Design and Implementation of Probabilistic Programming Language Anglican

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Abstract

Anglican is a probabilistic programming system designed to interoperate with Clojure and other JVM languages. We introduce the programming language Anglican, outline our design choices, and discuss in depth the implementation of the Anglican language and runtime, including macro-based compilation, extended CPS-based evaluation model, and functional representations for probabilistic paradigms, such as a distribution, a random process, and an inference algorithm.

We show that a probabilistic functional language can be implemented efficiently and integrated tightly with a conventional functional language with only moderate computational overhead. We also demonstrate how advanced probabilistic modeling concepts are mapped naturally to the functional foundation.

1. Introduction

For data science practitioners, statistical inference is typically just one step in a more elaborate analysis workflow. The first stage of this work involves data acquisition, pre-processing and cleaning. This is often followed by several iterations of exploratory model design and testing of inference algorithms. Once a sufficiently robust statistical model and a corresponding inference algorithm have been identified, analysis results must be post-processed, visualized, and in some cases integrated into a wider production system.

Probabilistic programming systems (Goodman et al. 2008; Mansinghka et al. 2014; Wood et al. 2014; Goodman and Stuhlmüller 2015) represent generative models as programs written in a specialized language that provides syntax for the definition and conditioning of random variables. The code for such models is generally concise, modular, and easy to modify or extend. Typically inference can be performed for any probabilistic program using one or more generic inference techniques provided by the system backend, such as Metropolis-Hastings (Wingate et al. 2011; Mansinghka et al. 2014; Yang et al. 2014), Hamiltonian Monte Carlo (Stan Development Team 2014), expectation propagation (Minka et al. 2010), and extensions of Sequential Monte

Carlo (Wood et al. 2014; van de Meent et al. 2015; Paige et al. 2014) methods. These generic techniques may be less statistically efficient than techniques tailored to a specific model, however probabilistic programming facilitates simpler implementations of models making the inference inherently faster.

While probabilistic programming systems shorten the iteration cycle in exploratory model design, they typically lack basic functionality needed for data I/O, pre-processing, and analysis and visualization of inference results. In this demonstration, we describe the implementation of Anglican (Tolpin et al. 2015; Wood et al.), a probabilistic programming language that tightly integrates with Clojure (Hickey 2008; Clo), a general-purpose programming language that runs on the Java Virtual Machine (JVM). Both languages share a common syntax, and can be invoked from each other. This allows Anglican programs to make use of a rich set of libraries written in both Clojure and Java. Conversely Anglican allows intuitive and compact specification of models for which inference may be performed as part of a larger Clojure project.

There are several ways to build a programming language on top or besides another language. The easiest to grasp is an interpreter — a program that reads a program, in its entirety or line-by-line, and executes it by applying operational semantics of a certain kind to the language. BASIC is famous for line-by-line interpreted implementations.

Another approach is to write a compiler, either to a virtual architecture, so called p-code or byte-code, or to real hardware. Here, the whole program is translated from the 'higher-level' source language to a 'lower-level' object language, which can be directly executed, either by hardware or by an interpreter — but the latter interpreter can be made simpler and more efficient than an interpreter for the source language.

On top of these two approaches are methods in which a new language is implemented 'inside' another language of the same level of abstraction. Different languages provide different means for this; Lisp is notorious for the macro facility that allows to extend the language almost without restriction — by writing *macros*, one adds new constructs to the existing language. There are several uses of macros — one is to extend the language *syntax*, for example, by adding new control structures; another is to keep the existing syntax but alter the *operational semantics* — the way programs are executed and compute their outputs.

Anglican is implemented in just this way — a macro facility provided by Clojure, a Lisp dialect, is used both to extend Clojure with constructs that delimit probabilistic code, and to alter the operational semantics of Clojure

expressions inside probabilistic code fragments. Anglican claims its right to count as a separate language because of the ubiquitous probabilistic execution semantics rather than a different syntax, which is actually an advantage rather than a drawback — Clojure programmers only need to know how to specify the boundaries of Anglican programs, but can use familiar Clojure syntax to write probabilistic code.

