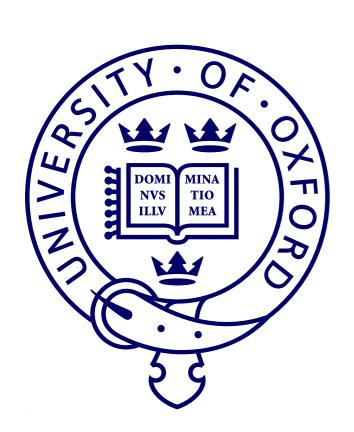
Introduction to Functional Programming and Clojure

Jan-Willem van de Meent





```
(ns examples.factorial
  (:gen-class))
(defn factorial
  "computes n * (n-1) * ... * 1"
  [n]
  (if (= n 1)
    (* n (factorial (- n 1)))))
(defn -main
  [& args]
  (doseq [arg args]
    (let [n (Long/parseLong arg)]
      (println "the factorial of" arg
               "is" (factorial n)))))
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Namespace declaration

```
(ns examples.factorial
  (:gen-class))

(defn factorial
  "computes n * (n-1) * ... * 1"
  [n]
  (if (= n 1)
        1
        (* n (factorial (- n 1)))))
```

Recursive function

```
(defn factorial
  "computes n * (n-1) * ... * 1"
  [n]
  (if (= n 1)
    (* n (factorial (- n 1)))))
(defn -main
  [& args]
  (doseq [arg args]
    (let [n (Long/parseLong arg)]
      (println "the factorial of" arg
               "is" (factorial n)))))
```

(ns examples.factorial

(:gen-class))

Main function

```
# get source code for this tutorial
git clone git@bitbucket.org:probprog/ppaml-summer-school-2016.git
cd ppaml-summer-school-2016/exercises/
# option 1: compile to jar and run via java
lein uberjar
java -cp target/uberjar/exercises-0.1.0-SNAPSHOT-standalone.jar \
  examples.factorial 1 2 5 20
# option 2: run using leiningen
lein run -m examples.factorial 1 2 5 20
# => the factorial of 1 is 1
# => the factorial of 2 is 2
# => the factorial of 5 is 120
# => the factorial of 20 is 2432902008176640000
```

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# option 2: run using leiningen
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examples.factorial 1 2 5 20

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# => the factorial of 20 is 2432902008176640000
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option 2: run using leiningen

lein run -m examples.factorial 1 2 5 20

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# => the factorial of 1 is 1
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# => the factorial of 5 is 120
# => the factorial of 20 is 2432902008176640000
```

Interactive Shell: the REPL

```
$ lein repl
# => nREPL server started on port 50240 on host
     127.0.0.1 - nrepl://127.0.0.1:50240
\# => REPL-y 0.3.7, nREPL 0.2.12
# => Clojure 1.8.0
# => Java HotSpot(TM) 64-Bit Server VM 1.8.0-b132
         Docs: (doc function-name-here)
# =>
# =>
                (find-doc "part-of-name-here")
# => Source: (source function-name-here)
# => Javadoc: (javadoc java-object-or-class-here)
# =>
          Exit: Control+D or (exit) or (quit)
# => Results: Stored in vars *1, *2, *3,
                an exception in *e
```

examples.core=>

Interactive Shell: the REPL

```
examples.core=> (require 'examples.factorial)
;; => nil
examples.core=> (ns examples.factorial)
;; => #object[clojure.lang.Namespace 0x42cd2abe
"examples.factorial"]
examples.factorial=> (-main "1" "2" "5" "20")
;; => the factorial of 1 is 1
;; => the factorial of 2 is 2
;; => the factorial of 5 is 120
;; => the factorial of 20 is 2432902008176640000
;; => nil
```

Gorilla REPL

\$ lein gorilla

```
Gorilla REPL - exercises
                                                                          C Reader
4 > 1 127.0.0.1:62175/worksheet.html
m !!!!
                (ns hello-world
                  (:require [examples.factorial]))
                nil
                (examples.factorial/-main "1" "2" "5" "10")
                the factorial of 1 is 1
                the factorial of 2 is 2
                the factorial of 5 is 120
                the factorial of 10 is 3628800
                 nil
```

```
(ns examples.factorial
  (:gen-class))
(defn factorial
  "computes n * (n-1) * ... * 1"
  [n]
  (if (= n 1)
    (* n (factorial (- n 1)))))
(defn -main
  [& args]
  (doseq [arg args]
    (let [n (Long/parseLong arg)]
      (println "the factorial of" arg
               "is" (factorial n))))
```

```
(defn factorial
  "computes n * (n-1) * ... * 1"
  [n]
  (if (= n 1)
    (* n (factorial (- n 1)))))
def factorial(n):
    '''computes n * (n - 1) * ... * 1'''
    if n == 1:
        return 1
    else:
        return n * factorial(n - 1)
```

```
Name
(defn factorial
  "computes n * (n-1) * ... * 1"
  [n]
  (if (= n 1)
    (* n (factorial (- n 1)))))
def factorial(n):
    '''computes n * (n - 1) * ... * 1'''
    if n == 1:
        return 1
    else:
        return n * factorial(n - 1)
```

```
(defn factorial
                                             Docstring
  "computes n * (n-1) * ... * 1"
  [n]
  (if (= n 1)
    (* n (factorial (- n 1)))))
def factorial(n):
    '''computes n * (n - 1) * ... * 1'''
    if n == 1:
        return 1
    else:
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```
(defn factorial
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def factorial(n):
    '''computes n * (n - 1) * ... * 1'''
    if n == 1:
        return 1
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```

Arguments

