

## Fall 2023 WEEK 9 STUDY GUIDE

## **The Big Picture**

More technique!

- We know how to find expectations of a function of a random variable. We now examine how to find the density of a function of another random variable that has a known density, and notice that we have to be careful when the function isn't monotone.
- An important transformation results in the process on which simulation of random variables is based
- To study the joint behavior of two random variables, we define their joint density, which is the analog of the discrete joint distribution. Probabilities and expectations are now double integrals.
- The family of *beta* densities is important for machine learning and offers a good example of how joint densities can be constructed.

## Week At a Glance

| Mon 10/16                            | Tue 10/17                                    | Wed 10/18  | Thu 10/19   | Fri 10/20                  |
|--------------------------------------|--|--|---|----------------------------|
|                                      | Lecture                                      | Sections   | Lecture   | Mega Sections              |
| Lab 6A Due<br>Lab 6B (Due Mon 10/23) |  |  | Lab 5B Party 10 AM to noon                            |                            |
| HW 8 Due<br>HW 9 (Due Mon 10/23)     |  |  |   | HW 9 Party 3 PM to 5 PM    |
| Skim Sec 16.1                        | Work through<br>Sections 16.1, 16.2,<br>16.4 | Review Lab 6A Part 3,<br>do Lab 6B Part 4, and<br>work through Section<br>16.3 | Work through Sec 17.1 carefully, skim Sections 17.2-3 | Work through<br>Chapter 17 |

## **Reading, Practice, and Class Meetings**

| Book  | Topic   | Lectures: Instructors                        | Sections: GSIs                      | Optional Additional Practice  |
|-------|---|--|-------------------------------------|---|
| Ch 16 | Densities of Transformations - 16.1 is about linear transformations; understanding this helps understand the non-linear case - 16.2 is about monotone transformations, linear or non-linear - 16.3 is for you to read, referring to Parts 3 and 4 of Lab 4: it's the process by which you can generate random variables with a specified distribution - 16.4 takes care of the non-monotone case, with particular reference to the square; in a typical semester, students read this one themselves too | Tuesday 10/17 - Densities of transformations | Wednesday 10/18 - Ch 16 Ex 1, 4, 6a | Ch 16 - All the exercises not covered in section. Be careful about signs in Ex 6b.  Ex 7 is a brain-teaser. |
| Ch 17 | Joint Densities - 17.1-17.3 are the 2-dimensional counterparts of Ch 15 and the density version of Chapter 4. The examples in the videos aren't always the same as those in the text 17.4 is one of the "big name" families of densities  | Thursday 10/19 - Joint densities             | Friday 10/20<br>- Ch 17 Ex 4, 5, 7  | Ch 17<br>- Ch 17 Ex 1, 9  |