An implementation of Anglican must therefore address three issues:

- the Clojure syntax to introduce probabilistic Anglican code inside Clojure modules;

- source-to-source transformation of Anglican programs into Clojure, so that probabilistic execution becomes possible;

- algorithms which run Clojure code, obtained by transforming Anglican programs, according to the probabilistic operational semantics.

Execution of probabilistic programs by inference algorithms is different from execution of deterministic programs. A probabilistic program is executed multiple times, often hundreds of thousands or even millions of times for a single inference task. Random choices may affect which parts of the program code are executed and how often. Many inference algorithms require re-running the program multiple times partially, from a certain point on. Different executions may employ different random choices, however for efficient inference a correspondence between random choices in different executions should be maintained. These are just some of the challenges which were faced and solved during development of Anglican.

Anglican language syntax, compilation, invocation, and runtime support of Anglican queries are discussed in detail in further sections.

2. Design Outline

An Anglican program, or *query*, is compiled into a Clojure function. When inference is performed with a provided algorithm, this produces a sequence of output values, or *predicts*. Anglican shares a common syntax with Clojure; Clojure functions can be called from Anglican code and vice versa. A simple program in Anglican can look like the following code:

```
(defquery model data
  "chooses a distribution
   which describes the data"
  (let [;; Guessing a distribution
        dist (sample (categorical
                       [[normal 0.5]
                        [gamma 0.5]]))
        a (sample (gamma 1 1))
        b (sample (gamma 1 1))
        d (dist a b)]

    ;; Observing samples from the distribution
    (loop [data data]
      (when (seq data)
        (let [[x & data] data]
          (observe d x))
        (recur data)))

    ;; Predicting a, b and the distribution
    (predict :a a)
    (predict :b b)
    (predict :d d)))
```

This query defines a probability distribution on three predicted variables, $d \in \{normal, gamma\}$ for a distribution type, and a and b for positive parameters for the type. Samples from this distribution can be obtained by running the query under one of Anglican's inference algorithms.

Internally, an Anglican query is represented by a computation in *continuation passing style* (CPS) (Appel and Jim 1989), and inference algorithms exploit the CPS structure of the code to intercept probabilistic operations in an algorithm-specific way[1]. Among the available inference algorithms there are Particle Cascade (Paige et al. 2014), Lightweight Metropolis-Hastings (Wingate et al. 2011), Iterative Conditional Sequential Monte-Carlo (Particle Gibbs) (Wood et al. 2014), and others. Inference on Anglican queries generates a lazy sequence of samples, which can be processed asynchronously in Clojure code for analysis, integration, and decision making.

Clojure (and Anglican) runs on the JVM and gets access to a wide choice of Java libraries for data processing, networking, presentation, and imaging. Conversely, Anglican queries can be called from Java and other JVM languages. Programs involving Anglican queries can be deployed as JVM *jars*, and run without modification on any platform for which JVM is available.

A probabilistic program, or query, mostly runs deterministic code, except for certain checkpoints, in which probabilities are involved, and normal, linear execution of the program is disrupted. In Anglican and similar languages there are two types of such checkpoints:

- drawing a value from a random source (sample);

- conditioning a computed value on a random source (observe).

Anglican can be mostly implemented as a regular programming language, except for the handling of these checkpoints. Depending on the *inference algorithm*, sample and observe may result in implicit input/output operations and control changes. For example, observe in particle filtering inference algorithms (Wood et al. 2014) is a non-deterministic control statement at which a particle can be either replicated or terminated. Similarly, in Metropolis-Hastings (Wingate et al. 2011), sample is both an input statement which 'reads' values from a random source, and a non-deterministic control statement (with delayed effect), eventually affecting acceptance or rejection of a sample.

