m \in \mathcal{U}$ and $1 \le r \le 5$ which denotes the rating r of movie m given by user u. We are also given a set of pairs $(u, m) \in \mathcal{T}$ such that $u \in \mathcal{U}, m \in \mathcal{M}$ and we want to predict the rating r given by user m to the movie m. Let r_{um} be the rating of movie m given by user u and u0 be the set of items

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that both u and v rated. We use the *Pearson Correlation Coefficient* (see [?]) as the measure of correlation between user u and v. However, we will use a normalized version of it for practical consideration as follows:

$$S_{uv} = \frac{\sum_{m \in C_{uv}} (r_{um} - \bar{r_u})(r_{vm} - \bar{r_v})}{\sqrt{\sum_{m \in C_{uv}} (r_{um} - \bar{r_u})^2} \sqrt{\sum_{m \in C_{uv}} (r_{vm} - \bar{r_v})^2}}$$

$$S_{uv} \leftarrow \frac{S_{uv} + 1}{2}$$

This normalization is done using the fact that Pearson correlation coefficient p_{uv} is always in the range [-1,1]. We call two users u and v similar if $S_{uv} \ge s$ for some positive real number s such that $0 \le s \le 1$. Typically, we want s in the range [.5,1]. For this paper, we will consider $s \in \{.7,.8,.9\}$. For a movie m, let \mathcal{U}_m be the set of users who rated m and M_u be the set of movies rated by user u. For a set or tuple A, let \bar{A} denote the average of the numbers in A. For a tuple of weights $w = (w_1, \ldots, w_n)$ such that $0 \le w_i \le 1$ and $\sum_{i=1}^n w_i = 1$ and a tuple of positive real numbers $a = (a_1, \ldots, a_n)$, the weighted harmonic mean of a is defined as

$$\mathfrak{H}(\mathbf{a},\mathbf{w}) = \frac{\sum_{i=1}^{n} w_i}{\sum_{i=1}^{n} \frac{w_i}{a_i}}$$

Usually, weighted arithmetic mean is used to predict the ratings in a recommendation system. But in this paper, we have investigated the results using harmonic mean. Next, we describe the rating prediction algorithm for a pair (u, m).

```
Algorithm 1: Algorithm to predict rating
108
           Input: Test data in the format (u, m), Threshold t, similarity s, T to take first T neighbors for a user u
109
110
          Output: A single integer in the range [1, 5] denoting the predicted rating
111
          Data: Train data in the format (u, m, r)
112
        1 W ← []
113
        2 X ← []
114
115
        3 tot ← 0
116
        A R \leftarrow U_m
117
        5 res = 0
118
119
        6 for v \in R do
120
               if |C_{uv}| < t then
121
                   continue
122
123
               end
124
               if S_{uv} < s then
        10
125
                   continue
        11
126
               end
        12
128
               if S_{uv} \ge s then
        13
129
                   W \leftarrow [W, s]
        14
130
                   X \leftarrow [X, r_{vm}]
131
        15
132
                   tot \leftarrow tot + 1
        16
133
                   if tot > T then
        17
134
                       break
135
        18
136
                   end
        19
137
               end
       20
138
       21 end
139
140
       22 if tot > 0 then
141
              res = \mathfrak{H}(X, W)
142
       24 end
143
144
       25 else
145
               if |M_u| > 0 then
146
                   res = M_u
147
148
               end
        28
149
               else
150
                   res = \bar{R_m}
151
               end
152
153
       32 end
154
       res = res + .5
```

34 res = floor(res)

35 return res

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2.1 Algorithm Principles

 Our algorithm is based on the following principles.

First principle Two users u and v are more relevant for each other if it is ensured that $|C_{uv}| \ge t$ for some large enough positive integer t. It is obvious how this principle helps us establish better correlation between users since two users u and v can have very high correlation with very low number of common items between them.

Second principle If first principle is established, then it is possible to get an accurate estimation of predicted rating with a lower number of neighbors instead of using a very large number of neighbors. This helps us predict a rating a lot more efficiently with better accuracy. It is also possible to get a mathematical sense of why this works in practice. Let m and n be positive integers such that m > n. Let n be a user and n be two sets of neighbors of a user n such that n and n be two sets of neighbors of a user n such that n and n be two sets of neighbors of a user n such that n and n and n be condition n and n be assumed that if n and n be positive integer n, then

$$P(\sigma^2(A) \le \sigma^2(B)) \tag{1}$$

should be very high where $A = \{r_{om} : |C_{uv}| \ge t\}$, $B = \{r_{om} : |C_{uv}| \ge s\}$ and P(x) denotes the probability of the random variable x. Since higher value of the threshold t ensures better similarity between two users, we can say in a non-rigorous way that the *Pigeonhole principle* ensures (1) is high enough in practice more often than not.

