**PROB 140** 



### Fall 2022

## **WEEK 3 STUDY GUIDE**

## **The Big Picture**

This week is largely about two of the principal families of distributions: the binomial and the Poisson.

- Random samples often result in random counts, such as the number of voters who favor a candidate. The distribution of the count depends on the method of sampling.
- If the sample is a fixed number of i.i.d. success/failure trials, the distribution of the number of successes is *binomial*. The shape of the distribution can be understood by using consecutive odds ratios.
- In some situations, the binomial distribution is well approximated by a *Poisson* distribution. The Poisson is our first distribution on infinitely many values.
- Randomizing parameters can have dramatic effects on dependence and independence. A Poisson number of i.i.d. success/failure trials has beautiful and powerful properties.

### Week At a Glance

Monday 9/5	Tuesday 9/6	Wednesday 9/7	Thursday 9/8	Friday 9/9
	Lecture	Sections: QUIZ 1	Lecture	Sections
	HW 2 Due AT NOON HW 3 (Due Mon 9/12)			HW 3 Party 3PM - 5PM
	Lab 1 Due Lab 2A (Due Mon 9/12)			Lab 2A Party 10AM - 1PM
	Read 6.1, 6.2, skim 6.5	Read Chapter 6	Skim 7.1, 7,2	Read Ch 7

# **Reading, Practice, and Class Meetings**

Book	Topic	Lectures: Prof. A.	Sections: GSIs	Optional Additional Practice
Ch 6	Binomial and its relatives  - 6.1 is about a fixed number of i.i.d. success/failure trials; the number of successes has a binomial distribution  - 6.2 has examples you should read  - 6.3 extend the binomial to the multinomial case where each trial has several possible outcomes, not two  - 6.4 compares the number of successes when sampling with replacement (binomial) and the number of successes when sampling without replacement (hypergeometric), and shows when the two are almost the same  - 6.5 examines the shape of the binomial histogram, and identifies the mode, by studying odds ratios  - 6.6 uses odds ratios to show that under some conditions the binomial has a Poisson limit	Tuesday 9/6  - Straightforward but important observations about success counts - Deeper dive into the math to explain what we see - An approximation, leading to a new class of distributions	Wednesday 9/7 - QUIZ 1 - Lab 2A Part I: a new look at total variation distance	Chapter 6 1, 4, 11, 12
Ch 7	Poissonization - 7.1 has properties of the Poisson distribution - 7.2 asks the same questions as 6.1, but with a Poisson number of trials - 7.3 extends this to trials with more than two categories, analogous to 6.3	Thursday 9/8  Poissonization: - Beautiful calculations with surprising results - Pay attention to the math because you'll need the methods again	Friday 9/9 Poisson approximation and Poissonization: - Ch 6 Ex 10 - Ch 7 Ex 2 - Ch 7 Ex 8 Relations with other exercises	Chapter 7 3, 4, 5

Lab 2 is about measuring the quality of the Poisson approximation in 6.6.