Because of the checkpoints, Anglican programs must allow the inference algorithm to step in, recording information and affecting control flow. This can be implemented through coroutines/cooperative multitasking, and parallel execution/preemptive multitasking, as well as through explicit maintenance of program continuations at checkpoints. Anglican follows the latter option. Clojure is a functional language, and continuation-passing style (CPS) transformation is a well-developed technique in the area of functional languages. Implementing a variant of CPS transformation seemed to be the most flexible and lightweight option — any other form of concurrency would put a higher burden on the underlying runtime (JVM) and the operating system. Consequently, Anglican has been implemented as a CPS-transformed computation with access to continuations in probabilistic checkpoints. Anglican 'compiler', represented by a set of functions in the anglican.trap namespace, ac-

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[1] (Goodman and Stuhlmüller 2015) also describe a CPS-based implementation of a probabilistic programming language.

cepts a Clojure subset and transforms it into a variant of CPS representation, which allows inference algorithms to intervene in the execution flow at probabilistic checkpoints.

Anglican is intended to co-exist with Clojure and be a part of the source of a Clojure program. To facilitate this, Anglican programs, or queries, are wrapped by macros (defined in the `anglican.emit` namespace), which call the CPS transformations and define Clojure values suitable for passing as arguments to inference algorithms (`defquery`, `query`). In addition to defining entire queries, Anglican promotes modularization of inference algorithms through the definitions of *probabilistic functions* using `defm` (Anglican counterparts of Clojure `defn`). Probabilistic functions are written in Anglican, may include probabilistic forms `sample` and `observe` (as well `predict` for the output), and can be seamlessly called from inside Anglican queries, just like functions locally defined within the same query.

Operational semantics of Anglican queries is different from that of Clojure code, therefore queries must be called through inference algorithms, rather than 'directly'. The `anglican.inference` namespace declares the (ad-hoc) polymorphic function `infer` using Clojure's multimethod mechanism. This function accepts an Anglican query and returns a lazy sequence of weighted samples from the distribution defined by the query. When inference is performed on an Anglican query, the query is run by a particular inference algorithm. Inference algorithms must provide an implementation for `infer`, as well as override the polymorphic function `checkpoint` (defined as a multimethod) so as to handle `sample` and `observe` in an algorithm-specific manner and to construct an appropriate result on the termination of a probabilistic program.

Finally, Anglican queries use 'primitive', or commonly known and used, distributions, to draw random samples and condition observations. Many primitive distributions are provided by the `anglican.runtime` namespace, and an additional distribution can be defined by the user by implementing a particular set of functions for the distribution (via Clojure's protocol mechanism). The `defdist` macro provides a convenient syntax for defining primitive distributions.

3. Language

The Anglican language is a subset of Clojure[2]. Anglican queries are defined within `defquery` as shown in the previous section, using `if`, `when`, `cond`, `case`, `let`, `and`, `or`, `fn` forms; other forms of Clojure may be supported in the future but are not now. In `let` bindings and `fn` argument lists, Clojure's pattern matching mechanism for vector data type (called vector destructuring) is supported. Also, compound literals for vectors, hash maps, and sets are supported just like in Clojure.

3.1 Core Library

All of Clojure's core library except for higher-order functions (functions that accept other functions as arguments) is available in Anglican. Higher-order functions cannot be reused from Clojure, as they have to be re-implemented to accept functional arguments in CPS form. The follow-

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[2] It would be possible to support almost full Clojure by expanding all macros in the Anglican source code, however in Clojure, unlike in Scheme (Sperber et al. 2010), or Common Lisp (Pitman and Chapman 1994), the result of macro-expansion of derived special forms is not well specified and implementation specific.

ing higher-order functions are implemented: `map`, `reduce`, `filter`, `some`, `repeatedly`, `comp`, `partial`.