```
"computes n * (n-1) * ... * 1"
  [n]
  (if (= n 1)
    (* n (factorial (- n 1))))
def factorial(n):
    '''computes n * (n - 1) * ... * 1'''
    if n == 1:
        return 1
    else:
        return n * factorial(n - 1)
```

(defn factorial

Function body

```
(defn factorial
  "computes n * (n-1) * ... * 1"
  [n]
  (if (= n 1)
                                            S-expression
    (* n (factorial (- n 1))))
def factorial(n):
    '''computes n * (n - 1) * ... * 1'''
    if n == 1:
                                            Block
        return 1
                                            statement
    else:
        return n * factorial(n - 1)
```

```
(defn factorial
  "computes n * (n-1) * ... * 1"
  [n]
  (if (= n 1)
        1
        (* n (factorial (- n 1)))))
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(defn factorial
  "computes n * (n-1) * ... * 1"
  [n]
  (if (= n 1)
      1
      (* n (factorial (- n 1)))))
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  [n]
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     1
     (* n (factorial (- n 1)))))
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expression ::= symbol | literal | (operator ...)
```

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expression ::= symbol | literal | (operator ...)
  operator ::= special | function | macro
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Anatomy of an Expression

```
(defn factorial
  "computes n * (n-1) * ... * 1"
  [n]
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expression ::= symbol | literal | (operator ...)
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Anatomy of an Expression

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(defn factorial
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expression ::= symbol | literal | (operator ...)
 operator ::= special | function | macro
   special ::= def | if | fn | let | loop | recur |
               do | new | . | throw | set! | quote | var
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Anatomy of an Expression

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(defn factorial
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expression ::= symbol | literal | (operator ...)
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               do | new | . | throw | set! | quote | var
```

Atomic

```
;; symbols
(symbol "ada"), ada
;; keywords
:ada
;; integers, doubles, ratios
1234, 1.234, 12/34
;; strings, characters
"ada", \a \d \a
;; booleans, null
true, false, nil
;; regular expressions
#"a*b"
```

```
;; lists
(list 1 2 3), (1 2 3)
;; hash maps
{:a 1 :b 2}
;; vectors
[1 2 3]
;; sets
#{1 2 3}
;; everything nests
{:a [[1 2] [3 4]]
 :b #{5 6 (list 7 8)}
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Atomic

