PROB 140 Spring 2022



Probability for Data Science

WEEK 3 STUDY GUIDE

The Big Picture

The week starts with another connection between the binomial and Poisson families, and moves on to the most important concept of the course, which is expectation. This can be thought of as a kind of center of the distribution of a random variable, or a good guess for the variable. All probabilities are expectations, the

variance of a random variable is an expectation, and least squares predictors are expectations. So please pay attention!

- Randomizing parameters can have dramatic effects on dependence and independence. A Poisson number of i.i.d. success/failure trials has beautiful and powerful properties.
- Expectation is the average of the possible values, weighted by their probabilities. Care is needed for variables that have infinitely many values.
- The definition helps us calculate some expectations, but almost always we calculate expectation using its properties, just as we calculate derivatives using properties of derivatives instead of the definition.
- A simple but powerful method helps us find the expectation of a function of a random variable.

Week At a Glance

Mon 1/31	Tue 2/1	Wed 2/2	Thu 2/3	Fri 2/4
	Lecture	Sections	Lecture	Sections
HW 2 Party 9-12 HW 2 Due HW 3 (Due Mon 2/7)				
Lab 1A due Lab 1B (Due Mon 2/7)				Lab 1B Party 3-5
Skim 7.1, 7.2	Work through Ch 7	Finish Ch 7, skim 8.1	Work through 8.1-8.2	Finish 8.1-8.3

Reading, Practice, and Live Sessions

Book	Topic	Lectures: Prof. A.	Sections: GSIs	Optional Additional Practice
Ch 7	Poissonization - 7.1 has properties of the Poisson distribution - 7.2 asks the same questions as 6.1, but with a Poisson number of trials - 7.3 extends this to trials with more than two categories, analogous to 6.3	Tue 2/1 Poissonization: - Beautiful calculations with surprising results - Pay attention to the math because you'll need the methods again	Wed 2/2 - Ch 7 Ex 6, 2, 4, 8	Chapter 7 All the exercises not covered in section
Ch 8	- 8.1 has the definition, interpretation, and a note on existence - 8.2 calculates the expectations of some of the famous distributions, in one case by introducing a new way of calculating expectation - 8.3 shows how to calculate expectations of linear and nonlinear functions of random variables	Thu 2/3 - Focused on 8.1-8.3 - Fine points, nonlinear functions, and some surprises	Fri 2/4 - Ch 8 Ex 2, 4, 10, 6	Chapter 8 Wait till next week; you need the remaining sections of Ch 8 for the remaining exercises in the chapter