3.2 Tail Call

Clojure provides special forms `loop` and `recur` for writing tail-recursive programs. Such forms are not necessary in Anglican, because Anglican programs are CPS-converted and do not use stacks. For instance, no recursive call in Anglican can lead to stack overflow. In fact, in Anglican, it is recommended to use recursive calls to functions instead of `recur`. However, `loop`/`recur` is provided in Anglican for convenience as a way to express loops. `recur` outside of `loop` will lead to unpredictable behaviour and hard-to-catch errors.

4. Macro-based Compilation

> **HY:** I found this section confusing in the following sense. First, it does not highlight the most interesting aspects of the compilation of Anglican. It gives a good overview on how the compilation is implemented, but a reader might want to see something unique and interesting about Anglican. To me, the most interesting part of the compilation is the treatment of probabilistic constructs in Anglican's CPS transformation. How are sample, observe and stochastic memoization compiled? How should the standard CPS transformation be modified in order to handle these constructs? The use of state can be one answer for the second question. The second most interesting part is about the use of trampolining the mix with Clojure code. Second, the section assumes that a reader is already familiar with Clojure or something specific to probabilistic programming. For instance, it might be that a reader has never heard about Clojure records and stochastic memoization. Then, she or he would have difficulties in following this section. What should we do? One option is not to do anything. Another is to take care of the second point. That is, we make the section easily followed by someone who does not know Clojure. The third is to restructure the section and to take care of my first criticism.

> **DT:** I believe I partially addressed the above comment, but need to think more about it.

Compilation of Anglican into Clojure is built around a variant of CPS transformation. In a basic CPS-transformed program, a continuation receives a single argument — the computed value. In Anglican, there are two flows of computation going in parallel: values are computed by functional code, and, at the same time, the state of the probabilistic program, used by inference algorithms, is updated by probabilistic forms. Because of that, in Anglican a continuation accepts *two* arguments:

- the computed value;
- the internal state, bound to the local variable `$state` in every lexical scope.

The compilation relies on the Clojure *macro* facility, and implemented as a library of *functions* in namespace `anglican.trap`, which are invoked by macros. The CPS transformation is organized in top-down manner. The top-level function is `cps-of-expression`, which receives an expression and a continuation, and returns the expression in the CPS form. For example, the CPS transformation of constant 1 with continuation `cont` thus takes the following form:

```
=> (cps-of-expression 1 'cont)
(cont 1 $state)
```

4.1 The State

The state ($state) is threaded through the computation and contains data used by inference algorithm. $state is a Clojure hash map:

```
(def initial-state
  "initial program state"
  {:log-weight 0.0
   :predicts []
   :result nil
   ::mem {}
   ::store nil
   ... })
```

The full list of map entries depends on the inference algorithm. Except for transformation of mem, the memoization form, CPS transformation routines are not aware of contents of $state, do not access or modify it directly, but rather just thread the state unmodified through the computation. Algorithm-specific handlers of checkpoints corresponding to the probabilistic forms (sample, observe) modify the state and reinject a new state into the computation.

4.2 Expression Kinds

There are three different kinds of inputs to CPS transformation:

- literals, which are passed as an argument to the continuation unmodified;

- value expressions (e.g. the fn form) (called *opaque* expressions in the code) which must be transformed to CPS, but the transformed object is passed to the continuation as a whole, opaquely;

- general expressions (let's call them *transparent*), through which the continuation is threaded in an expression-specific way, and can be called in multiple locations of the CPS-transformed code, such as in all branches of an if statement.

