$\tilde{\mathbf{x}}_{1:n} = \tilde{\mathbf{x}}_1 \times \cdots \times \tilde{\mathbf{x}}_n$