Rearranging Equations

LLE – Mathematics and Statistics ECO-5007A

Skills - Rearranging Equations

In each of the following expressions, make x the subject of the equation.

1.
$$x + y = 12$$

2.
$$5x - 4 = y$$

3.
$$ax - 3by = 9$$

4.
$$y = mx + c$$

5.
$$2 + 5xy = 6$$

6.
$$9x + 6y = 4x + 1$$

Tip: Gather all terms containing x on one side of the equation and all other terms on the opposite side. Then, factor out x.

7.
$$ax + by = 4x + 1$$

8.
$$ax - by = bx - 8$$

$$9. \ \frac{2ty + mx}{ty - mx} = 1$$

$$10. \ \frac{ty + mx}{ty - 3mx} = k$$

11.
$$9x^2 = 4y$$

12.
$$x^3 - 5m = t$$

13.
$$x^2 - 2x = 15$$

Tip: Rearrange this into the standard quadratic form $ax^2 + bx + c = 0$ and then consider using the quadratic formula or factoring.

14.
$$x^2 = 2 - qx$$

15.
$$x^2 - 8 = kx$$

Rearranging with Indices

Recall the rules of indices:

$$x^{a}x^{b} = x^{a+b}$$
$$\frac{x^{a}}{x^{b}} = x^{a-b}$$
$$(x^{a})^{b} = x^{ab}$$

It also useful to note that a number multiplied by its reciprocal is 1, e.g. $\frac{3}{4}\times\frac{4}{3}=1$

Examples:

Arrange to make x the subject of $x^{\frac{4}{9}} = y^{\frac{1}{3}}$

Solution:

$$x^{\frac{4}{9} \times \frac{9}{4}} = y^{\frac{1}{3} \times \frac{9}{4}}$$
$$x = y^{\frac{3}{4}}$$

Arrange to make x the subject of $x^{\frac{2}{3}}-y=10$

Solution:

$$x^{\frac{2}{3}} = 10 + y$$
$$x = (10 + y)^{\frac{3}{2}}$$

Practice Problems:

Rearrange the following to make \boldsymbol{x} the subject:

1.
$$x^{\frac{3}{4}} = y^{\frac{1}{2}}$$

2.
$$x^{\frac{3}{4}} = y^{\frac{1}{2}} - 2$$

3.
$$5x^8 - y = 0$$

4.
$$x^{\frac{3}{4}}y = 8my$$

5.
$$2x^{2.5} = 64$$

6.
$$x^2y^3x^5y^2 = a$$

7.
$$0.5x^{-0.5}y^{-0.5} \times 0.5x^{-0.5}y^{0.5} = 4$$

8.
$$0.8y^{-0.2}x^{0.2} \times 0.2y^{0.8}x^{-0.8} = 10$$

9.
$$\frac{\alpha y^{\alpha - 1} x^{\beta}}{\beta y^{\alpha} x^{\beta - 1}} = k$$