4.2.1 Literals

Literals are the same in Anglican and Clojure. They are left unmodified; literals are a subset of opaque expressions. However, the Clojure syntax has a peculiarity of using the syntax of compound literals (vectors, hash maps, and sets) for data constructors. Hence, compound literals must be traversed recursively, and if there is a nested non-literal component, transformed into a call to the corresponding data constructor. Functions cps-of-vector, cps-of-hash-map, cps-of-set, called from cps-of-expression, transform Clojure constructor syntax ([...], {...}, #{...}) into the corresponding calls:

```
=> (cps-of-vector [0 1 2] 'cont)
(cont (vector 0 1 2) $state)
=> (cps-of-hash-map {:a 1 :b 2} 'cont)
(cont (hash-map :a 1, :b 2) $state)
=> (cps-of-set #{0 1} 'cont)
(cont (set (list 0 1)) $state)
```

4.2.2 Opaque Expressions

Opaque, or value, expressions, have a different shape in the original and the CPS form. However, their CPS form follows the pattern (continuation transformed-expression), and thus the transformation does not depend on the continuation, and can be accomplished without passing the continuation as a transformation argument. Primitive (non-CPS) procedures used in Anglican code, (fn ...) forms, and (mem ...) forms are opaque and transformed by primitive-procedure-cps, fn-cps, and mem-cps, correspondingly: a slightly simplified CPS form of expression

```
(fn [x y]
  (+ x y))
```

would be

```
(fn [cont $state x y]
  (cont (+ x y) $state))
```

In the actual code an automatically generated fresh symbol is used instead of cont.

4.2.3 General Expressions

The most general form of CPS transformation receives an expression and a continuation, and returns the expression in CPS form with the continuation potentially called in multiple tail positions. General expressions can be somewhat voluntarily divided into several groups:

- binding forms — let and loop/recur;

- flow control — if, when, cond, case, and, or and do;

- function applications and apply;

- probabilistic forms — predict, observe, sample, store, and retrieve.

Functions that transform general expressions accept the expression and the continuation as parameters, and are consistently named cps-of-*form*, for example, cps-of-do, cps-of-store.

4.3 Implementation Highlights

So far we introduced the basics of Anglican compilation to Clojure. The described approaches and techniques are important for grasping the language implementation but relatively well-known. In the rest of the section we focus on challenges we met and resolved while implementing Anglican, as well as on implementation of unique features of Anglican as a probabilistic programming language.

4.3.1 Continuations

Continuations are functions that are called in tail positions with the computed value and state as their arguments — in CPS there is always a function call in every tail position and never a value. Continuations are passed to CPS transformers, and when transformers are called recursively, the continuations are generated on the fly.

There are two critical issues related to generation of continuations:

- unbounded *stack growth* in recursive code;

- code size *explosion* when a non-atomic continuation is symbolically substituted in multiple locations.

Managing stack size In implementations of functional programming languages stack growth is avoided through *tail call optimization* (TCO). However, Clojure does not support a general form of TCO, and CPS-transformed code that creates deeply nested calls will easily exhaust the stack. Anglican employs a workaround called *trampolining* — instead of inserting a continuation call directly, the transformer always wraps the call into a *thunk*, or parameterless function. The thunk is returned and called by the trampoline (Clojure provides function trampoline for this purpose) — this

way the computation continues, but the stack is collapsed on every continuation call. Function `continue` implements the wrapping and is invoked on every continuation call:

```
=> (continue 'cont 'value 'state)
(fn [] (cont value state))
```

Correspondingly, the full, wrapped CPS form of

```
(fn [x y] (+ x y))
```

becomes

```
(fn [cont $state x y]
  (fn []
    (cont (+ x y) $state)))
```

When the CPS-transformed function is called, it returns a *thunk* (a parameterless function) which is then re-invoked through the trampoline, with the stack collapsed.

Avoiding exponential code growth To realize potential danger of code size explosion, consider CPS transformation of code

```
(if (adult? person)
  (if (male? person)
      (choose-beer)
      (choose-wine))
  (choose-juice))
```

with continuation

```
(fn [choice _]
  (case (kind choice)
    :beer (beer-jar choice)
    :wine (wine-glass choice)
    :juice (juice-bottle choice)))
```

The code of the continuation, represented by the `fn` form, will be repeated three times. In general, CPS code can grow extremely large if symbolic continuations are inserted repeatedly.