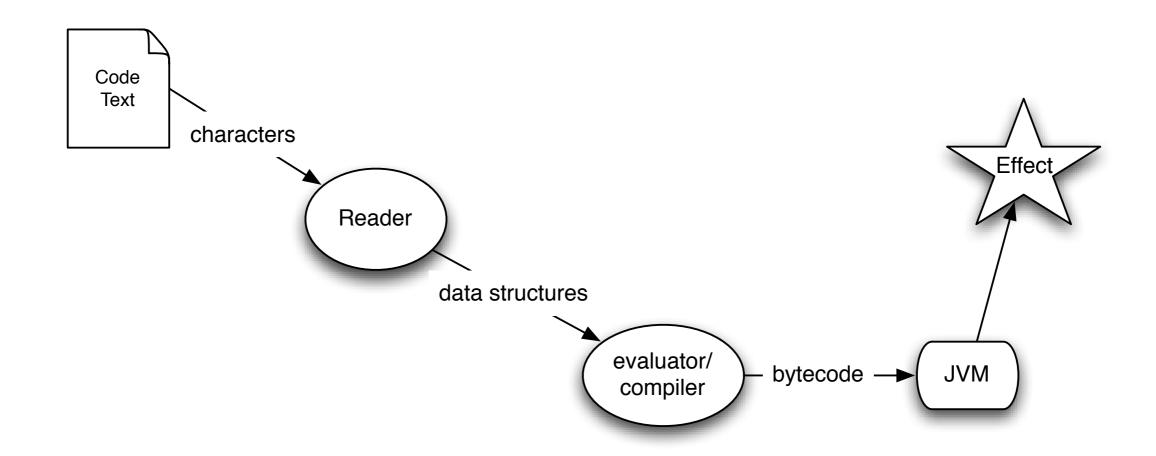
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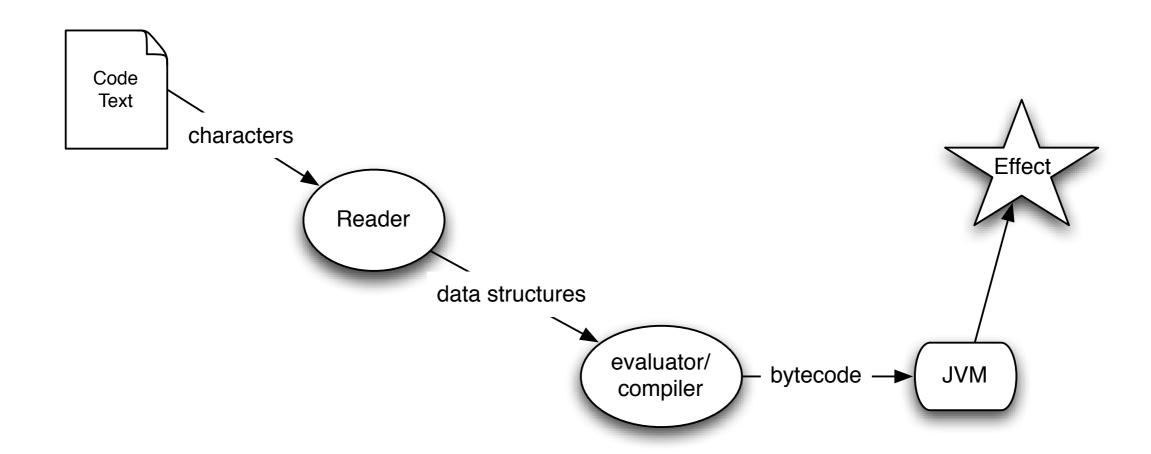
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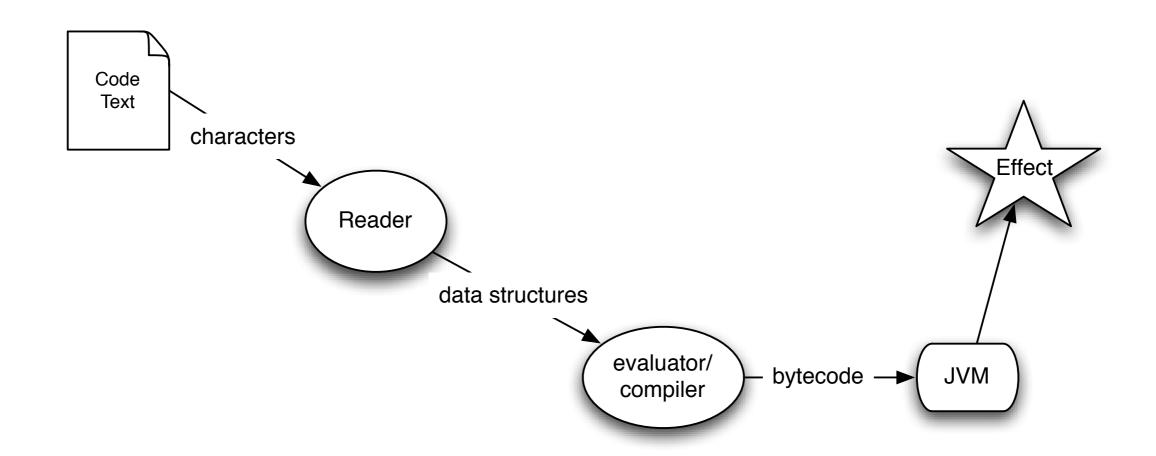
```
;; lists
(list 1 2 3), (1 2 3)
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{:a 1 :b 2}
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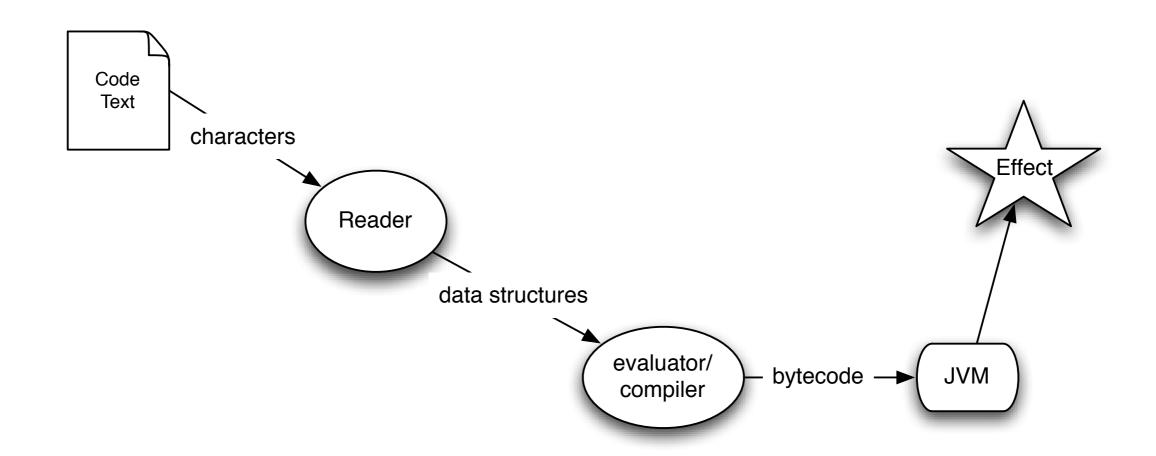
```
(let [expr (read-string "(+ 1 2)")]
  (prn expr); => (+ 1 2)
  (prn (class expr)); => clojure.lang.Persistentlist
