

$$\mathbb{E}_{p(x|y)}[f(x)] \approx \sum_{i=1}^N \frac{w(x_i)}{\sum_{j=1}^N w(x_j)} f(x_i)$$