To circumvent this inefficiency, CPS transformers for expressions with multiple continuation points (`if` and derivatives, `and`, `or`, and `case`) bind the continuation to a fresh symbol if it is not yet a symbol. Macro `defn-with-named-cont` establishes the binding automatically:

```
=> (cps-of-if '(c t f) '(fn [x] (* 2 x)))
(let [cont (fn [x] (* 2 x))]
  (if c
      (fn [] (cont t $state))
      (fn [] (cont f $state))))
```

4.3.2 Primitive Procedures

When an Anglican function is transformed into a Clojure function by `fn-cps`, two auxiliary parameters are added to the beginning of the parameter list — continuation and state. Correspondingly, when a function *call* is transformed (by `cps-of-application` or `cps-of-apply`), the current continuation and the state are passed to the called function. Anglican can also call Clojure functions; however Clojure functions do not expect these auxiliary parameters. To allow the mixing of Anglican (CPS-transformed) and Clojure function calls in Anglican code, the Anglican compiler must be able to recognize 'primitive' (that is, implemented in Clojure rather than in Anglican) functions.

Providing an explicit syntax for differentiating between Anglican and Clojure function calls would be cumbersome. Another option would be to use meta-data to identify Anglican function calls at runtime, however this would impact performance, and a good runtime performance is critical for probabilistic programs. The approach taken by Anglican is to maintain a list of unqualified names of primitive functions, as well as namespaces in which all functions are primitive, and recognize primitive functions by name — if a function name is not in the list, the function is an Anglican function. Global dynamically bound variables `*primitive-procedures*` and `*primitive-namespaces*` contain the initial lists of names and namespaces, correspondingly. Of course, local bindings can shade global primitive function names. For example, `first` is an Anglican function inside the let block in the following example:

```
(let [first (fn [[x & y]] x)]
  (first '[1 2 3]))
```

The Anglican compiler takes care of the shading by rebinding `*primitive-procedures*` in every lexical scope (fn-cps, cps-of-let). Macro `shading-primitive-procedures` automates the shading.

4.3.3 Probabilistic forms

There are two proper probabilistic forms turning Anglican into a probabilistic programming language — `sample` and `observe`. Their purpose is to interrupt deterministic computation and transfer control to the inference algorithm. Practically, this is achieved through returning **checkpoints** — Clojure values of the corresponding types (`anglican.trap.sample` or `anglican.trap.observe`). The types contain fields specific to each form, as well as the continuation; calling the continuation resumes the computation. Checkpoints expose the program state to the inference algorithm, and the updated state is re-injected into the computation when the continuation is called:

```
=> (cps-of-expression '(sample dist) 'cont)
(->sample dist cont $state)
=> (cps-of-expression '(observe dist val) 'cont)
(->observe dist val cont $state)
```

In addition to checkpoints, there are a few other special forms — `predict`, `store`, `retrieve`, `mem` — which modify program state. These forms are translated into expressions involving calls of functions from the `anglican.state` namespace. The `mem` form, which implements memoization, deserves a more detailed explanation.

Memoization The author of a probabilistic model might want to draw a feature of an entity randomly, but to retain the same drawn value for the same entity during a single run of the probabilistic program. For example, a person may have brown or green eyes with some probability, but the *same* person will always have the same eye color. This can be achieved memoized functions. In Anglican, one might write:

```
(let [eye-color (mem (fn [person]
                       (sample
                         (categorical
                           ['brown 0.5]
                           ['green 0.5]))))]
  (if (not= (eye-color 'bill) (eye-color 'john))
    (predict (eye-color 'bill))
    (predict (eye-color 'john))))
```