  (prn (class (first expr))); => clojure.lang.Symbol
  (eval expr)); => 3
```



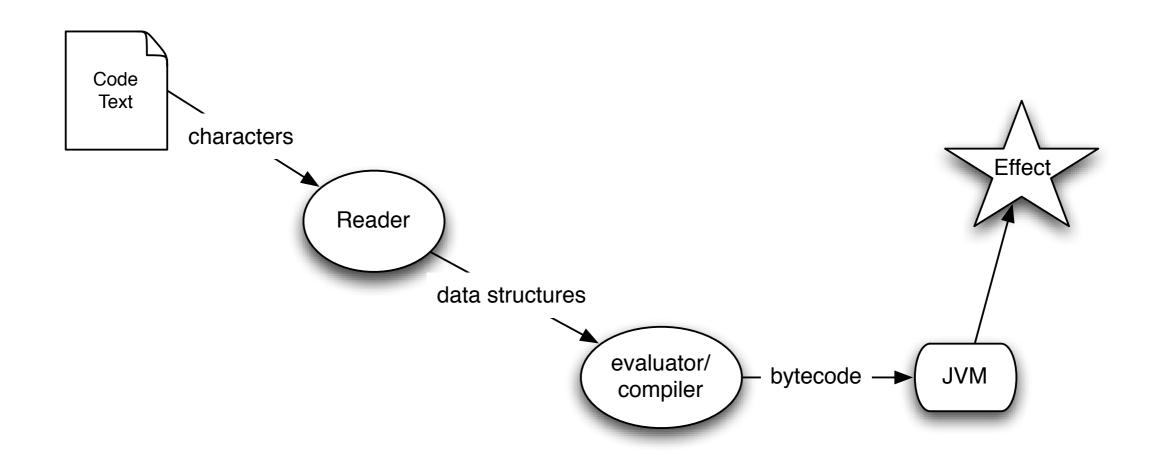
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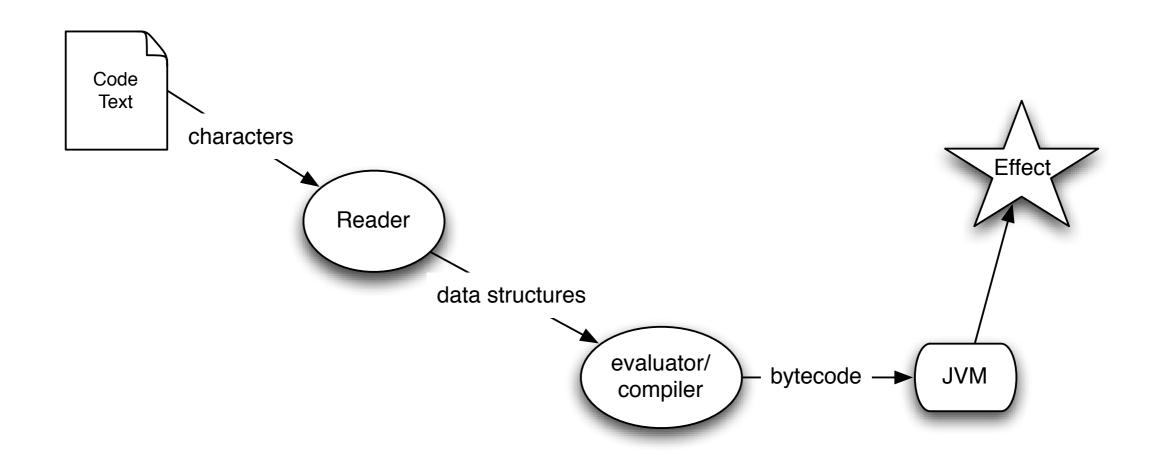
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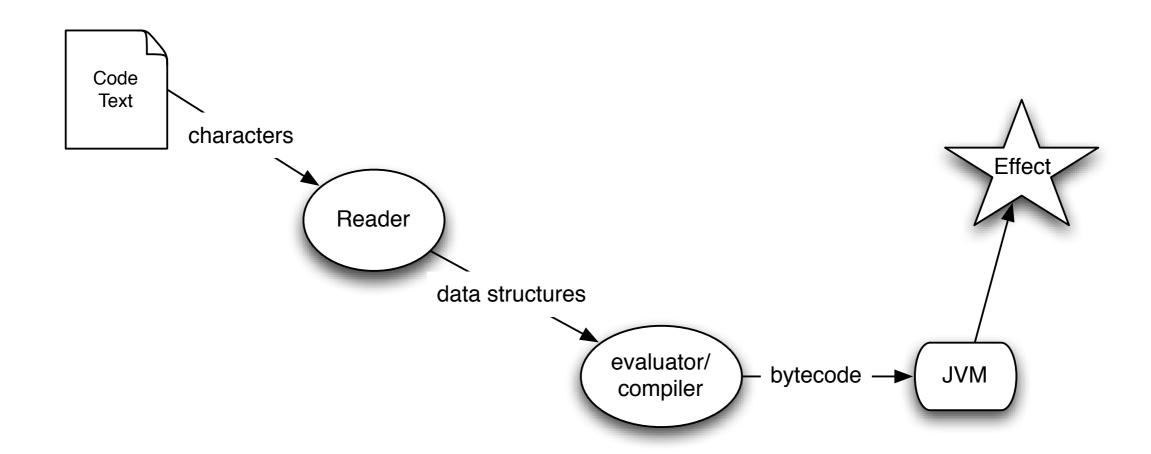
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```



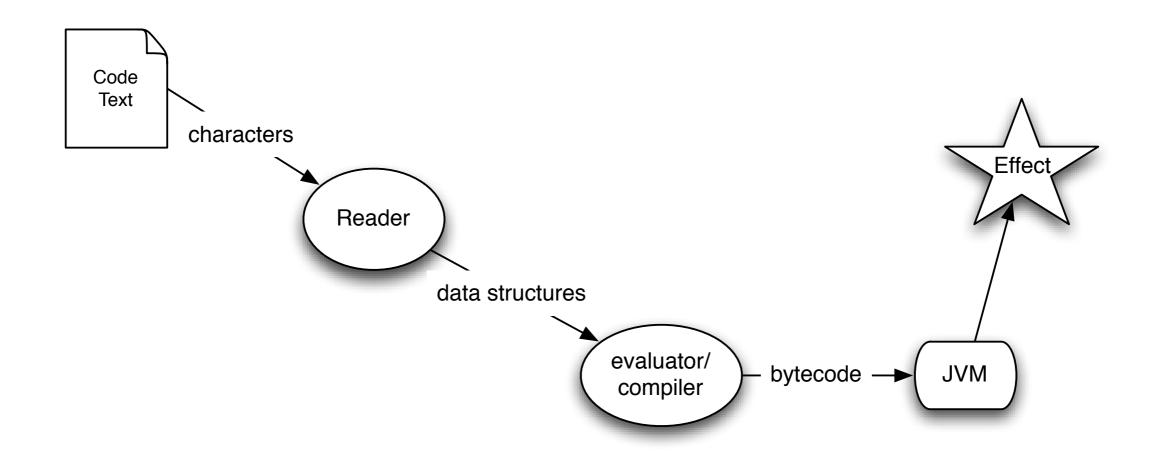
```
(let [expr (read-string "(+ 1 2)")]
  (prn expr); => (+ 1 2)
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```



