



Spring 2023

## WEEK 4 STUDY GUIDE

### The Big Picture

**Expectation is the most important concept in this course. Do not skip this week's sessions.**

- The most powerful property of expectation is additivity. We will cover many and varied uses of this.
- Expectation is used in the definition of the bias of an estimator, and hence also in the construction of unbiased estimators.
- In multi-stage experiments, expectation can be calculated iteratively by conditioning.

### Week At a Glance

| Mon 2/6  | Tue 2/7  | Wed 2/8                            | Thu 2/9            | Fri 2/10                      |
|--|--|------------------------------------|--------------------|-------------------------------|
|  | Lecture  | Sections                           | Lecture            | Sections                      |
| <b>Lab 2B Due</b><br>Lab 3 (Part A due Mon 2/13) |  |                                    | Lab 3A party 10-12 |                               |
| <b>HW 3 Due</b><br>HW 4 (Due Mon 2/13)           |  |                                    |                    | HW 4 party 3-5                |
| Skim Sections 8.4, 8.5                           | <b>Important:</b> Work through Sections 8.4, 8.5 | Review Chapter 8; skim Section 9.2 | Skim Chapter 9     | Work through Ch 9; it's short |

## Reading, Practice, and Live Sessions

| Book        | Topic   | Lecture: Prof A.  | Section: GSIs   | Optional Additional Practice                                 |
|-------------|---|---|---|--|
| 8.4,<br>8.5 | <b>Additivity of Expectation</b> <ul style="list-style-type: none"> <li>- 8.4 is about additivity: the expectation of a sum is the sum of the expectations, regardless of dependence or independence. Hugely powerful.</li> <li>- Additivity helps us construct unbiased estimators based on averages</li> <li>- 8.5 uses additivity to develop the method of indicators for finding expected counts</li> </ul>                 | <b>Tue 2/7</b> <ul style="list-style-type: none"> <li>- Additivity and some consequences:</li> <li>- Constructing unbiased estimators</li> <li>- Finding expected counts</li> </ul> | <b>Wed 2/8</b> <ul style="list-style-type: none"> <li>- Ch 8 Ex 11, 12, 9, 8</li> </ul> | <b>Chapter 8</b><br>All the exercises not covered in section |
| Ch 9        | <b>Expectation by Conditioning</b> <ul style="list-style-type: none"> <li>- 9.1 is the old multiplication rule combined with recursion, to find probabilities quickly</li> <li>- 9.2 shows how to find expectation by conditioning, building on the familiar calculation of finding an overall average as a weighted average of group averages</li> <li>- 9.3 has examples in the context of i.i.d. Bernoulli trials</li> </ul> | <b>Thu 2/9</b> <ul style="list-style-type: none"> <li>- Probabilities and expectation by conditioning and recursion</li> </ul>  | <b>Friday 2/10</b> <ul style="list-style-type: none"> <li>- Ch 9 Ex 2, 4, 6</li> </ul>  | <b>Chapter 9</b><br>All exercises not covered in section.    |