Memoization is often implemented on top of a mutable dictionary, where the key is the argument list and the value is the returned value. However, there are no mutable data structures in a probabilistic program, hence `mem`'s memory is stored as a nested dictionary in the program state (function

mem-cps). Every memoized function gets a unique automatically generated identifier. Each time a memoized function is called, one of two continuations is chosen, depending on whether the same function (a function with the same identifier) was previously called in the same run of the probabilistic program with the same arguments. If the memoized result is available, the continuation of the memoized function call is immediately called with the stored result. Otherwise, the argument of `mem` is called with a continuation which first creates an updated state with the memoized result, and then calls the 'outer' continuation with the result and the updated state:

```
=> (mem-cps '(foo))
(let [M (gensym "M")]
  (fn mem23623 [C $state & P]
    (if (in-mem? $state M P)
      ;; previously memoized result
      (fn []
        (C (get-mem $state M P) $state))
      ;; new computation
      (clojure.core/apply
        foo
        ;; memoize result in continuation
        (fn [V $state]
          (fn [] (C V (set-mem $state M P V))))
        $state
        P)))))
```

Memoized results are not shared among multiple runs of a probabilistic program, which is intended. Otherwise, it would be impossible to memoize functions with random results.

5.   Inference Algorithms

An inference algorithm is an implementation of the (ad-hoc) polymorphic function `infer` declared as Clojure's multimethod in the `anglican.inference` namespace. The function accepts an algorithm identifier, a query — the probabilistic program in which to perform the inference, an initial value for the query, and optional algorithm parameters.

5.1   The `infer` function

The sole purpose of the algorithm identifier of `infer` is to invoke an appropriate overloading or implementation of the function — conventionally, the identifier is a keyword related to the algorithm name (`:lmh` for Lightweight Metropolis-Hasting, `:pcascade` for Particle Cascade etc.). The second parameter is a query as defined by the `defquery` form or its anonymous version `query`. For instance, the following Clojure code invokes `infer` on an Anglican query defined anonymously via the `query` form:

```
(let [x 1]
  (infer :pgibbs (query (predict x)) nil))
```

A query is executed by calling the initial continuation of the query, which accepts a value and a state. The state is supplied by the inference algorithm, while the value is provided as a parameter of `infer`. A query does not have to have any parameters, in which case the value can be simply `nil`. When a query is defined with a binding for the initial value, the value becomes available inside the query. A query may accept multiple parameters using Clojure's structured binding. For instance, it may take multiple parameters as components of an input vector. In this case, the initial value is given as a structured value, such as a vector, and the components of this value gets pattern matched to the

corresponding parameters of the query via the destructuring mechanism of Clojure. For example,

```
(defquery my-query [mean sd]
  (predict (sample (normal mean sd))))

(def samples (infer :lmh my-query [1.0 3.0]))
```

Finally, any number of auxiliary arguments can be passed to `infer`. By convention, the arguments should be keyword arguments, and are interpreted in the algorithm-specific manner.

5.2   Internals of an inference algorithm

The simplest inference algorithm is *importance sampling*:

```
(derive ::algorithm
        :anglican.inference/algorithm)
(defmethod infer :importance [_ prog value & {}]
  (letfn
    [(sample-seq []
       (lazy-seq
         (cons
           (:state (exec ::algorithm prog value
                         initial-state))
           (sample-seq))))]
    (sample-seq)))
```

`anglican.importance/infer` just calls `anglican.inference/exec` and relies on default implementations of checkpoint handlers. A different inference algorithm would provide its own implementations of `checkpoint` for `sample`, `observe`, or both, as well as invoke `exec` from an elaborated conditional control flow. LMH (`anglican.lmh`) and SMC (`anglican.smc`) are examples of inference algorithms where either `observe` (SMC) or `sample` (LMH) handler is overridden. In addition, SMC runs multiple particles (program instances) simultaneously, while LMH re-runs programs from an intermediate continuation rather than from the beginning.

> **HY:** This subsection is also not quite self-contained. Someone who is not familiar with Clojure or Anglican codebase is likely to get lost. On the other hand, it is a good overview or guide for those who want to study the implemenation of Anglican. One way to address this presentation issue while keeping the benefits of the current text is to include some extended examples. For instance, in the beginning of the paper, we might include several Anglican examples. Then, we show that how these examples get cps-transformed. Next, we present the implementation of inference algorithms in Anglican using semi pseudo code; this is not quite an implementation in Clojure but gives a good sketch on how various functions are implemented in each inference algorithm. Finally, we show how these algorithms work on cps-tranformed examples.