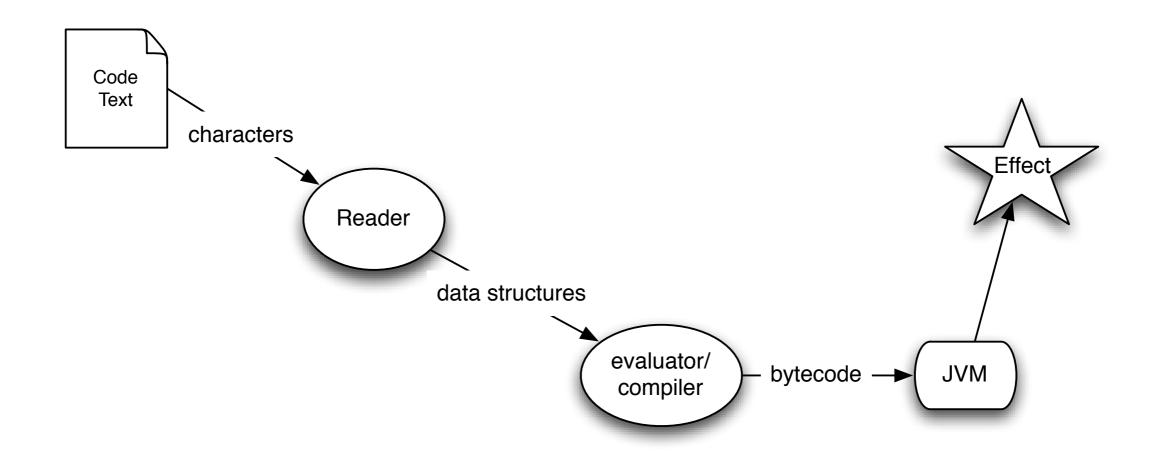
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(let [expr (read-string "(+ 1 2)")]
  (prn expr); => (+ 1 2)
  (prn (class expr)); => clojure.lang.Persistentlist
  (prn (class (first expr))); => clojure.lang.Symbol
  (eval expr)); => 3
```