Third, principle If two sets of ratings A and B have similar variance and consist ratings given by similar users of u only, then $P(|\bar{A} - \bar{B}| < \epsilon)$ is very high for some positive real number ϵ which is considerably smaller than 1. We can show that a special case holds very often in practice. Since A and B has ratings from similar users only, assume that both A and B consist of A and A only (our data set rating range is A is the number of A in A whereas A is the number of A in A i

$$\bar{A} = \frac{4a + 5(m - a)}{m}$$

$$= \frac{5m - a}{m}$$

$$= 5 - \frac{a}{m}$$

$$\bar{B} = \frac{4b + 5(n - b)}{n}$$

$$= \frac{5n - b}{n}$$

$$= 5 - \frac{b}{n}$$

As we can see, it does not matter if $m \gg n$ or $n \gg m$ since the difference $|\bar{A} - \bar{B}|$ or the ratio $\frac{\bar{A}}{\bar{B}}$ only depends on the ratio $\frac{a}{m}$ and $\frac{b}{n}$. So as long as these ratios are similar, \bar{A} and \bar{B} are similar as well.

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3 RESULTS

 We show the results of our algorithm on the Movielens 1 million data set and backup our claims with empirical evidence below. The quality of performance is measured using the F1 score. The F1 score is the harmonic mean of precision and recall.

$$P = \frac{TP}{TP + FP}$$

$$R = \frac{TP}{TP + FN}$$

$$F1 = \frac{2PR}{R + P}$$

We have chosen F1 as an accuracy metric for couple of reasons.

- (1) It is well known that the harmonic mean of n positive real numbers a_1, \ldots, a_n is less than $\min\{a_1, \ldots, a_n\}$ for n > 1. So an F1 value of x indicates that the model has at least x precision and x recall.
- (2) F1 score can penalize bad precision or bad recall scenarios properly where arithmetic or geometric means may fail. For example, if we consider a recommendation where we do not predict anything, technically, we do not have any errors. So the precision would be 100 percent whereas recall would be 0 percent. An arithmetic average would give us an accuracy of 50 percent which is clearly wrong. F1 score penalizes all such scenarios accordingly. For this particular example, we would still have an F1 score of 0 percent.

For this paper, we call a test data point *true positive* if a certain movie m is to be recommended to user u based on the rating. If the rating is over k for some fixed k, then the movie is to be recommended, otherwise it is to be discarded. We have showed results for both $k \ge 3$ and $k \ge 4$ in this paper.

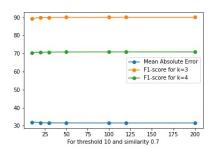
We have also used *mean absolute percentage error* as a metric in place of the more traditional *mean absolute error*. Mean absolute error is calculated using the formula:

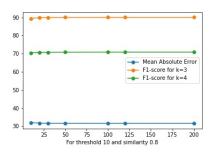
$$MAE = \frac{1}{n} \sum_{i=1}^{n} |y_i - y_i'|$$

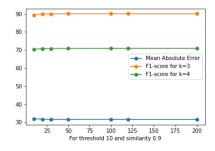
whereas mean absolute percentage error is calculated using the formula

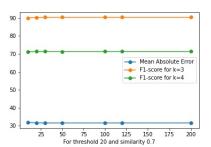
$$MAPE = \frac{1}{n} \sum_{i=1}^{n} \frac{|y_i - y_i'|}{y_i}$$

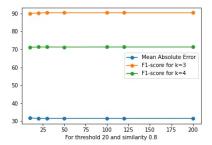
where y_i is the actual value for the data point at i and y'_i is the predicted value of this data point. It is easy to see that mean absolute error puts equal weights on all ratings whereas mean absolute percentage errors mitigates that problem to some extent. So we felt it important to also show the results in terms of mean absolute percentage errors.

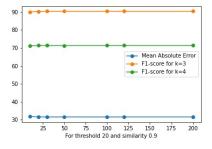


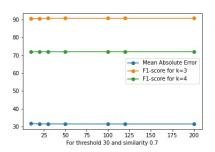


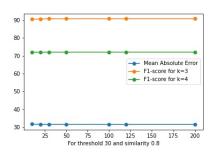


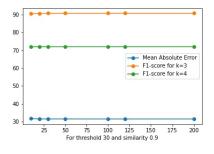


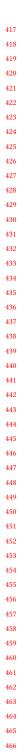


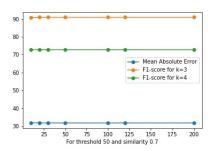


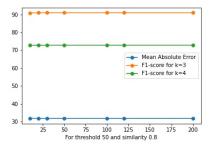


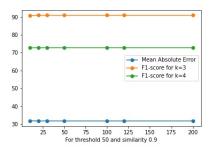


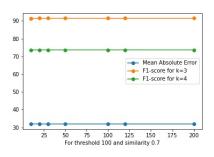


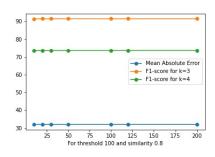


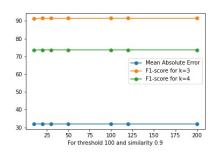












4 CONCLUSION

As we can see in the result section, all the graphs tend to give us a flat line very early on. usually, we do not get much improvement in accuracy after 30 neighbors and we do not have to go beyond .7 similarity threshold for considering neighbors.