6.   Definitions and Runtime Library

A Clojure namespace that includes a definition of an Anglican program imports ('requires') two essential namespaces: `anglican.emit` and `anglican.runtime`. The former provides macros for defining Anglican programs (`defquery`, `query`) and functions (`defm`, `fm`, `mem`), as well as Anglican bootstrap definitions that must be included with every program — first of all, CPS implementations of higher-order functions. `anglican.emit` can be viewed as the Anglican *compiler tool*, which helps transform Anglican code into Clojure before any inference is performed.

`anglican.runtime` is the Anglican runtime library. For convenience, it exposes common mathematical functions

(abs, `floor`, `sin`, `log`, `exp`, etc.), but most importantly, it provides definitions of common distributions. Each distribution object implements the `anglican.runtime/distribution` protocol, with two methods: `sample*` and `observe*`. The `sample*` *method* returns a random sample and roughly corresponds to the `sample` checkpoint, the `observe*` *method* returns the log probability of the value and roughly corresponds to the `observe` checkpoint. The methods can be, and sometimes are called from handlers of the corresponding checkpoints, but do not have to be. For example, in LMH either the `sample*` or the `observe*` *method* is called for a `sample` checkpoint, depending on whether the value is drawn or re-used.

Macro `defdist` should be used to define distributions. `defdist` takes care of defining a separate type for every distribution so that multimethods can be dispatched on distribution types when needed, e.g. for custom proposals. The Bernoulli distribution could be defined as follows:

```
(defdist bernoulli
  "Bernoulli distribution"
  [p]
  (sample* [this] (if (< (rand) p) 1 0))
  (observe* [this value]
    (Math/log (case value
                1 p
                0 (- 1. p)
                0.)))))
```

Similar to distributions, *random processes*, related to so called 'exchangeable random procedures'[3], are defined using macro `defproc` and implement the `anglican.runtime/random-process` protocol. The protocol has two methods — `produce`, which returns a distribution object, and `absorb`, which returns a new random process object obtained by absorbing a value drawn from the process. Here is a definition of the Poisson process:

```
(defproc PP
  "Poisson point process"
  [rate] [dist (exponential rate)]
  (produce [this] dist)
  (absorb [this value] this))
```

While distributions are random and non-functional, random processes are deterministic and functional, hence `produce` and `absorb` are called directly and do not have corresponding special forms in Anglican:

- Values produced by the process are sampled from the distribution returned by `produce`.

- When a value is observed from the distribution, a new process, with the observed value absorbed, is returned by `absorb`.

A common pattern of programming with processes in Anglican is recursively computing a new process based on the observed value:

```
(loop [process (HawkesPointProcess)
       [value & values] values]
  (let [dist (produce process)]
    (observe dist value)
    (recur (absorb process value) values)))
```

Unlike conventional implementations of random processes, Anglican's random processes do not have mutable state.

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[3] However, random sequences generated by Anglican random processes are not required to be exchangeable.

7. Summary

In this paper, we presented design and implementation internals of the *probabilistic programming system* Anglican. Implementing a language is an interesting endeavour, in particular when the language implements a new paradigm, in this case probabilistic programming. Functional programming is a natural complement of probabilistic programming — the latter allows both concise and expressive specification of probabilistic generative models and efficient implementation of inference algorithm.

Implementing a probabilistic language on top and in tight integration with a functional language, Clojure, both helped us to accomplish an ambitious goal in a short time span, and provided important insights on structure and semantics of probabilistic concepts incorporated in Anglican. Efficiency and expressive power of Anglican owe to adherence to the functional approach as much as to rich inference opportunities of the Anglican environment.

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