```
(let [expr (quote (+ 1 2))]
  (prn expr); => (+ 1 2)
  (prn (class expr)); => clojure.lang.Persistentlist
  (prn (class (first expr))); => clojure.lang.Symbol
  (eval expr)); => 6
```



```
(let [expr '(+ 1 2)]
  (prn expr); => (+ 1 2)
  (prn (class expr)); => clojure.lang.Persistentlist
  (prn (class (first expr))); => clojure.lang.Symbol
  (eval expr)); => 6
```

Macros

```
(def flavor :tasty)
                                 (unless (= flavor :tasty)
                                   :yuk
(defmacro unless
                                   :yum)
 "Inverted 'if"
  [pred then else]
                                 ; ~> (macro-expansion)
 (list 'if pred else then))
                                 (if (= flavor :tasty)
                                   :yum
                                   :yuk)
                                 ; => (evaluation)
                                 :yum
```

Macros

```
(defmacro dbg
 "Prints an expression and ; => [dbg] (+ 1 2) 3
 its value for debugging."
 [expr]
 `(let [value# ~expr]
    (println "[dbg]"
              '~expr
             value#)
    value#))
```

```
(dbg (+ 1 2))
; => 3
(macroexpand '(dbg (+ 1 2))
; => (let* [value__23707__auto__
            (+12)]
 (clojure.core/println
       "[dbg]"
        (quote (+ 1 2))
        value 23707 auto )
      value__23707__auto__)
```

Method Dispatch

Collections

```
(count (list 1 2 3))
; => 3
(count [1 2 3 4 5]))
; => 5
(count {:a 1, :b 2})
; = > 2
(conj (list 1 2 3) 0)
; => (0 1 2 3)
(conj [1 2 3] 4)
(conj {:a 1, :b 2} [:c 3])
; => \{:a \ 1 :b \ 2 :c \ 3\}
```

Sequences

```
(seq [1 2 3])
    ; => (1 2 3)
  (seq {:a 1, :b 2})
    ; => ([:a 1] [:b 2])
    (seq (list))
    ; => nil
    (first [1 2 3])
    ; => 1
    (rest [1 2 3])
    ; => (2 3)
(cons 0 [1 2 3])
    ; => (0 1 2 3)
```

Method Dispatch

Associative

(vectors, maps)

```
(get {:a 1 :b 2} :a)
; => 1
(get ["a" "b"] 0)
; => "a"

(assoc {:a 1 :b 2} :c 3)
; => {:a 1 :b 2 :c 3}
(assoc ["a" "b"] 2 "c")
; => ["a" "b" "c"]
```

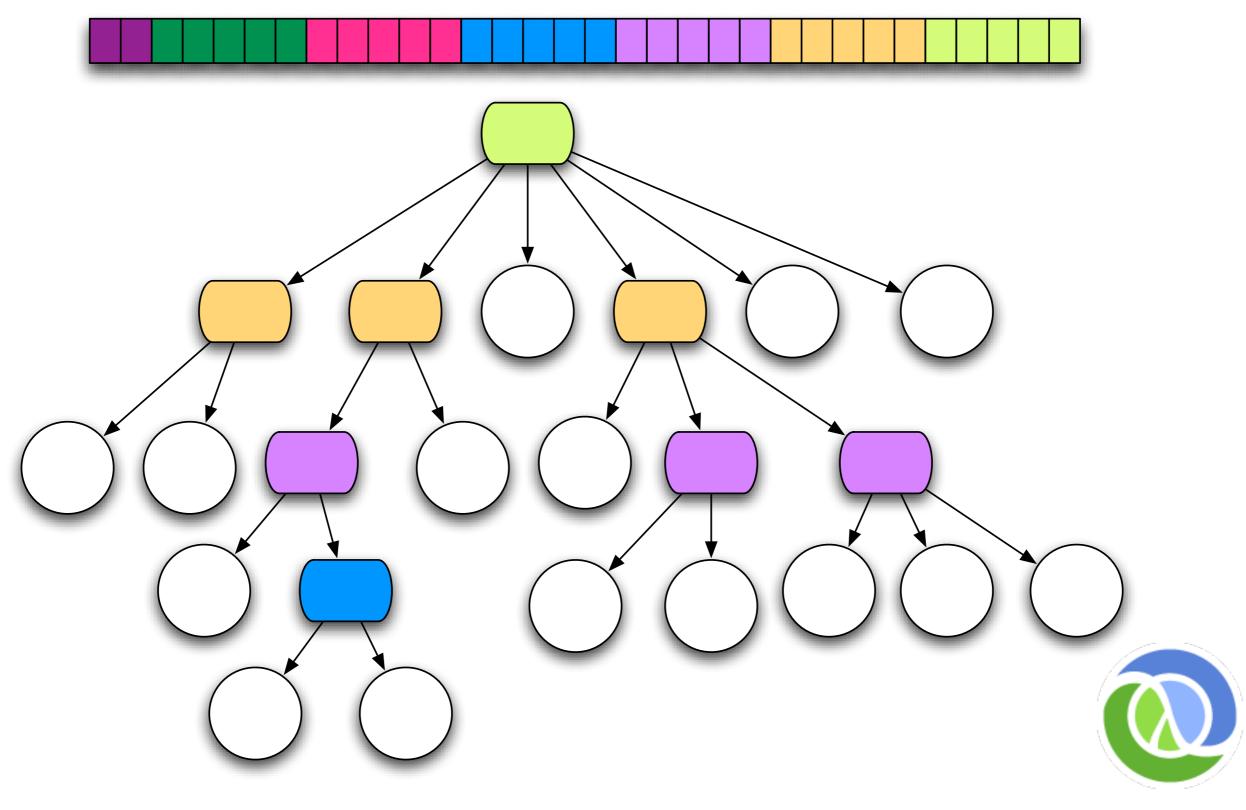
Stacks

(lists, vectors)

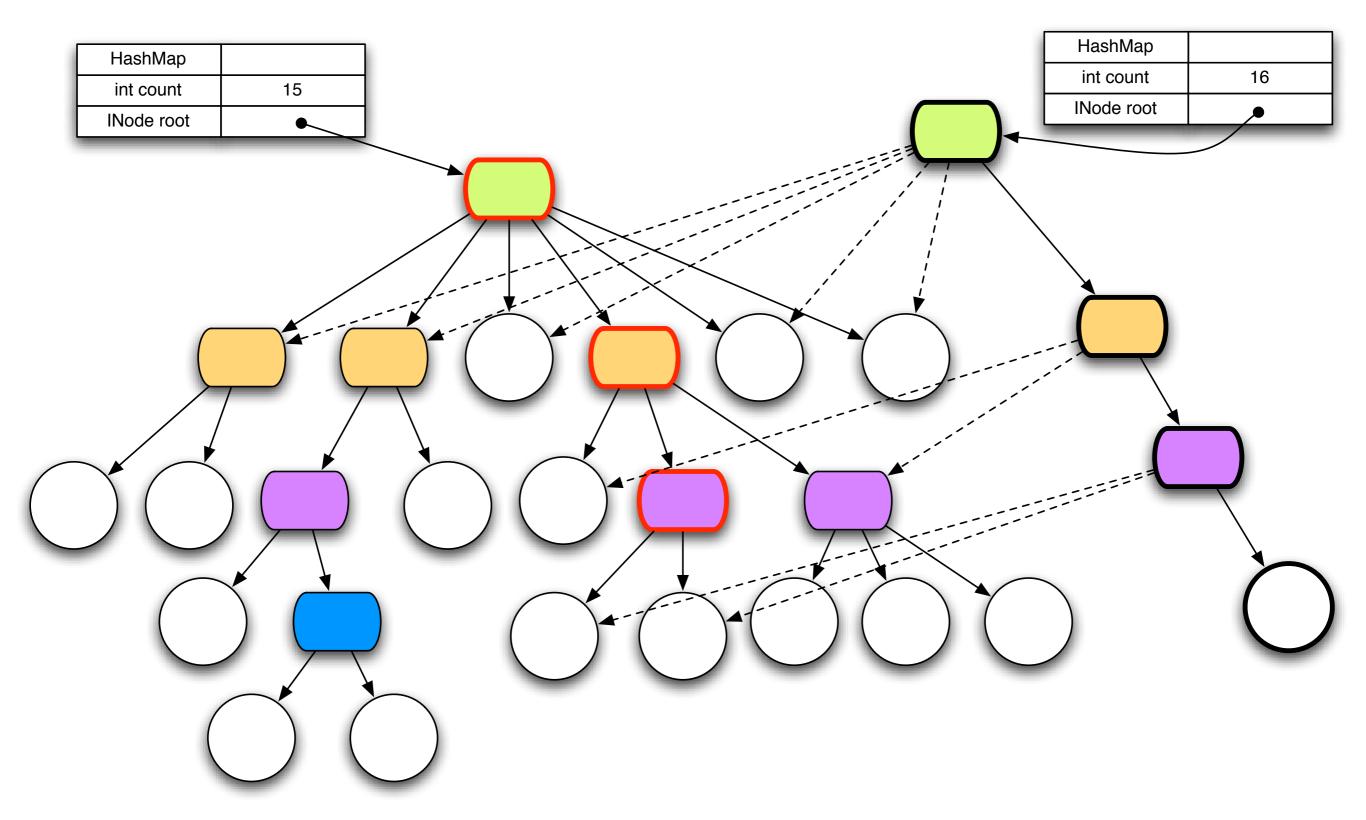
```
(peek (list 1 2 3))
; => 1
(peek [1 2 3])
; => 3

(pop (list 1 2 3))
; => (list 2 3)
(pop [1 2 3])
; => [1 2]
```

Bit-partitioned Hash Tries



Path Copying



```
(defn factorial
  "computes n * (n-1) * ... * 1"
  [n]
  (if (= n 1)
        1
        (* n (factorial (- n 1)))))
```

```
(defn factorial
  "computes n * (n-1) * ... * 1"
  [n]
  (if (= n 1)
    (* n (factorial (- n 1)))))
(factorial 21)
; => ArithmeticException integer overflow
     clojure.lang.Numbers.throwIntOverflow (Numbers.java:1501)
```

```
(defn factorial
  "computes n * (n-1) * ... * 1"
  [n]
  (if (= n 1)
    1N
    (* n (factorial (- n 1)))))
(factorial 21)
; => ArithmeticException integer overflow
     clojure.lang.Numbers.throwIntOverflow (Numbers.java:1501)
```

(defn factorial

```
(defn factorial
  "computes n * (n-1) * ... * 1"
  [n]
  (if (= n 1)
    (*' n (factorial (- n 1)))))
(factorial 10000)
; => StackOverflowError
     clojure.lang.Numbers.equal (Numbers.java:216)
```

```
(defn factorial
  "computes n * (n-1) * ... * 1"
  [n]
  (if (= n 1)
    (*' n (factorial (- n 1)))))
def factorial(n):
    '''computes n * (n - 1) * ... * 1'''
    if n == 1:
        return 1
    else:
        return n * factorial(n - 1)
```

```
(defn factorial
  "computes n * (n-1) * ... * 1"
  [n]
  (if (= n 1))
    (*' n (factorial (- n 1)))))
def factorial(n):
    '''computes n * (n - 1) * ... * 1'''
    result = 1
    for i in range(2, n + 1):
        result *= i
    return result
```

```
(defn factorial
  "computes n * (n-1) * ... * 1"
  [n]
  (if (= n 1))
    (*' n (factorial (- n 1)))))
def factorial(n):
    '''computes n * (n - 1) * ... * 1'''
    result = 1
    ivals = range(2, n + 1)
    while ivals:
        i = ivals.pop(0)
        result *= i
    return result
```

```
(defn factorial [n]
  "computes n * (n-1) * ... * 1"
  (loop [result 1
         ivals (range 2 (+ n 1))]
    (if (seq ivals)
      (recur (*' result (first ivals))
             (rest ivals))
      result)))
def factorial(n):
    '''computes n * (n - 1) * ... * 1'''
    result = 1
    ivals = range(2, n + 1)
    while ivals:
        i = ivals.pop(0)
        result *= i
    return result
```

```
(defn factorial [n]
  "computes n * (n-1) * ... * 1"
  (loop [result 1
         ivals (range 2 (+ n 1))]
    (if (seq ivals)
      (recur (*' result (first ivals))
             (rest ivals))
      result)))
def factorial(n):
    '''computes n * (n - 1) * ... * 1'''
    result = 1
    ivals = range(2, n + 1)
    while ivals:
        i = ivals.pop(0)
        result *= i
    return result
```

```
(defn factorial [n]
  "computes n * (n-1) * ... * 1"
                                            Initial values
  (loop [result 1
         ivals (range 2 (+ n 1))]
    (if (seq ivals)
      (recur (*' result (first ivals))
             (rest ivals))
      result)))
def factorial(n):
    '''computes n * (n - 1) * ... * 1'''
    result = 1
    ivals = range(2, n + 1)
    while ivals:
        i = ivals.pop(0)
        result *= i
    return result
```

```
(defn factorial [n]
  "computes n * (n-1) * ... * 1"
  (loop [result 1
         ivals (range 2 (+ n 1))]
                                           Any values
    (if (seq ivals)
      (recur (*' result (first ivals))
                                           for i remaining?
             (rest ivals))
      result)))
def factorial(n):
    '''computes n * (n - 1) * ... * 1'''
    result = 1
    ivals = range(2, n + 1)
    while ivals:
        i = ivals.pop(0)
        result *= i
    return result
```

```
(defn factorial [n]
  "computes n * (n-1) * ... * 1"
  (loop [result 1
         ivals (range 2 (+ n 1))]
    (if (seq ivals)
      (recur (*' result (first ivals))
             (rest ivals))
      result)))
def factorial(n):
    '''computes n * (n - 1) * ... * 1'''
    result = 1
    ivals = range(2, n + 1)
    while ivals:
        i = ivals.pop(0)
        result *= i
    return result
```

Compute values for next iteration

```
(defn factorial [n]
 "computes n * (n-1) * ... * 1"
 (loop [result 1 ◀
       (if (seq ivals)
     (recur (*' result (first ivals))... Passed by value
           (rest ivals))
                                    to next iteration
     result)))
def factorial(n):
   '''computes n * (n - 1) * ... * 1'''
   result = 1
   ivals = range(2, n + 1)
   while ivals:
      i = ivals.pop(0)
                                    Mutated in place
      result *= i
   return result
```

```
(defn factorial [n]
  "computes n * (n-1) * ... * 1"
  (loop [result 1
         ivals (range 2 (+ n 1))]
    (if (seq ivals)
      (recur (*' result (first ivals))
             (rest ivals))
      result)))
(factorial 10000)
 => 40238726007709377354370243392300398571937486421071463
    25437999104299385123986290205920442084869694048004799
    88610197196058631666872994808558901323829669944590997
```

Can split into separate function

```
(factorial 10000)
; => 40238726007709377354370243392300398571937486421071463
; 25437999104299385123986290205920442084869694048004799
; 88610197196058631666872994808558901323829669944590997
; ...
```

```
(defn floop
  "inner loop for factorial"
  [result ivals]
  (if (seq ivals)
    (floop (*' result (first ivals))
           (rest ivals))
    result))
(defn factorial [n]
  "computes n * (n-1) * ... * 1"
  (floop 1
         (range 2 (+ n 1))))
(factorial 10000)
; => StackOverflowError
     clojure.lang.Numbers.equal (Numbers.java:216)
```

recur allows tail call optimization

```
(defn floop
  "inner loop for factorial"
  [result ivals]
  (if (seq ivals)
                                           recur allows tail
    (recur (*' result (first ivals))
           (rest ivals))
                                           call optimization
   result))
(defn factorial [n]
  "computes n * (n-1) * ... * 1"
  (floop 1
         (range 2 (+ n 1))))
(factorial 10000)
 => 40238726007709377354370243392300398571937486421071463
     25437999104299385123986290205920442084869694048004799
     88610197196058631666872994808558901323829669944590997
```

Up Next: Exercises

\$ lein gorilla

